



proof by induction











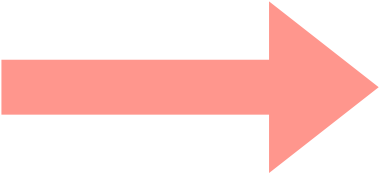








**Proof.**



# proof by induction

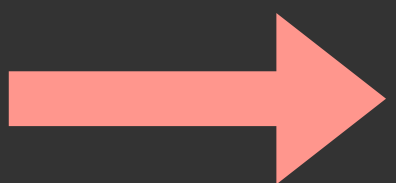
## Theorem

The sum of the first  $n$  powers of two is  $2^n - 1$ .



## Proof.

- Let  $P(n)$  be the statement "the sum of the first  $n$  powers of two is  $2^n - 1$ ."
- We prove by induction, that  $P(n)$  is true for all  $n \in \mathbb{N}$  from which the theorem follows
- The base case:
  - we need to show  $P(0)$  is true, meaning that the sum of the first zero powers of two is  $2^0 - 1$ .
  - since the sum of the first zero powers of two is zero and  $2^0 - 1 = 0$ , we see that  $P(0)$  is true. ✓



# proof by induction

## Theorem

The sum of the first  $n$  powers of two is  $2^n - 1$ .

Proof cont'd.

