

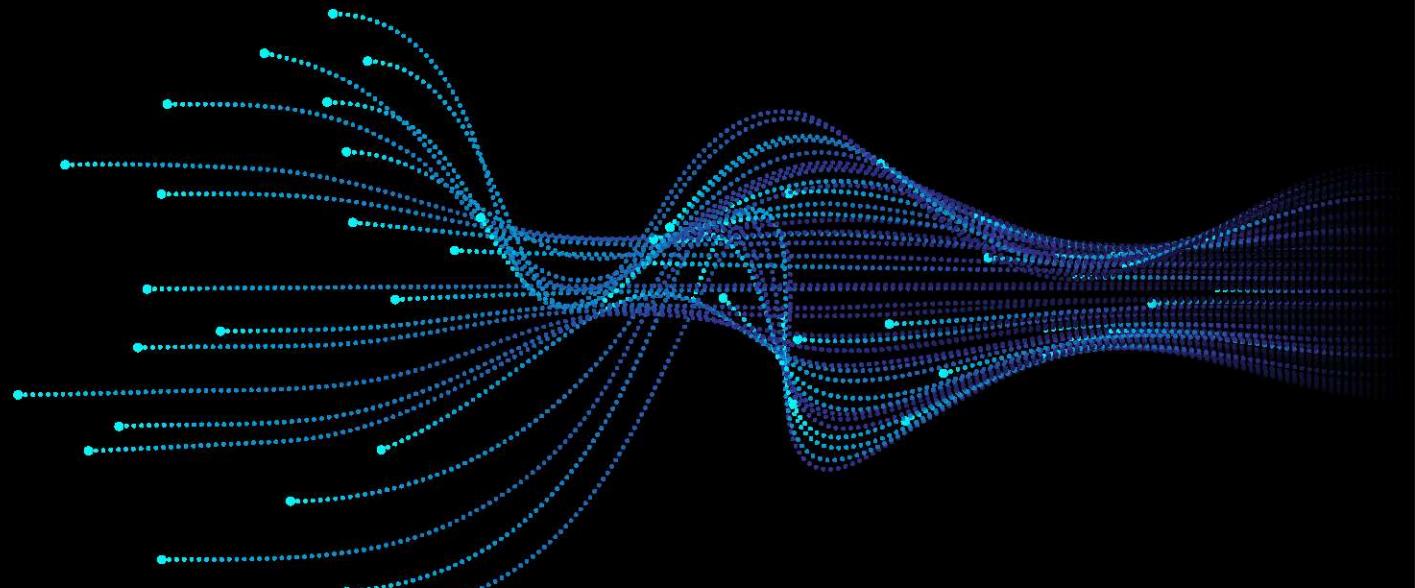
# Cheat Sheets for AI

## Neural Networks, Machine Learning, DeepLearning & Big Data

**The Most Complete List  
of Best AI Cheat Sheets**

BecomingHuman.AI

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## Data Science with Python

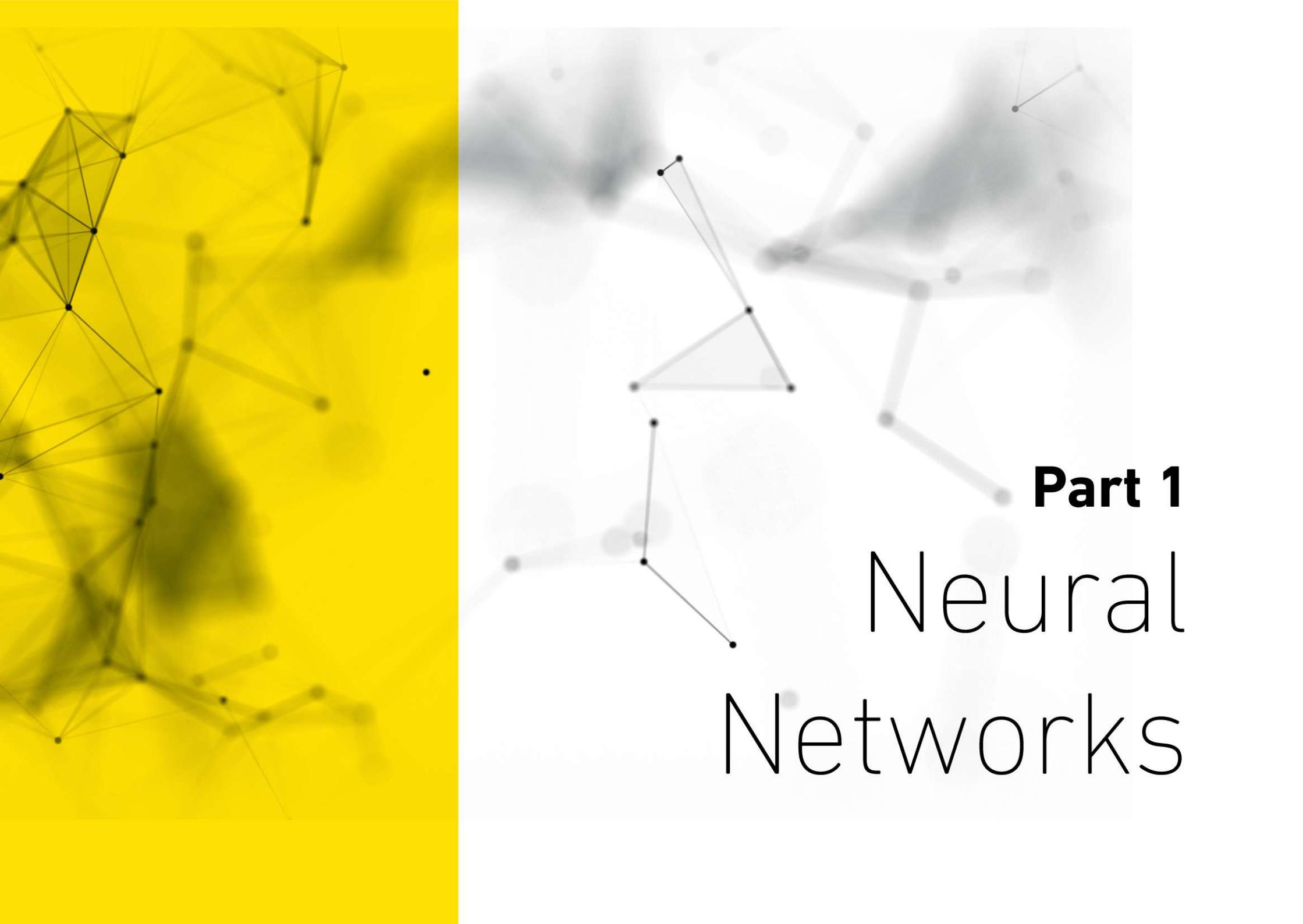
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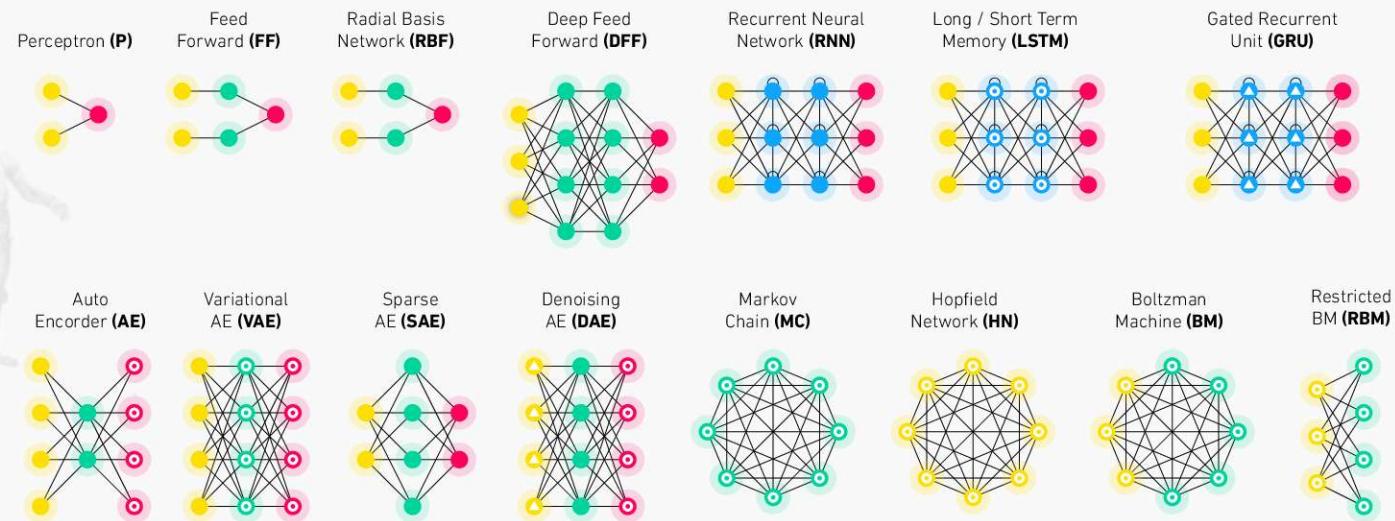
# Part 1

