





## "if P is true, then Q is true"



## "if Q is false, then P is false"





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### "if P is false, then Q is true"





# indirect proofs

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Proof by contrapositive

to prove the statement

"if P is true, then Q is true"

you instead prove the equivalent statement

"if Q is false, then P is false"

Proof by contradiction

to prove the statement

"if P is true, then Q is true"

and show that the following is not possible

"if P is false, then Q is true"

• Proof by counterexample (not technically a proof)

# indirect proofs: proof by contrapositive

#### **Theorem**

For any  $n \in \mathbb{Z} n$ , if  $n^2$  is even, then n is even.

