

Exercise 1

1. The dimension of the data (num. of rows, num. of columns) is (**67856**, **11**).
2. The first six lines of this data are

X	veh_value	exposure	clm	numclaims	claimcst0	veh_body	veh_age	gender	area	agecat
1	1.06	0.3039014	0	0	0	HBACK	3	F	C	2
2	1.03	0.6488706	0	0	0	HBACK	2	F	A	4
3	3.26	0.5694730	0	0	0	UTE	2	F	E	2
4	4.14	0.3175907	0	0	0	STNWG	2	F	D	2
5	0.72	0.6488706	0	0	0	HBACK	4	F	C	2
6	2.01	0.8542094	0	0	0	HDTOP	3	M	C	4

3. Using the R function `str()`, we get the structure of the data

```
'data.frame': 67856 obs. of 11 variables:
 $ X      : int  1 2 3 4 5 6 7 8 9 10 ...
 $ veh_value: num  1.06 1.03 3.26 4.14 0.72 2.01 1.6 1.47 0.52 0.38 ...
 $ exposure : num  0.304 0.649 0.569 0.318 0.649 ...
 $ clm      : int  0 0 0 0 0 0 0 0 0 0 ...
 $ numclaims: int  0 0 0 0 0 0 0 0 0 0 ...
 $ claimcst0: num  0 0 0 0 0 0 0 0 0 0 ...
 $ veh_body  : chr  "HBACK" "HBACK" "UTE" "STNWG" ...
 $ veh_age   : int  3 2 2 2 4 3 3 2 4 4 ...
 $ gender    : chr  "F" "F" "F" "F" ...
 $ area      : chr  "C" "A" "E" "D" ...
 $ agecat    : int  2 4 2 2 2 4 4 6 3 4 ...
```

4. We made use of the function `subset()` to delete the first column of `dataCar` and the function `transform()` to transform the variables `clm`, `numclaims`, `veh_body`, `veh_age`, `gender`, `area`, and `agecat` to a factor. The summary of the resulting data is

veh_value	exposure	clm	numclaims	claimcst0
Min. : 0	Min. :0.003	0:63232	0:63232	Min. : 0
1st Qu.: 1	1st Qu.:0.219	1: 4624	1: 4333	1st Qu.: 0
Median : 2	Median :0.446		2: 271	Median : 0
Mean : 2	Mean :0.469		3: 18	Mean : 137
3rd Qu.: 2	3rd Qu.:0.709		4: 2	3rd Qu.: 0
Max. :35	Max. :0.999			Max. :55922

veh_body	veh_age	gender	area	agecat
SEDAN :22233	1:12257	F:38603	A:16312	1: 5742
HBACK :18915	2:16587	M:29253	B:13341	2:12875
STNWG :16261	3:20064		C:20540	3:15767
UTE : 4586	4:18948		D: 8173	4:16189

TRUCK	: 1750	E: 5912	5:10736
HDTOP	: 1579	F: 3578	6: 6547
(Other)	: 2532		

5. Below is a Barplot of numclaims.

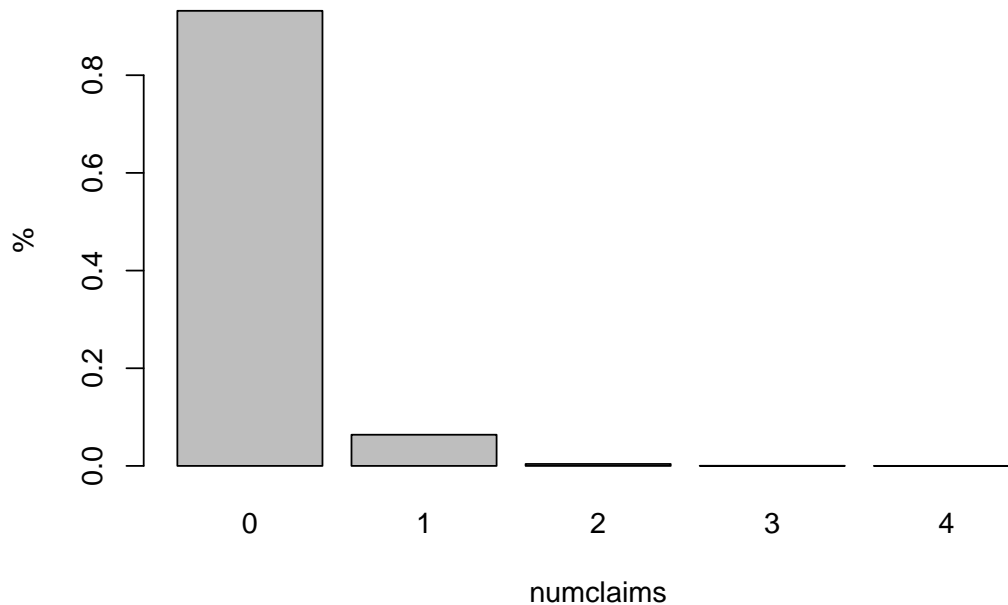


Figure 1: Barplot of 'numclaims'

