

- إن هذا النموذج أعد بشكل تطوعي من المؤلف دون أي مقابل بهدف تأمين مادة هدفها تدريبي فقط.
- حقوق التأليف محفوظة للمؤلف ويستطيع الزملاء الأعزاء والأحباء التلامذة الاستفادة منه فنيا وتعليميا بأي طريقة ممكنة مع حفظ الحقوق تقديرا للجهد المبذول في التأليف .
- يمنع منعاً باتاً مقارنة هذا النموذج بشكل مادي بأي طريقة من الطرق فهو نموذج مجاني بالمطلق وهدفه الخدمة العامة فقط.
- لا توجد صفة رسمية لمضمون النموذج فهو اجتهاد شخصي للمؤلف ولا علاقة له بأي شكل من الأشكال بأي لجان رسمية وغيرها، ومستوى النموذج مستقل كلياً عن مستوى الإمتحان الرسمي المفترض ، فهدف النموذج تدريبي محض.

- This exam includes five problems on four pages.
- The use of a non-programmable calculator is allowed.
- Always show the steps of the calculation.
- Any unjustified answers will not be graded.

I- (2 points)

In the table below, only one of the proposed answers is correct.

Choose the correct answer and justify your choice.

N°	Question	Proposed responses		
		A	B	C
1)	The value of the limit $\lim_{x \rightarrow +\infty} \frac{e^x + 1}{xe^x + 2x}$ is	$+\infty$	1	0
2)	The imaginary part of the complex number z such that $\left \frac{z-2i}{z+i} \right = 1$ is	$\frac{1}{2}$	$-\frac{3}{2}$	0
3)	The solution set of the inequality $\ln(e^{2x} - 2e^x + 1) \leq 0$ is $S =$	$]0 ; \ln 2]$	$] -\infty ; \ln 2]$	$[\ln 2 ; +\infty[$
4)	Let A and B be two events of a sample space Ω and P a probability. Given $P(A) = 0.3$, $P(B) = 0.5$ and $P(A \cup B) = 0.65$. Then $P(A/B) =$	0.8	0.3	0.5

II- (3½ points)

The complex plane is referred to an orthonormal system $(O ; \vec{u} ; \vec{v})$.

Consider the points A and B with respective affixes $z_A = i$ and $z_B = 1$.

For every point M of affix z we associate the point M' of affix z' such that: $z' = \frac{i\bar{z}-1}{\bar{z}-1}$ with $z \neq 1$.

- 1) In case where $z' = -1$ prove that z^{12} is a negative real number.
- 2) a) Show that for every point M distinct from B we have: $|z'| = \frac{AM}{BM}$.
b) Deduct the set of points M' when M describes the perpendicular bisector of $[AB]$.
- 3) a) Show that $\arg(z') = \frac{\pi}{2} + (\overrightarrow{AM} ; \overrightarrow{BM})[2\pi]$.
b) Determine the set of points M when z' is a strictly negative real number.
- 4) In this part suppose that $z = 1 + \sqrt{2}e^{i\theta}$ where θ is a real number.
a) Show that M describes the circle (\mathcal{C}) of center B and radius $\sqrt{2}$.
b) Calculate $(z' - i)(\bar{z} - 1)$.
c) Deduct the set of points M' when M describes the circle (\mathcal{C}) .

III- (3½ points)

Consider two urns:

- The urn U_1 containing three balls carrying the numbers 2, 2, and 3;
- The urn U_2 containing 9 balls of which 4 are green and each carrying the number 3, and 5 balls are red carrying the numbers 1, 2, 2, 3 and 4.

We draw a ball from the urn U_1 and we note n the number carried by this ball:

- If $n = 2$, two balls are drawn at random and successively without replacement from the urn U_2 ;
- If $n = 3$, three balls are drawn at random and simultaneously from the urn U_2 .

Consider the events:

E : "The ball drawn from the urn U_1 carries the number 2";

F : "The ball drawn from the urn U_1 carries the number 3";

A : "The balls drawn from the urn U_2 have the same color";

B : "The balls drawn from the urn U_2 carry the same number".