# Neural

# Networks

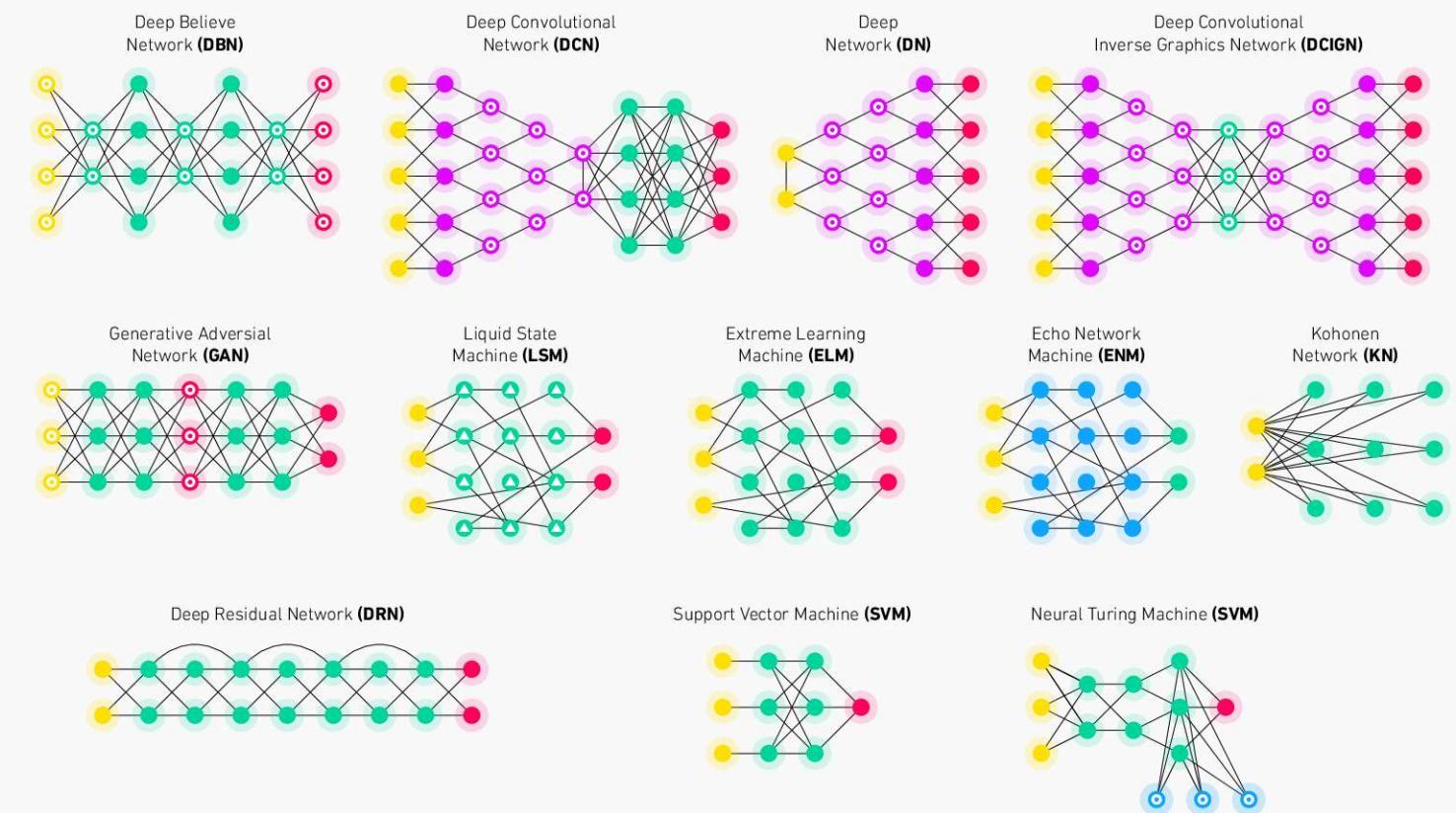
# Neural Networks Basic Cheat Sheet

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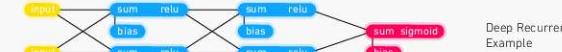
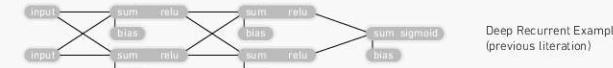
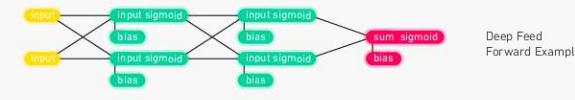
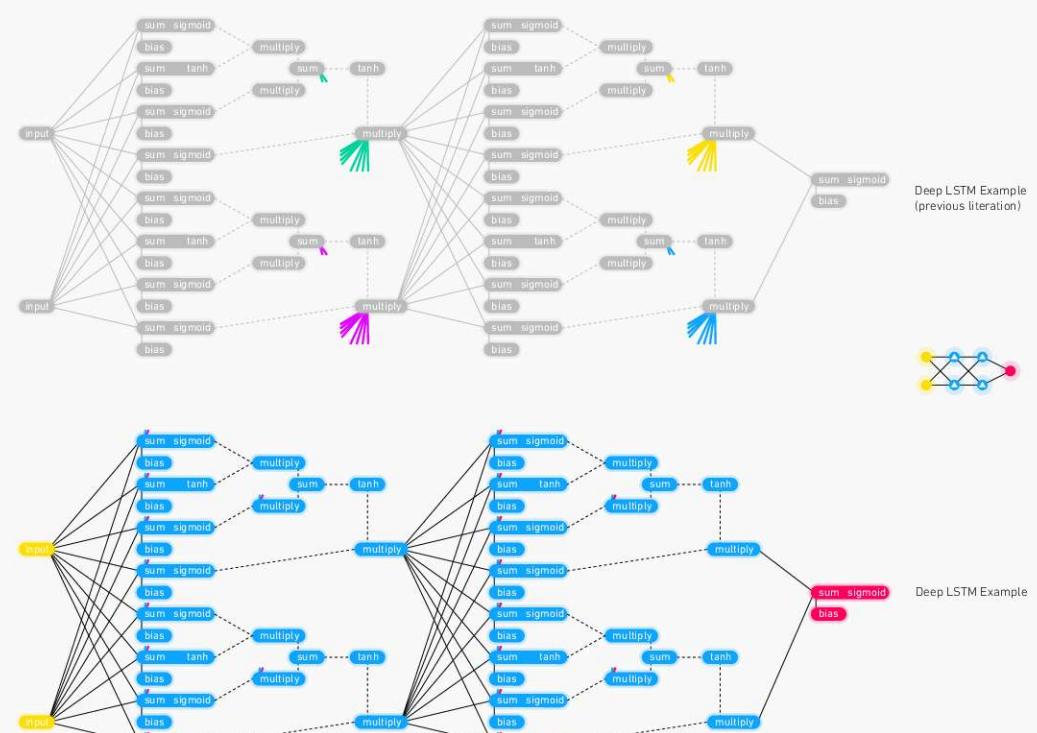
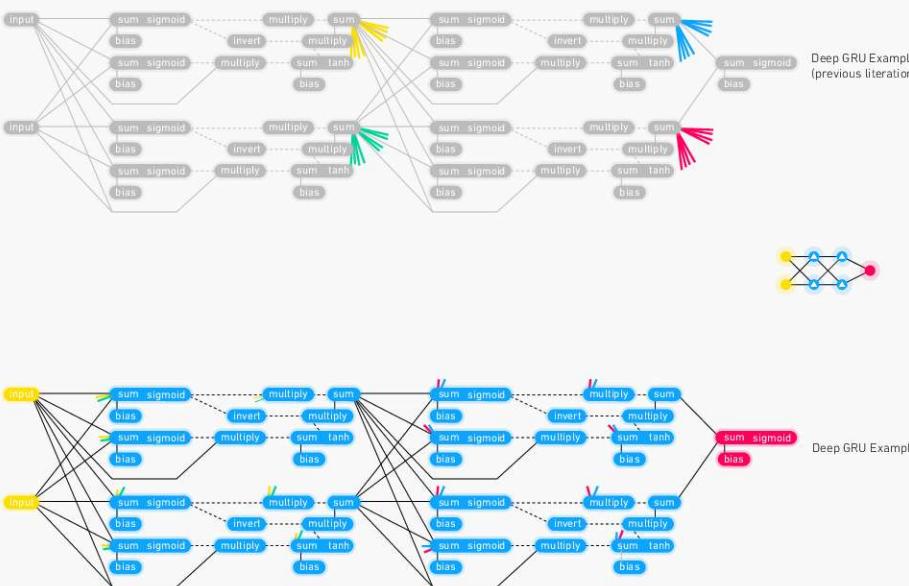
## Index

