micro Hayekian Market

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Contents

Introduction to a micro Hayekian Market		3	
1	The technical setup of the code	3	
2	The structure of the model and the warming up phase	3	
3	The hayekian version	5	
4	The unstructured version	6	
Bibliography		11	
Index		12	

List of Figures

1	An example of initial not overlapping demand and offer curves	1
2	Hayekian case: (i) an example of final demand and offer curves, (ii)	
	the history of mean prices, (iii) their coeffcients of variation within	
	each cycle	7
3	Hayekian case: (i) distribution of mean prices in each cycle and (ii)	
	of their standard deviations	8
4	Unstructured case: (i) an example of final demand and offer curves,	
	(ii) the history of mean prices, (iii) their coeffcients of variation	
	within each cycle	Ć
5	Unstructured case: (i) distribution of mean prices in each cycle and	
	(ii) of their standard deviations	10

Introduction to a micro Hayekian Market

The purpose of this note is that of showing a very simple agent-based model of a market, with emergent interesting price dynamics. A counter example is also introduced, showing implausible price dynamics.

The code uses the IPython language (interactive Python) and can be dowloaded from https://github.com/terna/microHayekianMarket using the Clone or download button; it is also possible to run it directly on line at https://mybinder.org/v2/gh/terna/microHayekianMarket/master?filepath=microHayekianMarket.ipynb.

A suggested reading about Hayek is a quite recent paper of Bowles et al. (2017).

1 The technical setup of the code

The The IPython¹ (or Python² 3.x) code requires the following starting setup:

Listing 1: Warming up of the model

```
%pylab inline
import statistics as s
import numpy as np
import pylab as plt
from IPython.display import clear_output
import time
```

%pylab inline is a magic command of Jupyter.³

¹https://ipython.org.

²https://www.python.org.

³http://jupyter.org.

2 The structure of the model and the warming up phase

Our agents are simply prices, to be interpreted as reservation prices:⁴

We have two price vectors: pL^b with item pL_i^b for the buyers, and pL^s with item pL_j^s for the sellers. The i^{th} or the j^{th} elements of the vectors are prices, but in this case we can use them also as agents.

Both in the hayekian perspective (Section 3) and in the unstructured one (Section 4) we have a common $warning\ up$ action.

In this phase we define:

- nCycles number of simulation cycles;
- *nBuyers* number of the buyers;
- *nSellers* number of the sellers;
- d_0 the lower bound for random uniform numbers, both for the buyers and the sellers in the warming up phase; in the running phase, the lower bound is 0;
- d_1 the upper bound for random uniform numbers for the buyers;
- d_2 the upper bound for random uniform numbers for the sellers;
- the initial buyer *i* reservation price, different for each buyer: $p_{b,i} = \frac{1}{1+u_i}$ with $u_i \sim \mathcal{U}(d_0, d_1)$;
- initial seller j reservation price, different for each seller: $p_{s,j} = 1 + u_j$ with $u_j \sim \mathcal{U}(d_0, d_2)$.

With $d_0 = 0.1$, $d_1 = 0.2$, $d_2 = 0.2$ and sorting in decreasing order the vector pL^b and in increasing order the vector pL^s we obtain two not overlapping price sequences that we can interpret as a demand and an offer curves (Fig. 1).

This is the warming up, or starting situation, of the model. To generate new examples related to Section 3 and to Section 4, it is necessary to repeat this phase.

The IPython (or Python 3.x) code is;

Listing 2: Warming up of the model

warming up

run it before executing both - the hayekian perspective or

⁴The max price a buyer could pay and the min one a seller could accept.

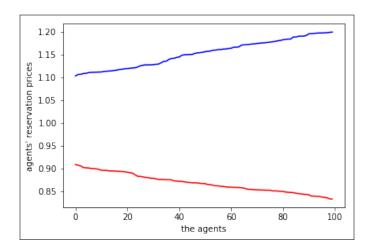


Figure 1: An example of initial not overlapping demand and offer curves

```
#
                                 - the unstructured case
d0 = 0.1
d1 = 0.2
d2 = 0.2
nCycles=10000
nBuyers= 100
nSellers=100
buyerPriceList=[]
sellerPriceList=[]
for i in range(nBuyers):
    buyerPriceList.append(1/(1+np.random.uniform(d0,d1)))
for j in range(nSellers):
    sellerPriceList.append(1+np.random.uniform(d0,d2))
plt.plot(np.sort(buyerPriceList)[::-1],"r");
plt.plot(np.sort(sellerPriceList),"b");
xlabel("the_agents")
ylabel("agents',∟reservation, prices")
```

3 The hayekian version

The buyers and the sellers meet randomly. Buyer i and seller j exchange if $pL_i^b \ge pL_i^s$; the deal is recorded at the price of the seller pL_i^s .

In this version, which is the important one in this note, the running prices are changing following the correction coefficients:

- for the buyer: (i) $c_b = \frac{1}{1+u_b}$ if the deal succeeds (trying the pay less next time) or (ii) $c_b = 1 + u_b$ if the deal fails (preparing to pay more next time); in (i) and (ii) we have $u_b \sim \mathcal{U}(0, d_1)$
- for the seller: (iii) $c_s = \frac{1}{1+u_s}$ if the deal succeeds (preparing to obtain a higher revenue next time) or (iv) $c_s = 1 + u_s$ if the deal fails (preparing to obtain a lower revenue next time); in (iii) and (iv) we have $u_s \sim \mathcal{U}(0, d_2)$.

