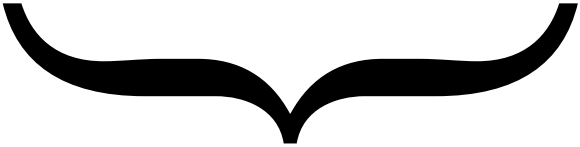




[tryitout:https://f1oswald.shinyapps.io/bias\_variance/

Expected **test MSE**

$$E \left( y_0 - \hat{f}(x_0) \right)^2 = \text{Var}(\hat{f}(x_0)) + \left[ \text{bias}(\hat{f}(x_0)) \right]^2 + \text{Var}(\epsilon)$$



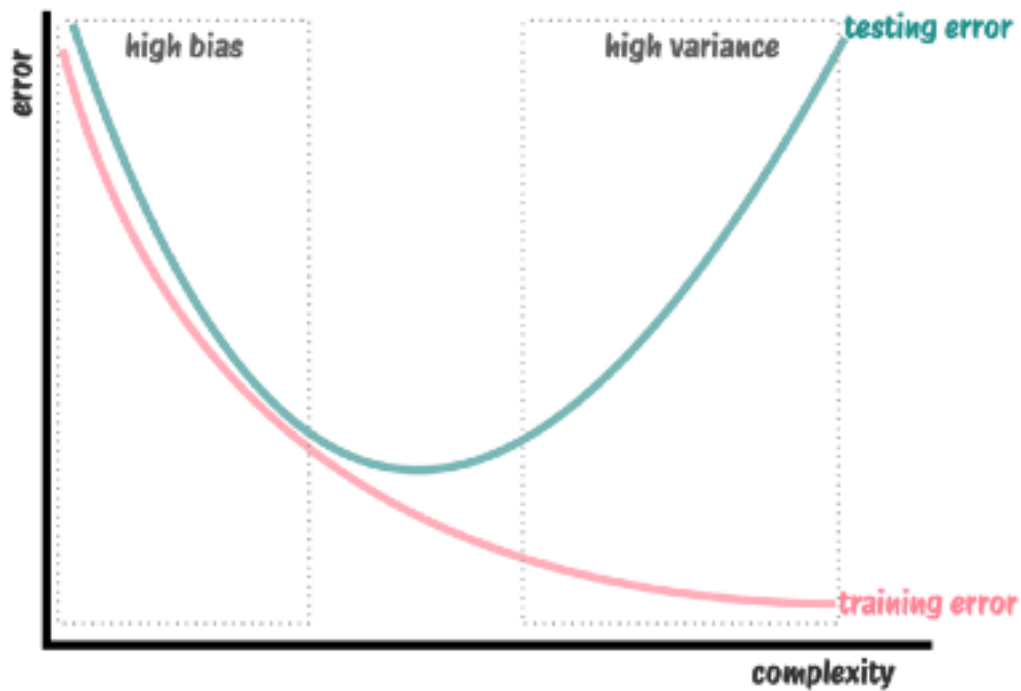
variance increases  
with complexity



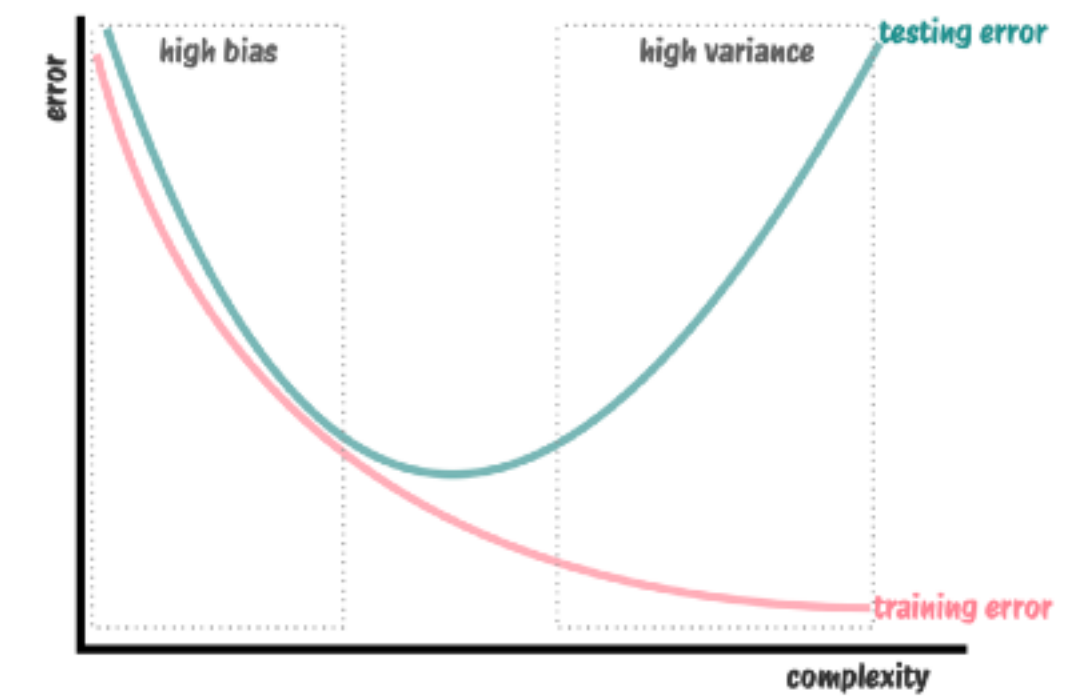
bias decreases  
with complexity

**Formalizing Bias-Variance Trade-Off**





# Formalizing Bias Variance Trade-Off



Expected **test MSE**

$$E \left( y_0 - \hat{f}(x_0) \right)^2 = \underbrace{\text{Var}(\hat{f}(x_0))}_{\text{variance increases with complexity}} + \underbrace{\left[ \text{bias}(\hat{f}(x_0)) \right]^2}_{\text{bias decreases with complexity}} + \text{Var}(\epsilon)$$

variance increases  
with complexity

bias decreases  
with complexity

# Bias Variance Trade-Off