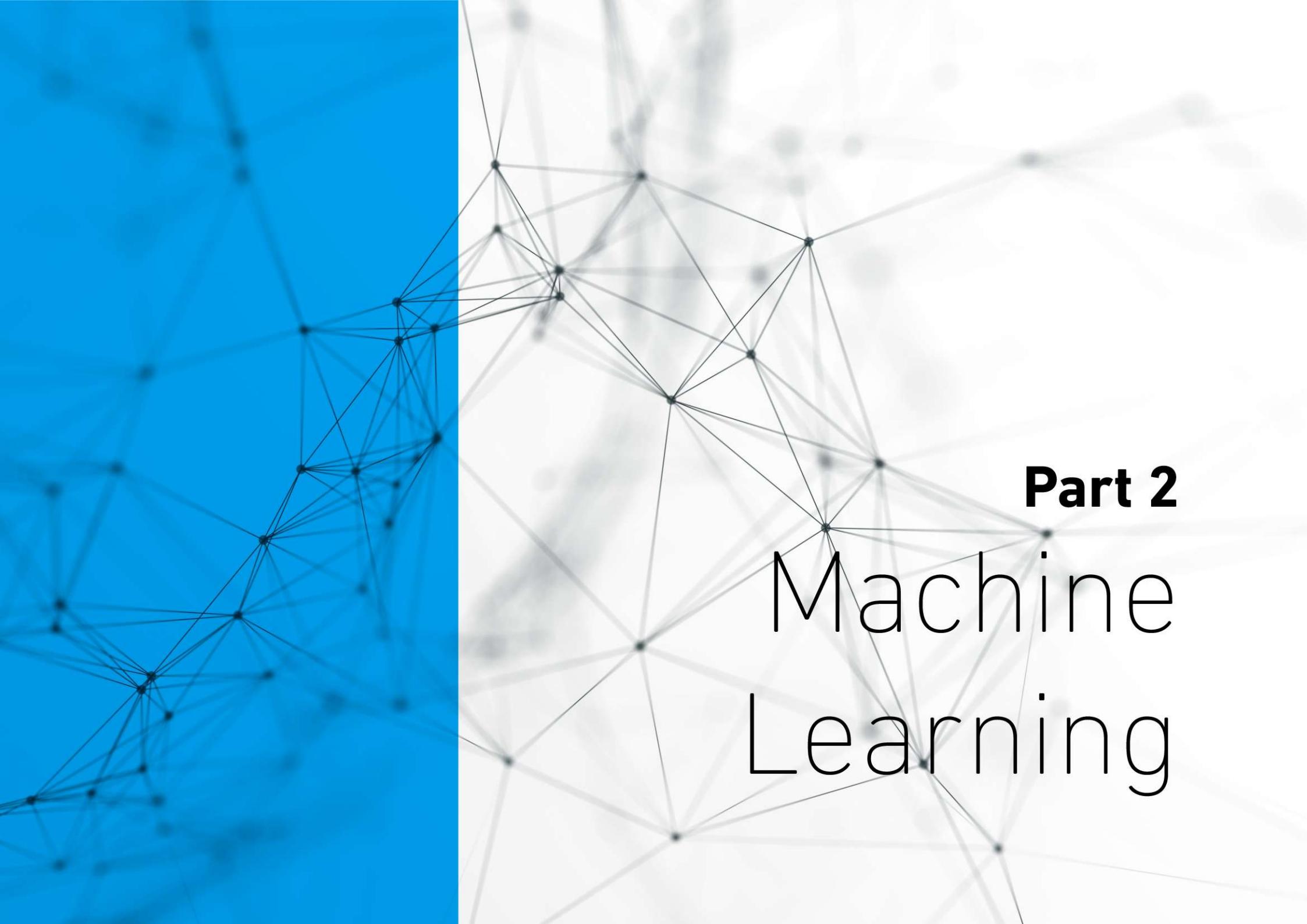
- Backfed Input Cell
- Input Cell
- △ Noisy Input Cell
- Hidden Cell
- Probabilistic Hidden Cell
- △ Spiking Hidden Cell
- Output Cell
- Match Input Output Cell
- Recurrent Cell
- Memory Cell
- △ Different Memory Cell
- Kernel
- Convolutional or Pool



# Neural Networks Graphs Cheat Sheet

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The background of the slide features a complex network graph composed of numerous small, semi-transparent black dots connected by thin gray lines, creating a sense of data connectivity and structure. The graph is divided into two main vertical sections: a blue-tinted section on the left and a white section on the right.

## **Part 2**

# Machine Learning

# MachineLearning Overview

## MACHINE LEARNING IN EMOJI

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#### SUPERVISED

#### UNSUPERVISED

#### REINFORCEMENT

#### BASIC REGRESSION

##### LINEAR

`linear_model.LinearRegression()`

Lots of numerical data



##### LOGISTIC

`linear_model.LogisticRegression()`

Target variable is categorical



#### CLUSTER ANALYSIS

##### K-MEANS

`cluster.KMeans()`

Similar datum into groups based on centroids



##### ANOMALY DETECTION

`covariance.EllipticalEnvelope()`

Finding outliers through grouping



#### CLASSIFICATION

##### NEURAL NET

`neural_network.MLPClassifier()`

Complex relationships. Prone to overfitting  
Basically magic.



##### K-NN

`neighbors.KNeighborsClassifier()`

Group membership based on proximity



##### DECISION TREE

`tree.DecisionTreeClassifier()`

If/then/else. Non-contiguous data.  
Can also be regression.



##### RANDOM FOREST

`ensemble.RandomForestClassifier()`

Find best split randomly  
Can also be regression



##### SVM

`svm.SVC()` `svm.LinearSVC()`

Maximum margin classifier. Fundamental Data Science algorithm



##### NAIVE BAYES

`GaussianNB()` `MultinomialNB()` `BernoulliNB()`

Updating knowledge step by step with new info



#### FEATURE REDUCTION

##### T-DISTRIB STOCHASTIC NEIB EMBEDDING

`manifold.TSNE()`



Visual high dimensional data. Convert similarity to joint probabilities

##### PRINCIPLE COMPONENT ANALYSIS

`decomposition.PCA()`



Distill feature space into components that describe greatest variance

##### CANONICAL CORRELATION ANALYSIS

`decomposition.CCA()`



Making sense of cross-correlation matrices

##### LINEAR DISCRIMINANT ANALYSIS

`lda.LDA()`



Linear combination of features that separates classes

#### OTHER IMPORTANT CONCEPTS

##### BIAS VARIANCE TRADEOFF

##### UNDERFITTING / OVERFITTING

##### INERTIA

##### ACCURACY FUNCTION $(TP+TN) / (P+N)$

##### Precision Function `manifold.TSNE()`

##### SPECIFICITY FUNCTION $TN / (FP+TN)$

##### SENSITIVITY FUNCTION $TP / (TP+FN)$

# Cheat-Sheet Skicit learn Phyton For Data Science

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## Skicit Learn

Skicit Learn is an open source Phyton library that implements a range if machine learning ,processing, cross validation and visualization algorithm using a unified

### A basic Example

```
>>> from sklearn import neighbors, datasets, preprocessing
>>> from sklearn.cross_validation import train_test_split
>>> from sklearn.metrics import accuracy_score
>>> iris = datasets.load_iris() >>> X, y = iris.data[:, :2], iris.target
>>> Xtrain, Xtest, y_train, y_test = train_test_split(X, y, random_state=33)
>>> scaler = preprocessing.StandardScaler().fit(X_train)
>>> X_train = scaler.transform(X_train)
>>> X_test = scaler.transform(X_test)
>>> knn = neighbors.KNeighborsClassifier(n_neighbors=5)
>>> knn.fit(X_train, y_train)
>>> y_pred = knn.predict(X_test)
>>> accuracy_score(y_test, y_pred)
```

## Prediction

### Supervised Estimators

```
>>> y_pred = svc.predict(np.random.rand(2,5))
>>> y_pred = lr.predict(X_test)
>>> y_pred = knn.predict_proba(X_test)
```

Predict labels  
Predict labels  
Estimate probability of a label

### Unsupervised Estimators

```
>>> y_pred = k_means.predict(X_test)
```

Predict labels in clustering algos

## Loading the Data

Your data needs to be nmueric and stored as NumPy arrays or SciPy sparse matric. other types that they are convertible to numeric arrays, such as Pandas Dataframe, are also acceptable

```
>>> import numpy as np >> X = np.random.random((10,5))
>>> y = np.array(['PH', 'IM', 'F', 'M', 'F', 'NI', 'tv', 'F', 'F'])
>>> X[X < 0.7] = 0
```

## Preprocessing The Data

### Standardization

```
>>> from sklearn.preprocessing import StandardScaler
>>> scaler = StandardScaler().fit(X_train)
>>> standardized_X = scaler.transform(X_train)
>>> standardized_X_test = scaler.transform(X_test)
```

### Normalization

```
>>> from sklearn.preprocessing import Normalizer
>>> scaler = Normalizer().fit(X_train)
>>> normalized_X = scaler.transform(X_train)
>>> normalized_X_test = scaler.transform(X_test)
```

### Binarization

```
>>> from sklearn.preprocessing import Binarizer
>>> binarizer = Binarizer(threshold=0.0).fit(X)
>>> binary_X = binarizer.transform(X)
```

### Encoding Categorical Features

```
>>> from sklearn.preprocessing import Imputer
>>> imp = Imputer(missing_values=0, strategy='mean', axis=0)
>>> imp.fit_transform(X_train)
```

### Imputing Missing Values

```
>>> from sklearn.preprocessing import Imputer
>>> imp = Imputer(missing_values=0, strategy='mean', axis=0)
>>> imp.fit_transform(X_train)
```

### Generating Polynomial Features

```
>>> from sklearn.preprocessing import PolynomialFeatures
>>> poly = PolynomialFeatures(5)
>>> poly.fit_transform(X)
```

## Evaluate Your Model's Performance

### Classification Metrics

#### Accuracy Score

```
>>> from sklearn.metrics import classification_report
>>> print(classification_report(y_test, y_pred))
```

Estimator score method  
Metric scoring functions

#### Classification Report

```
>>> from sklearn.metrics import confusion_matrix
>>> print(confusion_matrix(y_test, y_pred))
```

Precision, recall, f1-score and support

#### Confusion Matrix

```
>>> from sklearn.metrics import mean_absolute_error
>>> y_true = [3, -0.5, 2]
>>> mean_absolute_error(y_true, y_pred)
```

### Regression Metrics

#### Mean Absolute Error

```
>>> from sklearn.metrics import mean_squared_error
>>> mean_squared_error(y_true, y_pred)
```

#### Mean Squared Error

```
>>> from sklearn.metrics import r2_score
>>> r2_score(y_true, y_pred)
```

### Clustering Metrics

#### Adjusted Rand Index

```
>>> from sklearn.metrics import adjusted_rand_score
>>> adjusted_rand_score(y_true, y_pred)
```

