

## CS140 Homework 8[10 pts]

Due 11.10am Thursday February 28, 2019

### Problem 1 [6]

Determine the big-O expression for each of the following  $T(N)$  functions:

- (a)  $T(N) = 2N + N(N + 3)$
- (b)  $T(N) = 5$
- (c)  $T(N) = N + \log N^2$
- (d)  $T(N) = N(2 + \log N)$
- (e)  $T(N) = \log(2N)$
- (f)  $T(N) = 2N + N^2 + 2^N$

### Problem 2 [2]

Given an array list, determine following big-O costs:

- (a) Worst case cost associated with finding the  $i^{\text{th}}$  element.
- (b) Average cost for checking if a specific data value is present. All locations are equally likely.

### Problem 3 [2]

Given a linked list, determine following big-O costs:

- (a) Worst case cost associated with finding the  $i^{\text{th}}$  element.
- (b) Average cost for checking if a specific data value is present. All locations are equally likely.

### Problem 4 [Difficult -- Bragging rights only]

The big-O cost for executing the for-loop shown below is  $O(\sqrt{N}) = O(N^{1/2})$ . Give simple mathematical explanations why this is quadratically faster than  $O(N)$ , but exponentially slower than  $O(\log N)$ .

```
bool isprime(int N) {
    if (N<=1) return false;
    for (int i=2; i*i <= N; i++)
        if (number % i == 0) return false;
    return true;
};
```