

1.

a.) all correct

b.) D.

c.) iv. (posterior must be proper)

d.) iii (point mass @ mean)

e.)  $\theta | x_1, \dots, x_n \sim \text{Normal}(\mu, L^{-1})$

$$\mu = \frac{\lambda_0 \mu_0 + \lambda \sum_{i=1}^n x_i}{\lambda_0 + n\lambda}, \quad L = \lambda_0 + n\lambda$$

f. It is reasonable to assume the model in e in applications when the variance is known in practice. Otherwise, it would be approp. to place a prior on the variance / precision.

Ex: ht ex versus IQ score ex.

I would place a  $\text{Gamma}(a, b)$  prior on  $\lambda$  as it leads to  $(\mu, \lambda) | x_{1:n} \sim \text{Normal Gamma}$

dist<sup>n</sup>. (Another valid soln is stating that

$\lambda \sim \text{Gamma}(a, b)$  leads to a semi-conjugate update).

g.) I. + II.