#### Homogeneity

```
>>> from sklearn.metrics import homogeneity_score
>>> homogeneity_score(y_true, y_pred)
```

#### V-measure

```
>>> from sklearn.metrics import v_measure_score
>>> metrics.v_measure_score(y_true, y_pred)
```

### Cross-Validation

```
>>> from sklearn.cross_validation import cross_val_score
>>> print(cross_val_score(knn, X_train, y_train, cv=4))
>>> print(cross_val_score(lr, X, y, cv=2))
```

## Model Fitting

### Supervised learning

```
>>> lr.fit(X, y)
>>> knn.fit(X_train, y_train)
>>> svc.fit(X_train, y_train)
```

Fit the model to the data

### Unsupervised Learning

```
>>> k_means.fit(X_train)
>>> pca_model = pca.fit_transform(X_train)
```

Fit the model to the data  
Fit to data, then transform it

## Create Your Model

### Supervised Learning Estimators

#### Linear Regression

```
>>> from sklearn.linear_model import LinearRegression
>>> lr = LinearRegression(normalize=True)
```

#### Support Vector Machines (SVM)

```
>>> from sklearn.svm import SVC
>>> svc = SVC(kernel='linear')
```

#### Naive Bayes

```
>>> from sklearn.naive_bayes import GaussianNB
>>> gnb = GaussianNB()
```

#### KNN

```
>>> from sklearn import neighbors
>>> knn = neighbors.KNeighborsClassifier(n_neighbors=5)
```

### Unsupervised Learning Estimators

#### Principal Component Analysis (PCA)

```
>>> from sklearn.decomposition import PCA
>>> pca = PCA(n_components=0.95)
```

#### K Means

```
>>> from sklearn.cluster import KMeans
>>> k_means = KMeans(n_clusters=3, random_state=0)
```

## Training And Test Data

```
>>> from sklearn.cross_validation import train_test_split
>>> X_train, Xtest, y_train, y_test = train_test_split(X,
... random_state=0)
```

## Tune Your Model

### Grid Search

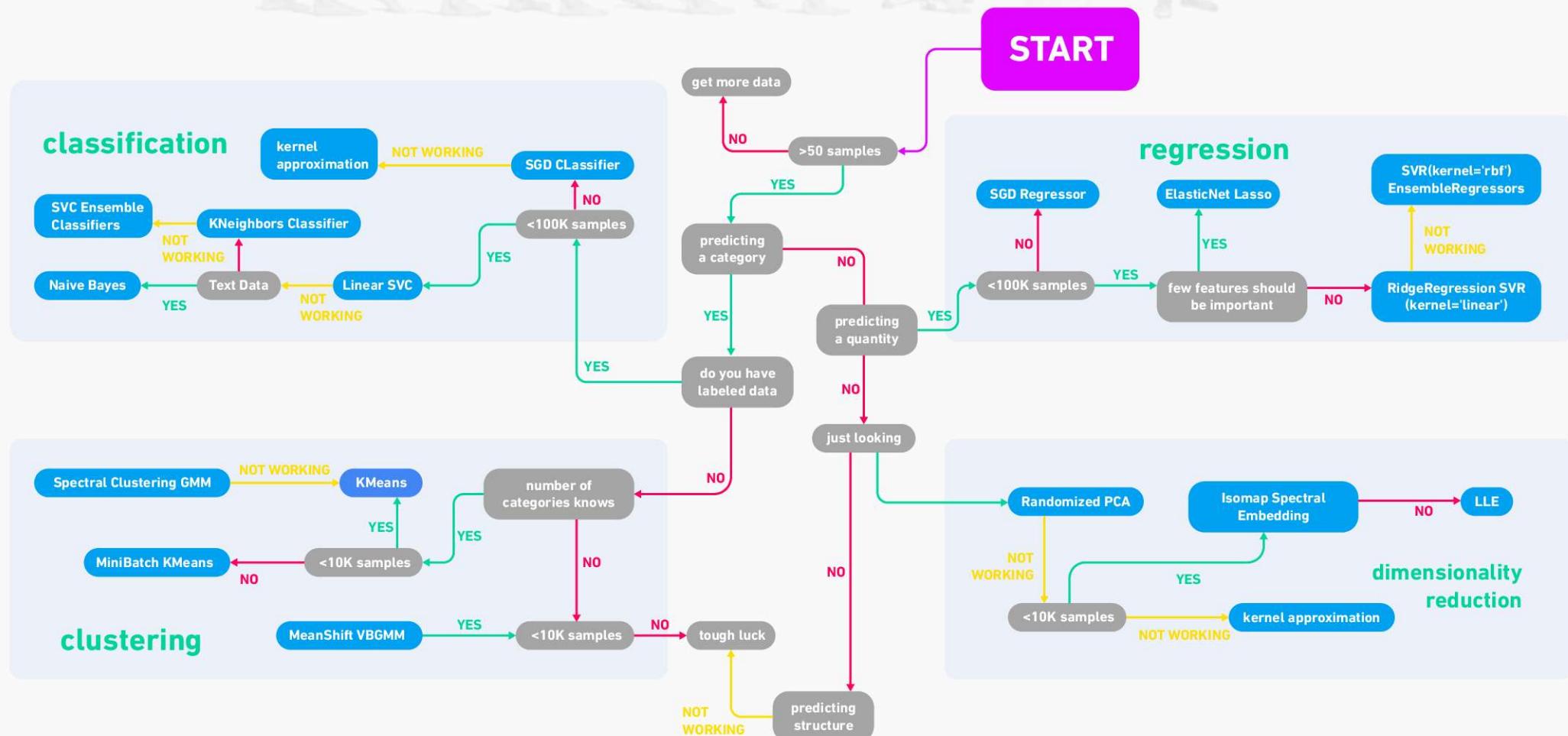
```
>>> from sklearn.grid_search import GridSearchCV
>>> params = {'n_neighbors': np.arange(1,3),
... 'metric': ['euclidean', 'cityblock']}
>>> grid = GridSearchCV(estimator=knn,
... param_grid=params)
>>> grid.fit(X_train, y_train)
>>> print(grid.best_score_)
>>> print(grid.best_estimator_.n_neighbors)
```

### Randomized Parameter Optimization

```
>>> from sklearn.grid_search import RandomizedSearchCV
>>> params = {'n_neighbors': range(1,5),
... 'weights': ['uniform', 'distance']}
>>> rsearch = RandomizedSearchCV(estimator=knn,
... param_distributions=params,
... cv=4,
... n_iter=8,
... random_state=5)
>>> rsearch.fit(X_train, y_train)
>>> print(rsearch.best_score_)
```

