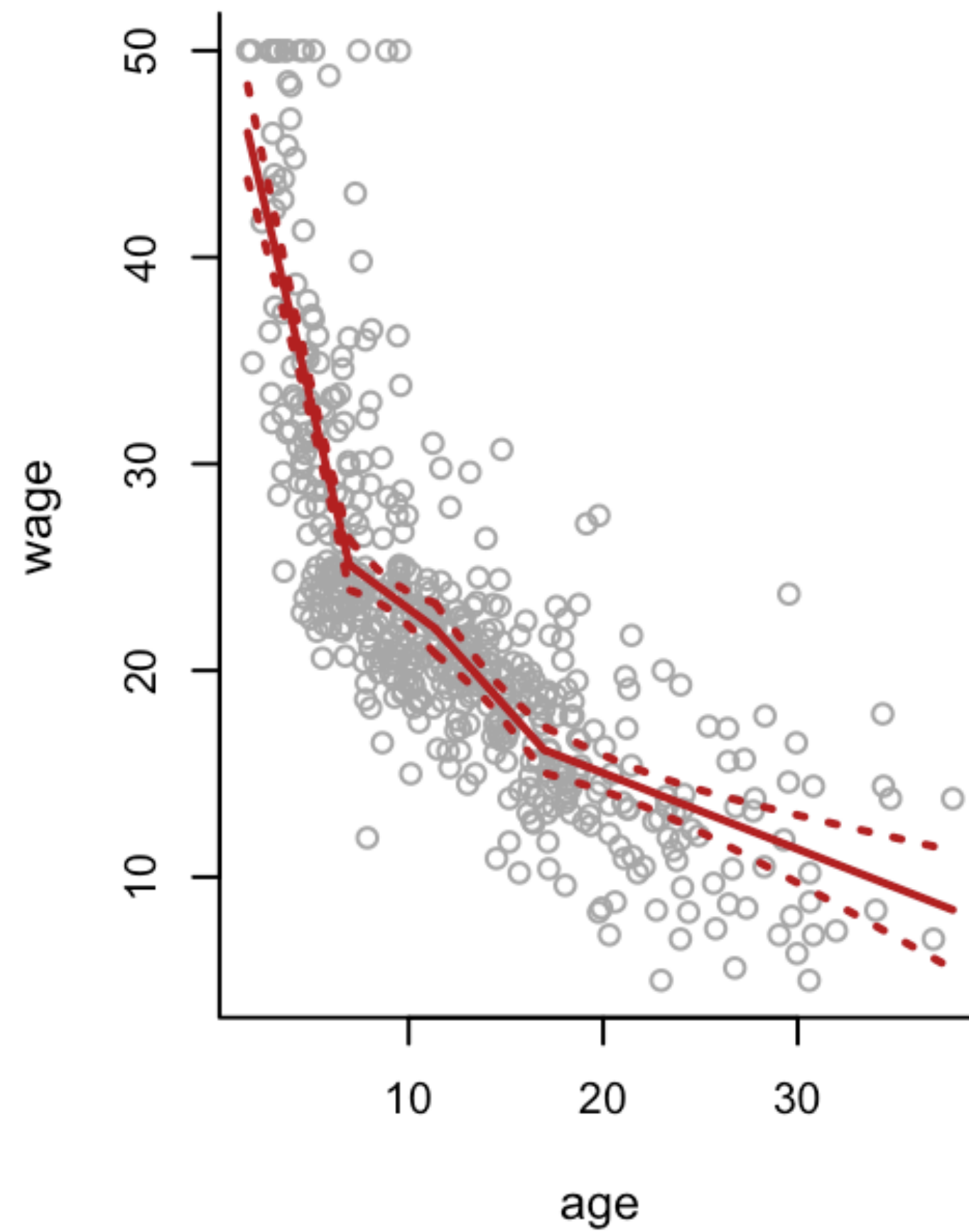


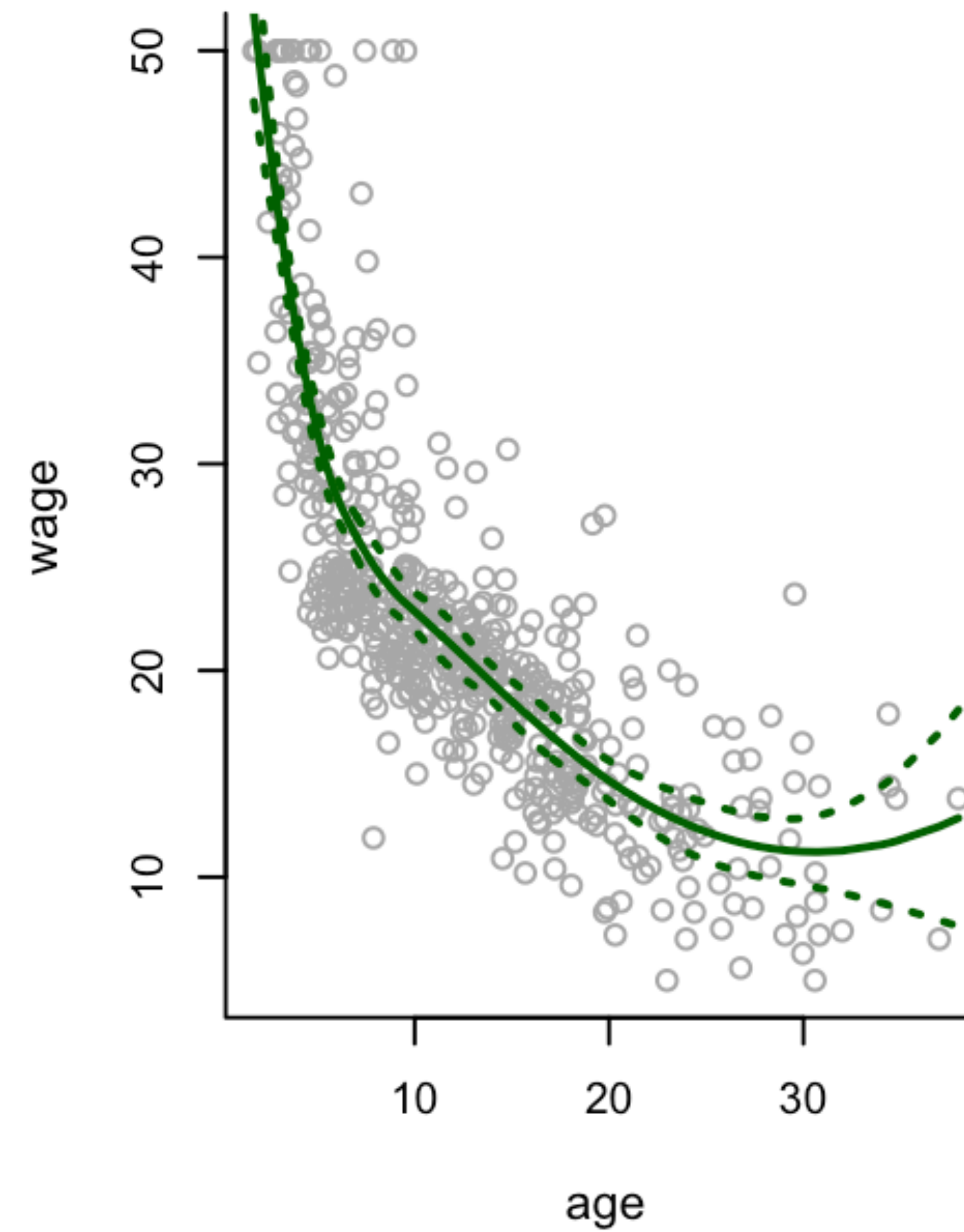
Regression Splines

Example: Wage (ISLR2)

