

Supplementary Information

1. BAYESIAN DATA ANALYSIS

This section outlines how the Bayesian Data Analysis was performed. We follow the recommendations and guidelines of [1, 2, 3] and assess the Markov Chain Monte Carlo (MCMC) chains and Posterior Predictive Checks. i

1.1. Assessing the MCMC chains. All analysis were conducted using the R programming language and the `cmdstanr` library. Each model was computed using four parallel chains using 2000 iterations and an additional 200 warmup iterations. None of the iteration diverged as can be seen in the traceplots Figures 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11 and 12 and therefore the MCMC simulation is considered valid.

In addition we investigate diagnostics of the posterior estimates, such as *Gelman-Rubin Potential Scale Reduction* (\hat{R}) [4] the number of *efficient samples* (n_{eff}). Tables 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11 and 12 contains three columns. The first column contains \hat{R} and the other two contains two different estimates of the number of effective samples. As a rule of thumb we should have $\hat{R} < 1.01$ which is satisfied in all scenarios. The number of efficient samples should be atleast 200, which is satisfied in all cases.

TABLE 1. Diagnostics for the posterior ranks (aggregated)

Variable	Rhat	ess_bulk	ess_tail
a_alg[1]	1.000	4363.596	4389.268
a_alg[2]	1.002	4310.666	4704.940
a_alg[3]	1.002	4506.676	4641.121
a_alg[4]	1.000	4511.913	5175.336
a_alg[5]	1.001	4179.552	5407.158
a_alg[6]	1.000	4421.190	4853.736
a_alg[7]	1.000	4431.419	4697.169
a_alg[8]	1.000	4429.212	4462.071
a_alg[9]	1.001	4518.639	4809.640
a_alg[10]	1.001	4581.093	4876.947
a_alg[11]	1.001	4409.779	5259.614
a_alg[12]	1.001	4903.602	5323.972
a_alg[13]	1.001	4561.385	5199.520
a_alg[14]	1.000	4635.099	4744.294
a_alg[15]	1.001	4431.587	5018.196
a_alg[16]	1.000	4328.026	4618.103
a_alg[17]	1.001	4493.896	4915.240

2. POSTERIOR PREDICTIVE CHECKS

For posterior predictive checks, we investigate how well the mean error rate is captured by the posterior distribution. Figures 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, and 24 shows the posterior distribution of the mean for each algorithm and the Figures show that the mean is well captured by the posterior distribution.

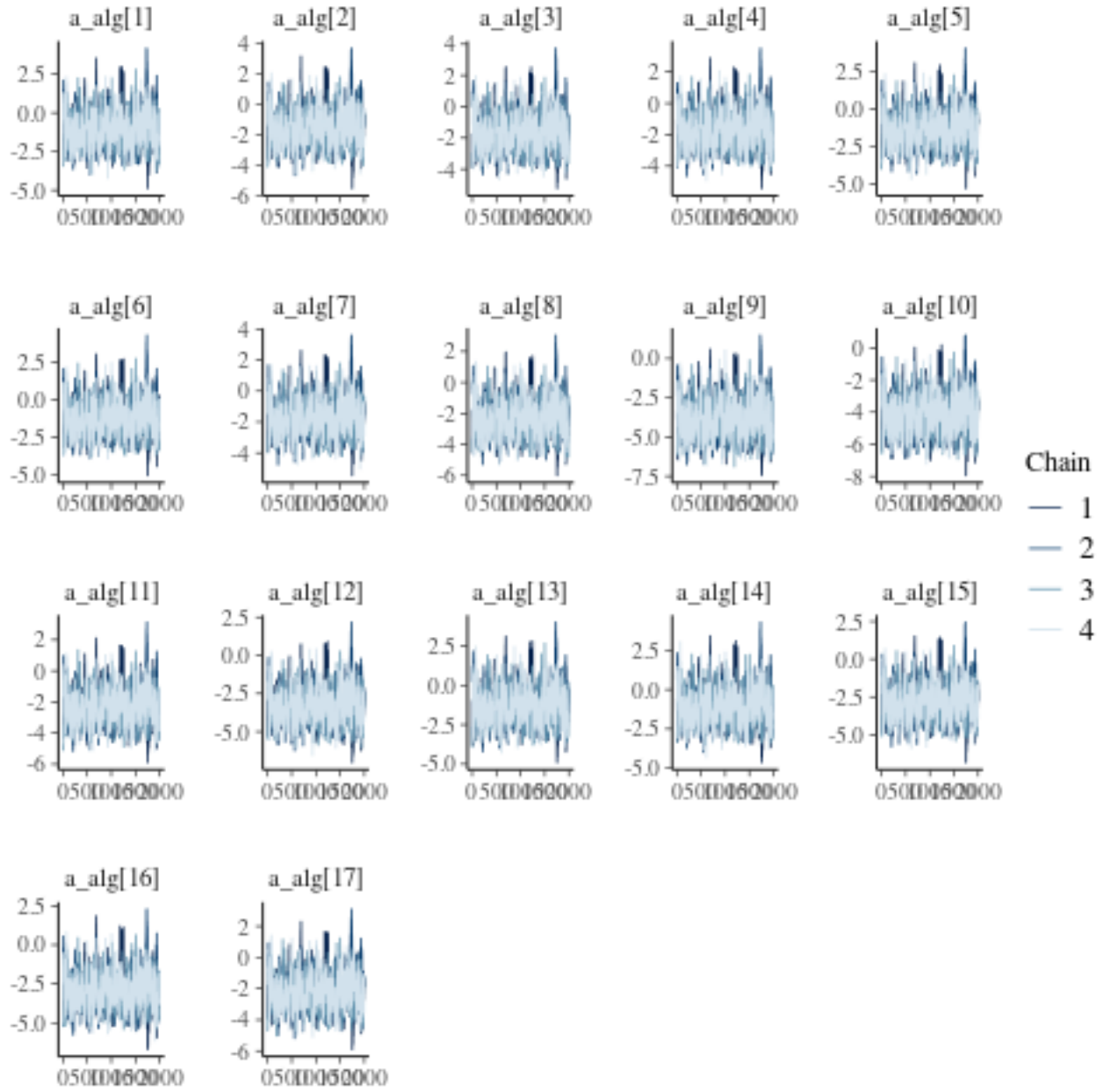


FIGURE 1. Simulated MCMC chains for the strength parameters (aggregated data).

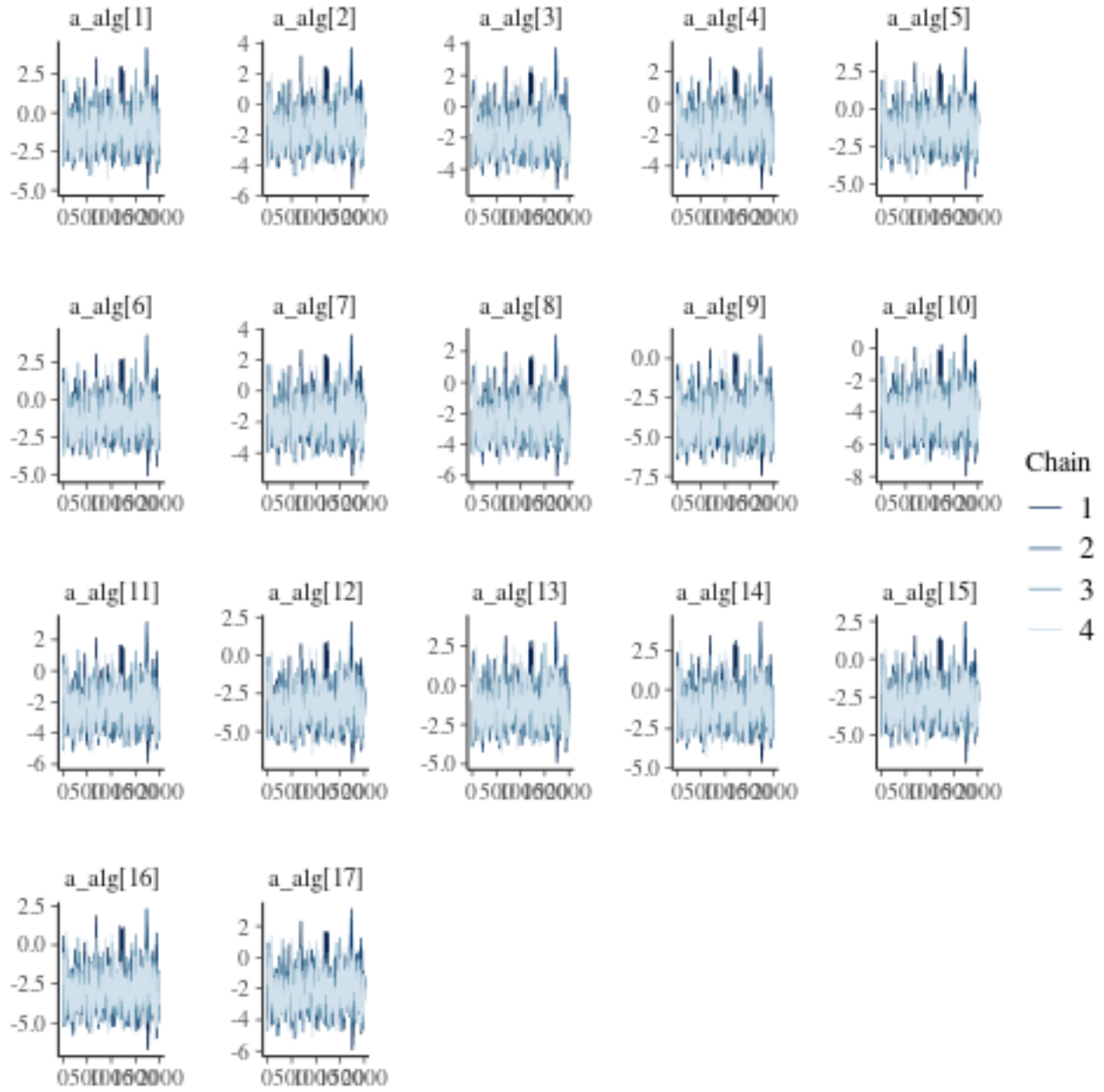


FIGURE 2. Simulated MCMC chains for the effect parameters (aggregated data).

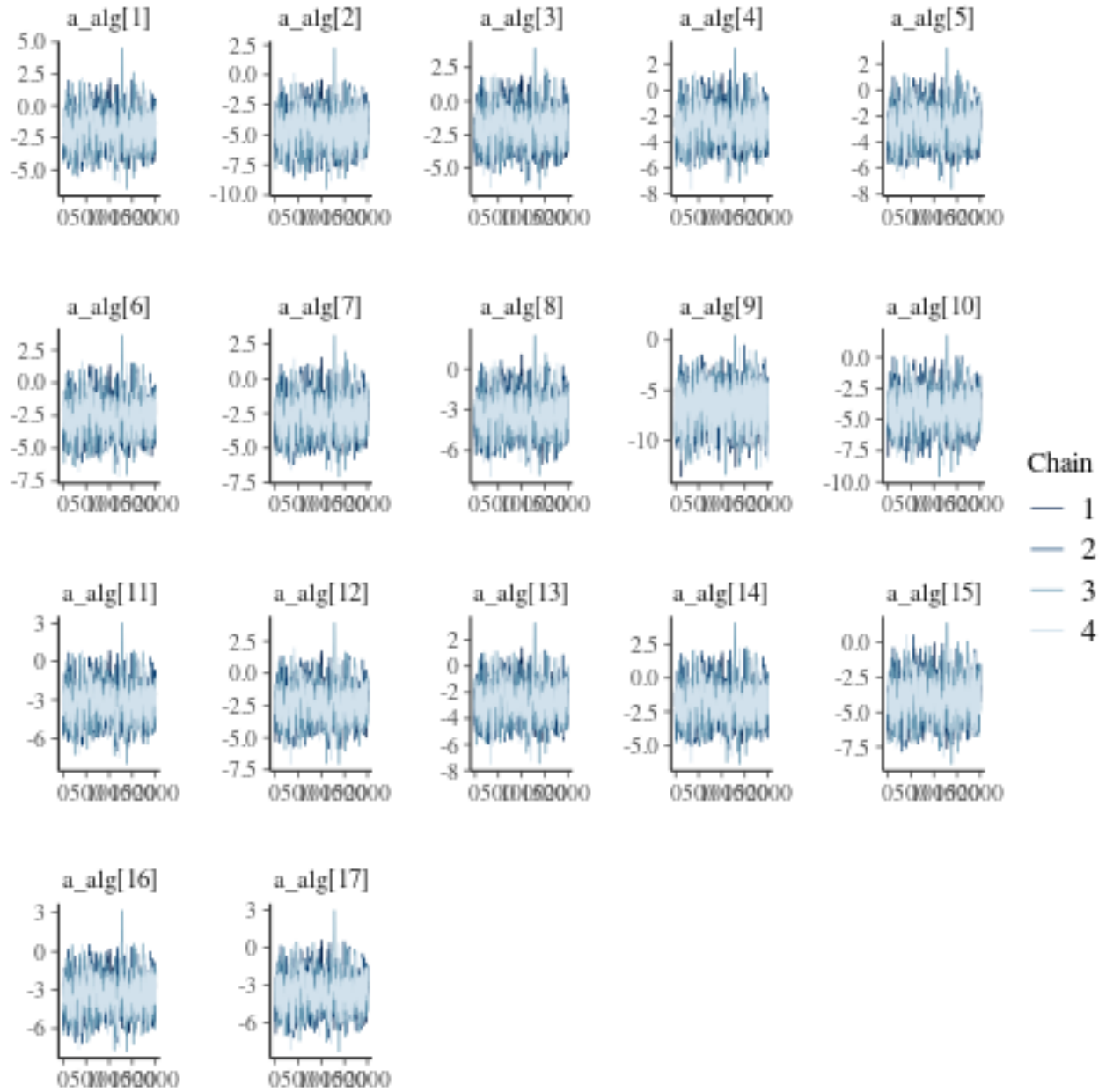


FIGURE 3. Simulated MCMC chains for the strength parameters (image data).