# Skicit-learn Algorithm

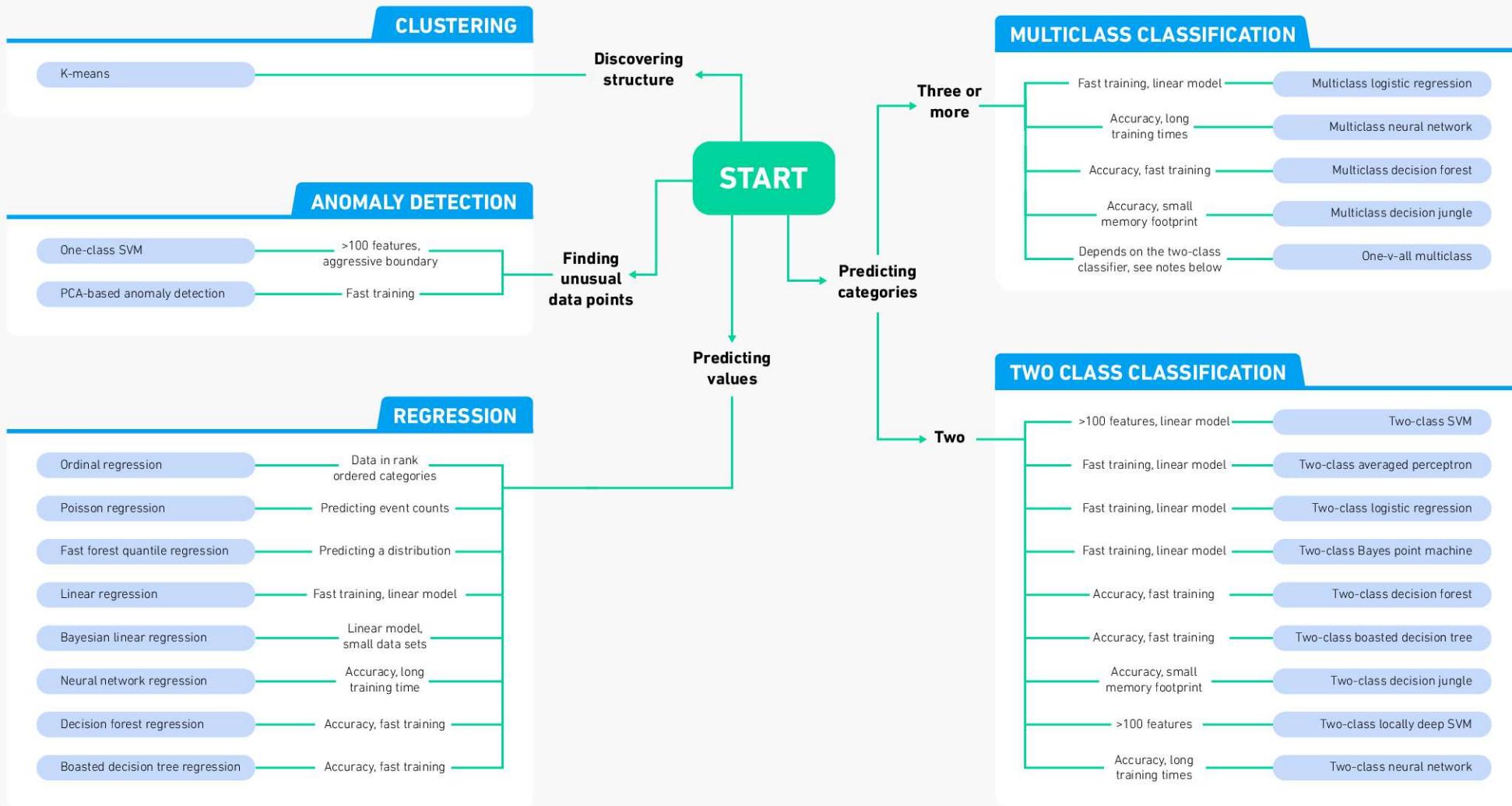
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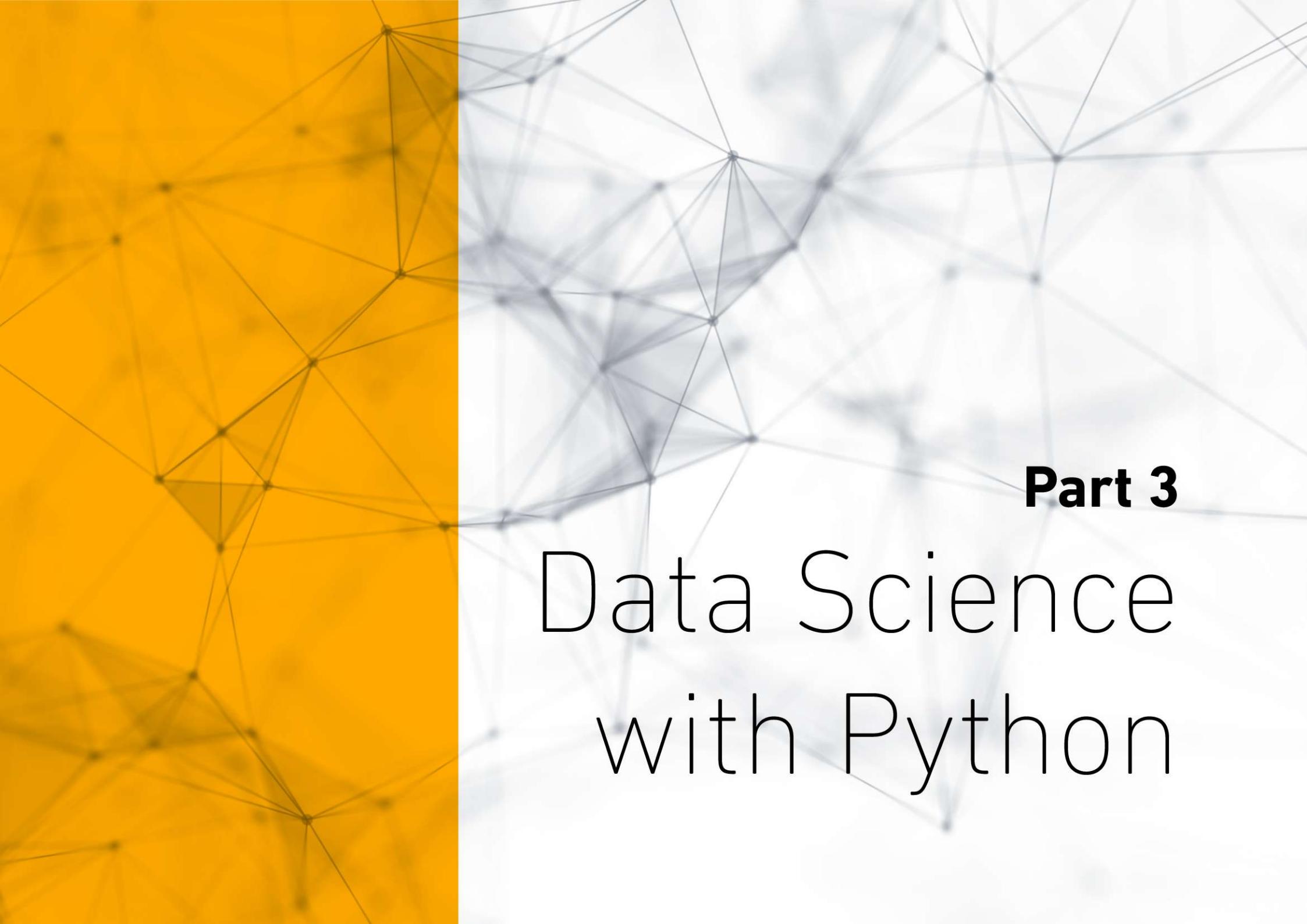


# Algorithm Cheat Sheet

## BecomingHuman.AI

This cheat sheet helps you choose the best Azure Machine Learning Studio algorithm for your predictive analytics solution. Your decision is driven by both the nature of your data and the question you're trying to answer.



The background features a complex network graph composed of numerous small, semi-transparent grey dots connected by thin grey lines. A vertical bar on the left side of the image is a solid, vibrant yellow color, providing a stark contrast to the white background and the grey network.

## **Part 3**

# Data Science with Python

# Tensor Flow Cheat Sheet

## BecomingHuman.AI



In May 2017 Google announced the second-generation of the TPU, as well as the availability of the TPUs in Google Compute Engine.[12] The second-generation TPUs deliver up to 180 teraflops of performance, and when organized into clusters of 64 TPUs provide up to 11.5 petaflops.

## Info

### TensorFlow

TensorFlow™ is an open source software library created by Google for numerical computation and large scale computation. Tensorflow bundles together Machine Learning, Deep learning models and frameworks and makes them useful by way of common metaphor.

### Keras

Keras is an open sourced neural networks library, written in Python and is built for fast experimentation via deep neural networks and modular design. It is capable of running on top of TensorFlow, Theano, Microsoft Cognitive Toolkit, or PlaidML.

### Skflow

Scikit Flow is a high level interface base on tensorflow which can be used like sklearn. You can build your own model on your own data quickly without rewriting extra code.provides a set of high level model classes that you can use to easily integrate with your existing Scikit-learn pipeline code.

## Installation

### How to install new package in Python

```
pip install <package-name>
```

Example: pip install requests

### How to install tensorflow?

```
device = 'cpu/gpu'
python_version = cp27/cp34
sudo pip install
https://storage.googleapis.com/tensorflow/linux/$device/tensorflow-0.8.0-$python_version-none-linux_x86_64.whl
sudo pip install
```

### How to install Skflow

```
pip install sklearn
```

### How to install Keras

```
pip install keras
update ~/keras/keras.json - replace "theano" by "tensorflow"
```

## Helpers

### Python helper Important functions

```
type(object)
Get object type

help(object)
Get help for object (list of available methods, attributes, signatures and so on)

dir(object)
Get list of object attributes (fields, functions)

str(object)
Transform an object to string object?
Shows documentations about the object

globals()
Return the dictionary containing the current scope's global variables.

locals()
Update and return a dictionary containing the current scope's local variables.

id(object)
Return the identity of an object. This is guaranteed to be unique among simultaneously existing objects.

import_builtin_
dir_builtin_
Other built-in functions
```

## Tensor Flow

### Main classes

```
tf.Graph()
tf.Operation()
tf.Tensor()
tf.Session()
```

### Some useful functions

```
tf.get_default_session()
tf.get_default_graph()
tf.reset_default_graph()
ops.reset_default_graph()
tf.device('/cpu:0')
tf.name_scope(value)
tf.convert_to_tensor(value)
```

### TensorFlow Optimizers

```
GradientDescentOptimizer
AdadeltaOptimizer
AdagradOptimizer
MomentumOptimizer
AdamOptimizer
FtrlOptimizer
RMSPropOptimizer
```

### Reduction

```
reduce_sum
reduce_prod
reduce_min
reduce_max
reduce_mean
reduce_all
reduce_any
accumulate_n
```

### Activation functions

```
tf.nn?
relu
relu6
elu
softplus
softsign
dropout
bias_add
sigmoid
tanh
sigmoid_cross_entropy_with_logits
softmax
log_softmax
softmax_cross_entropy_with_logits
sparse_softmax_cross_entropy_with_logits
weighted_cross_entropy_with_logits
etc.
```

## Skflow

### Main classes

```
TensorFlowClassifier
TensorFlowRegressor
TensorFlowDNNClassifier
TensorFlowDNNRegressor
TensorFlowLinearClassifier
TensorFlowLinearRegressor
TensorFlowRNNClassifier
TensorFlowRNNRegressor
TensorFlowEstimator
```

### Each classifier and regressor have following fields

**n\_classes=0** (Regressor), **n\_classes** are expected to be input (Classifier)

```
batch_size=32,
steps=200, // except
TensorFlowRNNClassifier - there is 50
optimizer='Adagrad',
learning_rate=0.1,
```

### Each class has a method fit

```
fit(X, y, monitor=None, logdir=None)
X: matrix or tensor of shape [n_samples, n_features...]. Can be iterator that returns arrays of features. The training input samples for fitting the model.
Y: vector or matrix [n_samples] or [n_samples, n_outputs]. Can be iterator that returns array of targets. The training target values (class labels in classification, real numbers in regression).
monitor: Monitor object to print training progress and invoke early stopping
logdir: the directory to save the log file that can be used for optional visualization.
predict (X, axis=1, batch_size=None)
Args:
X: array-like matrix, [n_samples, n_features...] or iterator.
axis: Which axis to argmax for classification.
By default axis 1 (next after batch) is used. Use 2 for sequence predictions.
batch_size: If test set is too big, use batch size to split it into mini batches. By default the batch_size member variable is used.
Returns:
y: array of shape [n_samples]. The predicted classes or predicted value.
```