- 1) a) Calculate the probabilities $P(E)$ and $P(F)$.
b) Calculate $P(A/E)$, and justify that $P(A \cap E) = \frac{8}{27}$.
c) Calculate $P(A \cap F)$ and deduce that $P(A) = \frac{19}{54}$.
d) The balls drawn from the urn U_2 are of different colors, calculate the probability that the ball drawn from U_1 carries the number 3.
- 2) Calculate $P(B)$.
- 3) Justify that $P(A \cap B) = \frac{55}{378}$. Are the events A and B independent? Justify.
- 4) Calculate the probability of the event C : "Among the balls drawn from the urn U_2 there is exactly one red ball".

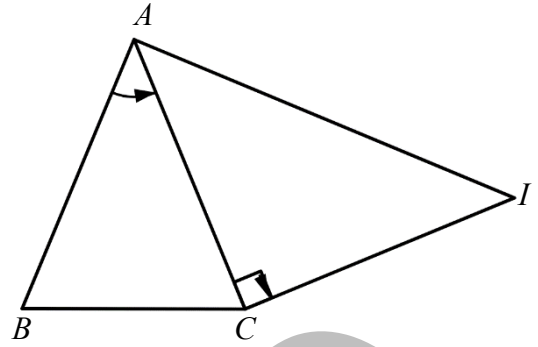
IV- (3½ points)

ABC is an isosceles triangle such that $AB = AC$ and

$$(\overrightarrow{AB}; \overrightarrow{AC}) = \frac{\pi}{4}(2\pi).$$

I is the point such that the triangle CAI is isosceles and

$$\text{right with } (\overrightarrow{CA}; \overrightarrow{CI}) = -\frac{\pi}{2}(2\pi).$$



- 1) Let R_A be the rotation of center A which transforms B into C and R_C the rotation of center C and angle $-\frac{\pi}{2}$.

$$\text{Let } f = R_C \circ R_A.$$

- Determine $f(A)$ and $f(B)$.
 - Prove that f is a rotation whose center O and angle to be specified.
 - What is the nature of the quadrilateral $ABOC$? Justify.
- 2) Let S be the direct plane similitude of center O which transforms A into B . Let H be the midpoint of $[BC]$, $C' = S(C)$ and $H' = S(H)$.
- Give a measure of the angle of S and show that C' belongs to the straight line (OA) .
 - Give $S([OA])$ and show that H' is the midpoint of $[OB]$.
 - Show that $(C'H') \perp (OB)$. Deduce that C' is the center of the circle circumscribed about the triangle OBC .
- 3) Consider the transformation $S_n = \underbrace{S \circ S \circ \dots \circ S}_{n \text{ fois}}$ where n is a natural number such that $n \geq 2$.
Determine the set of values of n for which S_n is a negative dilation.

V- (7½ points)

Part A

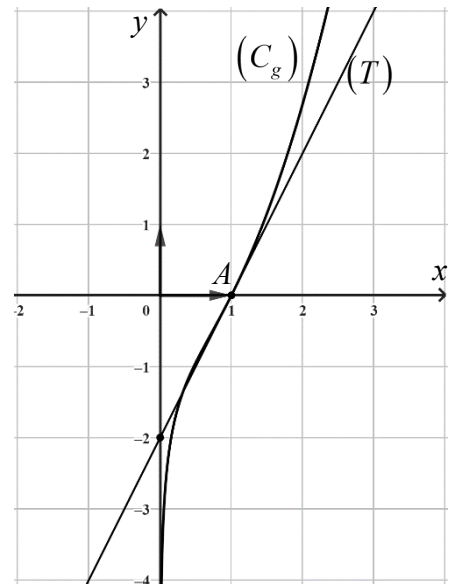
Let g be the function defined over $]0; +\infty[$ by

$$g(x) = ax^2 + bx + \ln x, \text{ where } a \text{ and } b \text{ are two real numbers.}$$

The opposite curve (C_g) is the representative curve of g in an orthonormal system.

The straight line (T) is tangent to (C_g) at the point $A(1; 0)$.

- By graphical reading:
 - Determine $g(1)$ and $g'(1)$.
 - Determine the sign of $g(x)$ over $]0; +\infty[$.
- Show that $a = 1$ and $b = -1$.
- Is the point A an inflection point for the curve (C_g) ? Justify.



