## diagonalization theorem

An  $n \times n$  matrix A is diagonalizable if if and only if A has n linearly independent eigenvectors.

simply put: a matrix is diagonalizable if it has distinct eigenvalues or, if it has repeated eigenvalues, it still has enough independent eigenvectors to match its dimensionality

- the eigenvalues determine the entries of the diagonal matrix
- ullet the eigenvectors form the columns of a matrix  $oldsymbol{Q}$
- ullet the transformation reflects how the original matrix A can be simplified, highlighting the intrinsic properties of A

 $\overrightarrow{v_1}, \overrightarrow{v_2}, \ldots, \overrightarrow{v_n}$  are linearly independent eigenvectors, and  $\lambda_1, \lambda_2, \ldots, \lambda_n$  are the corresponding eigenvalues

the process continued...

$$A = QDQ^{-1}$$