# Phyton For Data Science

# Cheat-Sheet Phyton Basic

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## Variables and Data Types

### Variable Assignment

```
>>> x=5  
>>> x  
5
```

### Calculations With Variables

	Sum of two variables
>>> x+2	7
>>> x-2	Subtraction of two variables
3	
>>> x*2	Multiplication of two variables
10	
>>> x**2	Exponentiation of a variable
25	
>>> x%2	Remainder of a variable
1	
>>> x/float(2)	Division of a variable
2.5	

### Calculations With Variables

str()	'5', '3.45', 'True'	Variables to strings
int()	5, 3, 1	Variables to integers
float()	5.0, 1.0	Variables to floats
bool()	True, True, True	Variables to booleans

## Asking For Help

```
>>> help(str)
```

## Lists

Also see NumPy Arrays

```
>>> a = 'is'  
>>> b = 'nice'  
>>> my_list = ['my', 'list', a, b]  
>>> my_list2 = [[4,5,6,7], [3,4,5,6]]
```

### Selecting List Elements

Index starts at 0

**Subset**  
>>> my\_list[1]  
>>> my\_list[-3]  
**Slice**  
>>> my\_list[1:3]  
>>> my\_list[1:-1]  
>>> my\_list[:3]  
>>> my\_list[::]  
**Subset Lists of Lists**  
>>> my\_list2[1][0]  
>>> my\_list2[1][1:2]

Select item at index 1  
Select 3rd last item

Select items at index 1 and 2  
Select items after index 0  
Select items before index 3  
Copy my\_list

my\_list[[list][itemOfList]]

### List Operations

```
>>> my_list + my_list  
['my', 'list', 'is', 'nice', 'my', 'list', 'is', 'nice']  
>>> my_list * 2  
['my', 'list', 'is', 'nice', 'my', 'list', 'is', 'nice']  
>>> my_list2 > 4  
True
```

### List Methods

```
>>> my_list.index('a')  
>>> my_list.count('!')  
>>> my_list.append('!')  
>>> my_list.remove('!')  
>>> del(my_list[0:1])  
>>> my_list.reverse()  
>>> my_list.extend('!')  
>>> my_list.pop(-1)  
>>> my_list.insert(0,'!')  
>>> my_list.sort()
```

Get the index of an item  
Count an item

Append an item at a time  
Remove an item  
Reverse the list  
Append an item  
Remove an item  
Insert an item  
Sort the list

## Numpy Arrays

Also see Lists

```
>>> my_list = [1, 2, 3, 4]  
>>> my_array = np.array(my_list)  
>>> my_2darray =  
np.array([[1,2,3],[4,5,6]])
```

### Selecting Numpy Array Elements

Index starts at 0

**Subset**  
>>> my\_array[1]  
2  
**Slice**  
>>> my\_array[0:2]  
array([1, 2])  
**Subset 2D Numpy arrays**  
>>> my\_2darray[:,0]  
array([1, 4])  
Select item at index 1

Select items at index 0 and 1

my\_2darray[rows, columns]

### Numpy Array Operations

```
>>> my_array > 3  
array([False, False, False, True], dtype=bool)  
>>> my_array * 2  
array([2, 4, 6, 8])  
>>> my_array + np.array([5, 6, 7, 8])  
array([6, 8, 10, 12])
```

### Numpy Array Operations

```
>>> my_array.shape  
Get the dimensions of the array  
>>> np.append(other_array)  
Append items to an array  
>>> np.insert(my_array, 1, 5)  
Insert items in an array  
>>> np.delete(my_array,[1])  
Delete items in an array  
>>> np.mean(my_array)  
Mean of the array  
>>> np.median(my_array)  
Median of the array  
>>> my_array.corrcoef()  
Correlation coefficient  
>>> np.std(my_array)  
Standard deviation
```

## Strings

Also see NumPy Arrays

```
>>> my_string = 'thisStringIsAwesome'  
>>> my_string  
'thisStringIsAwesome'
```

### String Operations

```
>>> my_string * 2  
'thisStringIsAwesomethisStringIsAwesome'  
>>> my_string + 'Innit'  
'thisStringIsAwesomeInnit'  
>>> 'm' in my_string  
True
```

### String Operations

Index starts at 0

```
>>> my_string[3]  
>>> my_string[4:9]
```

### String Methods

>>> my_string.upper()	String to uppercase
>>> my_string.lower()	String to lowercase
>>> my_string.count('w')	Count String elements
>>> my_string.replace('e', 'i')	Replace String elements
>>> my_string.strip()	Strip whitespaces

## Libraries

```
Import libraries  
>>> import numpy  
>>> import numpy as np  
Selective import  
>>> from math import pi
```

## Install Python



Leading open data science platform  
powered by Python



Free IDE that is included  
with Anaconda



Create and share  
documents with live code,  
visualizations, text, ...

# Python For Data Science Cheat Sheet

## PySpark - RDD Basics

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PySpark is the Spark Python API that exposes the Spark programming model to Python.

### Initializing Spark

#### SparkContext

```
>>> from pyspark import SparkContext  
>>> sc = SparkContext(master = 'local[2]')
```

#### Calculations With Variables

```
>>> sc.version          Retrieve SparkContext version  
>>> sc.pythonVer       Retrieve Python version  
>>> sc.master          Master URL to connect to  
>>> str(sc.sparkHome)  Path where Spark is installed on worker nodes  
>>> str(sc.sparkUser)   Retrieve name of the Spark User running SparkContext  
>>> sc.appName          Return application name  
>>> sc.applicationId   Retrieve application ID  
>>> sc.defaultParallelism  Return default level of parallelism  
>>> sc.defaultMinPartitions Default minimum number of partitions for RDDs
```

#### Configuration

```
>>> from pyspark import SparkConf, SparkContext  
>>> conf = (SparkConf()  
...     .setMaster("local")  
...     .setAppName("My app")  
...     .set("spark.executor.memory","1g"))  
>>> sc = SparkContext(conf = conf)
```

#### Configuration

In the PySpark shell, a special interpreter-aware SparkContext is already created in the variable called `sc`.

```
$ ./bin/spark-shell --master local[2]  
$ ./bin/pyspark --master local[4] --py-files code.py
```

Set which master the context connects to with the `--master` argument, and add Python .zip, .egg or .py files to the runtime path by passing a comma-separated list to `--py-files`.

### Loading Data

#### Parallelized Collections

```
>>> rdd = sc.parallelize([(a,7),(a,2),(b,2)])  
>>> rdd2 = sc.parallelize([(a,2),(d,1),(b,1)])  
>>> rdd3 = sc.parallelize(range(100))  
>>> rdd4 = sc.parallelize([(a,"x"),(b,"y"),(c,"z"),  
...     (b,"p"),(c,"r")])
```

#### External Data

Read either one text file from HDFS, a local file system or any Hadoop-supported file system URI with `textFile()`, or read in a directory of text files with `wholeTextFiles()`.

```
>>> textFile = sc.textFile('/my/directory/*.txt')  
>>> textFile2 = sc.wholeTextFiles('/my/directory/')
```

### Retrieving RDD Information

#### Basic Information

```
>>> rdd.getNumPartitions()           List the number of partitions  
>>> rdd.count()                   Count RDD instances  
3  
>>> rdd.countByKey()              Count RDD instances by key  
defaultdict(<type 'int'>,[(b,2),(a,2),(a,7)])  
>>> rdd.countByValue()            Count RDD instances by value  
defaultdict(<type 'int'>,[(b,2),(a,2),(a,7)])  
>>> rdd.collectAsMap()            Return (key,value) pairs as a dictionary  
{(a, 2), (b, 2)}  
>>> rdd3.sum()                   Sum of RDD elements  
4950  
>>> sc.parallelize().isEmpty()    Check whether RDD is empty  
True
```

#### Summary

```
>>> rdd3.max()                  Maximum value of RDD elements  
99  
>>> rdd3.min()                  Minimum value of RDD elements  
0  
>>> rdd3.mean()                 Mean value of RDD elements  
49.5  
>>> rdd3.stdev()                Standard deviation of RDD elements  
28.86070047722118  
>>> rdd3.variance()              Compute variance of RDD elements  
833.25  
>>> rdd3.histogram(3)            Compute histogram by bins  
([0,33.66,99],[33,33,34])  
>>> rdd3.stats()                Summary statistics (count, mean, stdev, max & min)
```

### Reshaping Data

#### Reducing

```
>>> rdd.reduceByKey(lambda x,y: x+y)      Merge the rdd values for  
[(a,9),(b,2)]  
>>> rdd.reduce(lambda a, b: a + b)        Merge the rdd values  
(a,7,a,2,b,2)
```

#### Grouping by

```
>>> rdd3.groupBy(lambda x: x % 2)        Return RDD of grouped values  
.mapValues(list)  
.collect()  
>>> rdd.groupByKey()                    Group rdd by key  
.mapValues(list)  
.collect()  
[(a,[7,2]),(b,[2])]
```

#### Aggregating

```
>>> seqOp = (lambda x,y: (x[0]+y,x[1]+1))  
>>> combOp = (lambda x,y:(x[0]+y[0],x[1]+y[1]))  
>>> rdd3.aggregate((0,0),seqOp,combOp)    Aggregate RDD elements of each partition and then the results  
(4950,100)  
>>> rdd3.aggregateByKey((0,0),seqOp,combOp) Aggregate values of each RDD key  
.collect()  
[(a,(9,2)),(b,(2,1))]  
>>> rdd3.fold(0,add)                     Aggregate the elements of each 4950 partition, and then the results  
4950  
>>> rdd.foldByKey(0,add)                 Merge the values for each key  
.collect()  
[(a,(b,2))]  
>>> rdd3.keyBy(lambda x: x+x).collect() Create tuples of RDD elements by applying a function
```