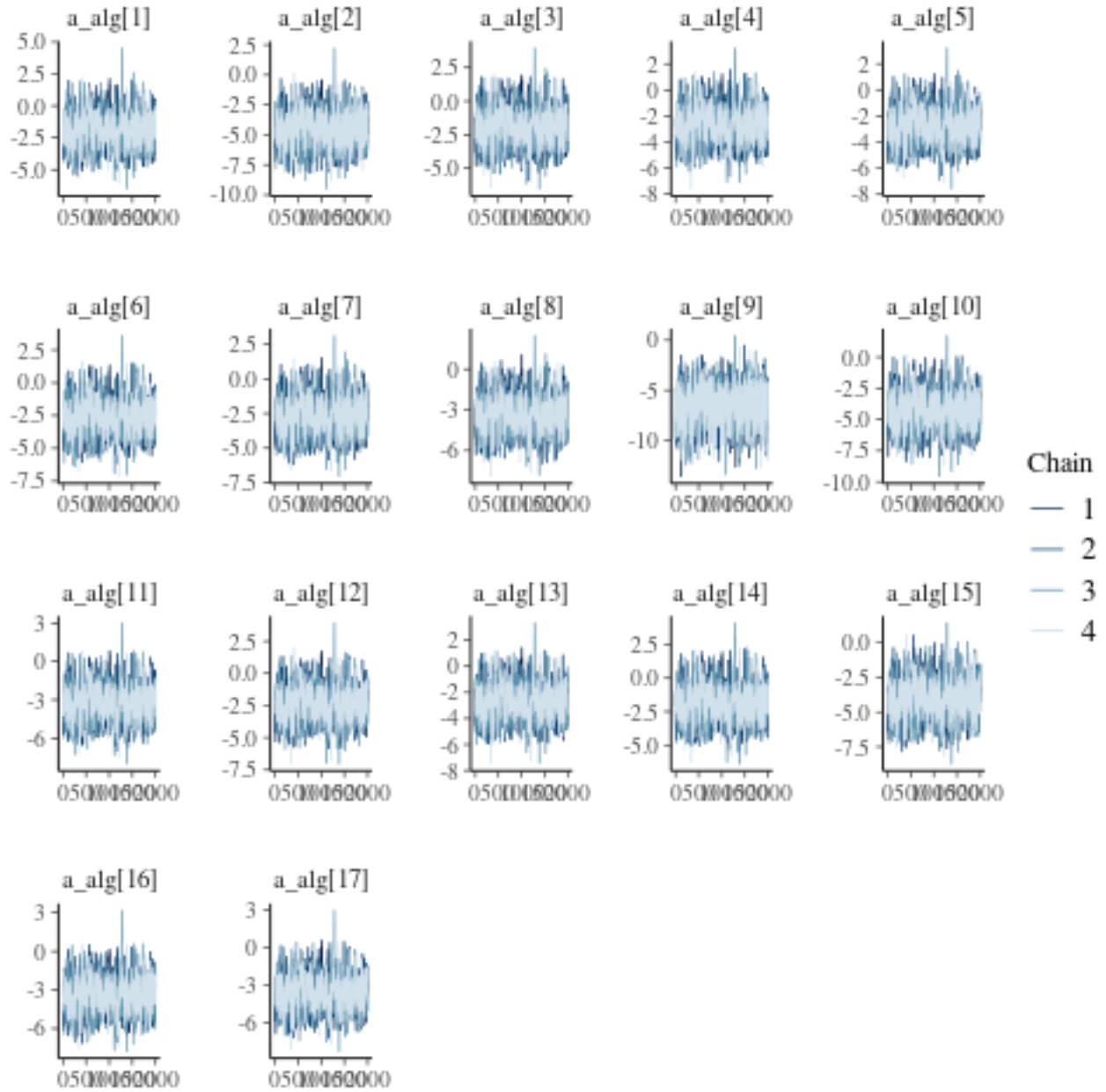


FIGURE 4. Simulated MCMC chains for the effect parameters (image data).

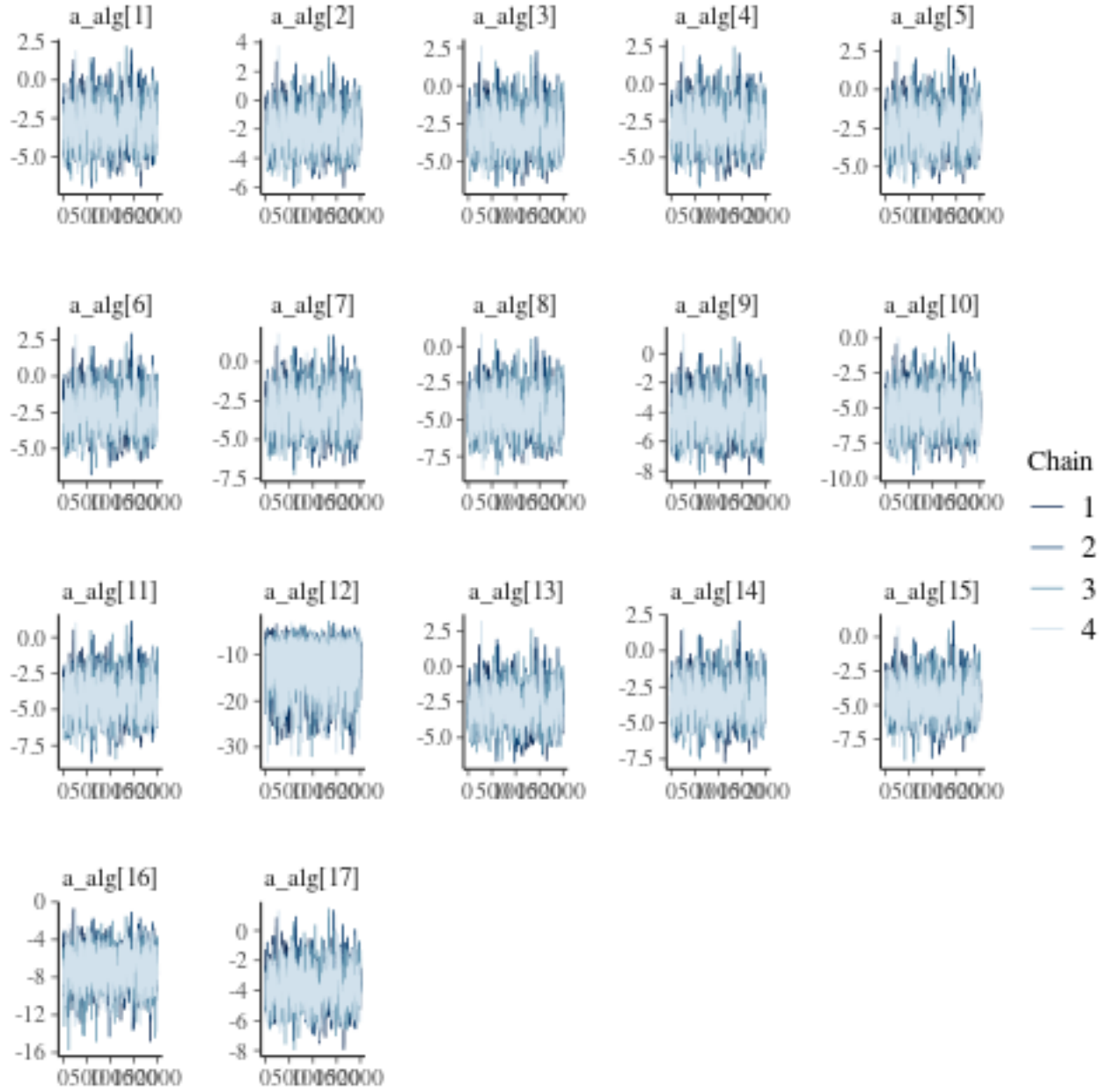


FIGURE 5. Simulated MCMC chains for the strength parameters (text data).

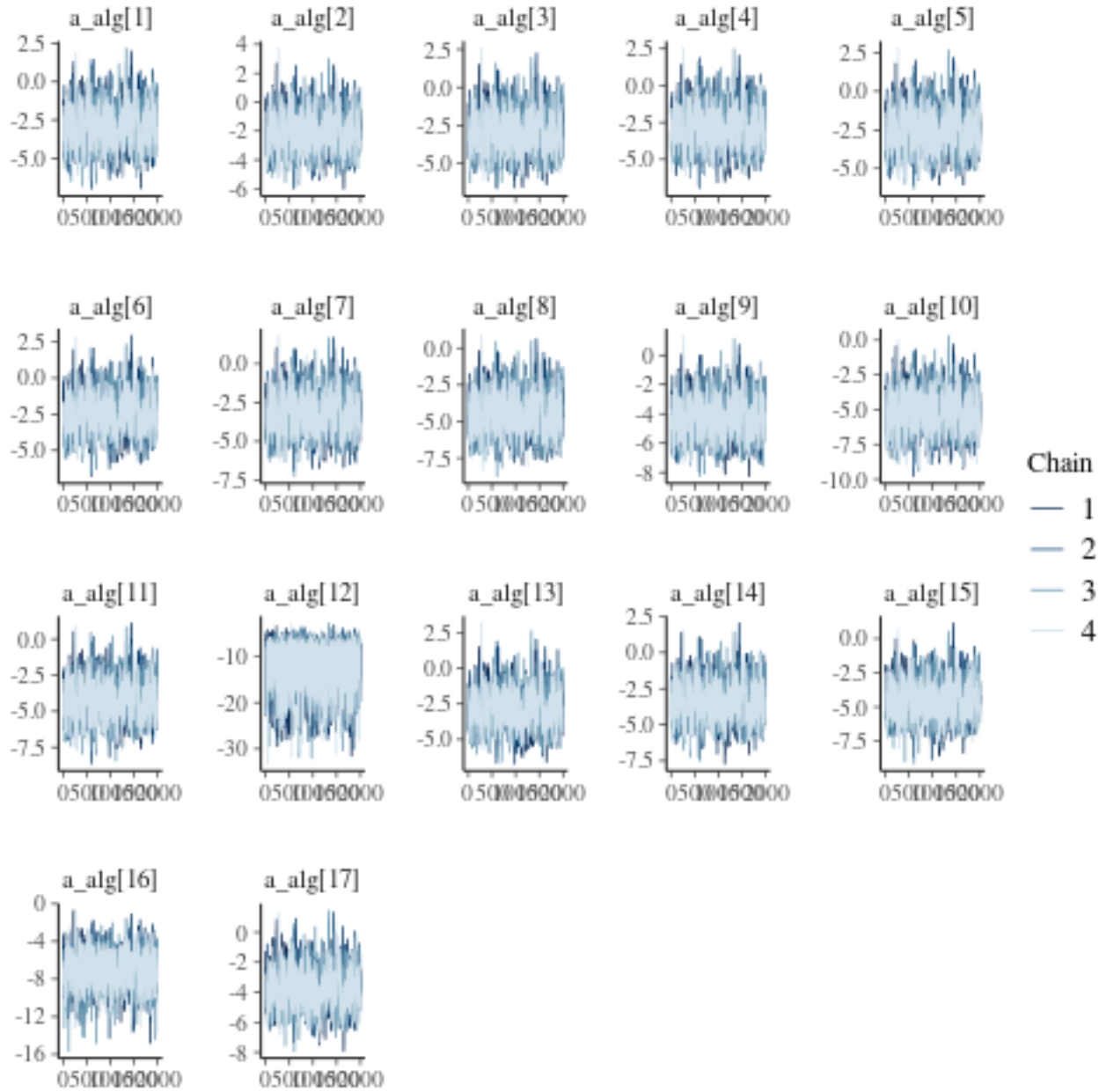


FIGURE 6. Simulated MCMC chains for the effect parameters (text data).