Part B

Let f be the function defined over $]0; +\infty[$ by $f(x) = (x-1)^2 + (\ln x)^2$.

Denote by (C_f) the representative curve of f in an orthonormal system $(O; \vec{i}; \vec{j})$.

- Calculate $\lim_{x \rightarrow 0^+} f(x)$ and $\lim_{x \rightarrow +\infty} f(x)$.

- 2) a) Show that for every $x \in]0 ; +\infty[$, $f'(x) = 2 \frac{g(x)}{x}$.
- b) Set up the table of variations of the function f .
- 3) Let u be the function defined over $]0 ; 1]$ by $u(x) = f(x) - x$.
- a) Set up the table of variation of u over $]0 ; 1]$. Deduce that there exists a unique real number α in $]0 ; 1]$ such that $f(\alpha) = \alpha$ and that $\frac{1}{2} < \alpha < 1$.
- b) Show that (C_f) admits at $+\infty$ a parabolic branch of direction $(O ; \vec{j})$.
- 4) Draw the straight line (d) of equation $y = x$ and the curve (C_f) .
- 5) Let h be the function defined by $h(x) = e^{f(x)}$.
- a) Determine the domain of definition of h .
- b) Set up the table of variations of h .
- c) Solve in the interval $]0 ; 1]$ the equation $h(x) = e^x$.

QI	Answers	2 pts
1)	$\lim_{x \rightarrow +\infty} \frac{e^x + 1}{xe^x + 2x} = \lim_{x \rightarrow +\infty} \frac{e^x \left(1 + \frac{1}{e^x}\right)}{e^x \left(x + \frac{2x}{e^x}\right)} = \frac{1+0}{+\infty+0} = 0$ OR we apply the Hospital's rule. The correct answer is C.	$\frac{1}{2}$
2)	Let $z = x + iy$ ($x \in \mathbb{R}, y \in \mathbb{R}$) ; $\left \frac{z-2i}{z+i} \right = 1$; $\left \frac{x+i(y-2)}{x+i(y+1)} \right = 1$ ($x \neq 0$ and $y \neq -1$) ; $\frac{\sqrt{x^2 + (y-2)^2}}{\sqrt{x^2 + (y+1)^2}} = 1$; $(y-2)^2 = (y+1)^2$; $-6y = -3$; $y = \frac{1}{2}$. The correct answer is A.	$\frac{1}{2}$
3)	Condition of existence: $e^{2x} - 2e^x + 1 > 0$; $(e^x - 1) > 0$, then $x \in]-\infty ; 0[\cup]0 ; +\infty[$; $\ln(e^{2x} - 2e^x + 1) \leq 0$ is equivalent to $\ln(e^{2x} - 2e^x + 1) \leq \ln 1$, $e^{2x} - 2e^x + 1 \leq 1$, $e^{2x} - 2e^x \leq 0$ so $x \in [\ln 2 ; +\infty[$. The solution set is therefore: $S = (]-\infty ; 0[\cup]0 ; +\infty[) \cap ([\ln 2 ; +\infty[) = [\ln 2 ; +\infty[$. The correct answer is C.	$\frac{1}{2}$
4)	$P(A \cup B) = P(A) + P(B) - P(A \cap B)$; $0.65 = 0.3 + 0.5 - P(A \cap B)$; $P(A \cap B) = 0.15$; $P(A/B) = \frac{P(A \cap B)}{P(B)} = \frac{0.15}{0.5} = 0.3$. The correct answer is B.	$\frac{1}{2}$

