

the span









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- Given some vectors we now ask: what is the set of all vectors that you can get from a linear combination of these specific vectors?
- The answer is "the span of these vectors". Because of the rules of vector addition, any such linear combination will be in the vector space.

The set of all linear combinations of vectors $\overrightarrow{v_1}, \overrightarrow{v_2}, ..., \overrightarrow{v_n}$ is denoted by $span(\overrightarrow{v_1}, \overrightarrow{v_2}, ..., \overrightarrow{v_n})$ and called the linear span of these vectors.

example

What is the span of the vectors
$$\overrightarrow{v_1} = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$$
, $\overrightarrow{v_2} = \begin{bmatrix} 1 \\ 1 \end{bmatrix}$?

We can actually get to any other vector in the plane, by taking a linear combination of $\overrightarrow{v_1}$ and $\overrightarrow{v_2}$. In other words, the span of $\overrightarrow{v_1}$ and $\overrightarrow{v_2}$ is \mathbb{R}^2 , i.e. the whole plane.

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