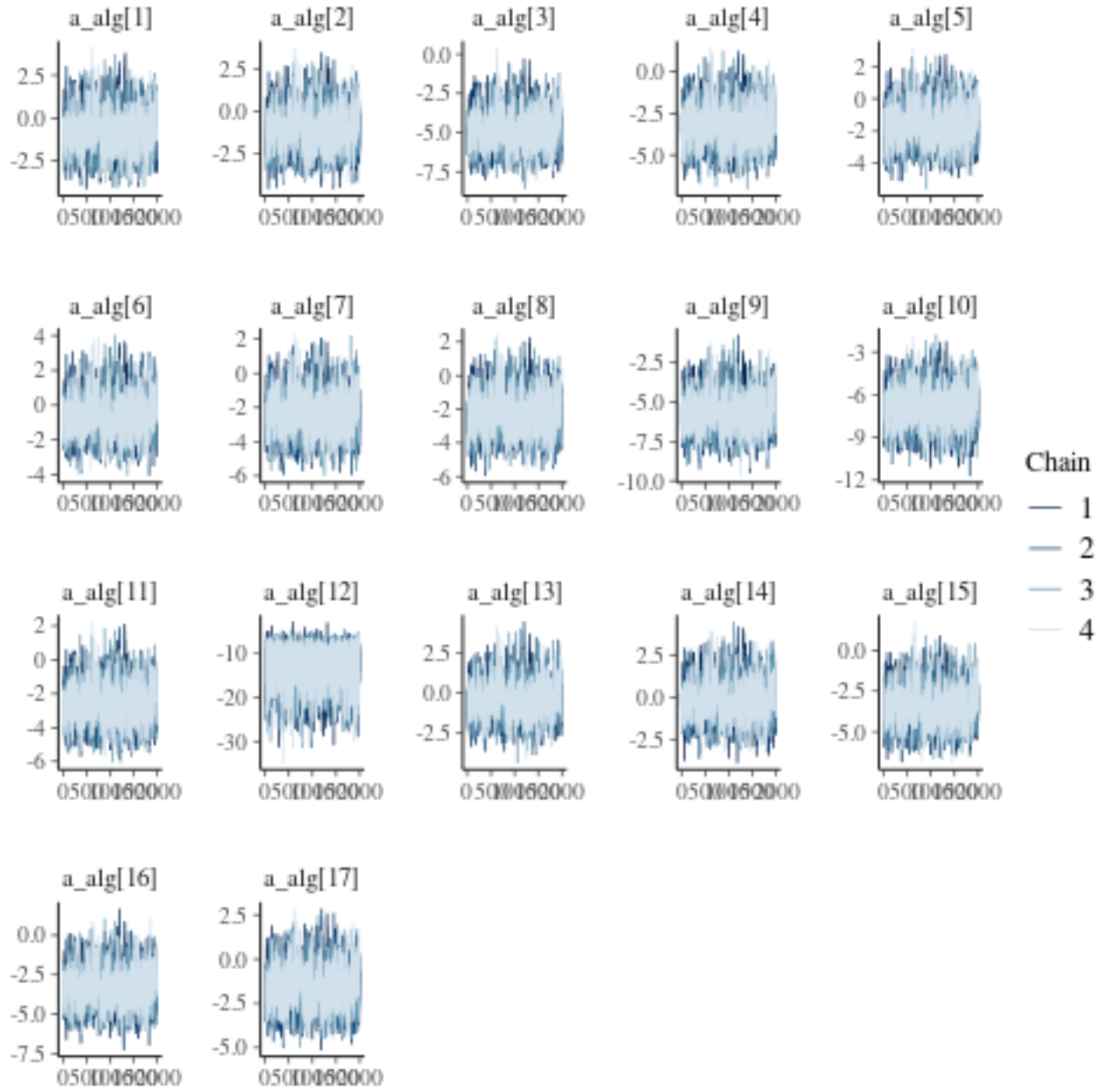


FIGURE 7. Simulated MCMC chains for the strength parameters (audio data).

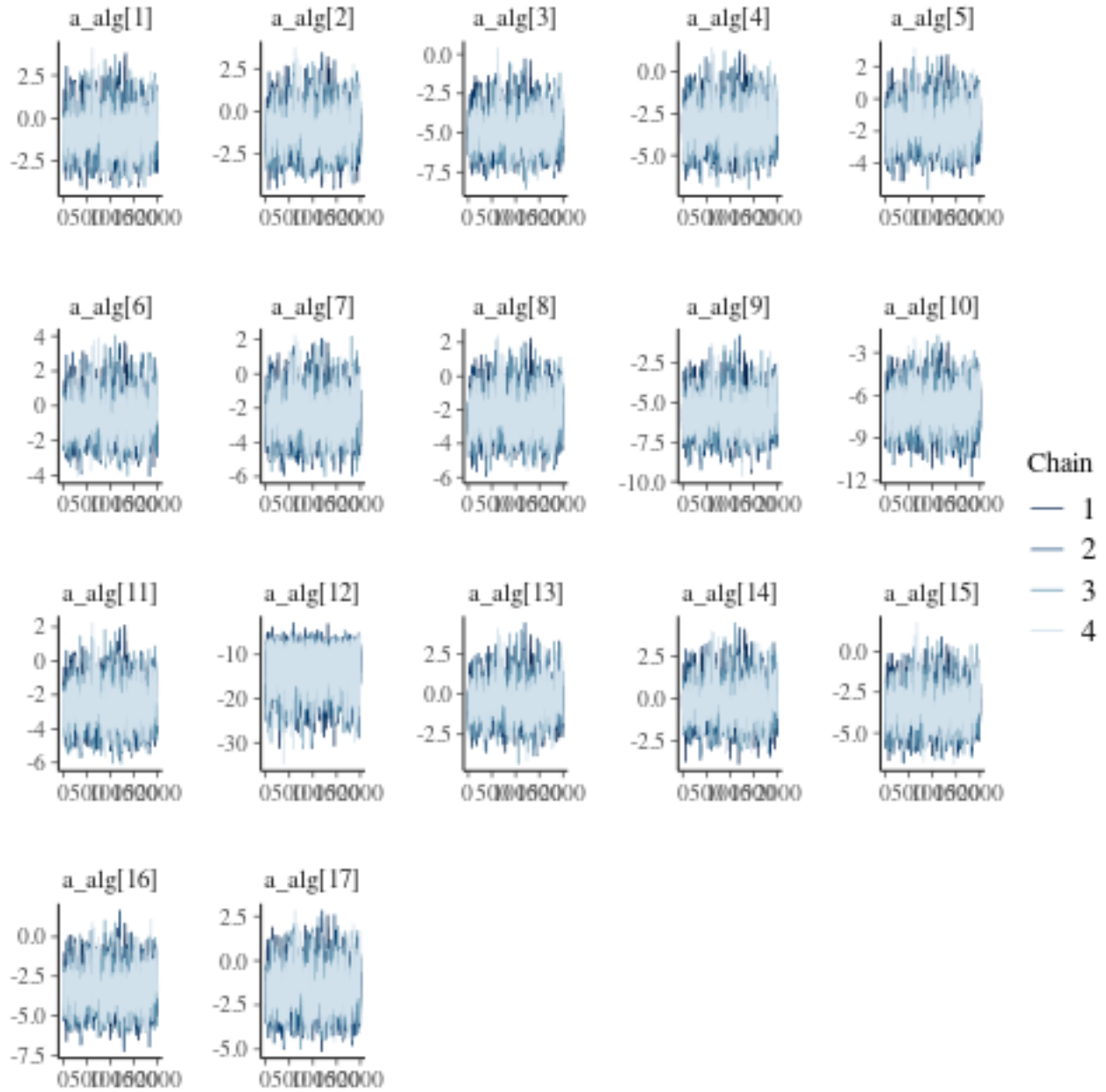


FIGURE 8. Simulated MCMC chains for the effect parameters (audio data).

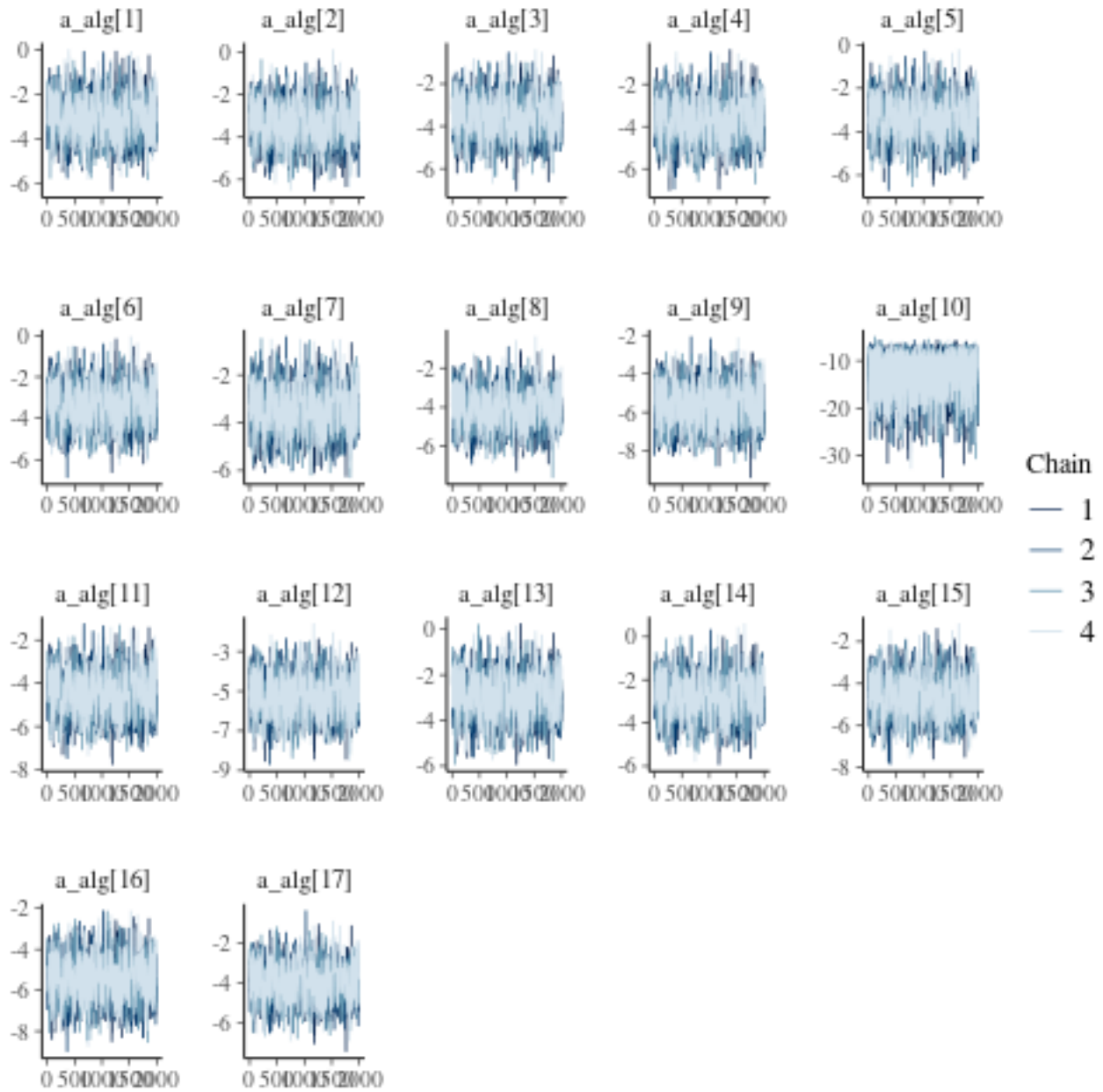


FIGURE 9. Simulated MCMC chains for the strength parameters (small allocation of data).

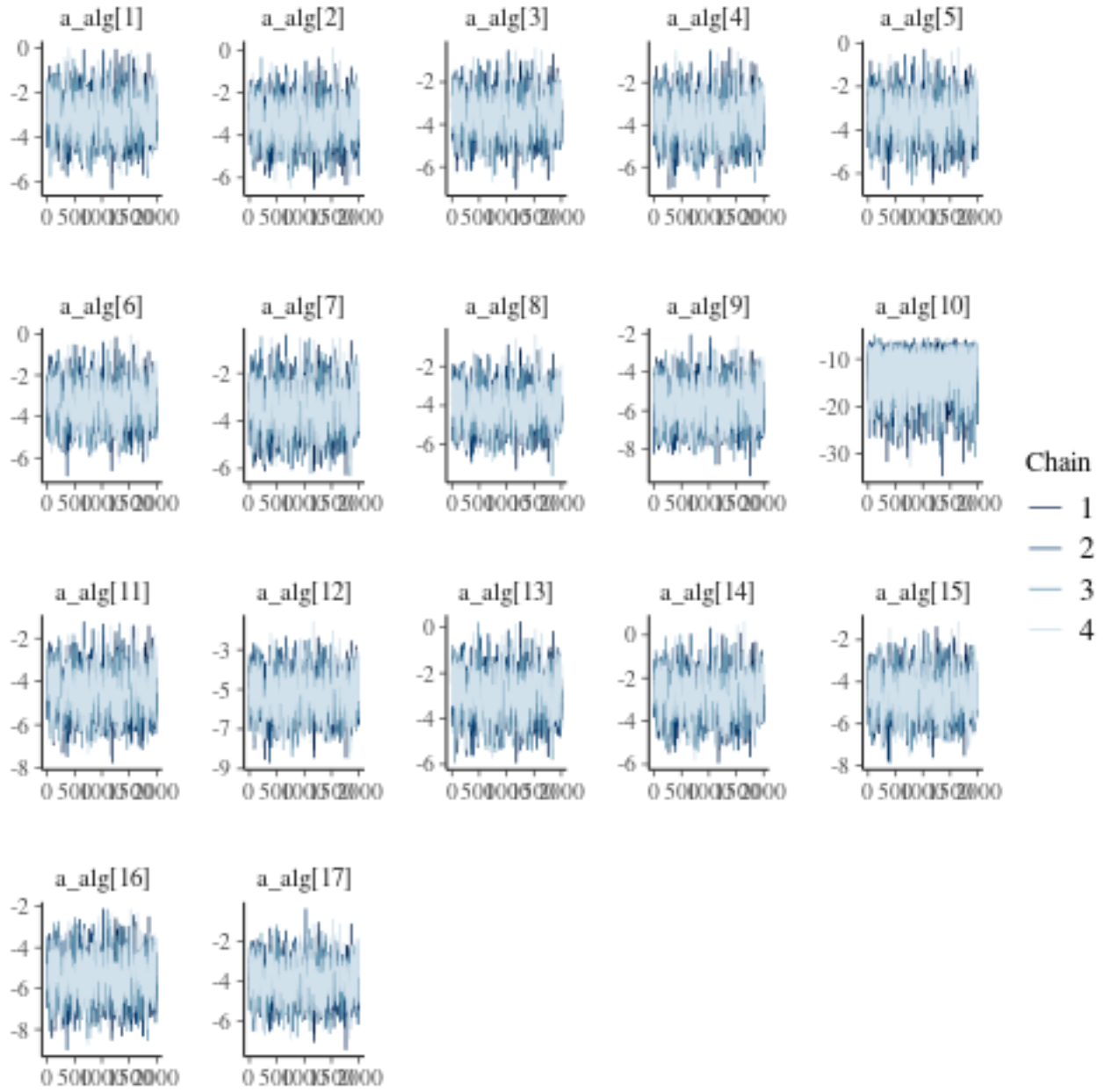


FIGURE 10. Simulated MCMC chains for the effect parameters a_i (small allocation of data)

