

Stage-Wise School Reopening using Reinforcement Learning

Introduction

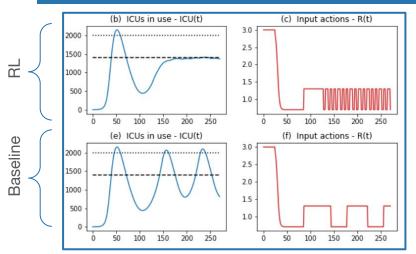
- COVID-19
 - is unprecedented
 - has delayed transmission time, lag in onset symptoms, hard to predict
- Lockdown
 - Pros: keep community healthier
 - o Cons: economic, mental health, productivity decline...

How to best regulate school reopening at different degrees?

- Use reinforcement learning
- Reinforcement learning: agent learns best actions to take in an environment that will maximize cumulative reward
- RL is fitting for this problem; we want our current decision to be good for the current time and for the future time.

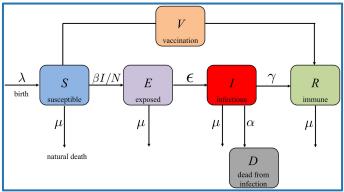


Related Works



Mauricio Arango and Lyudmil Pelov. Covid-19 pandemic cyclic lockdown optimization using reinforcement learning, CoRR, abs/2009.04647.2020.

- Lockdown/reopen (2 actions) represented by R (effective reproduction number)
- Agent learns optimized cyclic lockdowns in day increments
- Goal: maximize opening while avoid exceeding a threshold



Zhe Xu, Bo Wu, and Ufuk Topcu. Control strategies for covid-19 epidemic with vaccination, shield immunity and quarantine. A metric temporal logic approach. PLOS ONE, 16, 03 2021.

- SEIR that models vaccinations
- Multiple levels of reopening actions (2~5) represented by R (effective reproduction number)
- Agent learns optimized cyclic lockdowns in day, week, biweekly increments
- Goal: maximize opening while avoid exceeding a threshold
- Include vaccination considerations



Problem Formulation

State:

continuous, 12-dimension: (S, E, I, R, D, $n^{[7]}$, $n^{[6]}$, $n^{[5]}$, $n^{[4]}$, $n^{[3]}$, $n^{[2]}$, n^[1]), normalized

Action:

 $\beta = \gamma R$

discrete {0, 1, 2}; representing $R = \{0.7, 1.2, 1.5\}$

Reward:

$$\operatorname{reward}_{1}(t) = \begin{cases} 0, & \text{if } action = 0 \\ \alpha_{1}, & \text{if } action = 1 \\ \alpha_{2}, & \text{if } action = 2 \end{cases}$$

$$ext{reward}_2(t) = \begin{cases} 0, & ext{if } m_t < m_{threshold} \\ rac{-lpha_1}{m_{threshold}} m_t, & ext{if } m_t \geq m_{threshold} \end{cases}$$

 $reward_{total}(t) = reward_1(t) + \alpha_{linear} reward_2(t)$

State transition:

$$\begin{aligned} & \text{SEIR} \\ & \text{differential} \\ & \text{equations} \end{aligned} \qquad \begin{cases} S_{t+1} \leftarrow S_t - \frac{\beta I_t}{N} S_t - V \\ E_{t+1} \leftarrow E_t - \epsilon E_t + \frac{\beta I_t}{N} S_t \\ I_{t+1} \leftarrow I_t + \epsilon E_t - (\gamma + \alpha) I_t \\ R_{t+1} \leftarrow R_t + \gamma I_t + V \\ D_{t+1} \leftarrow R_t + \alpha I_t \end{cases}$$

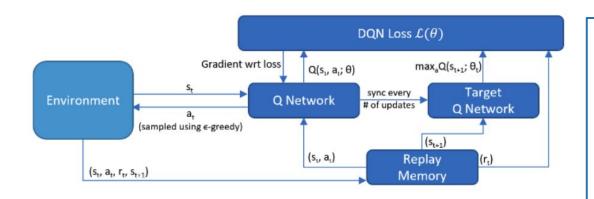
$$(n_{t+1}^{[7]}, n_{t+1}^{[6]}, n_{t+1}^{[5]}, n_{t+1}^{[4]}, n_{t+1}^{3]}, n_{t+1}^{[2]}, n_{t+1}^{[1]}) \leftarrow (n_{t}^{[6]}, n_{t}^{[5]}, n_{t}^{[4]}, n_{t}^{[3]}, n_{t}^{[2]}, n_{t}^{[1]}, \epsilon E_{t})$$

tracking the last 7 days of new cases

of new cases at current time t



Proposed Solution / Algorithm



- DQN [Off Policy] with Experience Replay and Target Network.
- Neural Network (Function approximator) replaces Q-Table.
- Uses MSE loss function.
- Takes considerable time to converge.

1. Experience Replay

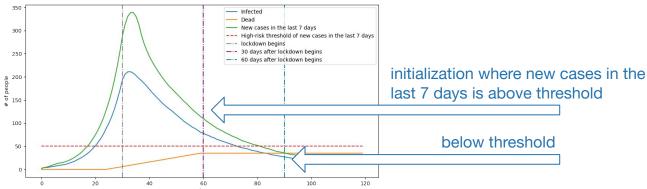
- Memory bank that stores states,actions,rewards created.
- Sample random experiences.
- Sequential dependency eliminated.

