

eigenvalue decomposition summarized

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$$A = QDQ^{-1} \quad \text{eigenvalue decomposition}$$

$$Q^{-1}AQ = D \quad \text{diagonalization of } A$$

- Under what condition would Q^{-1} exist?
 - ▶ If the columns of Q are linearly independent
 - ▶ i.e. if A has n linearly independent eigenvectors
 - ▶ i.e. if A has n distinct eigenvalues



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- If A is symmetric, we get an even more convenient situation
 - ▶ The eigenvalues are orthogonal