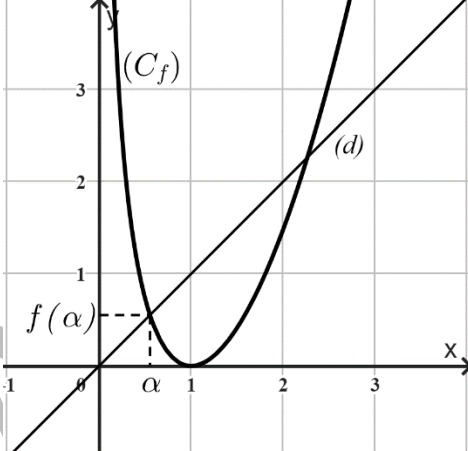
QII	Answers	3½ pts
1)	$z' = -1$; $\frac{i\bar{z}-1}{\bar{z}-1} = -1$ and $z \neq 1$; $i\bar{z}-1 = -\bar{z}+1$; $\bar{z}(i+1) = 2$; $\bar{z} = \frac{2}{1+i} = 1-i$ then $z = 1+i$; $z^{12} = (1+i)^{12} = \left(\sqrt{2}e^{i\frac{\pi}{4}}\right)^{12} = (\sqrt{2})^{12} e^{3i\pi} = -64$ which is a negative real number.	$\frac{1}{2}$
2) a)	$z' = \frac{i(\bar{z}+i)}{\bar{z}-1} = \frac{i(\overline{z-i})}{\bar{z}-1}$ therefore $ z' = \frac{ i \overline{z-i} }{ \bar{z}-1 } = \frac{ z-i }{ z-1 } = \frac{ z_M - z_A }{ z_M - z_B } = \frac{ z_{\overline{AM}} }{ z_{\overline{BM}} } = \frac{AM}{BM}$.	$\frac{1}{2}$
2) b)	M describes the perpendicular bisector of the segment $[AB]$ so $MA = MB$, therefore $ z' = \frac{AM}{BM} = 1$, then $OM' = 1$; The set of points M' is the circle of center O and radius 1.	$\frac{1}{4}$
3) a)	$z' = \frac{i(\overline{z-i})}{\bar{z}-1}$; $\arg(z') = \arg\left[\frac{i(\overline{z-i})}{\bar{z}-1}\right]$; $\arg(z') = \arg(i) + \arg(\overline{z-i}) - \arg(\bar{z}-1)$; $\arg(z') = \frac{\pi}{2} - \arg(z-i) + \arg(z-1)$; $\arg(z') = \frac{\pi}{2} - \arg(z_{\overline{AM}}) + \arg(z_{\overline{BM}})$; $\arg(z') = \frac{\pi}{2} - (\vec{u} ; \overline{AM}) + (\vec{u} ; \overline{BM})$; $\arg(z') = \frac{\pi}{2} + (\overline{AM} ; \overline{BM})[2\pi]$.	$\frac{1}{2}$

3) b)	z' is a strictly negative real number so $\arg(z') = \pi[2\pi]$, therefore, $\frac{\pi}{2} + (\overrightarrow{AM}; \overrightarrow{BM}) = \pi[2\pi]$, $(\overrightarrow{AM}; \overrightarrow{BM}) = \frac{\pi}{2}[2\pi]$, so the set of points M is the circle of diameter $[AB]$ deprived of A and B .	$\frac{1}{2}$
4) a)	$z-1 = \sqrt{2}e^{i\theta}$, $ z-1 = \sqrt{2}e^{i\theta} $, $ z-1 = \sqrt{2}$, $BM = \sqrt{2}$, so M describes the circle (\mathcal{C}) of center B and radius $\sqrt{2}$.	$\frac{1}{4}$
4) b)	$(z'-i)(\bar{z}-1) = \left(\frac{i\bar{z}-1}{\bar{z}-1} - i\right)(\bar{z}-1) = i\bar{z}-1-i\bar{z}+i = -1+i (z \neq 1)$.	$\frac{1}{2}$
4) c)	$ (z'-i)(\bar{z}-1) = -1+i $; $ z'-i \bar{z}-1 = \sqrt{2}$; $ z'-i z-1 = \sqrt{2}$; $AM' \times BM = \sqrt{2}$; M describes the circle (\mathcal{C}) so $BM = \sqrt{2}$, so $AM' = 1$ then the set of points M' is the circle of center A and radius 1.	$\frac{1}{2}$