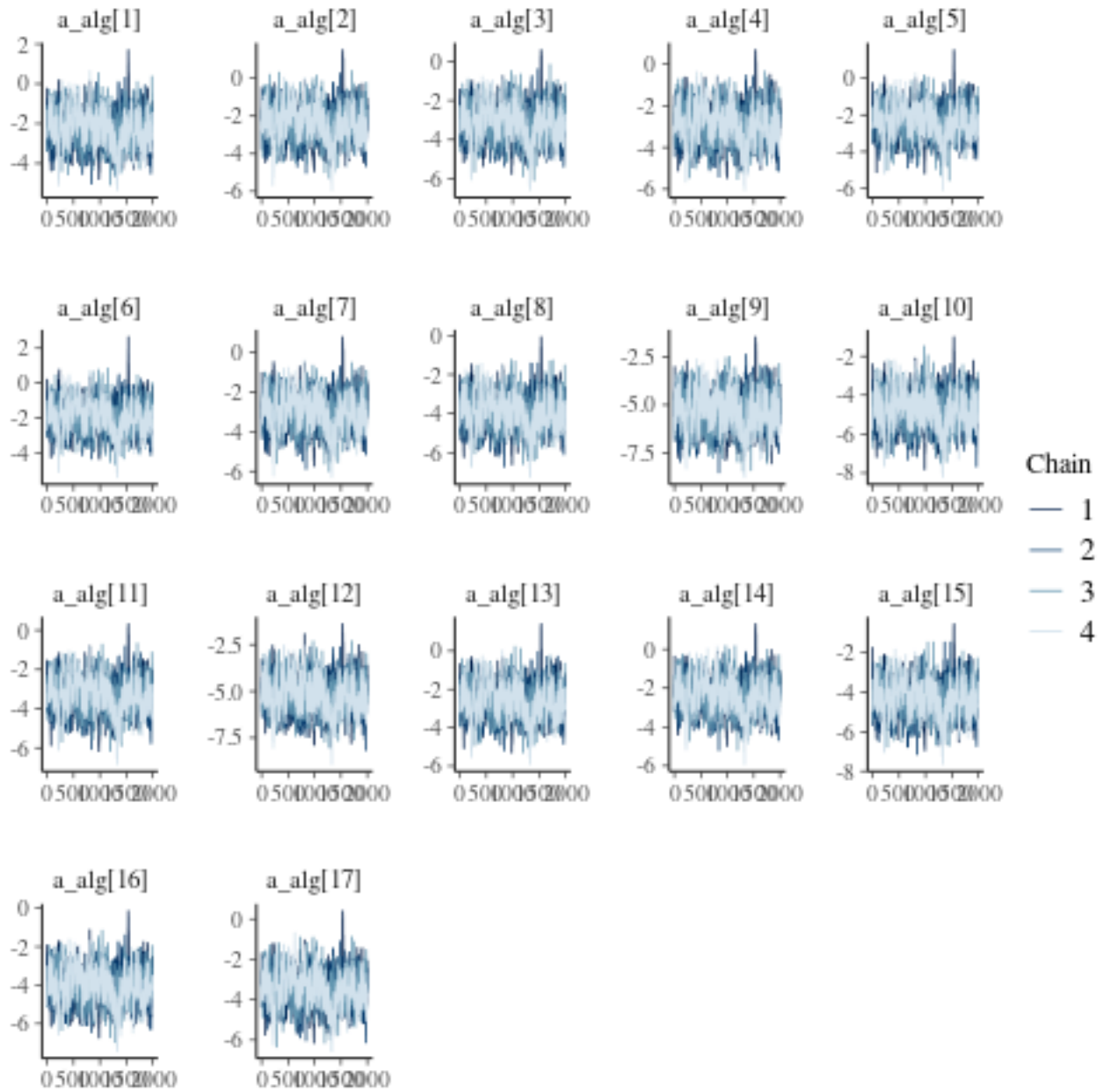


FIGURE 11. Simulated MCMC chains for the strength parameters (large allocation of data).

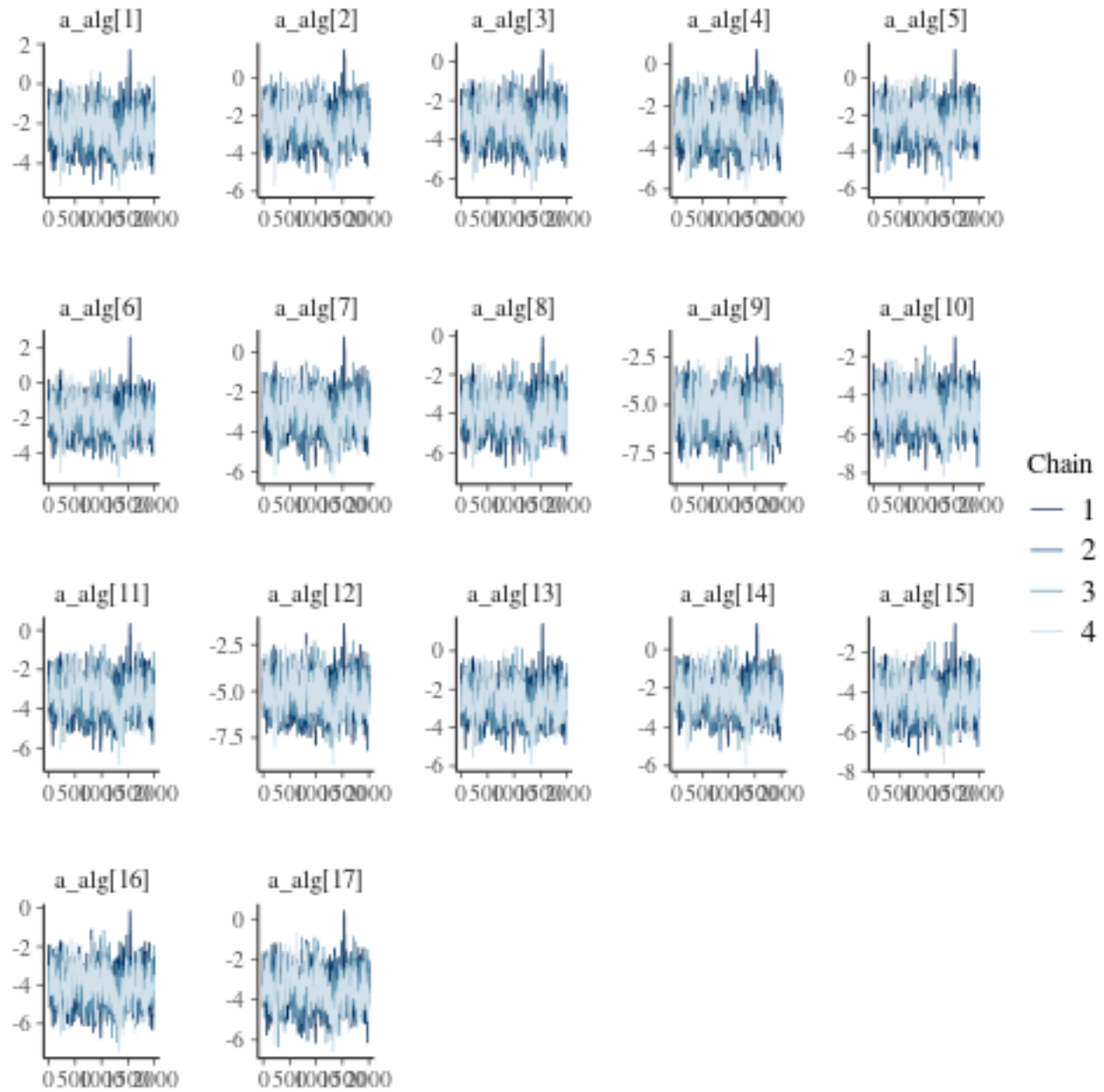


FIGURE 12. Simulated MCMC chains for the strength parameters (large allocation of data).

TABLE 2. Diagnostics for the posterior ranks (image datatype)

Variable	Rhat	ess_bulk	ess_tail
a_alg[1]	1.001	5569.827	4926.560
a_alg[2]	1.000	5384.131	5833.872
a_alg[3]	1.000	5453.536	5380.084
a_alg[4]	1.000	4758.031	5284.870
a_alg[5]	1.000	4738.275	4432.089
a_alg[6]	1.000	5421.547	5321.455
a_alg[7]	1.000	5538.582	5961.318
a_alg[8]	1.000	5458.517	5340.038
a_alg[9]	1.000	5314.767	5418.474
a_alg[10]	1.000	5526.175	5679.398
a_alg[11]	1.000	5530.860	6031.030
a_alg[12]	1.000	4838.689	5512.851
a_alg[13]	1.000	5119.155	5921.655
a_alg[14]	1.000	5301.094	5466.499
a_alg[15]	1.000	5222.151	5542.210
a_alg[16]	1.000	4757.067	5744.937
a_alg[17]	1.001	5019.732	5372.783

TABLE 3. Diagnostics for the posterior ranks (text datatype)

Variable	Rhat	ess_bulk	ess_tail
a_alg[1]	1.001	3950.014	5012.816
a_alg[2]	1.001	3967.102	4947.424
a_alg[3]	1.001	4034.655	5302.354
a_alg[4]	1.001	4110.053	4768.079
a_alg[5]	1.000	4124.764	5175.381
a_alg[6]	1.001	4085.174	4895.489
a_alg[7]	1.001	3927.361	4756.549
a_alg[8]	1.001	4303.844	4836.293
a_alg[9]	1.001	4407.529	5267.432
a_alg[10]	1.000	4110.240	4805.624
a_alg[11]	1.001	4178.923	5332.661
a_alg[12]	1.001	4659.343	5859.878
a_alg[13]	1.000	4142.509	5047.237
a_alg[14]	1.001	3822.927	4777.553
a_alg[15]	1.001	3859.451	4303.521
a_alg[16]	1.000	4199.281	5302.039
a_alg[17]	1.001	4283.987	5291.580

TABLE 4. Diagnostics for the posterior ranks (audio datatype)

Variable	Rhat	ess_bulk	ess_tail
a_alg[1]	1.002	8472.718	5296.022
a_alg[2]	1.000	9903.935	5834.777
a_alg[3]	1.000	9027.025	5998.672
a_alg[4]	1.000	9146.187	5669.856
a_alg[5]	1.001	8125.924	5011.553
a_alg[6]	1.001	8687.339	5981.227
a_alg[7]	1.000	8628.567	5128.435
a_alg[8]	1.000	8184.104	5895.332
a_alg[9]	1.001	8197.165	6069.792
a_alg[10]	1.001	7761.948	5446.681
a_alg[11]	1.001	8807.185	5967.099
a_alg[12]	1.001	8913.463	6830.820
a_alg[13]	1.001	8633.998	5469.254
a_alg[14]	1.000	8748.116	5787.659
a_alg[15]	1.001	8118.402	5409.835
a_alg[16]	1.001	8752.863	6160.065
a_alg[17]	1.000	9061.207	5681.185

TABLE 5. Diagnostics for the posterior ranks (small allocation)

Variable	Rhat	ess_bulk	ess_tail
a_alg[1]	1.000	4735.897	4112.013
a_alg[2]	1.000	4793.097	4387.702
a_alg[3]	1.001	4694.239	4751.959
a_alg[4]	1.001	4675.820	4336.875
a_alg[5]	1.001	4835.159	4383.011
a_alg[6]	1.000	4435.438	4177.937
a_alg[7]	1.000	4555.595	4329.844
a_alg[8]	1.000	4474.490	4002.949
a_alg[9]	1.000	4748.329	4499.903
a_alg[10]	1.000	4955.164	4542.496
a_alg[11]	1.001	5020.975	4230.675
a_alg[12]	1.001	5478.078	4698.688
a_alg[13]	1.001	4471.626	3814.573
a_alg[14]	1.001	4459.145	4289.903
a_alg[15]	1.000	4488.908	4743.348
a_alg[16]	1.001	4503.813	4560.218
a_alg[17]	1.001	4666.474	3592.517

TABLE 6. Diagnostics for the posterior ranks (large allocation)