### Selecting Data

#### Getting

```
>>> rdd.collect()                   Return a list with all RDD elements  
[(a, 7), (a, 2), (b, 2)]  
>>> rdd.take(2)                   Take first 2 RDD elements  
[(a, 7), (a, 2)]  
>>> rdd.first()                  Take first RDD element  
(a, 7)  
>>> rdd.top(2)                   Take top 2 RDD elements  
[(b, 2), (a, 7)]
```

#### Sampling

```
>>> rdd3.sample(False, 0.15, 81).collect()  Return sampled subset of rdd3  
[3,42,31,40,41,42,43,60,76,79,80,86,97]
```

#### Filtering

```
>>> rdd.filter(lambda x: "a" in x)      Filter the RDD  
.collect()  
[(a,7),(a,2)]  
>>> rdd5.distinct().collect()          Return distinct RDD values  
[(a,2),(b,7)]  
>>> rdd.keys().collect()             Return (key,value) RDD's keys  
[(a, 'a'), (b, 'b')]
```

### Iterating

#### Getting

```
>>> def g(x): print(x)  
>>> rdd.foreach(g)  
(a, 7)  
(b, 2)  
(a, 2)
```

### Applying Functions

```
>>> rdd.map(lambda x: x+(x[1]*0))    Apply a function to each RDD element  
[(a,7.7,a),(a,2.2,a),(b,2.2,b)]  
>>> rdd5 = rdd.flatMap(lambda x:  
...     x+(x[1]*x[0]))  
>>> rdd5.collect()                  Apply a function to each RDD element and flatten the result  
[(a,7.7,a),(a,2.2,a),(b,2.2,b)]  
>>> rdd4 = rdd.flatMapValues(lambda x:  
...     collect())  
[(a,'x'),(a,'y'),(a,'z'),(b,'p'),(b,'r')]
```

### Mathematical Operations

```
>>> rdd.subtract(rdd2)              Return each rdd value not contained  
.collect()  
[(b,2),(a,7)]  
>>> rdd2.subtractByKey(rdd)        Return each (key,value) pair of rdd2 with no matching key in rdd2  
.collect()  
[(d, 1)]  
>>> rdd.cartesian(rdd2).collect() Return the Cartesian product of rdd and rdd2
```

### Sort

```
>>> rdd2.sortBy(lambda x: x[1]).collect() Sort RDD by given function  
[(d,1),(b,1),(a,2)]  
>>> rdd2.sortByKey().collect()      RDD by key  
[(a,2),(b,1),(d,1)]
```

### Reshaping Data

```
>>> rdd.repartition(4)             New RDD with 4 partitions  
>>> rdd.coalesce(1)              Decrease the number of partitions in the RDD to 1
```

### Saving

```
>>> rdd.saveAsTextFile('rdd.txt')  
>>> rdd.saveAsHadoopFile ('hdfs://namenodehost/parent/child',  
...     'org.apache.hadoop.mapred.TextOutputFormat')
```

### Stopping SparkContext

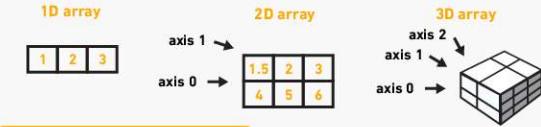
```
>>> sc.stop()
```

### Execution

```
$ ./bin/spark-submit examples/src/main/python/pi.py
```

# NumPy Basics Cheat Sheet

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## Creating Arrays

```
>>> a = np.array([1,2,3])
>>> b = np.array([(1.5,2,3), (4,5,6)], dtype = float)
>>> c = np.array([(1.5,2,3), (4,5,6)], [(3,2,1), (4,5,6)]),dtype = float
```

## Initial Placeholders

>>> np.zeros((3,4))	Create an array of zeros
>>> np.ones((2,3,4),dtype=np.int16)	Create an array of ones
>>> d = np.arange(1.0,25.5)	Create an array of evenly spaced values (step value)
>>> np.linspace(0,2,9)	Create an array of evenly spaced values (number of samples)
>>> e = np.full((2,2),7)	Create a constant array
>>> f = np.eye(2)	Create a 2X2 identity matrix
>>> np.random.random((2,2))	Create an array with random values
>>> np.empty((3,2))	Create an empty array

## I/O

### Saving & Loading On Disk

```
>>> np.save('my_array',a)
>>> np.savetxt('array.npz', a, b)
>>> np.load('my_array.npy')
```

### Saving & Loading Text Files

```
>>> np.loadtxt('myfile.txt')
>>> np.genfromtxt('my_file.csv', delimiter=',')
>>> np.savetxt('myarray.txt', a, delimiter=' ')
```

## Inspecting Your Array

>>> a.shape	Array dimensions
>>> len(a)	Length of array
>>> b.ndim	Number of array dimensions
>>> a.size	Number of array elements
>>> b.dtype	Data type of array elements
>>> b.dtype.name	Name of data type
>>> b.astype(int)	Convert an array to a different type

## Data Types

>>> np.int64	Signed 64-bit integer types
>>> np.float32	Standard double-precision floating point
>>> np.complex	Complex numbers represented by 128 floats
>>> np.bool	Boolean type storing TRUE and FALSE
>>> np.object	Python object type values
>>> np.string_	Fixed-length string type
>>> np.unicode_	Fixed-length unicode type

## Asking For Help

```
>>> np.info(np.ndarray.dtype)
```

## Array Mathematics

### Arithmetic Operations

>>> g = a - b array([-0.5, 0., 0., [-3., -3., -3.]])	Subtraction
>>> np.subtract(a,b)	Subtraction
>>> b + a array([[ 2.5, 4., 6.], [ 5., 7., 9.]])	Addition
>>> np.add(b,a)	Addition
>>> a / b array([[ 0.66666667, 1.], [ 0.25, 0.4, 0.5]])	Division
>>> np.divide(a,b)	Division
>>> a * b array([[ 1.5, 4., 9.], [ 4., 10., 18.]])	Multiplication
>>> np.multiply(a,b)	Multiplication
>>> np.exp(b)	Exponentiation
>>> np.sqrt(b)	Square root
>>> np.sin(a)	Print sines of an array
>>> np.cos(b)	Element-wise cosine
>>> np.log(a)	Element-wise natural logarithm
>>> e.dot(f) array([[ 7., 7.], [ 7., 7.]])	Dot product

### Comparison

>>> a == b array([[ True, True, True], [ False, False, False]], dtype=bool)	Element-wise comparison
>>> a < 2 array([True, False, False], dtype=bool)	Element-wise comparison
>>> np.array_equal(a, b)	Array-wise comparison

### Aggregate Functions

>>> a.sum()	Array-wise sum
>>> a.min()	Array-wise minimum value
>>> b.max(axis=0)	Maximum value of an array row
>>> b.cumsum(axis=1)	Cumulative sum of the elements
>>> a.mean()	Mean
>>> b.median()	Median

## Copying Arrays

>>> h = a.view()	Create a view of the array with the same data
>>> np.copy(a)	Create a copy of the array
>>> h = a.copy()	Create a deep copy of the array

## Sorting Arrays

>>> a.sort()	Sort an array
>>> c.sort(axis=0)	Sort the elements of an array's axis

## Subsetting, Slicing, Indexing

### Subsetting

>>> a[2]	Select the element at the 2nd index
3	
>>> b[1,2]	Select the element at row 1 column 2 (equivalent to b[1][2])
6.0	

### Slicing

>>> a[0,2]	Select items at index 0 and 1
array([1, 2, 3])	
>>> b[0,2,1]	Select items at rows 0 and 1 in column 1
array([[[ 1, 2, 3], [ 4, 5, 6]]])	
>>> b[1:]	Select all items at row 0 (equivalent to b[0:,1,:])
array([[[ 1, 2, 3], [ 4, 5, 6]]])	
>>> c[1,...]	Same as [1,:,:]
array([[[ 3, 2, 1], [ 4, 5, 6]]])	
>>> a[:,1]	Reversed array a
array([[[ 3, 2, 1], [ 4, 5, 6]]])	

### Boolean Indexing

>>> a[a<2]	Select elements from a less than 2
array([1])	

### Fancy Indexing

>>> b[[1, 0, 1, 0], [0, 1, 2, 0]]	Select elements (1,0),(0,1),(1,2) and (0,0)
array([[ 4., 2., 6., 1.5]])	
>>> b[[1, 0, 1, 0]][[0, 1, 2, 0]]	Select a subset of the matrix's rows and columns
array([[ 4., 5., 6., 4.], [ 1.5, 2., 3., 1.5], [ 4., 5., 6., 4.], [ 1.5, 2., 3., 1.5]])	

## Array Manipulation

### Transposing Array

>>> i = np.transpose(b)	Permute array dimensions
>>> i.T	Permute array dimensions

### Changing Array Shape

>>> b.ravel()	Flatten the array
>>> g.reshape(3,-2)	Reshape, but don't change data

### Combining Arrays

>>> np.concatenate((a,d),axis=0)	Concatenate arrays
array([ 1, 2, 3, 10, 15, 20])	
>>> np.vstack((a,b))	Stack arrays vertically (row-wise)
array([[ 1, 2, 3, 1.], [ 4, 5, 6, 1.5], [ 1.5, 2., 3., 1.5], [ 4., 5., 6., 4.], [ 1.5, 2., 3., 1.5]])	
>>> np.r_[e,f]	Stack arrays vertically (row-wise)
>>> np.hstack((e,f))	Stack arrays horizontally (column-wise)
array([[ 7., 7., 1., 0., 1.]])	
>>> np.column_stack((a,d))	Create stacked column-wise arrays
array([[ 1, 2, 3, 10], [ 1, 2, 3, 15], [ 1, 2, 3, 20], [ 4, 5, 6, 10], [ 4, 5, 6, 15], [ 4, 5, 6, 20]])	
>>> np.c_[a,d]	Create stacked column-wise arrays



# Bokeh Cheat Sheet

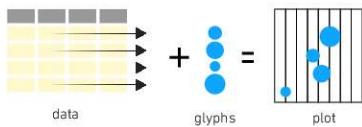
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## Data Types

The Python interactive visualization library Bokeh enables high-performance visual presentation of large datasets in modern web browsers.

