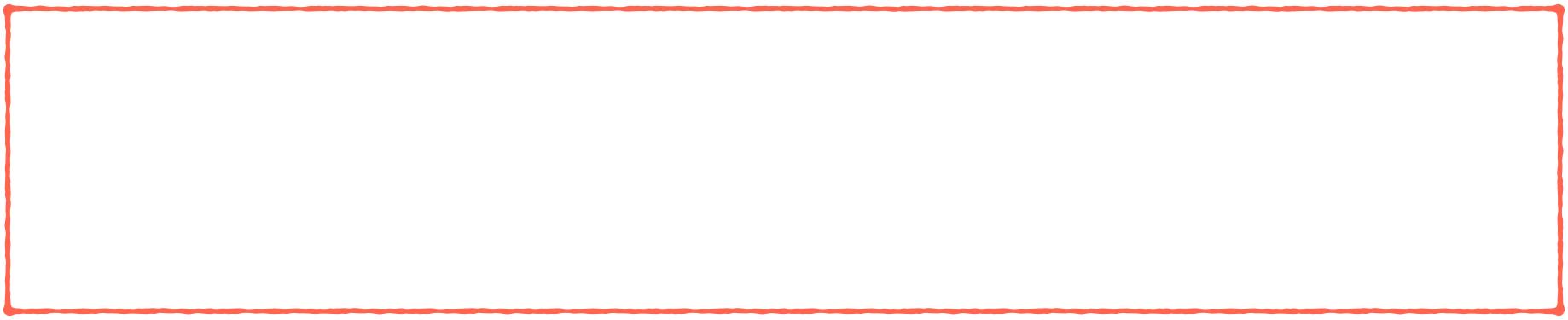


the product rule





the product rue

If f and g are differentiable, then

$$\frac{d}{dx}\left(f(x)g(x)\right) = f'(x)g(x) + f(x)g'(x)$$

example

Differentiate the function $f(x) = (x^2 + 1)(x^3 - 1)$.

Here we set
$$f(x) = x^2 + 1 \implies f'(x) = 2x$$

 $g(x) = x^3 - 1 \implies g'(x) = 3x^2$

and use the product rule:

$$\frac{d}{dx} ((x^2 + 1)(x^3 - 1)) = 2x(x^3 - 1) + (x^2 + 1)3x^2$$
$$= 2x^4 - 2x + 3x^4 + 3x^2$$
$$= 5x^4 + 3x^2 - 2x$$

the chain rule