QIII	Answers	3½ pts
1) a)	$P(E) = \frac{2}{3}$; $P(F) = \frac{1}{3}$.	$\frac{1}{2}$
1) b)	$P(A/E) = \frac{A_4^2 + A_5^2}{A_9^2} = \frac{4}{9}$; $P(A \cap E) = P(A/E) \times P(E) = \frac{4}{9} \times \frac{2}{3} = \frac{8}{27}$.	$\frac{1}{2}$
1) c)	$P(A \cap F) = P(A/F) \times P(F) = \frac{C_4^3 + C_5^3}{C_9^3} \times \frac{1}{3} = \frac{1}{6} \times \frac{1}{3} = \frac{1}{18}$; Using the formula of total probabilities: $P(A) = P(A \cap E) + P(A \cap F) = \frac{8}{27} + \frac{1}{18} = \frac{19}{54}$.	$\frac{1}{2}$
1) d)	$P(F/\bar{A}) = \frac{P(F \cap \bar{A})}{P(\bar{A})} = \frac{P(\bar{A}/F) \times P(F)}{1 - P(A)}$; $P(\bar{A}/F) = 1 - P(A/F) = 1 - \frac{1}{6} = \frac{5}{6}$; $P(F/\bar{A}) = \frac{\frac{5}{6} \times \frac{1}{3}}{1 - \frac{19}{54}} = \frac{3}{7}$.	$\frac{1}{2}$
2)	$P(B) = P(B \cap E) + P(B \cap F) = P(B/E) \times P(E) + P(B/F) \times P(F)$; $P(B) = \frac{A_5^2 + A_2^2}{A_9^2} \times \frac{2}{3} + \frac{C_5^3}{C_9^3} \times \frac{1}{3} = \frac{46}{189}$.	$\frac{1}{2}$
3)	$P(A \cap B) = P(\text{the balls drawn from the urn } U_2 \text{ have the same color and carry the same number}) = \frac{A_4^2 + A_2^2}{A_9^2} \times \frac{2}{3} + \frac{C_4^3}{C_9^3} \times \frac{1}{3} = \frac{55}{378}$; $P(A) \times P(B) = \frac{19}{54} \times \frac{46}{189} = \frac{437}{5103}$, so $P(A \cap B) \neq P(A) \times P(B)$, so the events A and B are not independent.	$\frac{1}{2}$
4)	$P(C) = P(C \cap E) + P(C \cap F) = P(C/E) \times P(E) + P(C/F) \times P(F)$; $P(C) = \frac{A_5^1 \times A_4^1}{A_9^2} \times \frac{2}{3} + \frac{C_5^1 \times C_4^2}{C_9^3} \times \frac{1}{3} = \frac{185}{378}$.	$\frac{1}{2}$

QIV	Answers	3½ pts
1) a)	<ul style="list-style-type: none"> $f(A) = R_C \circ R_A(A) = R_C[R_A(A)] = R_C(A) = I$ since: $R_A(A) = A$ since A is the center of R_A; $R_C(A) = I$ since $CA = CI$ and $(\overrightarrow{CA}; \overrightarrow{CI}) = -\frac{\pi}{2}(2\pi)$. $f(B) = R_C \circ R_A(B) = R_C[R_A(B)] = R_C(C) = C$ since: $R_A(B) = C$ by the definition of R_A; $R_C(C) = C$ since C is the center of R_A. 	½
1) b)	<p>Let $\alpha_1 = \frac{\pi}{4}$ and $\alpha_2 = -\frac{\pi}{2}$ be the angles of R_A and R_C respectively;</p> <p>$f = R_C \circ R_A$ is a rotation of angle $\alpha_1 + \alpha_2 = \frac{\pi}{4} - \frac{\pi}{2} = -\frac{\pi}{4}$ and center O:</p> <p>$f(A) = I$ then $OA = OI$ then O belongs to the perpendicular bisector of $[AI]$;</p> <p>$f(B) = C$ then $OB = OC$ then O belongs to the perpendicular bisector of $[BC]$;</p> <p>So O is the point of intersection of the perpendicular bisectors of $[AI]$ and $[BC]$.</p>	½
1) c)	<p>$AB = AC$ and $(\overrightarrow{AB}; \overrightarrow{AC}) = \frac{\pi}{4}(2\pi)$ (given);</p> <p>$f(B) = C$ and $f = r\left(O; -\frac{\pi}{4}\right)$ then $OB = OC$ and $(\overrightarrow{OB}; \overrightarrow{OC}) = -\frac{\pi}{4}(2\pi)$; So, the two isosceles triangles ABC and OBC are congruent so $AB = AC = OB = OC$, then the quadrilateral $ABOC$ is a rhombus.</p>	½
2) a)	<p>Let α be a measure of the angle of S; $S(A) = B$ therefore $\alpha = (\overrightarrow{OA}; \overrightarrow{OB}) = \frac{\pi}{8}(2\pi)$.</p> <p>$S(C) = C'$ so $(\overrightarrow{OC}; \overrightarrow{OC'}) = \alpha = \frac{\pi}{8}(2\pi)$ then C' belongs to the straight line (OA) since $(\overrightarrow{OC}; \overrightarrow{OA}) = \frac{\pi}{8}(2\pi)$.</p>	½
2) b)	<p>$S(O) = O$ and $S(A) = B$ therefore $S([OA]) = [OB]$;</p> <p>H is the midpoint of $[OA]$ so $S(H)$ is the midpoint of $S([OA])$ since the similitude preserves the midpoints so H' is the midpoint of $[OB]$.</p>	½
2) c)	<p>$(CH) \perp (OH)$ so $S((CH)) \perp S((OH))$ since the similitude preserves orthogonality, but $S((CH)) = (C'H')$ and $S((OH)) = S((OA)) = (OB)$ then $(C'H') \perp (OB)$.</p> <p>In the isosceles triangle OCB, C' belongs to (OA) which is the perpendicular bisector of $[BC]$; $(C'H')$ is perpendicular to the segment $[OB]$ at its midpoint H' so $(C'H')$ is the perpendicular bisector of $[OB]$, so C' is the point of intersection of the perpendicular bisectors of the triangle OCB so C' is the center of the circle circumscribed about this triangle.</p>	½
3)	<p>The angle of S_n is $\frac{n\pi}{8}$. S_n is a negative dilation if $\frac{n\pi}{8} = \pi + 2k\pi$ with $k \in \mathbb{N}$; So $n = 8 + 16k$ with $k \in \mathbb{N}$, n is a multiple of 8 which is not a multiple of 16.</p>	½

