



substitution step by step















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*If there are still terms containing  $x$  at this stage, stop and consider another choice of  $u$ .*





# substitution step by step

1. Choose a suitable  $u = u(x)$ . Your choice should not be a constant function
2. Work out  $u'(x)$  and write down an expression for  $dx = du/u'(x)$ . If you are considering a definite integral, work out  $u(a)$  and  $u(b)$  where  $a$  and  $b$  are the limits of the integral
3. Next
  - replace every instance of  $u(x)$  with the letter  $u$
  - replace  $dx$  with  $d(u)/u'(x)$  and cancel
  - (for definite integrals only) replace  $a$  with the value  $u(a)$  and  $b$  with  $u(b)$

**Warning:** by now the integral should be solely in terms of  $u$ .

*If there are still terms containing  $x$  at this stage, stop and consider another choice of  $u$ .*

4. If you can, work out the integral (don't forget  $+C$  if you are working with indefinite integrals)
5. This step only for indefinite integrals: Your antiderivative should be in terms of  $u$ . Replace every instance of  $u$  with the original function  $u(x)$ .

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