

# SEC I1013 DISCRETE STRUCTURE

## Assignment 1

### Group members:

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$$1. A = \{-3, 2\}$$

$$B = \{-3, 1, 2, 4\}$$

$$C = \{2, 3, 4\}$$

$$(a) A' = \{x \in \mathbb{Z} \mid x \neq -3, x \neq 2\}$$

$$(b) B - A = B \cap A'$$

$$= \{1, 4\}$$

$$(B - A) \cap C = \{4\}$$

$$(c) B \cap C = \{2, 4\}$$

$$P(B \cap C) = \{\emptyset, \{2\}, \{4\}, \{2, 4\}\}$$

$$|P(B \cap C)| = 4$$

$$2. ((P \cup Q) \cap R)' \cup Q' \text{ is}$$

$$= ((P \cup Q) \cap R)'' \cap Q'' \quad (\text{De Morgan's Law})$$

$$= ((P \cup Q) \cap R) \cap Q \quad (\text{Double complement laws})$$

$$= ((P \cup Q) \cap Q) \cap R \quad (\text{Associative laws})$$

$$= Q \cap R \quad (\text{Absorption laws})$$

$$= \text{RHS} \quad (\text{Shown})$$

3. Let  $A$  = Students in the art class  
 $S$  = Students in the science class

(a)  $|A \cap S| = 12$

$$\begin{aligned}|A \cup S| &= |A| + |S| - |A \cap S| \\&= 35 + 57 - 12 \\&= 80\end{aligned}$$

$\therefore$  There are 80 students who are either in art class or in science class.

- (b) Two classes meet at same hour,  $|A \cap S| = 0$

$$\begin{aligned}|A \cup S| &= |A| + |S| - |A \cap S| \\&= 35 + 57 - 0 \\&= 92\end{aligned}$$

$\therefore$  There are 92 students who are either in art class or in science class.

4. (a) Let  $p$  = You try hard.

$q$  = You have a talent

$r$  = You will get rich

Ans:  $(p \wedge q) \rightarrow r$

- (b) Statement was a lie even try hard :  $(p \wedge q) \rightarrow r$  is false.

In order to get a false statement,  $(p \wedge q)$  must be true,  $r$  must be false.

$p \wedge q$	$r$	$(p \wedge q) \rightarrow r$
T	F	F

$\because p \wedge q$  is true,  
 $\therefore p$  is true  $\Rightarrow$  You try hard  
 $q$  is true  $\Rightarrow$  You have a talent  
 $r$  is false  $\Rightarrow$  You did not get rich.

$\therefore$  Conclusion: ~~If~~ You did not get rich, statement

4.(c) You are rich :  $r$  is true

You do not try hard or have talent :  $(\neg p \vee \neg q)$  is true

$\therefore (p \wedge q)$  is false because either  $p$  or  $q$  is false.

$r$  is true.

$p \wedge q$	$r$	$(p \wedge q) \rightarrow r$
F	T	T

$\therefore$  The Statement is true.

5.

A:

$p$	$q$	$r$	$r \rightarrow p$	$q \wedge (r \rightarrow p)$	$p \vee (q \wedge (r \rightarrow p))$	$\neg(p \vee (q \wedge (r \rightarrow p)))$
T	T	T	T	T	T	F
T	T	F	T	T	T	F
T	F	T	T	F	T	F
T	F	F	T	F	T	F
F	T	T	F	F	F	T
F	T	F	T	T	T	F
F	F	T	F	F	F	T
F	F	F	T	F	F	T

B:

$p$	$q$	$r$	$\neg p$	$q \rightarrow r$	$\neg p \wedge (q \rightarrow r)$
T	T	T	F	T	F
T	T	F	F	F	F
T	F	T	F	T	F
T	F	F	F	T	F
F	T	T	T	T	T
F	T	F	T	F	F
F	F	T	T	T	T
F	F	F	T	T	T

$$\therefore \neg(p \vee (q \wedge (r \rightarrow p))) \equiv \neg p \wedge (q \rightarrow r) \quad \therefore A \equiv B$$

6. Let

$$x = 2m+1 \text{ for some integer } m$$

$$y = 2n \text{ for some integer } n$$

$$x^2 - 2y = (2m+1)^2 - 2(2n)$$

$$= 4m^2 + 4m + 1 - 4n$$

$$= 2(2m^2 + 2m - 2n) + 1$$

$$= 2k + 1$$

∴ Since  $(2m^2 + 2m - 2n)$  is an integer, so  $x^2 - 2y = 2k + 1$ , which is an representation of odd number.

∴  $x^2 - 2y$  is odd integer.