Variable	Rhat	ess_bulk	ess_tail
a_alg[1]	1.000	9164.379	5867.408
a_alg[2]	1.001	9215.643	5816.067
a_alg[3]	1.000	9621.344	5915.346
a_alg[4]	1.000	9415.307	5461.207
a_alg[5]	1.000	9607.589	5958.987
a_alg[6]	1.001	8800.023	5865.614
a_alg[7]	1.000	9822.973	6074.739
a_alg[8]	1.001	8850.728	5606.480
a_alg[9]	1.000	8739.513	5854.369
a_alg[10]	1.003	9746.317	5910.605
a_alg[11]	1.001	8805.959	5627.071
a_alg[12]	1.001	9520.813	6643.876
a_alg[13]	1.001	8688.475	6033.553
a_alg[14]	1.001	8779.775	6017.763
a_alg[15]	1.000	9485.947	5613.972
a_alg[16]	1.001	9502.301	6621.634
a_alg[17]	1.001	9140.726	5586.761

TABLE 7. Diagnostics for the posterior effects (aggregated)

variable	rhat	ess_bulk	ess_tail
a_alg[1]	1.006	440.182	541.622
a_alg[2]	1.006	439.851	507.177
a_alg[3]	1.006	437.147	522.022
a_alg[4]	1.006	442.510	523.726
a_alg[5]	1.006	440.479	535.330
a_alg[6]	1.005	439.403	531.731
a_alg[7]	1.006	441.416	530.607
a_alg[8]	1.006	443.915	552.155
a_alg[9]	1.006	455.324	549.392
a_alg[10]	1.005	454.539	548.766
a_alg[11]	1.005	436.243	532.145
a_alg[12]	1.005	446.804	552.072
a_alg[13]	1.006	443.509	522.109
a_alg[14]	1.006	436.285	518.366
a_alg[15]	1.005	447.754	514.499
a_alg[16]	1.005	446.589	518.547
a_alg[17]	1.006	438.401	525.700

TABLE 8. Diagnostics for the posterior effects (image datatype)

Variable	Rhat	ess_bulk	ess_tail
a_alg[1]	1.002	694.306	1165.395
a_alg[2]	1.002	848.293	1373.391
a_alg[3]	1.002	711.569	1215.024
a_alg[4]	1.002	705.012	1163.763
a_alg[5]	1.002	714.125	1100.587
a_alg[6]	1.001	696.947	1189.039
a_alg[7]	1.002	696.537	1208.653
a_alg[8]	1.002	746.903	1307.071
a_alg[9]	1.001	1298.246	2323.478
a_alg[10]	1.001	753.645	1406.142
a_alg[11]	1.002	703.356	1172.664
a_alg[12]	1.002	684.666	1234.366
a_alg[13]	1.002	713.963	1315.901
a_alg[14]	1.002	716.643	1163.742
a_alg[15]	1.002	766.597	1409.595
a_alg[16]	1.002	728.488	1288.008
a_alg[17]	1.001	723.604	1322.541

TABLE 9. Diagnostics for the posterior effects (text datatype)

variable	rhat	ess_bulk	ess_tail
a_alg[1]	1.011	600.486	901.568
a_alg[2]	1.011	619.436	935.044
a_alg[3]	1.012	613.667	910.521
a_alg[4]	1.011	628.431	891.711
a_alg[5]	1.012	605.999	902.718
a_alg[6]	1.012	612.309	950.841
a_alg[7]	1.012	612.771	850.828
a_alg[8]	1.011	636.753	905.439
a_alg[9]	1.011	649.210	961.074
a_alg[10]	1.010	693.142	1043.443
a_alg[11]	1.010	629.357	961.024
a_alg[12]	1.000	4197.822	4444.723
a_alg[13]	1.011	599.856	811.524
a_alg[14]	1.011	626.391	906.396
a_alg[15]	1.009	646.797	888.692
a_alg[16]	1.005	1014.138	1357.790
a_alg[17]	1.012	620.882	895.637

TABLE 10. Diagnostics for the posterior effects (audio datatype)

variable	rhat	ess_bulk	ess_tail
a_alg[1]	1.003	870.761	1374.035
a_alg[2]	1.004	849.701	1351.964
a_alg[3]	1.003	770.054	1325.369
a_alg[4]	1.003	833.502	1442.465
a_alg[5]	1.003	842.617	1358.068
a_alg[6]	1.003	770.569	1398.594
a_alg[7]	1.002	862.501	1389.156
a_alg[8]	1.003	845.793	1565.068
a_alg[9]	1.003	841.420	1339.853
a_alg[10]	1.003	1028.792	1773.255
a_alg[11]	1.003	839.701	1495.961
a_alg[12]	1.001	4585.525	4785.559
a_alg[13]	1.003	764.878	1392.853
a_alg[14]	1.003	799.794	1362.592
a_alg[15]	1.003	832.628	1402.115
a_alg[16]	1.003	830.624	1467.762
a_alg[17]	1.003	879.117	1481.837

TABLE 11. Diagnostics for the posterior effects (small allocation)

variable	rhat	ess_bulk	ess_tail
a_alg[1]	1.003	614.066	1004.753
a_alg[2]	1.004	618.395	1045.639
a_alg[3]	1.003	627.256	1019.701
a_alg[4]	1.004	616.507	1038.961
a_alg[5]	1.004	617.869	955.493
a_alg[6]	1.004	615.979	1151.694
a_alg[7]	1.003	630.325	1006.059
a_alg[8]	1.004	632.262	1038.843
a_alg[9]	1.003	717.147	1206.127
a_alg[10]	1.001	3588.698	3392.161
a_alg[11]	1.003	623.126	1198.584
a_alg[12]	1.003	684.711	1284.887
a_alg[13]	1.003	623.283	1096.985
a_alg[14]	1.003	611.306	1008.557
a_alg[15]	1.003	648.600	1073.667
a_alg[16]	1.002	694.782	1184.188
a_alg[17]	1.004	629.064	1135.959

TABLE 12. Diagnostics for the posterior effects (large allocation)

variable	rhat	ess_bulk	ess_tail
a_alg[1]	1.023	258.317	463.035
a_alg[2]	1.021	268.310	538.120
a_alg[3]	1.021	253.876	458.608
a_alg[4]	1.023	248.612	503.228
a_alg[5]	1.022	258.077	465.426
a_alg[6]	1.023	255.613	533.282
a_alg[7]	1.022	252.546	457.869
a_alg[8]	1.021	263.317	584.556
a_alg[9]	1.019	301.839	709.768
a_alg[10]	1.018	289.796	539.473
a_alg[11]	1.021	264.149	504.409
a_alg[12]	1.021	281.814	665.613
a_alg[13]	1.022	257.686	480.975
a_alg[14]	1.022	252.151	576.368
a_alg[15]	1.020	262.272	499.345
a_alg[16]	1.020	266.885	570.303
a_alg[17]	1.023	259.107	516.268

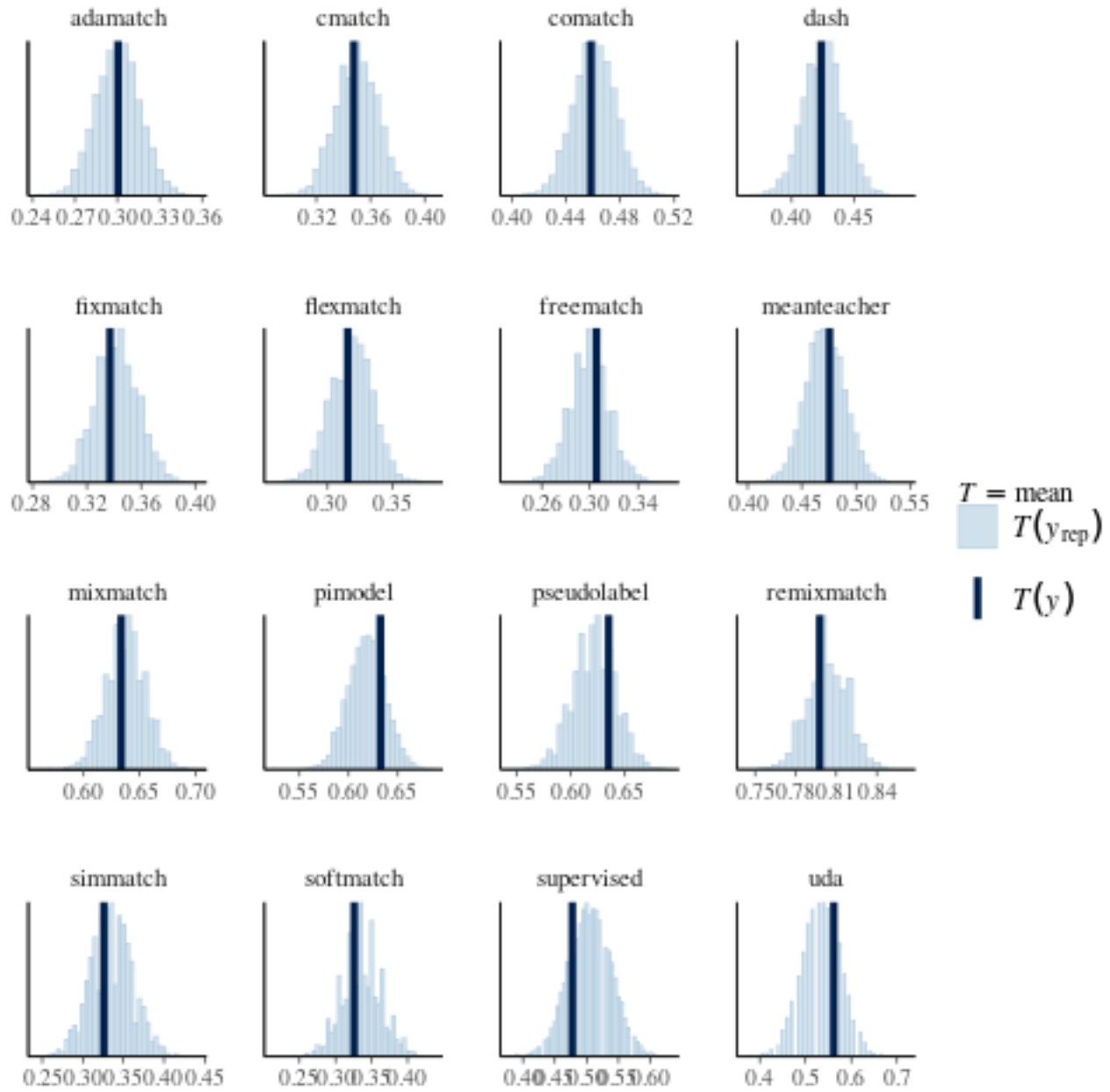


FIGURE 13. Posterior predictive check of the ranks for each algorithm (aggregated)

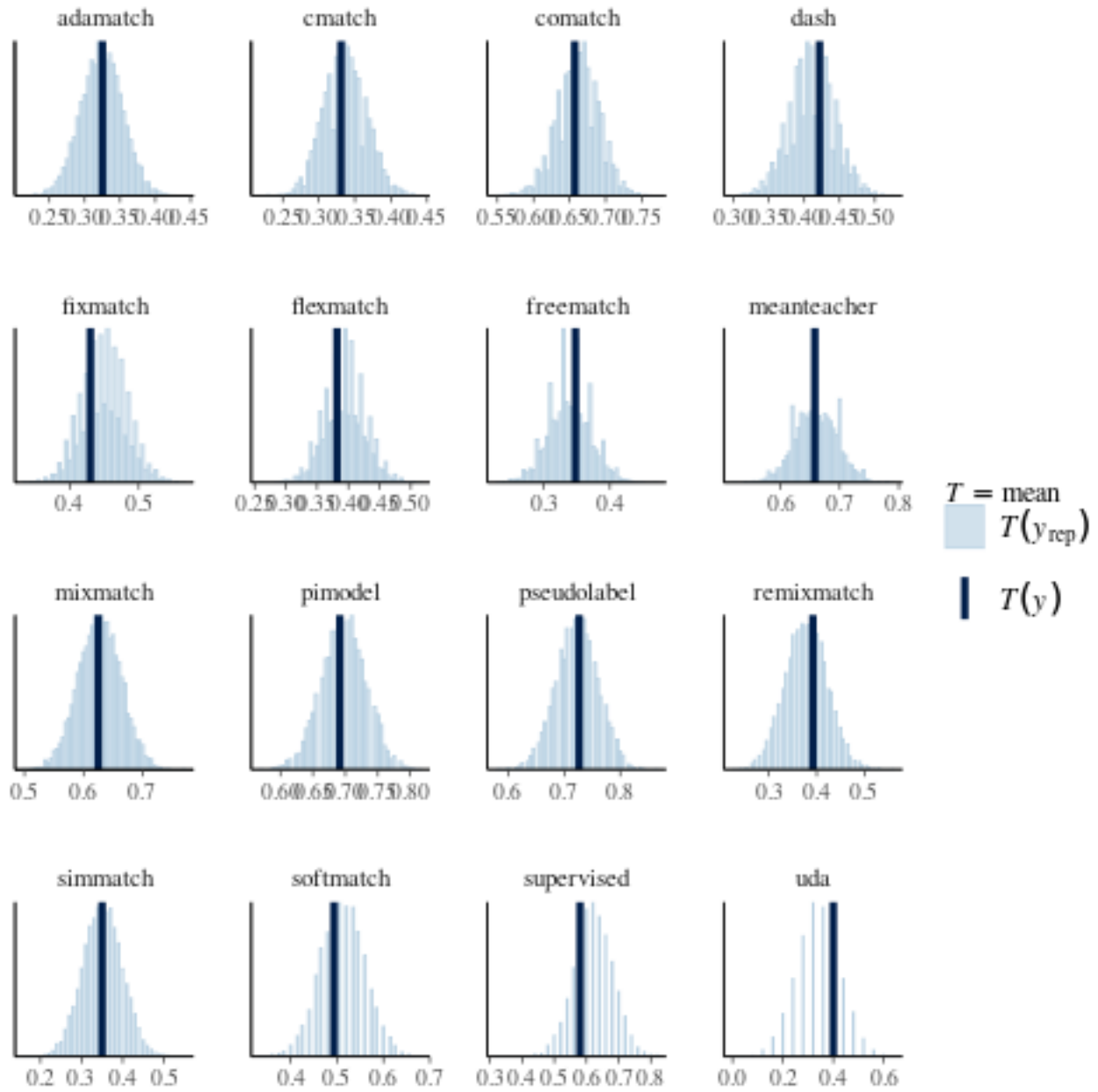


FIGURE 14. Posterior predictive check of the ranks for each algorithm (image datatype)

