The Evolution of the Velocity-Dispersion Profile of Dark Matter Particles in the Halo of M33

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1. INTRODUCTION

The topic of this study focuses on the tidal evolution of dark matter in satellite galaxies, specifically examining how the kinematics of dark matter halos evolve under external tidal forces from host galaxies. The interaction between the host and satellite galaxy can have a significant effect on the structure of the dark matter halo of the satellite galaxy, and since galaxies are defined by having a large component of their mass in the form of dark matter (C. S. Frenk & S. D. M. White (2012)), understanding how dark matter evolves helps us better understand the galaxy as a whole. These tidal forces affect the dark matter distribution and therefore, the velocity-dispersion profile of the particles. The velocity distribution can help us understand how the distributions of both dark matter and baryonic matter change within the satellite galaxy under external influences of a host galaxy, as well as provide insight into the nature of dark matter itself.

Understanding the evolution of dark matter halos in satellite galaxies helps our broader understanding of galaxy evolution. Dark matter not only contributes most of the galaxy's mass, but its behavior also influences how galaxies form and evolve. In context of a host and satellite galaxy, how satellite interacts with larger structures. Tidal interactions can lead to, namely, mass loss of the satellite as well as changes in the internal dynamics of dark matter halos (J. Wolf & et al. (2010)), which could lead to disruption of the very structure of the galaxy itself. Studying these effects helps us understand how galaxy assembly occurs, the histories of potential mergers and the overall impact of tidal forces on the growth and transformation of galaxies. Specifically, these interactions can help create better models of galaxy formation as whole.
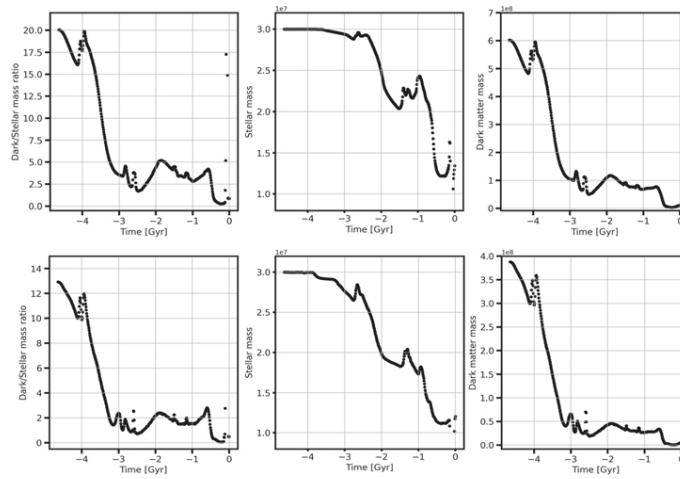

Figure 1. Shows the dark matter, baryonic matter, and the ratio of the two over a period of 4.7 Gyr's of Sagittarius dwarf spheroidal galaxy, a satellite of the Milky Way Galaxy. The top line shows the aforementioned three graphs at a radius of 5 kpc of its center and the bottom line at a radius of 2 kpc.

As our satellite galaxies orbit the host galaxy, tidal forces cause stripping of mass, namely dark matter, although baryonic matter is also lost. This can be seen in Figure 1 (H.-F. Wang et al. (2022)), where over time most of the matter is getting stripped from the satellite galaxy, where now today, almost no dark matter is present. It also shows that these stripping events occur in waves, or periodically and that there are differences in the percentage of matter being stripped between baryonic and dark matter.

It is important to understand how the velocity dispersion within the inner dark matter due to its association with the stability and survival of the satellite itself. Questions such as does the velocity dispersion within the half-mass radius of the dark matter halo increase or decrease as the galaxy is tidally stripped? Or how does the Jacobi radius evolve over time within the satellite? Overall, how does tidal stripping affect overall stability of the halo?

2. PROPOSAL

2.1. *This Proposal*

My question that I will be answering will be how the average velocity dispersion of dark matter particles evolves over time within the half-mass radius of the M33 halo.

