

# Report: Homework 3 Math/CS 471

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## Abstract

This report will explore two methods of approximating the following integral

$$I = \int_{-1}^1 e^{\cos(kx)} dx,$$

for  $k = \pi$  or  $\pi^2$ . The first method is known as the trapezoidal rule and the second as Gauss quadrature.

## 1 Trapezoidal Rule

The trapezoidal rule is given by the following expression

$$\int_{X_L}^{X_R} f(x) dx \approx h \left( \frac{f(x_0) + f(x_n)}{2} + \sum_{i=1}^{n-1} f(x_i) \right)$$

where the grid is given by  $x_i = X_L + ih$ ,  $i = 0, \dots, n$ ,  $h = \frac{X_R - X_L}{n}$ .

## 2 Gauss Quadrature

[?]In Gauss quadrature the location of the grid-points and weights,  $\omega_i$ , are chosen so that the order of the approximation to the weighted integral

$$\int_{-1}^1 f(z) w(z) dz \approx \sum_{i=0}^n \omega_i f(z_i),$$

is maximized. (The function  $w(z)$  is positive and integrable. In this report we will only consider the case when  $w(z) = 1$  in order to simplify things.

### **3 Methods**

Here is how the programs were executed...

### **4 Results**

Here are the results...

## 5 Appendix

In order to compile and execute the code for this assignment perl is used.  
The directory in which the code can be found is:

*/Homework/Homework2/Code/*

Once in this directory the following command will compile and execute the code:

*\$ perl newtonS.p*

## References

- [1] Daniel Appelo *Homework 3*. referenced Sep. 26, 2015