6. We define `dataCar0` to be the subset data with *only variables* `claimcst0` and `veh_value` and *only subjects* with $(\text{claimcst0} > 0)$ and $(\text{agecat} = 3 \text{ or } 4)$. In the flowing we will work with this data. Its summary appears below.

	claimcst0	veh_value
Min.	: 200	Min. : 0.00
1st Qu.:	354	1st Qu.: 1.07
Median :	748	Median : 1.56
Mean :	1929	Mean : 1.84
3rd Qu.:	2035	3rd Qu.: 2.31
Max. :	47297	Max. : 11.54

7. We fit a linear regression model with `veh_value` as independent variable and `claimcst0` as dependent variable. We also fit another linear model but this time with $\log(\text{claimcst0})$ as independent variable. The summary of each model is given below.

- `claimcst0 ~ veh_value`

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	2053.3584	131.83266	15.575490	5.511928e-52
veh_value	-67.4188	60.78594	-1.109118	2.674995e-01

					confint	
	Estimate	Std. Error	t value	Pr(> t)	2.5 %	97.5 %
claimcst0 ~ veh_value						
(Intercept)	2053.358	131.833	15.575	0.000	1794.830	2311.887
veh_value	-67.419	60.786	-1.109	0.267	-186.622	51.785
log(claimcst0) ~ veh_value						
(Intercept)	6.834	0.047	145.356	0.000	6.741	6.926
veh_value	-0.023	0.022	-1.076	0.282	-0.066	0.019

- `log(claimcst0) ~ veh_value`

```

              Estimate Std. Error    t value Pr(>|t|)
(Intercept)  6.83354029 0.04701249 145.355840 0.0000000
veh_value    -0.02333101 0.02167671  -1.076317 0.2819028

```

8. We compute, for each model, a 95% confidence intervals (confint) for the intercept and the slope parameters. We then use the `kableExtra` functions `kbl()`, `kable_styling()`, `pack_rows()` and `add_header_above()`, to construct the following table.

9. Figure 2 below show the scatterplots `claimcst0~veh_value` and `log(claimcst0)~veh_value` (side by side) with the corresponding least squares regression lines.

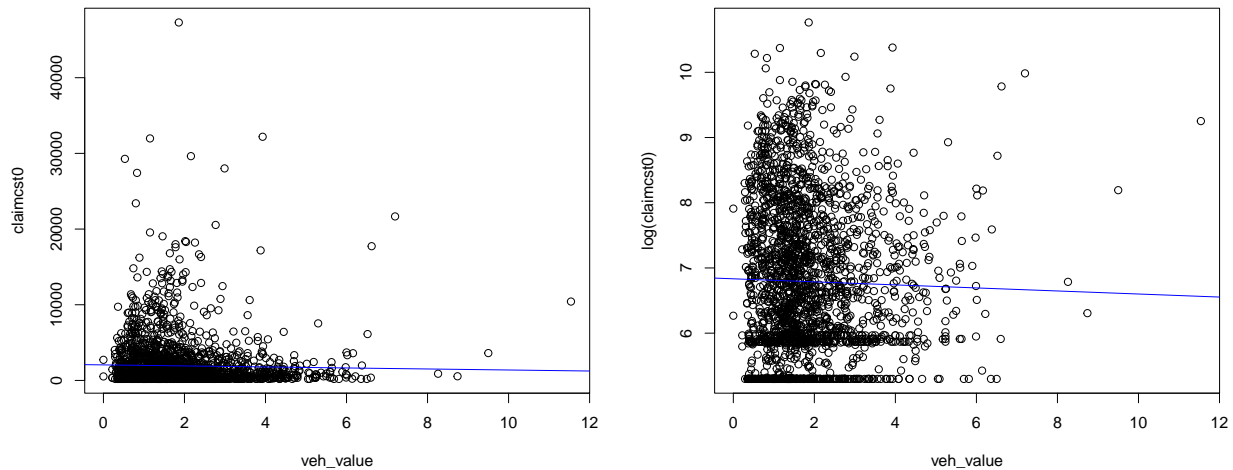


Figure 2: Least Squares Regression Lines; (a) $Y = \text{claimcst0}$ and (b) $Y = \log(\text{claimcst0})$

To learn more about linear regression, visit the website of [Introduction to Modern Statistics](#).