



**Formalizing Bias-Variance Trade-Off**

[tryitout:[https://flosswald.shinyapps.io/bias\\_variance/](https://flosswald.shinyapps.io/bias_variance/)]

Expected **test MSE**

$$E \left( y_0 - \hat{f}(x_0) \right)^2 = \text{Var}(\hat{f}(x_0)) + \left[ \text{bias}(\hat{f}(x_0)) \right]^2 + \text{Var}(\epsilon)$$

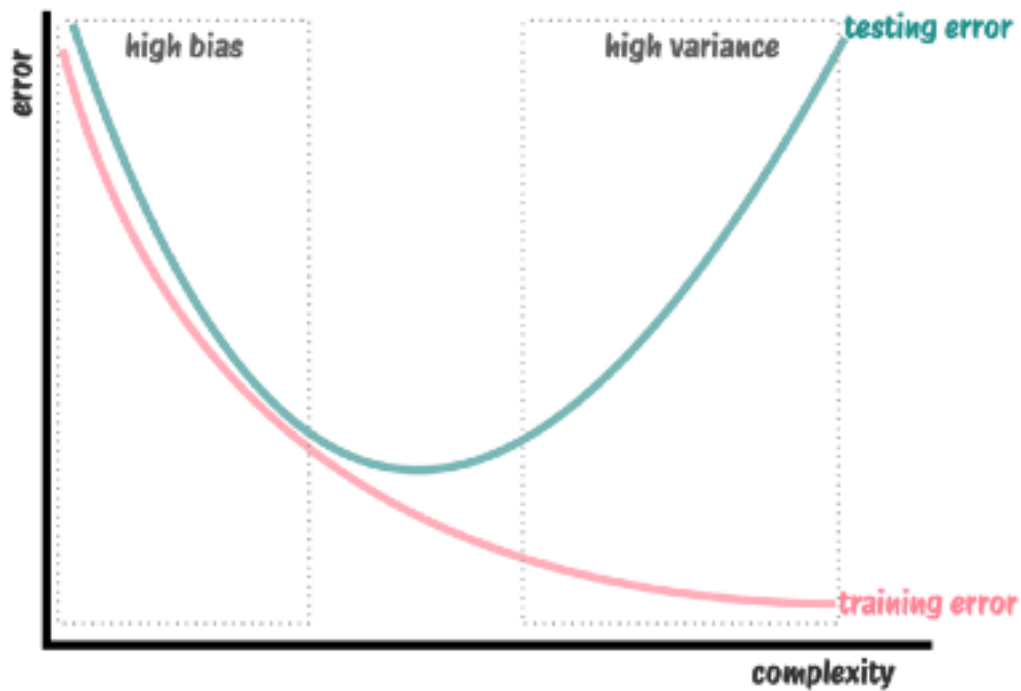
expected MSE at  $x_0$  if we  
repeatedly estimated  $f(x)$   
with different training sets