2.2. *Methods*

The first calculation would be obtaining the velocity dispersion or σ. This value can be calculated using the standard deviation formula by first calculating the mean velocity and then the squared average deviation from the mean:

$$V_{mean} = \frac{1}{N} \sum_i^N v_i \tag{1}$$

$$\sigma = \sqrt{\frac{1}{N} \sum_i^N (v_i - V_{mean})^2} \tag{2}$$

Next, I would need to calculate the half-mass radius of each galaxy, which can be mass, that is the radius. This could be achieved by obtaining the radius of each particle in the simulation, then summing the mass of all the particles contained within the radius. By taking steps out from the center of our galaxy, we would continue until we got to half of our total mass.

Naturally, this is going to change overtime due to the described by summing the mass at increasing radii and once I get to half of the total nature of the process we are investigating, so doing this at different time steps will naturally allow us to show how the velocity distribution changes, as well as the mass. We can obtain all of this information directly from our simulation, and I would want to use all of the snapshots before the merging of the Milky Way and M31, and possibly after as the simulation shows M33 is not merged when the other galaxies do. This can partially be shown as in Figure 2, with a plot of the average velocity dispersion of the satellite galaxy and another of the distance of the satellite from its host galaxy. I would want to plot the velocity dispersion specifically within the half-mass radius rather than the entire galaxy and perhaps show how the half-mass radius changes over time as well.

2.3. *Hypothesis*

I propose that overtime, the amount of dark matter in the system will decrease periodically. This periodicity is caused by the orbit of the satellite around the host galaxy and throughout this periodicity, the velocity distribution within the half-mass radius will undergo periods of increasing velocity, while generally the trend of the velocity will decrease over time. As dark matter is stripped from the outside of the dark matter halo, the dark matter will become more concentrated near the center of the satellite or within the half-mass radius itself, causing this increase in velocity dispersion. However, mass is still lost, so overtime the total velocity dispersion will decrease, and so will the velocity dispersion within the half-mass radius. I think this will occur because naturally, overtime if you lose mass within a system, you are losing energy. If you lose energy, you will lose velocity. The reason of the peaks in velocity distribution initially are due to a loss of gravitational potential energy from this loss of outer mass in the satellite, which condenses the mass towards the center of the satellite, so within that area, there will be a spike in average velocity dispersion.
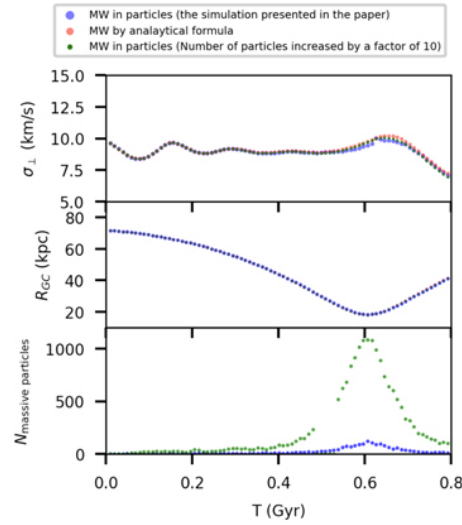
Figure 2. This figure is taken from H.-F. Wang et al. (2022), and displays the average-velocity dispersion, distance, and number of massive particles over a small period of time of the satellite galaxy Sagittarius around the Milky Way galaxy for two types of simulated data and from analytic formulas.

3. RESULTS

The first figure created was the velocity dispersion within the Jacobi radius (km/s) of M33 over time (Myr). The plot shows a cyclical nature of the velocity dispersion overtime, with a distinct peak around the time in our simulation when M31 and the Milk Way galaxy collide. This is then followed by a period of cyclical increase and decrease in velocity dispersion over time. It shows that the velocity dispersion is cyclical with periods of contraction and expansion of M33 by tidal stripping.
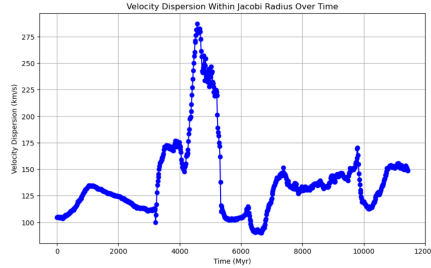