QV	Answers	7½ pts												
A) 1) a)	By graphical reading: • $g(1)=0$ since the curve (C_g) passes through the point $A(1 ; 0)$; • $g'(1)=$ slope of $(T)=\frac{0-(-2)}{1-0}=2$.	½												
A) 1) b)	By graphical reading: $g(x)<0$ if $x\in]0 ; 1[$; $g(x)=0$ if $x=1$; $g(x)>0$ if $x\in]1 ; +\infty[$.	½												
A) 2)	$g(x)=ax^2+bx+\ln x$; $x\in]0 ; +\infty[$; $g(1)=0$, $a+b=0$; $g'(x)=2ax+b+\frac{1}{x}$ therefore $g'(1)=2$ gives $2a+b=1$; We obtain the system: $\begin{cases} a+b=0 \\ 2a+b=1 \end{cases}$, so $a=1$ and $b=-1$.	¾												
A) 3)	g is twice differentiable over $]0 ; +\infty[$; $g'(x)=2x-1+\frac{1}{x}$ and $g''(x)=2-\frac{1}{x^2}=\frac{2x^2-1}{x^2}$; Sign of $g''(x)$: <table><tr><td>x</td><td>0</td><td>$\frac{\sqrt{2}}{2}$</td><td>$+\infty$</td></tr><tr><td>$g''(x)$</td><td>■</td><td>-</td><td>0 +</td></tr></table> $g''(x)$ is equal to 0 at $x=\frac{\sqrt{2}}{2}$ and changes the sign, so (C_g) admits an inflection point of abscissa $\frac{\sqrt{2}}{2}$, so the point A is not an inflection point of (C_g) .	x	0	$\frac{\sqrt{2}}{2}$	$+\infty$	$g''(x)$	■	-	0 +	¾				
x	0	$\frac{\sqrt{2}}{2}$	$+\infty$											
$g''(x)$	■	-	0 +											
B) 1)	$\lim_{x\rightarrow 0^+} f(x)=(0-1)^2+(-\infty)^2=+\infty$; The straight line of equation $x=0$ is a vertical asymptote to (C_f) ; $\lim_{x\rightarrow +\infty} f(x)=(+\infty)^2+(+\infty)^2=+\infty$.	½												
B) 2) a)	$f'(x)=2(x-1)+2\frac{\ln x}{x}=2\frac{x^2-x+\ln x}{x}=2\frac{g(x)}{x}$; $f'(x)$ have same sign as $g(x)$ for every $x\in]0 ; +\infty[$.	½												
B) 2) b)	Table of variations of: f <table><tr><td>x</td><td>0</td><td>1</td><td>$+\infty$</td></tr><tr><td>$f'(x)$</td><td>■</td><td>-</td><td>0 +</td></tr><tr><td>$f(x)$</td><td>■</td><td>$+\infty$ ↘</td><td>0 ↗ $+\infty$</td></tr></table>	x	0	1	$+\infty$	$f'(x)$	■	-	0 +	$f(x)$	■	$+\infty$ ↘	0 ↗ $+\infty$	¾
x	0	1	$+\infty$											
$f'(x)$	■	-	0 +											
$f(x)$	■	$+\infty$ ↘	0 ↗ $+\infty$											