irreducible error

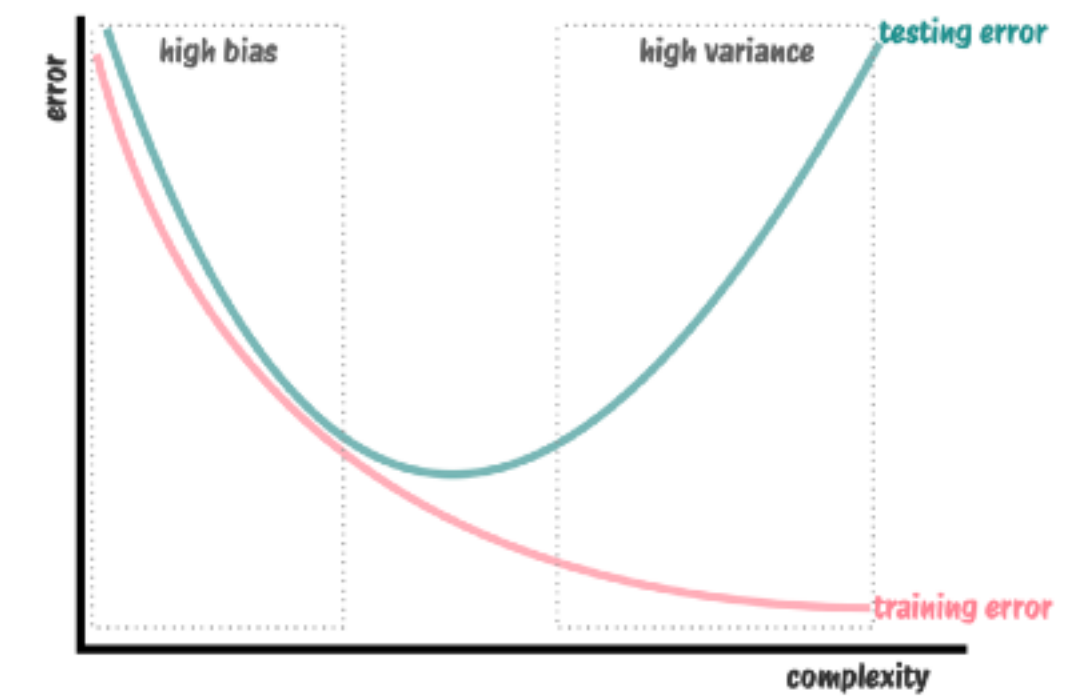








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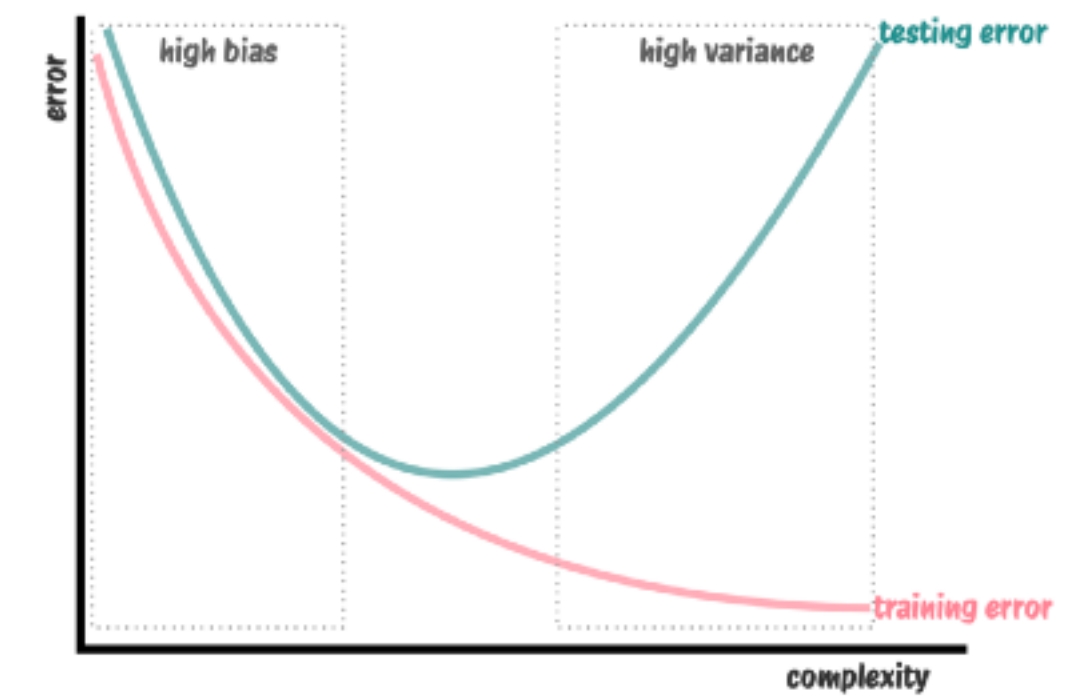
Expected **test MSE**

$$\underbrace{E \left( y_0 - \hat{f}(x_0) \right)^2}_{\text{expected MSE at } x_0 \text{ if we repeatedly estimated } f(x) \text{ with different training sets}} = \text{Var}(\hat{f}(x_0)) + \left[ \text{bias}(\hat{f}(x_0)) \right]^2 + \underbrace{\text{Var}(\epsilon)}_{\text{irreducible error}}$$

expected MSE at  $x_0$  if we repeatedly estimated  $f(x)$  with different training sets

irreducible error

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Expected **test MSE**

$$E \left( y_0 - \hat{f}(x_0) \right)^2 = \text{Var}(\hat{f}(x_0)) + \left[ \text{bias}(\hat{f}(x_0)) \right]^2 + \text{Var}(\epsilon)$$