

# Posterior Probabilities



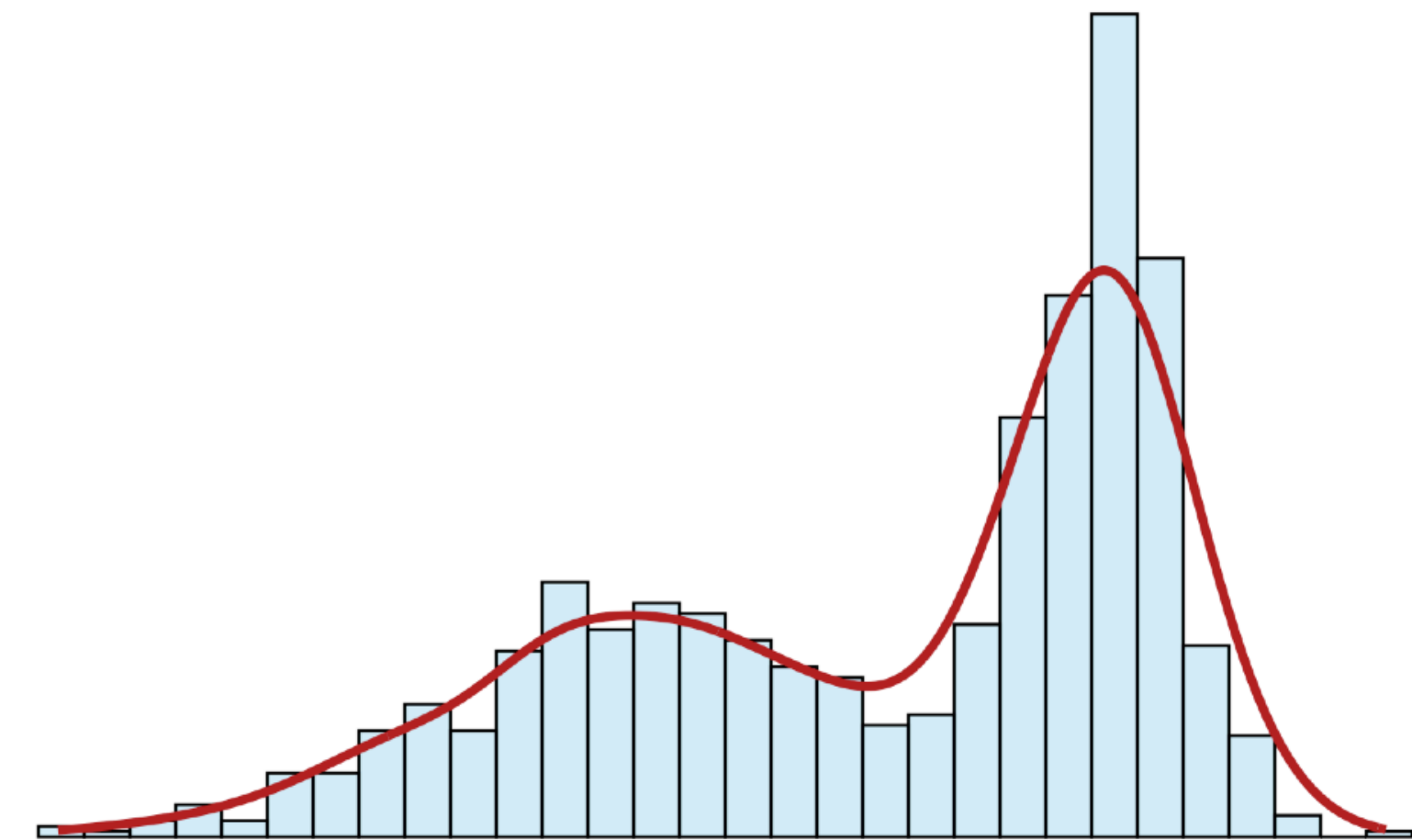
$$p(x) = w_k \mathcal{N}(x | \mu_k, \Sigma_k)$$

prior probability of  
being in group  $k$

likelihood of seeing  
 $x$  in group  $k$

$$p(\text{cluster } k | x) = \frac{w_k \mathcal{N}(x | \mu_k, \Sigma_k)}{\sum_{j=1}^K w_j \mathcal{N}(x | \mu_j, \Sigma_j)}$$

posterior probability  
of being in cluster  $k$



# Maximum Likelihood Estimation



$$p(x) = \sum_{k=1}^K w_k \mathcal{N}(x | \mu_k, \Sigma_k)$$

$$p(\mathbf{X} | \mathbf{w}, \mu, \Sigma) = p(x_1, x_2, \dots, x_n | \mathbf{w}, \mu, \Sigma) = \prod_{n=1}^N \sum_{k=1}^K w_k \mathcal{N}(x_n | \mu_k, \Sigma_k)$$

$$\log p(\mathbf{X} | \mathbf{w}, \mu, \Sigma) = \sum_{n=1}^N \log \left[ \sum_{k=1}^K w_k \mathcal{N}(x_n | \mu_k, \Sigma_k) \right]$$

Goal: choose  $w, \mu, \Sigma$  that maximizes the log likelihood