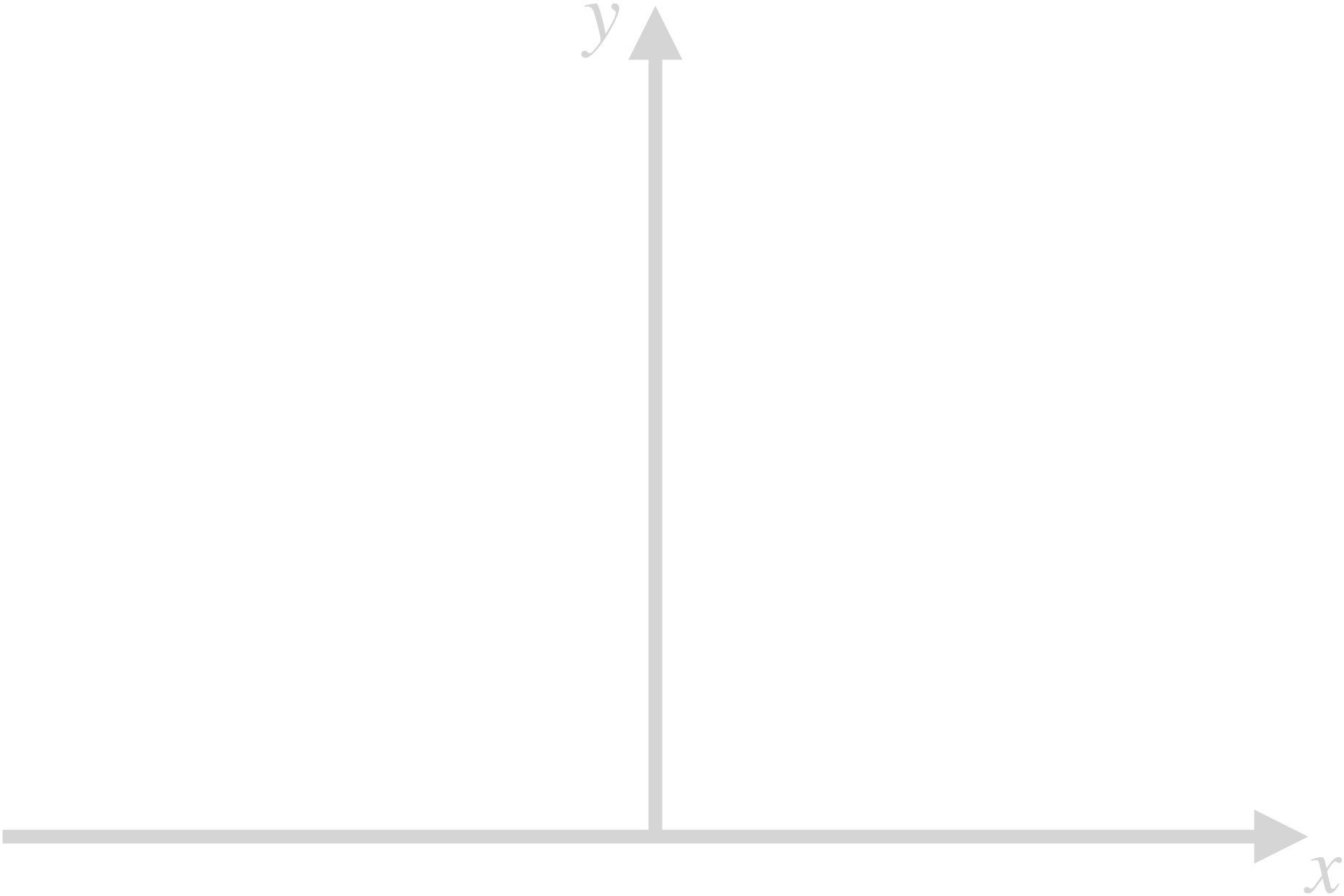


derivative of a function

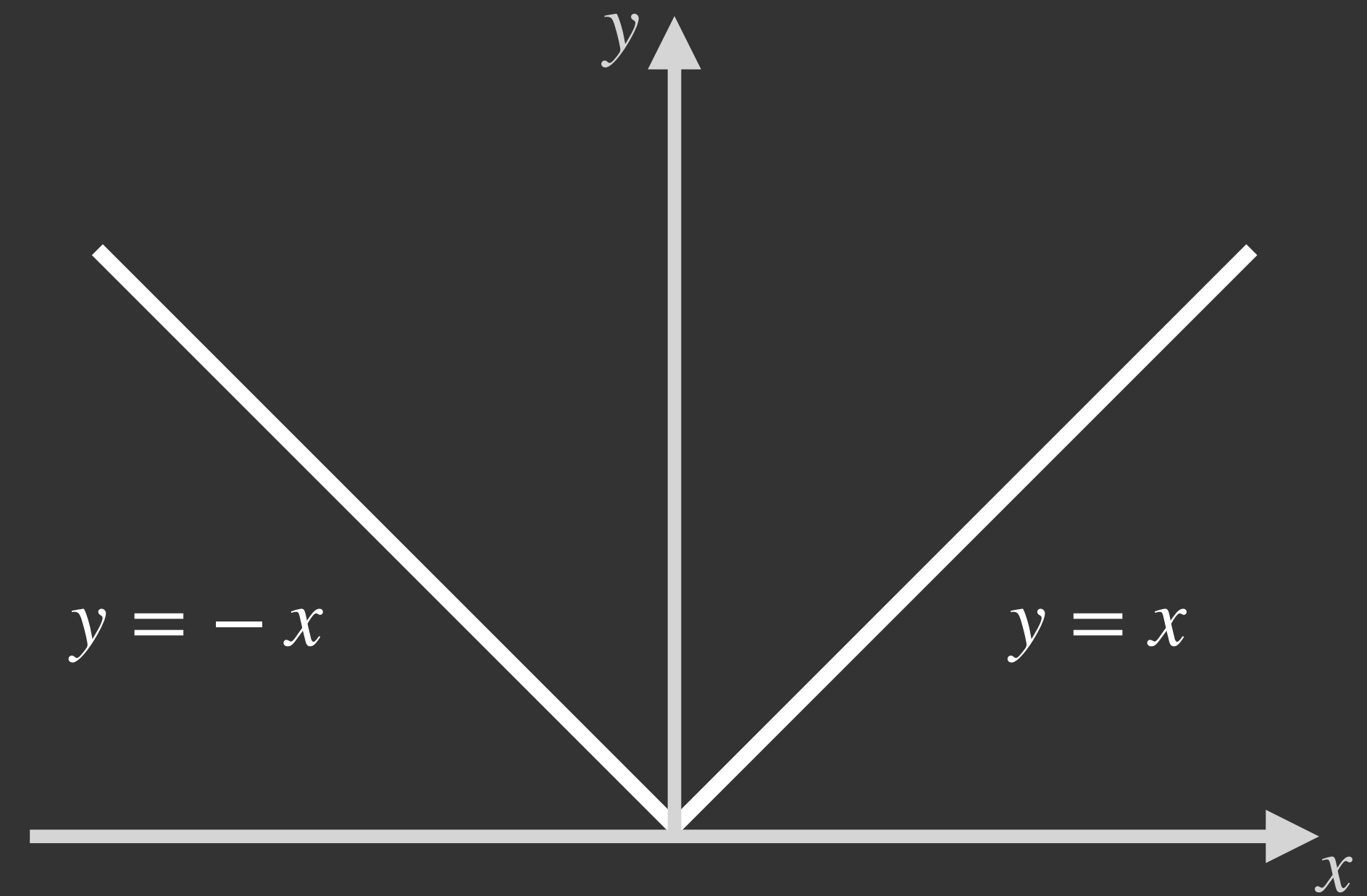
example



derivative of a function

example

$$f(x) = |x| = \begin{cases} x & \text{if } x \geq 0 \\ -x & \text{if } x < 0 \end{cases}$$



is not differentiable at a certain point because it is not continuous at $(0,0)$, we can draw many many many tangent lines there. Also:

$$\text{for } h > 0, \quad \frac{f(0+h) - f(0)}{h} = \frac{h - 0}{h} = 1$$

$$\text{for } h < 0, \quad \frac{f(0+h) - f(0)}{h} = \frac{-h - 0}{h} = -1$$

i.e. $\lim_{h \rightarrow 0} \frac{f(0+h) - f(0)}{h}$ does not exist since taking the limit from both sides must give the same answer.

derivative of a function