<div><div>B) 3)</div><div>a)</div></div>	<p>u is differentiable over $]0 ; 1]$ and $u'(x) = f'(x) - 1 < 0$ for every $x \in]0 ; 1]$ because $f'(x) < 0$ for every $x \in]0 ; 1]$.</p> <p>Table of variations of u over $]0 ; 1]$:</p> <table><tr><td>x</td><td>0</td><td>1</td></tr><tr><td>$u'(x)$</td><td>-</td><td>-</td></tr><tr><td>$u(x)$</td><td>$+\infty$</td><td>-1</td></tr></table> <p>The function u is continuous and strictly decreasing over $]0 ; 1]$ and changes the sign, so using the intermediate value theorem there exists a unique real number $\alpha \in]0 ; 1]$ such that $u(\alpha) = 0$ then $f(\alpha) = \alpha$.</p> <p>In addition, $u\left(\frac{1}{2}\right) \approx 0.2 > 0$ and $u(1) = -1 < 0$ therefore $\frac{1}{2} < \alpha < 1$.</p>	x	0	1	$u'(x)$	-	-	$u(x)$	$+\infty$	-1	<div><div>1/2</div></div>			
x	0	1												
$u'(x)$	-	-												
$u(x)$	$+\infty$	-1												
<div><div>B) 3)</div><div>b)</div></div>	<p>$\lim_{x \rightarrow +\infty} f(x) = +\infty$ and $\lim_{x \rightarrow +\infty} \frac{f(x)}{x} \stackrel{HR}{=} \lim_{x \rightarrow +\infty} \left[2(x-1) + 2\frac{\ln x}{x} \right] = +\infty + 0 = +\infty$; therefore (C_f) admits at $+\infty$ a parabolic branch of direction $(O ; \vec{j})$.</p>	<div><div>1/2</div></div>												
<div><div>B) 4)</div></div>		<div><div>3/4</div></div>												
<div><div>B) 5)</div><div>a)</div></div>	<p>h is defined when f is defined so the domain of definition of h is $D_h =]0 ; +\infty[$.</p>	<div><div>1/2</div></div>												
<div><div>B) 5)</div><div>b)</div></div>	<p>h is differentiable over $]0 ; +\infty[$ and $h'(x) = f'(x)e^{f(x)}$ which has the same sign of $f'(x)$ since $e^{f(x)} > 0$ for every $x \in]0 ; +\infty[$;</p> <p>Table of variations of h:</p> <table><tr><td>x</td><td>0</td><td>1</td><td>$+\infty$</td></tr><tr><td>$h'(x)$</td><td>-</td><td>0</td><td>+</td></tr><tr><td>$h(x)$</td><td>$+\infty$</td><td>1</td><td>$+\infty$</td></tr></table>	x	0	1	$+\infty$	$h'(x)$	-	0	+	$h(x)$	$+\infty$	1	$+\infty$	<div><div>1/2</div></div>
x	0	1	$+\infty$											
$h'(x)$	-	0	+											
$h(x)$	$+\infty$	1	$+\infty$											
<div><div>B) 5)</div><div>c)</div></div>	<p>$h(x) = e^x$; $e^{f(x)} = e^x$; $f(x) = x$ since the function $x \mapsto \exp(x)$ is continuous and strictly increasing over \mathbb{R}, and as $x \in]0 ; 1]$ then $x = \alpha$.</p>	<div><div>1/2</div></div>												