

examples of vector spaces

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- Real n -dimensional space \mathbb{R}^n :

The set of all n -tuples of real numbers (e.g., $\mathbb{R}^2, \mathbb{R}^3$) with standard addition and scalar multiplication

- Example: $\vec{u} = [1, 2, 3], \vec{v} = [4, 5, 6]$ and $2\vec{u} = [2, 4, 6]$

- Polynomials of degree n or less P_n :

The set of all polynomials of degree $\leq n$ with real coefficients

- Example: $P_2 = \{a_0 + a_1x + a_2x^2 \mid a_0, a_1, a_2 \in \mathbb{R}\}$

- Matrices of fixed size $M_{m \times n}$:

The set of all $m \times n$ matrices with real (or complex) entries.

- Example: The set of 2×2 matrices $A = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}, B = \begin{bmatrix} 0 & 5 \\ 1 & -2 \end{bmatrix}$.

examples that are **not** vector spaces

example