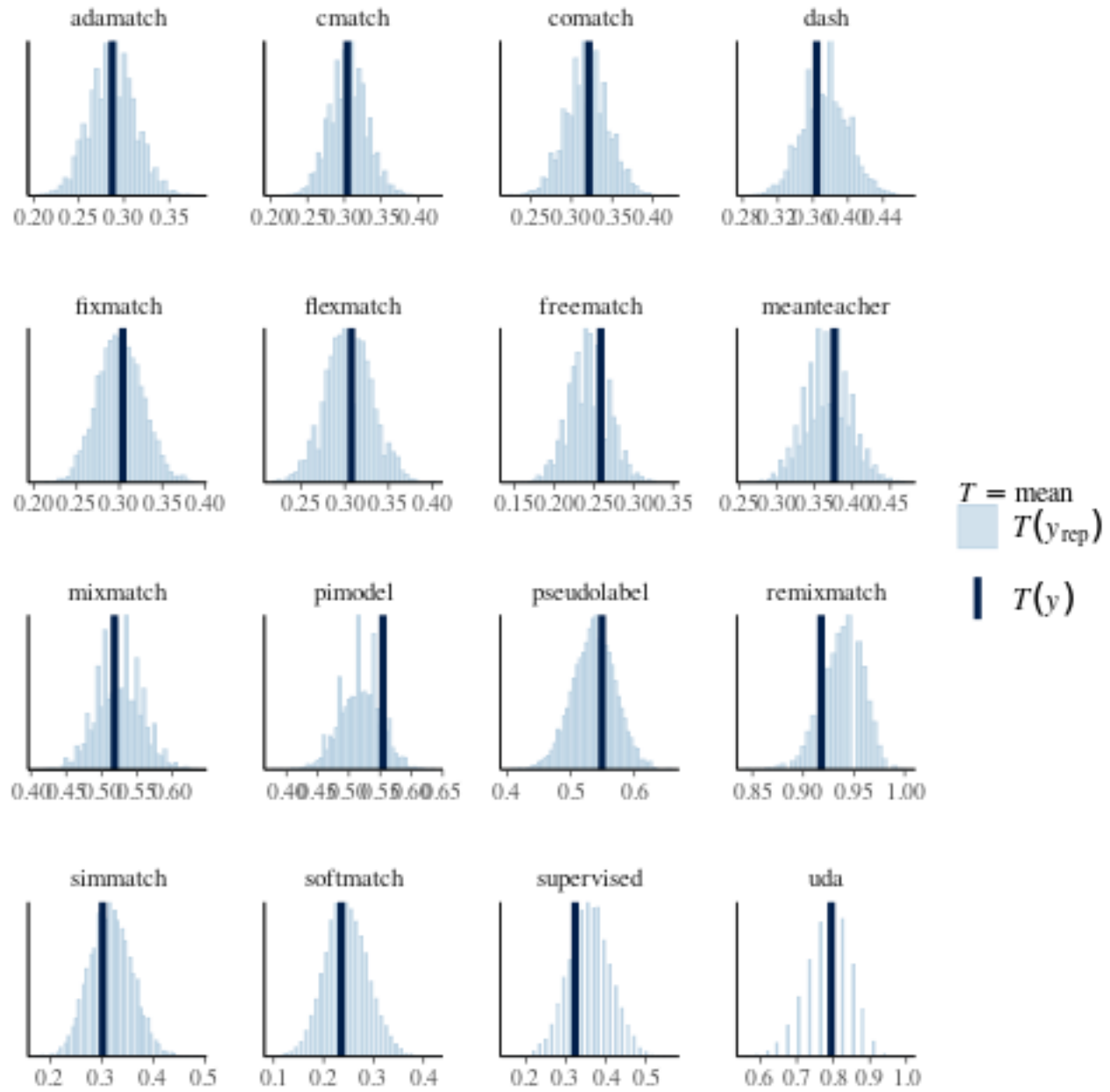


FIGURE 15. Posterior predictive check of the ranks for each algorithm (text datatype)

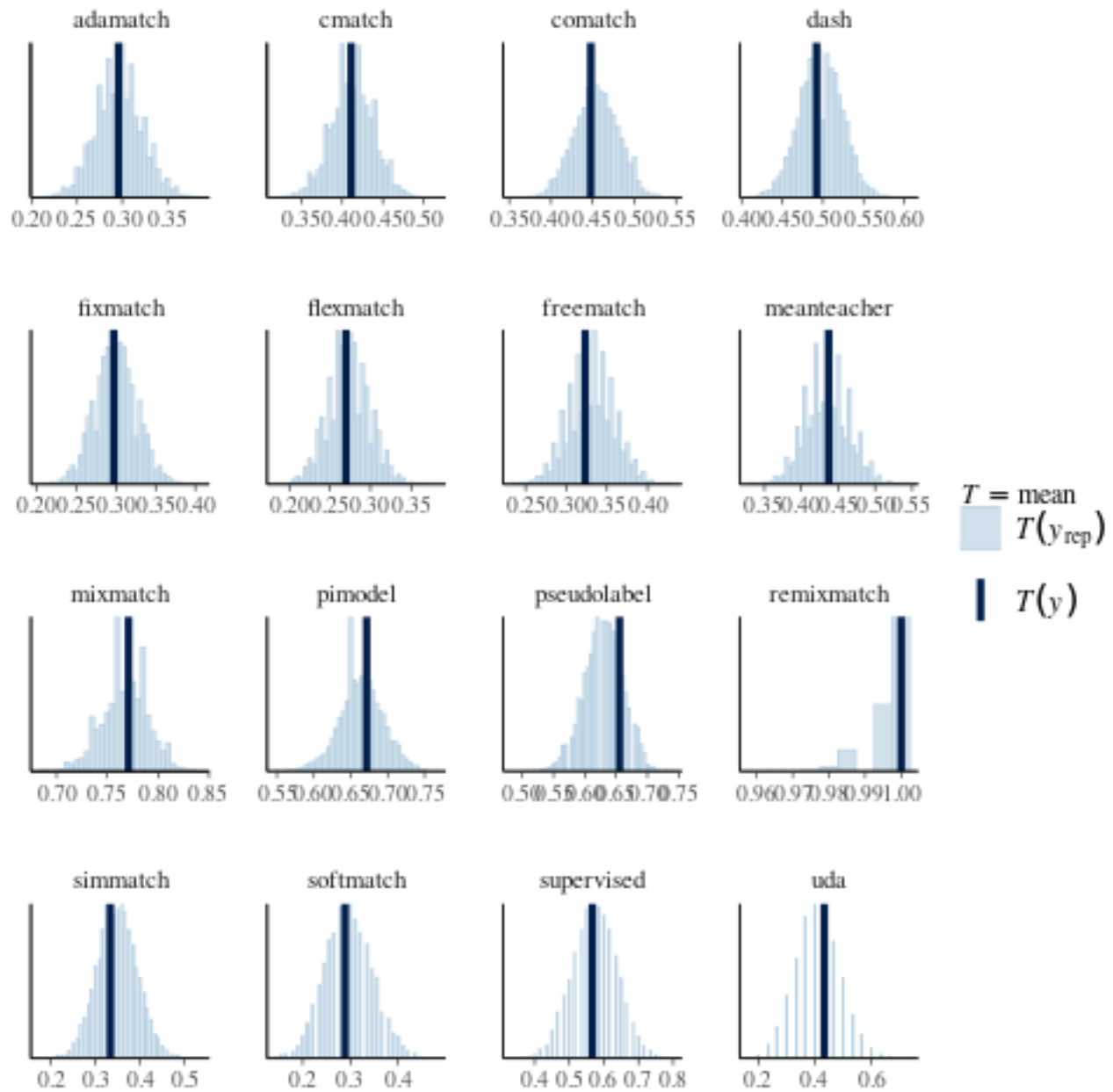


FIGURE 16. Posterior predictive check of the ranks for each algorithm (audio datatype)

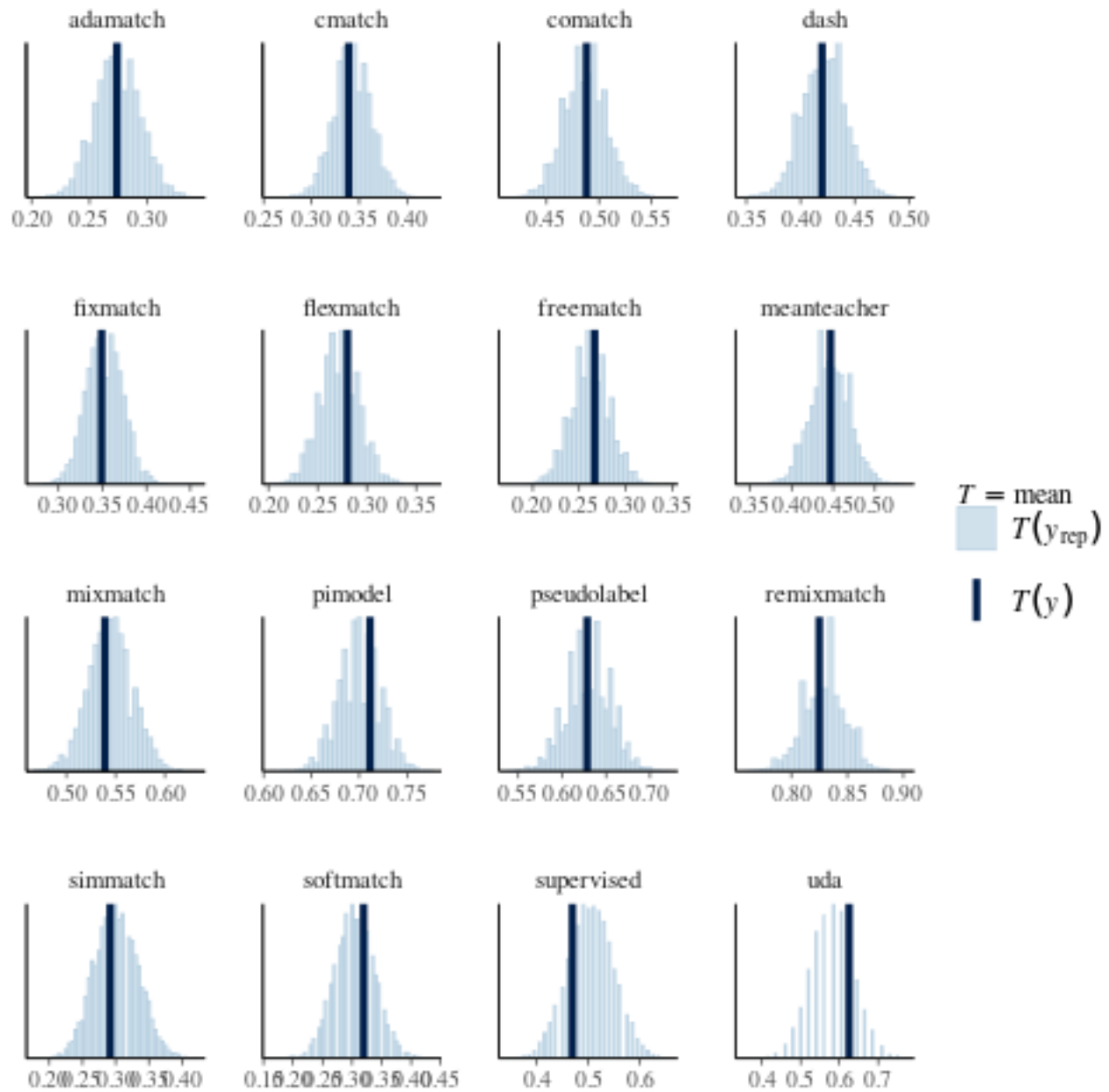


FIGURE 17. Posterior predictive check of the ranks for each algorithm (small allocation)