Figure 3. This figure is taken from my code, and displays the average velocity dispersion (km/s) overtime (Myr). The blue dots correlate to a time in the future. This plot shows the predicted cyclical nature of the velocity dispersion within M33, going through periods of increased and decreased speeds.
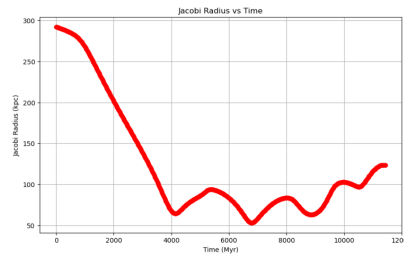

Figure 4. This figure is taken from my code, and displays how the Jacobi radius(kpc) changes over time (Myr). The red line correlate to a time in the future. This plot shows the gradual tidal stripping of M33 halo from M31 overtime, and how that stripping is interrupted through the interaction of M31 and the Milky Way Galaxy.

The second figure displays how the Jacobi radius (kpc) changes over time. As we can see the Jacobi radius steadily decreases overtime as M31 and M33 draw closer together, with their respective masses remaining the same. However, as M31 and the Milky Way Galaxy collide, the radius begins to increase and decrease, as M31 and Milky Way perform a dance around one another and their respective masses begin to interact with one another greatly. This displays the gradual degradation of the Jacobi radius as M31 and M33 travel closer together and how when M31 and the Milky Way Galaxy collide, the cyclical nature of the Jacobi radius through the interaction of M31 and the Milk Way's matter.

4. DISCUSSION

As discussed in the results of the average velocity dispersion over time, the velocity dispersion displays a cyclical increase and decrease overtime as well as the Jacobi radius gradually becoming smaller overtime as M31 and M33 travel closer together and how the radius begins cyclically alternating between periods of expansion and contraction, due to its interaction from the collided M31 and the Milky Way. This matches well part of our hypothesis, that being that as material is being stripped away from M33 by M31, the velocity dispersion within the Jacobi radius will go through periods of contraction and expansion. As material is stripped away initially, the overall potential energy of the M33 halo structure decreases, leading to particles "falling" closer to the galaxies center, or more material being concentrated with the Jacobi radius. This causes an increase in velocity dispersion, but mass is still being lost due to the ever present tidal stripping, which can be seen initially. However, when the Milky Way Galaxy and M31 get close enough, they begin to strip so much material from M33, that an abundant amount of material is contracted inside the Jacobi radius, leading to the large spike in average velocity dispersion at roughly 4.5 Byr, with the Jacobi radius itself being relatively small compared to other times within the plot. However, the velocity dispersion does not show a general decrease in value, due to the collision of M31 and M33, in contrast to our hypothesis.

Our results shown in this paper do agree in part to the hypothesis displayed in (J. Wolf & et al. (2010)), which argues that the structure of the dark matter of a satellite galaxy can be disrupted by its host galaxy. This is shown in part in Figure 3, through the interaction of M33, M31, and the Milky Way galaxy interaction as M31 and the Milky Way initially collide, the velocity dispersion increases dramatically, which indicates a massive ejection of material from the Jacobi radius of M33 itself. This can be seen in Figure 1, as the dark matter mass is decreasing within the Jacobi radius as material is being stripped by the larger host. This result shows that a host galaxy is able to effectively disrupt the dark matter kinematics within a satellite galaxy through tidal stripping and in addition, its collision with another similarly sized galaxy. The uncertainties with my analysis are with how the masses of the system are treated.

The particles in the simulation are never changed from being a blank galaxy particle, meaning the particles of M33 may actually be closer to M31, which we can of course say doesn't matter anyway because of our definition of the Jacobi radius itself. However, I think this fails to consider the considerable impact of the Milky Way- M31 collision, as it would have a great impact on our results, even simply looking at the mass actually acting on M33 not being stagnant. To provide a better analysis, use of the Milky Way's dark halo mass or simply a combination of M31 and the Milky Way's halo mass could be sufficient. Additionally, to better support the findings, showing the amount of original M33 dark matter halo particles within the Jacobi radius could better support the hypothesis as a whole.

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