$$\frac{2.7.5}{456} = \frac{1}{100} =$$

(c)
$$AY = \begin{bmatrix} 2 \\ 5 \end{bmatrix}$$

$$\frac{2.7.11}{A = \left[\begin{array}{c} 0 & 0 & 6 \\ 1 & 2 & 3 \\ 0 & 4 & 5 \end{array}\right]} \begin{array}{c} Row & 1 \rightarrow Row^{3} \\ Row & 3 \rightarrow Row^{2} \\ Row^{2} \rightarrow Row^{1} \end{array} \longrightarrow \begin{array}{c} P = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{array}$$

$$PA = \begin{cases} 0 & 1 & 0 & 0 & 6 \\ 0 & 0 & 1 & 0 & 0 & 6 \\ 1 & 0 & 0 & 0 & 0 & 1 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0$$

Multiplying A on the right by P2 will exchange the columns of

$$50 \left[\frac{600}{540} \right] = \left[\frac{100}{000} \right] \left[\frac{000}{045} \right] \left[\frac{000}{000} \right]$$

$$A = \begin{bmatrix} 1 & 2 & 0 \\ 2 & 4 & 1 \end{bmatrix} \xrightarrow{Row 2-2} \xrightarrow{Row 1} \begin{bmatrix} 1 & 2 & 0 \\ 0 & 0 & 1 \end{bmatrix} \xrightarrow{Row 3-Row 1} \begin{bmatrix} 1 & 2 & 0 \\ 0 & -1 & 1 \end{bmatrix} \xrightarrow{Row 3-2} \xrightarrow{Row 1} \begin{bmatrix} 1 & 2 & 0 \\ 0 & -1 & 1 \end{bmatrix} \xrightarrow{Row 3-2} \xrightarrow{Row 1} \begin{bmatrix} 1 & 2 & 0 \\ 0 & -1 & 1 \end{bmatrix} \xrightarrow{Row 3-2} \xrightarrow{Row 1} \begin{bmatrix} 1 & 2 & 0 \\ 0 & -1 & 1 \end{bmatrix} \xrightarrow{Row 3-2} \xrightarrow{Row 1} \begin{bmatrix} 1 & 2 & 0 \\ 0 & -1 & 1 \end{bmatrix} \xrightarrow{Row 3-2} \xrightarrow{Row 1} \begin{bmatrix} 1 & 2 & 0 \\ 0 & -1 & 1 \end{bmatrix} \xrightarrow{Row 3-2} \xrightarrow{Row 1} \xrightarrow{Row 1$$

(b) I has 0's off diagonal: $\vec{q}_i \vec{q}_j = 0$ if $i \neq j$.

(c)
$$Q = \begin{cases} \cos \theta & q_{12} \\ -q_{21} & q_{22} \end{cases}$$
 $\cos^2 \theta + q_{21}^2 = 1 \rightarrow q_{21} = \pm \sqrt{1-\cos^2 \theta}$ = $\pm \sin \theta$

With Then $q_{12}\cos\theta\pm q_{22}\sin\theta=0$ can take 912=5in 0, 922=7cos 0

One example:
$$Q = \begin{bmatrix} 2in \theta - \cos \theta \end{bmatrix}$$
 Another: $\begin{bmatrix} \cos \theta & \sin \theta \end{bmatrix}$

$$\frac{1}{2}A = \frac{1}{2}\begin{bmatrix} 2 & -2 \\ 2 & -2 \end{bmatrix} = \begin{bmatrix} 1 & -1 \\ -1 & -1 \end{bmatrix}, \quad A = \begin{bmatrix} -2 & 2 \\ -2 & 2 \end{bmatrix}$$

$$2^{1/2} + 2^{1/2} + 1^{1/2} + 1^{1/2} = 5$$

 5 mallest subspace = 5 pan $(2^{2} - 2) = 5$ et of all $(2^{2} - 2) = (2c - 2c)$
 $(2^{2} - 2) = (2c - 2c)$

$$3.1.10$$
 (a) Subspace : (ontains $0 = (0,0,0)$ (since $0 = 0$)

(b) Not a subspace:
$$\vec{b} = (1,0,0)$$
 is in the set, but $2 \cdot (1,0,0) = (2,0,0)$ is not (not closed under scalar multiplication, for example)

(c) Not a subspace:
$$(1,0,1)$$
 and $(0,1,0)$ are in the set, but $(1,0,1)+(0,1,0)=(1,1,1)$ is not (not closed under addition)

(e) Subspace: We could check the 3 conditions, or we could notice this set = all
$$\begin{bmatrix} b_1 \\ b_2 \\ -b_1-b_2 \end{bmatrix}$$
 = all $b_1 \begin{bmatrix} 1 \\ 0 \end{bmatrix} + b_2 \begin{bmatrix} 0 \\ 1 \end{bmatrix} =$

$$= span \left(\begin{bmatrix} 1 \\ 2 \end{bmatrix}, \begin{bmatrix} 2 \\ -1 \end{bmatrix} \right), a subspace.$$

(4) Not a subspace:
$$(1,2,3)$$
 is in the set, but $-1\cdot(1,2,3) = -(-1,-2,-3)$ is not (not closed under scalar multiplication)