With $d_1 = 0.2$, $d_2 = 0.2$ and nCycles set to 10,000 we obtain sequences of mean prices (mean in each cycle) quite realistic, with a very low variance within each cycle (see Fig. 2 and 3).

The coefficient of variation is calculated as $\frac{standard\ deviation}{mean}$

A comment: we have a plausible series of mean price, with a complicated behavior, and with a high stability of the dispersion of the values within each cycle.

The right side of the buyer and seller curves shows another plausible situation with agents not exchanging.

4 The unstructured version

The buyers and the sellers meet randomly as in Section 3. Buyer i and seller j exchange in any case; the deal is recorded at the mean of the price of the seller pL_j^s and of the price of the buyer.

In this version the running prices are changing following the correction coefficients:

- with equal probability for the buyer: (i) $c_b = \frac{1}{1+u_b}$ or (ii) $c_b = 1+u_b$); in (i) and (ii) we have $u_b \sim \mathcal{U}(0, d_1)$
- with equal probability for the seller: (iii) $c_s = \frac{1}{1+u_s}$ or (iv) $c_s = 1 + u_s$; in (iii) and (iv) we have $u_s \sim \mathcal{U}(0, d_2)$.

With $d_1 = 0.2$, $d_2 = 0.2$ and nCycles set to 10,000 we obtain exploding sequences of mean prices (mean in each cycle), and explodinf variance within each cycle (see Fig. 4 and 5).

⁵In the *mall* sell price are public.

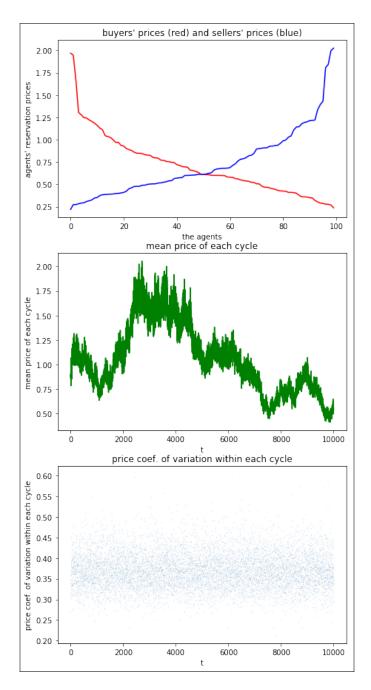


Figure 2: Hayekian case: (i) an example of final demand and offer curves, (ii) the history of mean prices, (iii) their coeffcients of variation within each cycle

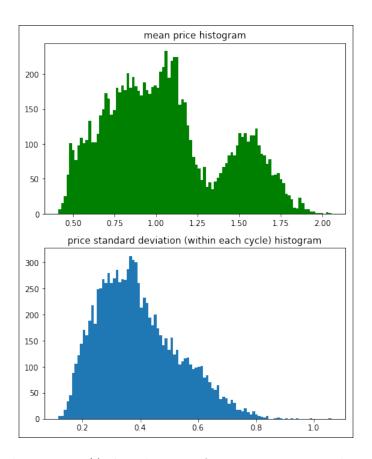


Figure 3: Hayekian case: (i) distribution of mean prices in each cycle and (ii) of their standard deviations

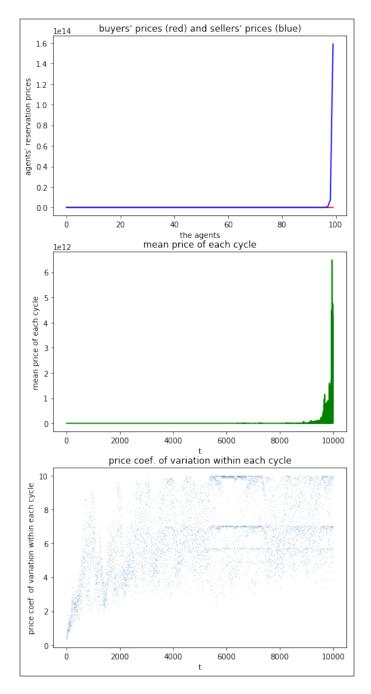


Figure 4: Unstructured case: (i) an example of final demand and offer curves, (ii) the history of mean prices, (iii) their coeffcients of variation within each cycle

mean price histogram

10000

8000

4000

2000

price standard deviation (within each cycle) histogram

10000

4000

2000

4000

2000

4000

2000

The coefficient of variation is calculated as $\frac{standard\ deviation}{mean}$.

Figure 5: Unstructured case: (i) distribution of mean prices in each cycle and (ii) of their standard deviations

1.5

2.0

2.5

3.0

10

0.5

0.0

A comment: this counter-example shows the missing the intelligent correction of the price that implicitly propagate the price among all the agents, a system of pure random price settings is absolutely far from being plausible.

Bibliography

Bowles, S., Kirman, A. and Sethi, R. (2017). *Retrospectives: Friedrich Hayek and the Market Algorithm*. In «Journal of Economic Perspectives», vol. 31(3), pp. 215-30.

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Index