## gradient

The gradient of a scalar function  $f(x_1, x_2, ..., x_n)$  is a vector field that points in the direction of the greatest rate of increase of f.

For a function  $f: \mathbb{R}^n \to \mathbb{R}$ , the gradient is denoted as:

$$\nabla f = \left(\frac{\partial f}{\partial x_1}, \frac{\partial f}{\partial x_2}, \dots, \frac{\partial f}{\partial x_n}\right)$$

where each component is a partial derivative of f with respect to one of the variables.

**Direction:** The gradient points in the direction of the steepest ascent of f

Magnitude: The magnitude  $||\nabla f||$  represents the rate of the steepest increase.

**Zero Gradient**: If  $\nabla f = 0$ , the point is a critical point (possible max, min, or saddle point).

## gradient

The gradient captures all the partial derivative information of a multivariable function.

## example

For  $f(x, y) = x^2 + y^2$ , the gradient is:

$$\nabla f = \left(\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}\right) = (2x, 2y)$$



