

Report: Homework 3 Math/CS 471

Teo Brandt and Brennan Collins

September 17, 2015

Abstract

This report will explore two methods of approximating the following integral

$$I = \int_{-1}^1 e^{\cos(kx)} dx,$$

for $k = \pi$ or π^2 . The first method is known as the trapezoidal rule and the second as Gauss quadrature.

1 Trapezoidal Rule

The trapezoidal rule is given by the following expression

$$\int_{X_L}^{X_R} f(x) dx \approx h \left(\frac{f(x_0) + f(x_n)}{2} + \sum_{i=1}^{n-1} f(x_i) \right)$$

where the grid is given by $x_i = X_L + ih$, $i = 0, \dots, n$, $h = \frac{X_R - X_L}{n}$.

2 Gauss Quadrature

[?]In Gauss quadrature the location of the grid-points and weights, ω_i , are chosen so that the order of the approximation to the weighted integral

$$\int_{-1}^1 f(z) w(z) dz \approx \sum_{i=0}^n \omega_i f(z_i),$$

is maximized. (The function $w(z)$ is positive and integrable. In this report we will only consider the case when $w(z) = 1$ in order to simplify things.

3 Methods

Here is how the programs were executed...

4 Results

Figure 1: Plot of error against \mathbf{n}

In the figure shown above, different rates of convergence are observed for each of the methods and for each of the values of k . The trapezoidal method where $k = \pi^2$ is the only case in which the order of the method may be read from the slope of its plot. This slope is ≈ -3 which is consistent with the theory as shown for

5 Appendix

In order to compile and execute the code for this assignment perl is used.
The directory in which the code can be found is:

/Homework/Homework2/Code/

Once in this directory the following command will compile and execute the code:

\$ perl newtonS.p

References

- [1] Daniel Appelo *Homework 3*. referenced Sep. 26, 2015