



limitation





# limit of a function

Let  $f(x)$  be a function defined on some open interval that contains  $a$ , except possibly at  $a$  itself. We say that the limit of  $f(x)$  as  $x$  approaches  $a$  is  $L$ , and we write:

$$\lim_{x \rightarrow a} f(x) = L$$

if, for every number  $\epsilon > 0$  there exists a number  $\delta > 0$  such that whenever  $0 < |x - a| < \delta$ , it follows that  $|f(x) - L| < \epsilon$ .

- $\epsilon$ : this represents how close we want  $f(x)$  to be to  $L$ . We can choose  $\epsilon$  to be any small positive number, indicating the "closeness" level we desire
- $\delta$ : this represents how close  $x$  needs to be to  $a$  in order for  $f(x)$  to be within  $\epsilon$  of  $L$

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