binomial random variable

- A r.v. modeling the number of successes in a fixed number of independent Bernoulli trials.
- Discrete outcomes $\{0,1,2,3...,n\}$
- Two parameter
 - p probability of a success for each trial
 - *n* number of trials
- Shorthand notation: $X \sim \text{Binom}(n, p)$
- E(X) = np, V(X) = np(1 p)

$$P(X = x | n, p) = {n \choose x} p^{x} (1 - p)^{n-x}$$

$$X \quad P(X = x)$$

$$0 \quad \binom{n}{0} p^{0} (1-p)^{n}$$

$$1 \quad \binom{n}{1} p^{1} (1-p)^{n-1}$$

$$2 \quad \binom{n}{2} p^{2} (1-p)^{n-2}$$

$$\vdots \qquad \vdots$$

$$n-1 \quad \binom{n}{(n-1)} p^{n-1} (1-p)^{1}$$

$$n \quad \binom{n}{n} p^{n} (1-p)^{0}$$

omomia random variable

example (cont'd...)



Toss a coin 3 times: the sample space is Ω : {H,T} \times {H,T}

Define the random variable: X = the number of heads

What is the probability distribution of X?

$$X \sim Bin(n = 3, p = 0.5)$$

$$\implies P(X = x) = \binom{n}{x} p^{x} (1 - p)^{n - x} = \binom{n}{x} 0.5^{x} (0.5)^{3 - x}$$