مباراة الدخول 2015 – 2016

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الجامعة اللبنانية

مسابقة في الرياضيات

المدة: ساعة واحدة

I- Calculer les intégrales suivantes:

a)
$$\int_{1}^{2} \frac{x^2 + x - 2}{x - 1} dx$$

b)
$$\int \left(\frac{e^{\sqrt{x}}}{\sqrt[4]{x}} + 1 \right) dx$$

$$(10 + 15)$$
 pts

II- Résoudre le system suivant dans IR:

$$\begin{cases} 2x - e^y = 1 \\ x + e^y = 2 \end{cases}$$

(10) pts

III- Trouver A et B tels que:
$$\frac{5x-3}{x^2-2x-3} = \frac{A}{x+1} + \frac{B}{x-3}$$

(10) pts

IV- Calculer:
$$\lim_{x\to 0} \frac{\sqrt{x+1}-1-\frac{x}{2}}{x^2}$$

(15) pts

V- Considérons la fonction suivante:
$$f(x) = \frac{x^2 + 4x - 3}{x + 6}$$

(15 + 20) pts

a) Démontrer que f(x) admet deux asymptotes: x = -6 et y = x - 2.

b) Etudier les variations et tracer le graphe de cette fonction.

Bonne Chanc

1- Calculate the following integrals:

a)
$$\int_{1}^{2} \frac{x^2 + x - 2}{x - 1} dx$$

b)
$$\int \left(\frac{e^{\sqrt{x}}}{\sqrt{x}} + 1 \right) dx$$

$$(10 + 15)$$
 pts

II- Solve the following system in IR:

$$\begin{cases} 2x - e^y = 1\\ x + e^y = 2 \end{cases}$$

(10) pts

III- Find A and B such that:
$$\frac{5x-3}{x^2-2x-3} = \frac{A}{x+1} + \frac{B}{x-3}$$

(10) pts

IV- Calculate:
$$\lim_{x \to 0} \frac{\sqrt{x+1} - 1 - \frac{x}{2}}{x^2}$$

(15) pts

V Consider the following function:
$$f(x) = \frac{x^2 + 4x - 3}{x + 6}$$

(15 + 20) pts

a) Prove that f(x) admits two asymptotes: x = -6 and y = x - 2.

b) Study the variations and draw the corresponding graph.

Coodi