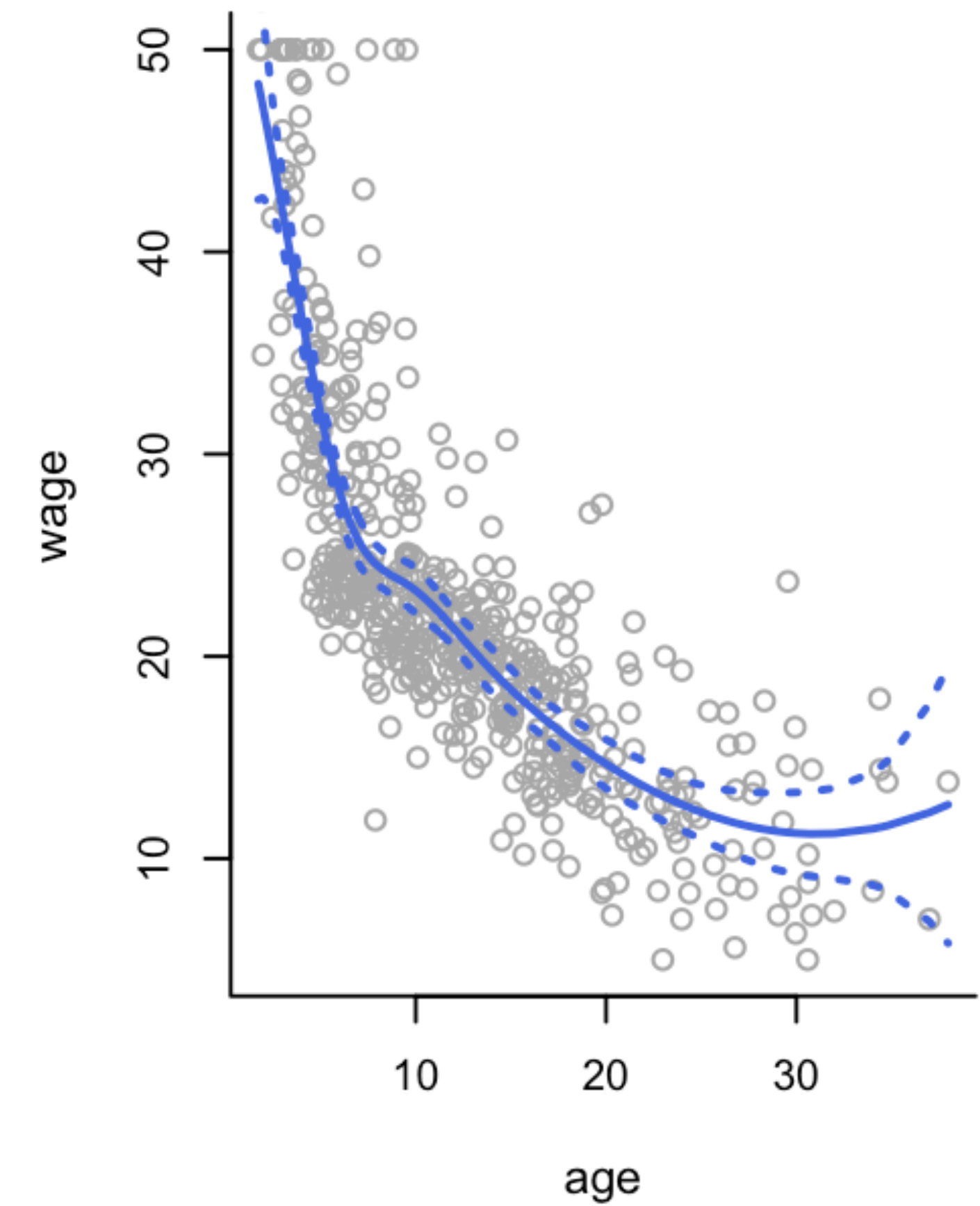
Linear Spline



Quadratic Spline



Cubic Spline



Regression Splines

Constraints and Degrees of Freedom

- In the previous example, we started with a cubic piecewise polynomial with 8 unconstrained parameters, so we started with 8 **degrees of freedom** (df)
- We initially imposed one constraint, which restricted one parameter, so we lost a degree of freedom $8 - 1 = 7$
- With the further two constraints: $8 - 3 = 5$ df
- In general, a cubic spline with K knots has $4 + K$ degrees of freedom. In R we can specify either the number of knots or just the degrees of freedom.

A degree- d regression spline is a piecewise degree- d polynomial with continuity in derivatives up to degree $d - 1$ at each knot