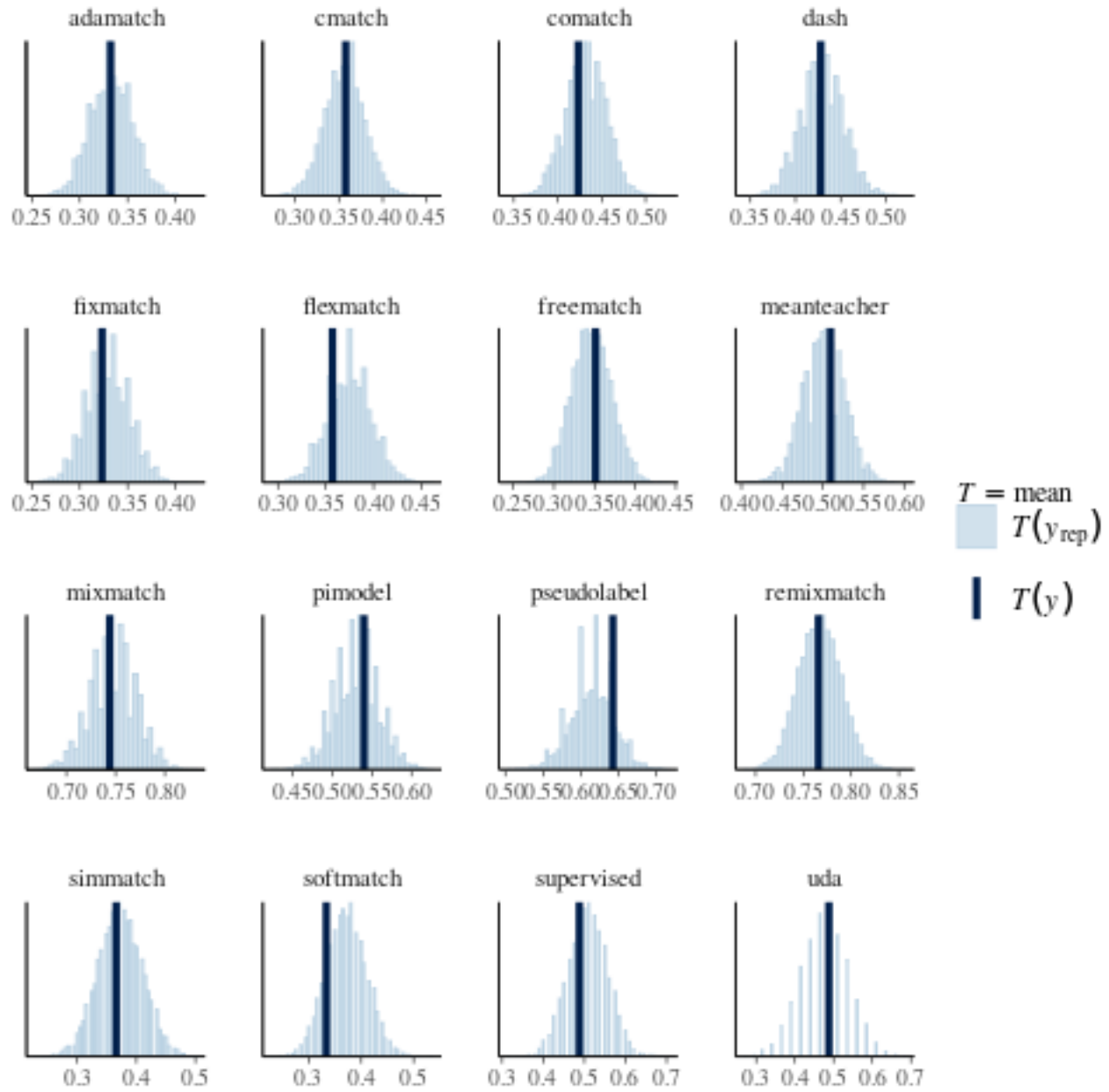


FIGURE 18. Posterior predictive check of the ranks for each algorithm (large allocation)

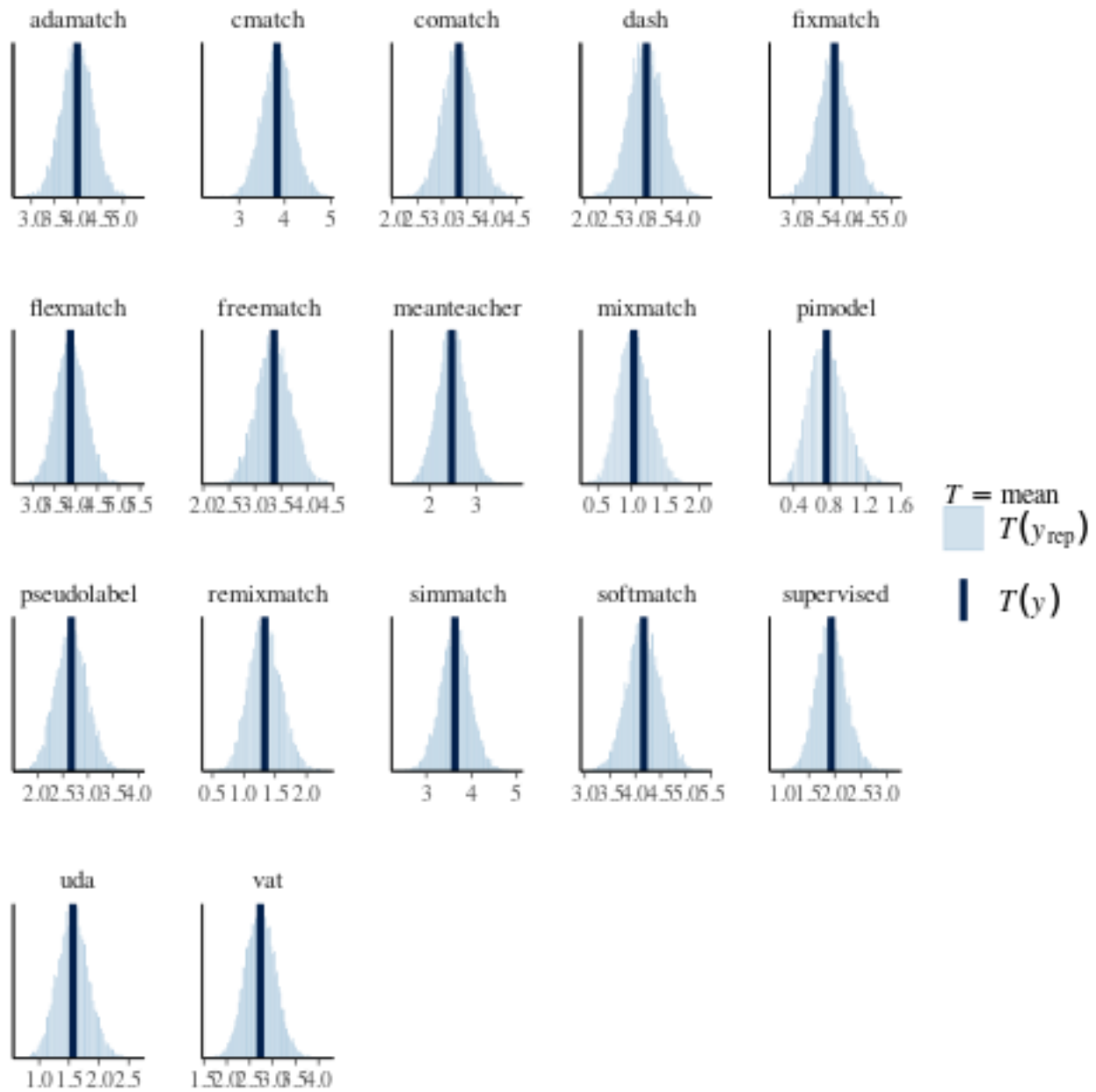


FIGURE 19. Posterior predictive check of the effects for each algorithm (aggregated)

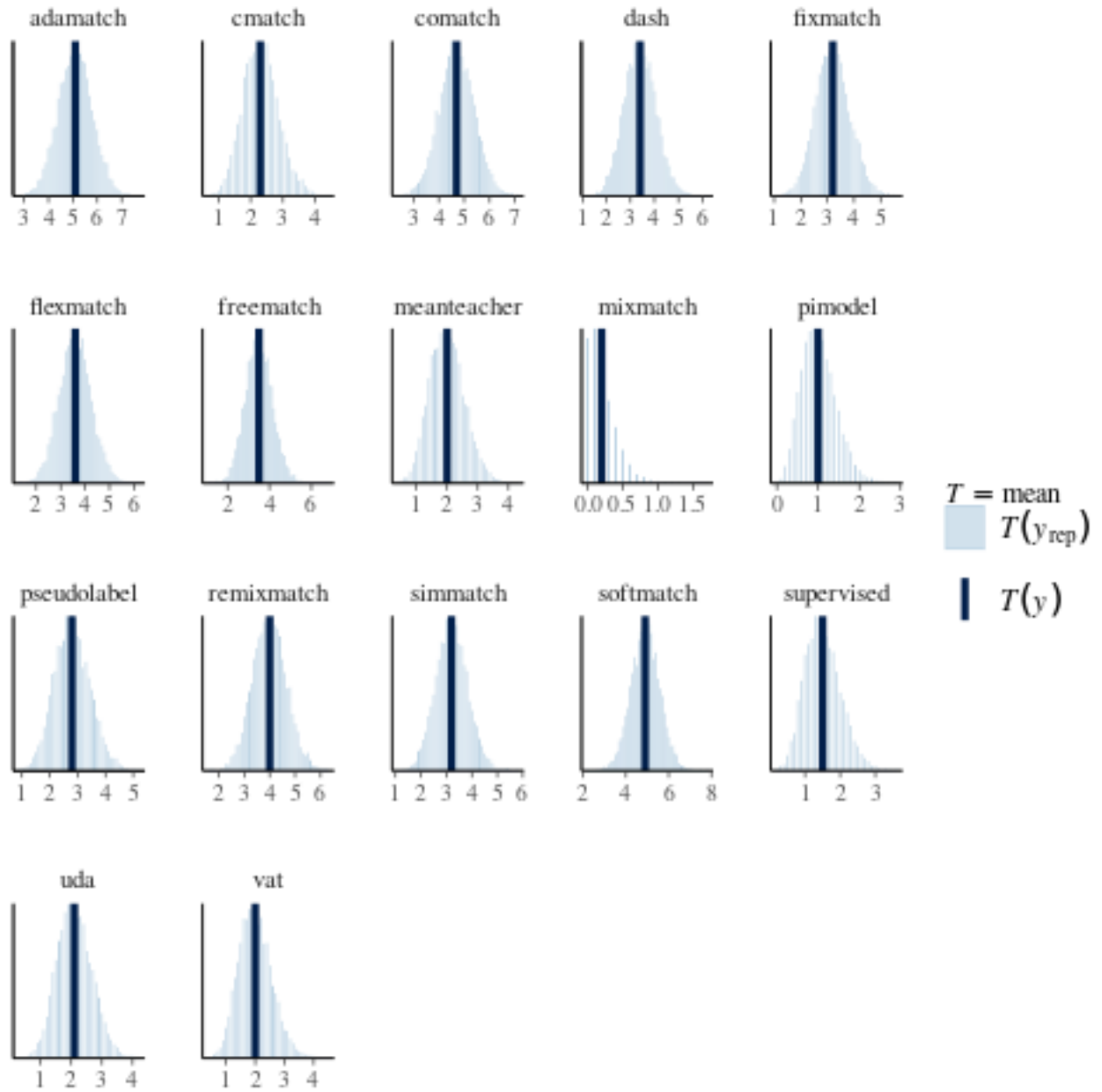


FIGURE 20. Posterior predictive check of the effects for each algorithm (image datatype)

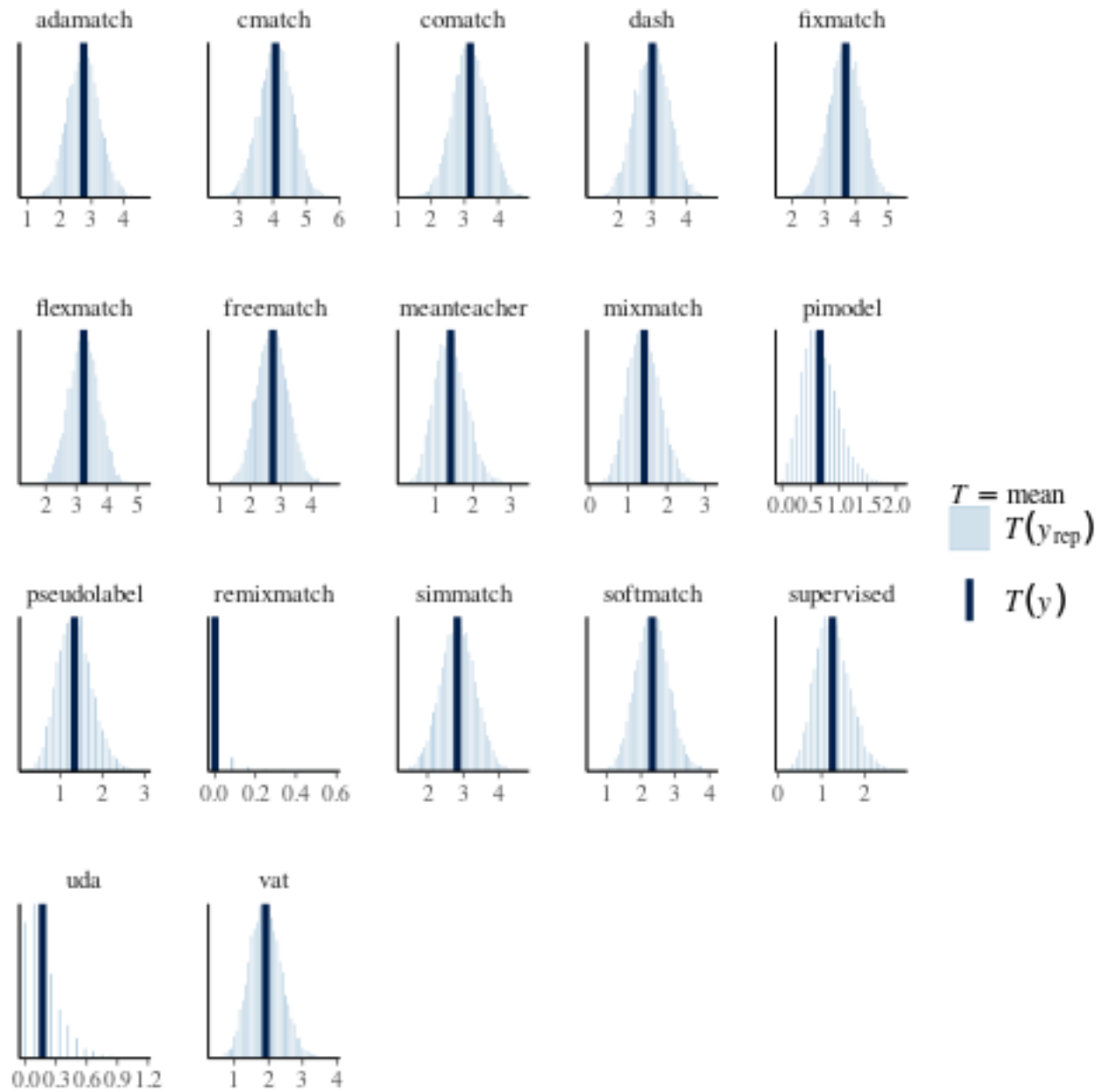


FIGURE 21. Posterior predictive check of the effects for each algorithm (text datatype)

