

Bayes Rule

providing miles



{rule of total probability}

the Bayesian interpretation

probability rules

Bayes Rule

If events A_1, A_2, \dots, A_k constitute a partition of the sample space Ω and $P(A_i) \neq 0 \ \forall i$, then
or any event B in Ω such that $P(B) \neq 0$

$$\begin{aligned} P(A_i | B) &= \frac{P(A_i)P(B | A_i)}{P(A_1)P(B | A_1) + P(A_2)P(B | A_2) + \dots + P(A_k)P(B | A_k)} \\ &= \frac{P(A_i)P(B | A_i)}{\sum_{j=1}^k P(A_j | B)P(A_j)} \quad \{\text{rule of total probability}\} \\ &= \frac{P(A_i)P(B | A_i)}{P(B)} \end{aligned}$$

This theorem is consistent with **the Bayesian interpretation** of probability theory

probability rules

exercise 5

In an experiment on human memory, participants have to memorize a set of words (B_1), numbers (B_2), and pictures (B_3). These occur in the experiment with the probabilities $P(B_1) = 0.5$, $P(B_2) = 0.4$, $P(B_3) = 0.1$.

Then participants have to recall the items (where A is the recall event). The results show that $P(A | B_1) = 0.4$, $P(A | B_2) = 0.2$, $P(A | B_3) = 0.1$.

- (a) Compute $P(A)$, the probability of recalling an item.
- (b) What is the probability that an item that is correctly recalled (A) is a picture (B_3)?