

Ex 1

$$f(-2) = -3, f(-1) = -3$$

(a) Not one-to-one, because exist of $(-2, -3)$ and $(-1, -3)$.

- Onto Y. ~~As~~ The range of f is Y.

- Not bijection. The function is not one-to-one function.

- f is function as every element of X appears exactly once on ~~in~~ domain of f.

(b) f is not a function as domain of f, $\{-2, 1, 2\}$ does not equal to X.

(c) f is not a function ~~as~~ from X to Y as $(-3, -1)$ and $(-3, 0)$ but $-1 \neq 0$

Ex 2

(a) $f(x) = 4x + 2, x \in \mathbb{R}$

$$y = 4x + 2$$

$$x = \frac{y-2}{4}$$

$$f^{-1}(x) = \frac{x-2}{4}, x \in \mathbb{R}$$

(b) $f(x) = 3 + \frac{1}{x}, x \in \mathbb{R}$

$$f(0) = 3 + \frac{1}{0}$$

undefined

$\therefore f^{-1}(x)$ does not exists as $f(x)$ is not a one-to-one function.

Ex 3

$$(a) f \circ f = (n^2)^2 \\ = n^4$$

$$(b) g \circ g = 2^{(2^n)}$$

$$(c) f \circ g = (2^n)^2 \\ = 2^{2n}$$

$$(d) g \circ f = 2^{n^2}$$