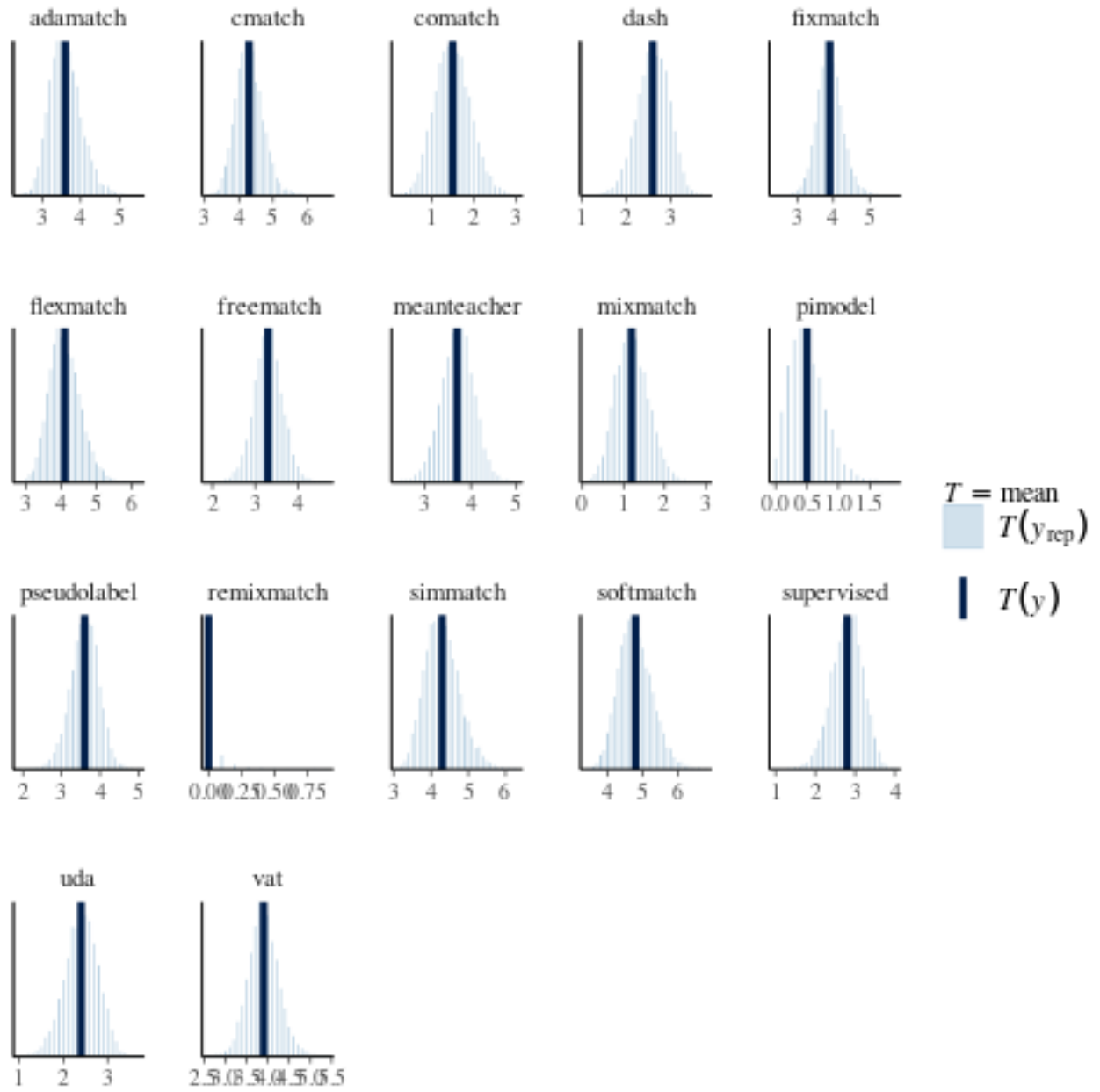


FIGURE 22. Posterior predictive check of the effects for each algorithm (audio datatype)

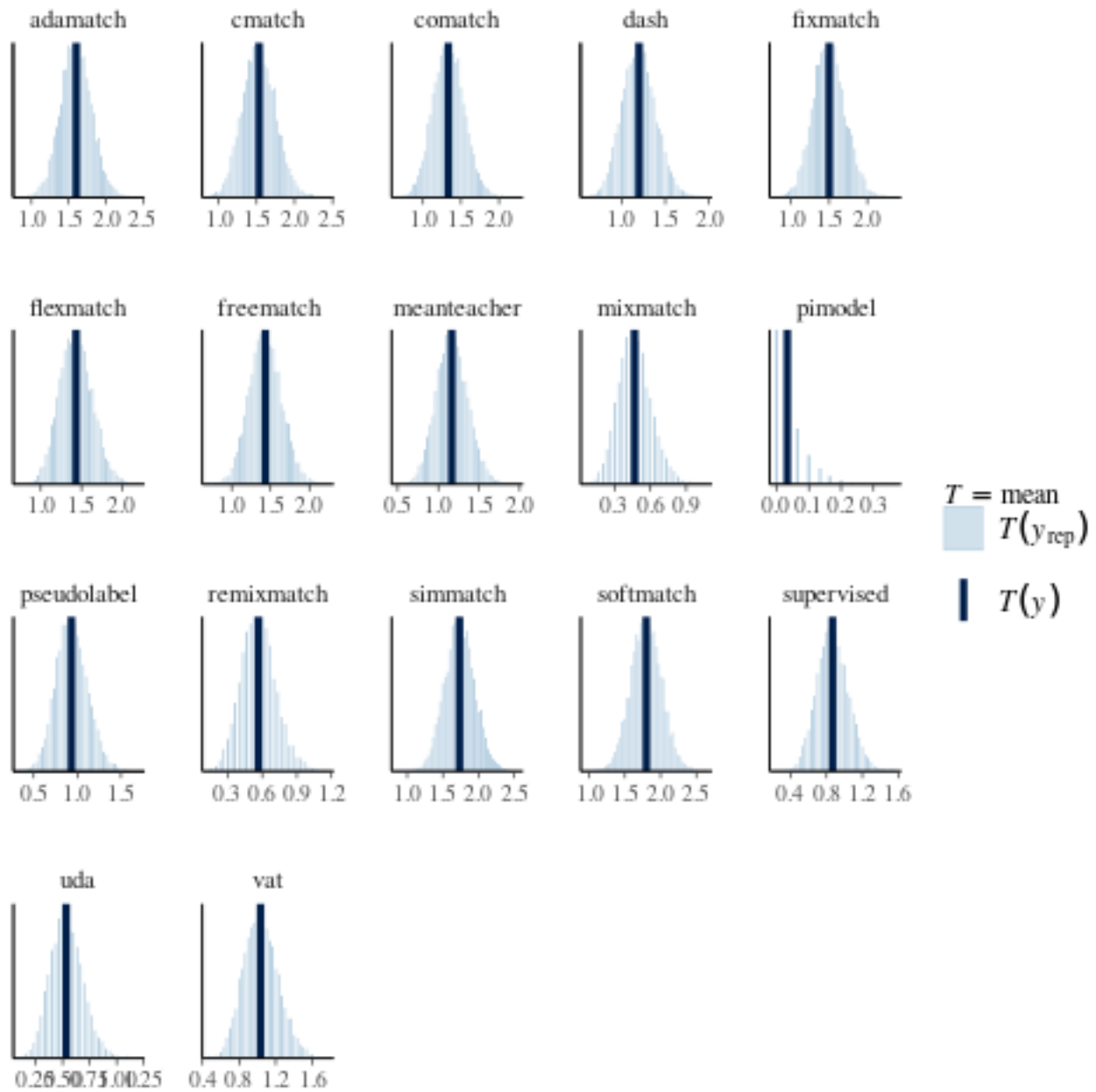


FIGURE 23. Posterior predictive check of the effects for each algorithm (small allocation)

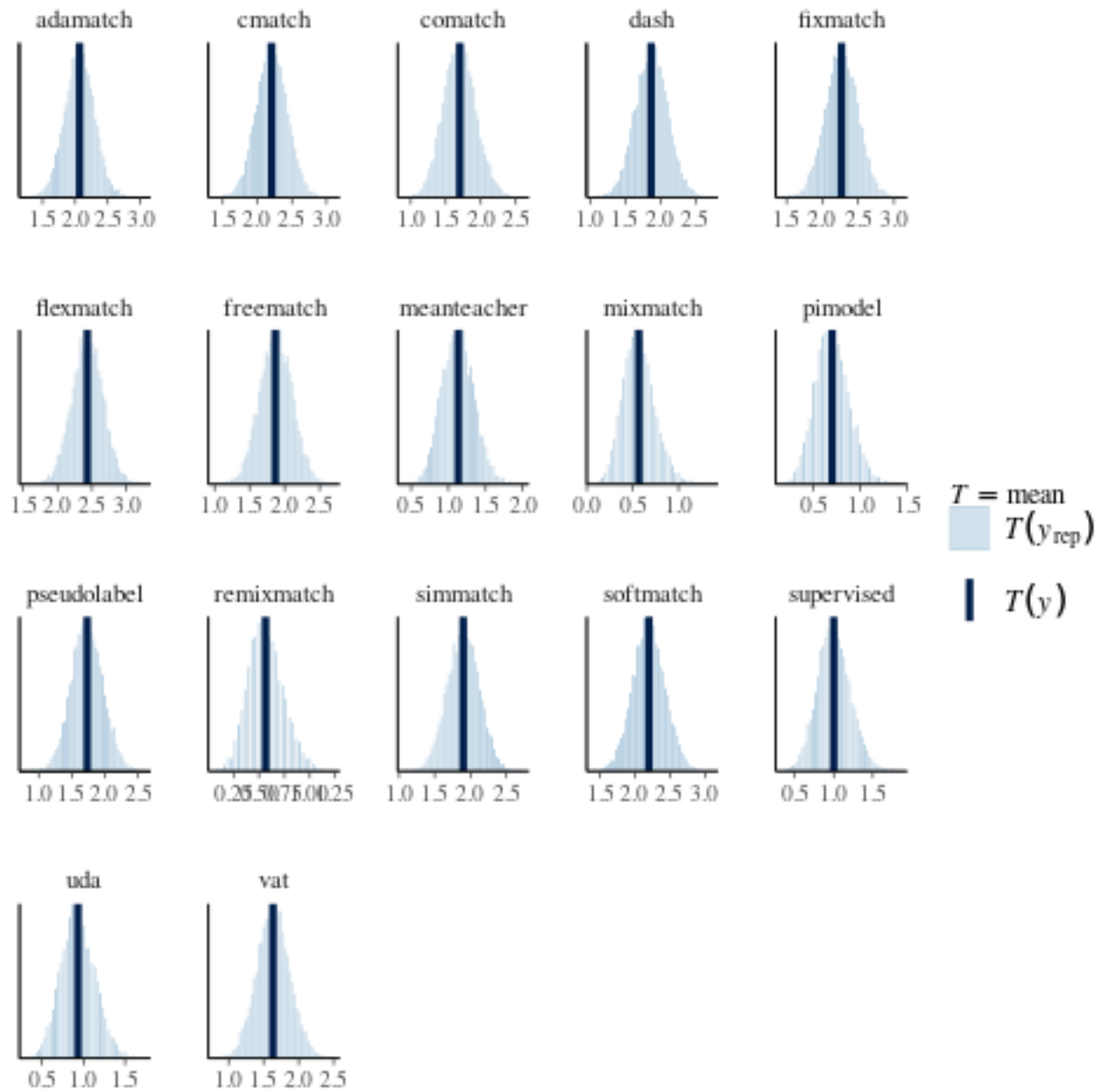


FIGURE 24. Posterior predictive check of the effects for each algorithm (large allocation)

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- [4] Richard McElreath. *Statistical rethinking: A Bayesian course with examples in R and Stan*. CRC press, 2020.