2. Target Network

- DQN updates entire network each step.
- Target always moving, hence backprop error not consistent.
- Target Network copy of Neural Network but only copied every N time steps.



Performance Metric / Initialization

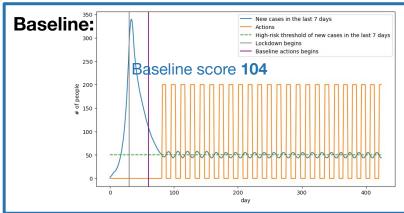


Metric Score Function:

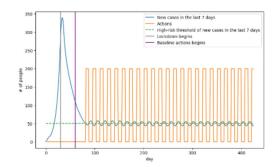
$$score_1(t) = \begin{cases} 0, & \text{if } action = 0 \\ 1, & \text{if } action = 1 \\ 2, & \text{if } action = 2 \end{cases}$$

$$score_2(t) = \begin{cases} 0, & \text{if } m_t < m_{threshold} \\ \frac{-m_t}{m_{threshold}}, & \text{if } m_t \ge m_{threshold} \end{cases}$$

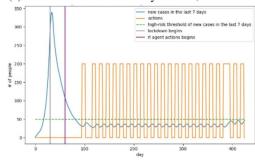
$$\mathsf{score} = round\left(\sum_{t=1}^{365} \mathsf{score}_1(t) + \mathsf{score}_2(t)\right)$$



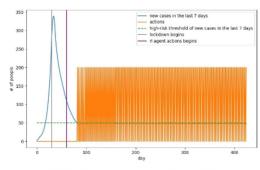
Results - Action Frequency



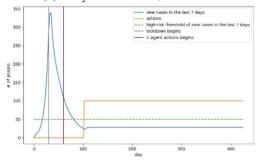
(a) Baseline model with daily actions; Score:104



(c) Weekly-action model; Score:303



(b) Daily-action model; Score:351

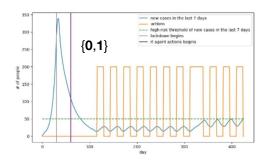


(d) Bi-weekly-action model; Score:291

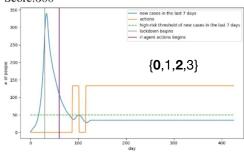
- Daily Action model not feasible despite high metric score.
- Weekly Action model more practical but lower metric score due to frequent shutdowns.
- Bi-Weekly Action model most preferable due to practical considerations.
- Conservative policy (Prefers Action 1 over Action 2) in order to keep a check on new cases.



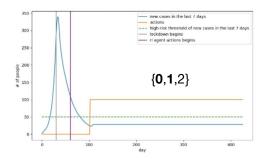
Results - Action Space Size



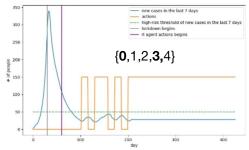
(a) Bi-weekly action, 2-dimensional action space; Score:300



(c) Bi-weekly action, 4-dimensional action space; Score:400



(b) Bi-weekly action, 3-dimensional action space; Score: 300

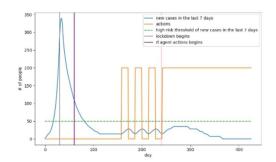


(d) Bi-weekly action, 5-dimensional action space; Score:390

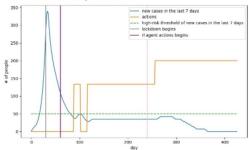
- 2-stage action space allows agent to choose between fully reopen and complete shutdown.
- 3-stage action space allows half-open option that agent chooses most of the time.
- 4-stage and 5-stage action
 [4-stage picks action 2,
 5-stage picks action 3]
 space allows for higher
 diversity by allowing
 varying degrees of
 openness.
- Greater action space size generally results in a higher metric score.



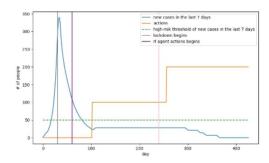
Results - Vaccination Inclusion



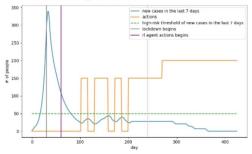
(a) Bi-weekly action, 2-dimensional action space, with vaccination; Score:193



(c) Bi-weekly action, 4-dimensional action space, with vaccination: Score:785



(b) Bi-weekly action, 3-dimensional action space, with vaccination;; Score:461



(d) Bi-weekly action, 5-dimensional action space, with vaccination; Score:969

- Vaccination introduced on day 240. (180 days after simulation starts)
- Effect of vaccination clearly seen as number of new cases decrease.
- For all action space sizes, RL agent picks least restrictive action (Action 2), full reopening as vaccination takes shape.
- Higher Action space sizes result in larger metric score as more freedom allowed.



Conclusion

- Agent with larger action space options or higher action frequency tends to score higher. (Not necessarily the optimal policy)
- Good idea to include a larger action space, even if agent picks only a few select actions.
- Five stages of reopening preferred, no concerns over inconvenience since agent only picks subset of actions. The agent still picks good actions.
- Actions designed to be taken Weekly and Bi-Weekly.
- **Future Work**: Actions taken after arbitrary number of days after looking at past progress/ feasibility of frequency of action change.
- **Future Work**: Move from DQN to Actor-Critic methods to check effect on policy.

Questions?

