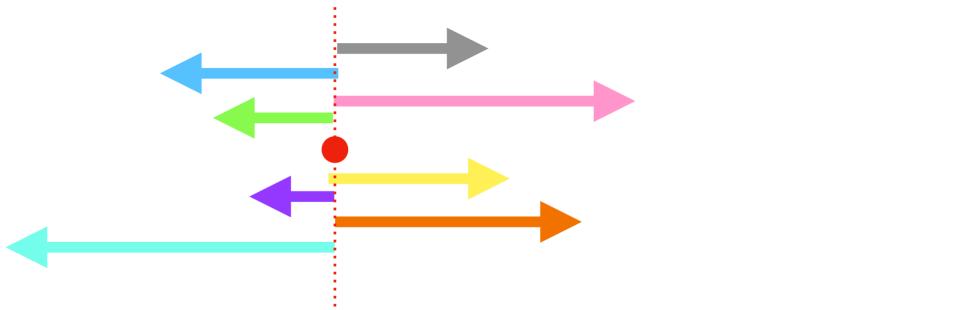
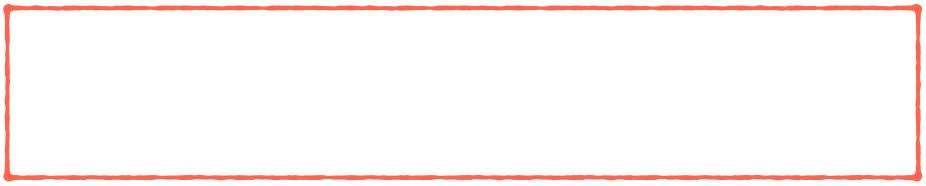
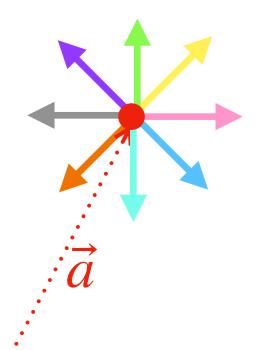


gradient



directional derivatives





$\max \nabla f(a,b)$ $\|\vec{v} = 1\|$

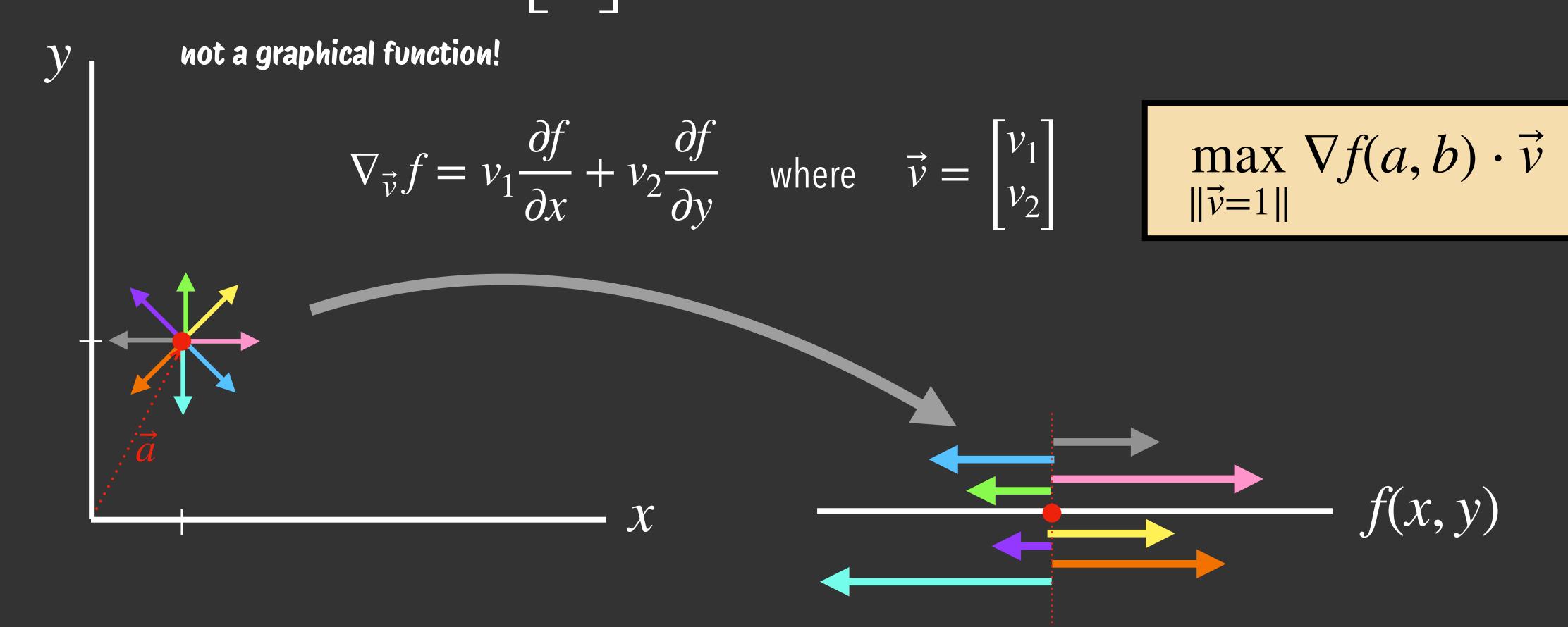
gradient

$$f(x,y) = x^2 + y^2 \Longrightarrow \nabla f = \begin{bmatrix} \frac{\partial f}{\partial x} \\ \frac{\partial f}{\partial y} \end{bmatrix} = \begin{bmatrix} 2x \\ 2y \end{bmatrix}$$

$$V = \text{not a graphical function!}$$

directional derivatives

$$\nabla_{\vec{v}} f(\vec{a}) = \lim_{h \to \infty} \frac{f(\vec{a} + h \cdot \vec{v}) - f(\vec{a})}{h}$$



gradient

Zero Gradient:

If $\nabla f = 0$, the point is a critical point (max, min, or saddle point)

example

For $f(x, y) = x^2 + y^2$, the gradient is:

$$\nabla f = \left(\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}\right) = (2x, 2y)$$

Find minimum (we see from image):

$$\nabla f = \begin{bmatrix} \frac{\partial f}{\partial x} \\ \frac{\partial f}{\partial y} \end{bmatrix} = \begin{bmatrix} 2x \\ 2y \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix} = \vec{0}$$

