[try it out: https://floswald.shinyapps.io/bias variance/l

Expected test MSE

$$F\left(v_{\alpha} - \hat{f}(v_{\alpha})\right)^{2} - Var\theta$$

$$E\left(y_0 - \hat{f}(x_0)\right)^2 = \operatorname{Var}(\hat{f}(x_0)) + \left[\operatorname{bias}(\hat{f}(x_0))\right]^2 + \operatorname{Var}(\epsilon)$$

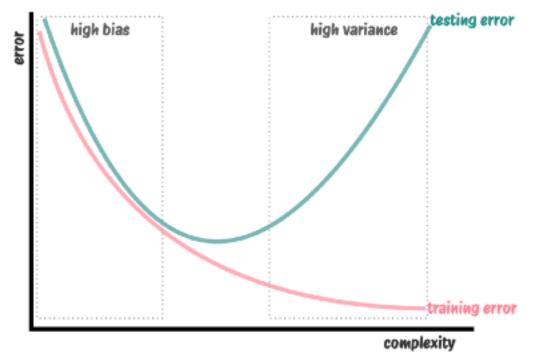


variance increases with complexity

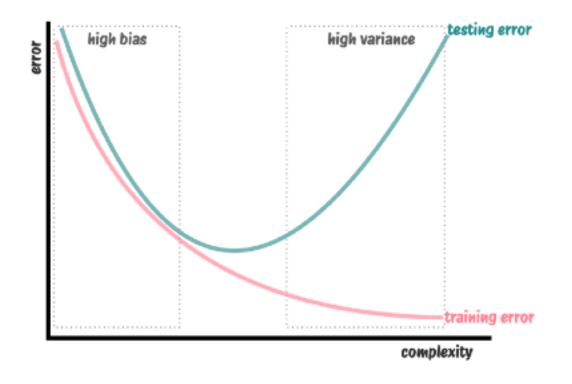


bias decreases with complexity

Formalizing Bias Variance Trade-Off



Formalizing Bias Variance Trade-Off



Expected test MSE

$$E\left(y_0 - \hat{f}(x_0)\right)^2 = \operatorname{Var}(\hat{f}(x_0)) + \left[\operatorname{bias}(\hat{f}(x_0))\right]^2 + \operatorname{Var}(\epsilon)$$

$$\begin{array}{c} \text{variance increases} \\ \text{with complexity} \end{array} \quad \begin{array}{c} \text{bias decreases} \\ \text{with complexity} \end{array}$$

Bias Variance Trade-Off