Bokeh's mid-level general purpose bokeh.plotting interface is centered around two main components: **data** and **glyphs**.



The basic steps to creating plots with the bokeh.plotting interface are:

1. Prepare some data:  
Python lists, NumPy arrays, Pandas DataFrames and other sequences of values
2. Create a new plot
3. Add renderers for your data, with visual customizations
4. Specify where to generate the output
5. Show or save the results

```
>>> from bokeh.plotting import figure
>>> from bokeh.io import output_file, show
>>> x = [1, 2, 3, 4, 5] step 1
>>> y = [6, 7, 2, 4, 5]
>>> p = figure(title="simple line example", step 2
             x_axis_label=x,
             y_axis_label=y)
>>> p.line(x, y, legend="Temp", line_width=2) step 3
>>> output_file("lines.html") step 4
>>> show(p) step 5
```

## Data

[Also see Lists, NumPy & Pandas](#)

Under the hood, your data is converted to Column Data Sources. You can also do this manually:

```
>>> import numpy as np
>>> import pandas as pd
>>> df = pd.DataFrame(np.array([[33.9, 4.65, 'US'],
                               [32.4, 4.66, 'Asia'],
                               [21.4, 4.109, 'Europe']]),
                     columns=['mpg', 'cyl', 'hp', 'origin'],
                     index=['Toyota', 'Fiat', 'Volvo'])
```

```
>>> from bokeh.models import ColumnDataSource
>>> cds_df = ColumnDataSource(df)
```

## Plotting

```
>>> from bokeh.plotting import figure
>>> p1 = figure(plot_width=300, tools='pan,box_zoom')
>>> p2 = figure(plot_width=300, plot_height=300,
               x_range=(0, 8), y_range=(0, 8))
>>> p3 = figure()
```

## Show or Save Your Plots

```
>>> show(p1) step 1
>>> show(layout) step 2
>>> save(p1) step 3
>>> save(layout) step 4
```

## Renderers & Visual Customizations

### Glyphs



#### Scatter Markers

```
>>> p1.circle(np.array([1,2,3]), np.array([3,2,1]),
             fill_color='white')
>>> p2.square(np.array([1.5,3.5,5.5]), [1,4,3],
             color='blue', size=1)
```



#### Line Glyphs

```
>>> p1.line([1,2,3,4], [3,4,5,6], line_width=2)
>>> p2.multi_line(pd.DataFrame([[1,2,3],[5,6,7]]),
                  pd.DataFrame([[3,4,5],[3,2,1]]),
                  color="blue")
```

### Rows & Columns Layout

#### Rows

```
>>> from bokeh.layouts import row
>>> layout = row(p1,p2,p3)
```

#### Columns

```
>>> from bokeh.layouts import columns
>>> layout = column(p1,p2,p3)
```

#### Nesting Rows & Columns

```
>>> layout = row(column(p1,p2),p3)
```

### Grid Layout

```
>>> from bokeh.layouts import gridplot
>>> row1 = [p1,p2]
>>> row2 = [p3]
>>> layout = gridplot([[p1,p2],[p3]])
```

### Legends

#### Legend Location

```
>>> p.legend.location = 'bottom_left'
```

#### Inside Plot Area

```
>>> p.legend.location = 'inside'
```

#### Outside Plot Area

```
>>> r1 = p2.asterisk(np.array([1,2,3]), np.array([3,2,1]))
>>> r2 = p2.line([1,2,3,4], [3,4,5,6])
>>> legend = Legend(items=[('One', [p1,r1]), ('Two', [r2])], location=(0, -30))
>>> p.add_layout(legend, 'right')
```

### Output

#### Output to HTML File

```
>>> from bokeh.io import output_file, show
>>> output_file("my_bar_chart.html", mode="cdn")
```

#### Notebook Output

```
>>> from bokeh.io import output_notebook, show
>>> output_notebook()
```

#### Standalone HTML

```
>>> from bokeh.embed import file_html
>>> html = file_html(p, CDN, "my_plot")
```

#### Components

```
>>> from bokeh.embed import components
>>> script, div = components(p)
```

### Customized Glyphs



#### Selection and Non-Selection Glyphs

```
>>> p = figure(tools='box_select')
>>> p.circle('mpg', 'cyl', source=cds_df,
             selection_color='red',
             nonselection_alpha=0.1)
```



#### Hover Glyphs

```
>>> hover = HoverTool(tooltips=None, mode='vline')
>>> p3.add_tools(hover)
```



#### Colormapping

```
>>> color_mapper = CategoricalColorMapper(
      factors=['US', 'Asia', 'Europe'],
      palette=['blue', 'red', 'green'])
>>> p3.circle('mpg', 'cyl', source=cds_df,
             color=dict(fields='origin',
                        transform=color_mapper),
             legend='Origin')
```

### Linked Plots

#### Linked Axes

```
>>> p2.x_range = p1.x_range
>>> p2.y_range = p1.y_range
```

#### Linked Brushing

```
>>> p4 = figure(plot_width=100, tools='box_select,lasso_select')
>>> p4.circle('mpg', 'cyl', source=cds_df)
>>> p5 = figure(plot_width=200, tools='box_select,lasso_select')
```

### Tabbed Layout

```
>>> from bokeh.models.widgets import Panel, Tabs
```

```
>>> tab1 = Panel(child=p1, title="tab1")
```

```
>>> tab2 = Panel(child=p2, title="tab2")
```

```
>>> layout = Tabs(tabs=[tab1, tab2])
```

### Legend Orientation

```
>>> p.legend.orientation = "horizontal"
>>> p.legend.orientation = "vertical"
```

### Legend Background & Border

```
>>> p.legend.border_line_color = "navy"
>>> p.legend.background_fill_color = "white"
```

## Statistical Charts With Bokeh

Bokeh's high-level bokeh.charts interface is ideal for quickly creating statistical charts

#### Bar Chart

```
>>> from bokeh.charts import Bar
>>> p = Bar(df, stacked=True, palette=[red, blue])
```

#### Box Plot

```
>>> from bokeh.charts import BoxPlot
>>> p = BoxPlot(df, values='vals', label='cyl',
                legend='bottom_right')
```

#### Histogram

```
>>> from bokeh.charts import Histogram
>>> p = Histogram(df, title='Histogram')
```

#### Scatter Plot

```
>>> from bokeh.charts import Scatter
>>> p = Scatter(df, x='mpg', y='hp',
                marker='square',
                xlabel='Miles Per Gallon',
```

# Keras Cheat Sheet

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**K** Keras is a powerful and easy-to-use deep learning library for Theano and TensorFlow that provides a high-level neural networks API to develop and evaluate deep learning models.

## A Basic Example

```
>>> import numpy as np
>>> from keras.models import Sequential
>>> from keras.layers import Dense
>>> data = np.random.random((1000,100))
>>> labels = np.random.randint(2,size=(1000,1))
>>> model = Sequential()
>>> model.add(Dense(32,
    activation='relu',
    input_dim=100))
>>> model.add(Dense(1, activation='sigmoid'))
>>> model.compile(optimizer='rmsprop',
    loss='binary_crossentropy',
    metrics=['accuracy'])
```

## Data

Also see NumPy, Pandas & Scikit-Learn

Your data needs to be stored as NumPy arrays or as a list of NumPy arrays. Ideally, you split the data in training and test sets, for which you can also resort to the `train_test_split` module of `sklearn.cross_validation`.

## Keras Data Sets

```
>>> from keras.datasets import boston_housing,
    mnist,
    cifar10,
    imdb
>>> (x_train,y_train),(x_test,y_test) = mnist.load_data()
>>> (x_train2,y_train2),(x_test2,y_test2) = boston_housing.load_data()
>>> (x_train3,y_train3),(x_test3,y_test3) = cifar10.load_data()
>>> (x_train4,y_train4),(x_test4,y_test4) = imdb.load_data(num_words=20000)
>>> num_classes = 10
>>> model.fit(data,labels,epochs=10,batch_size=32)
>>> predictions = model.predict(data)
```

## Other

```
>>> from urllib.request import urlopen
>>> data = np.loadtxt(urlopen('http://archive.ics.uci.edu/ml/machine-learning-databases/pima-indians-diabetes/pima-indians-diabetes.data'),delimiter=',')
>>> X = data[:,0:8]
>>> y = data[:,8]
```

## Model Architecture

### Sequential Model

```
>>> from keras.models import Sequential
>>> model = Sequential()
>>> model2 = Sequential()
>>> model3 = Sequential()
```

### Multilayer Perceptron (MLP)

#### Binary Classification

```
>>> from keras.layers import Dense
>>> model.add(Dense(12,
    input_dim=8,
    kernel_initializer='uniform',
    activation='relu'))
>>> model.add(Dense(8,kernel_initializer='uniform',activation='relu'))
>>> model.add(Dense(1,kernel_initializer='uniform',activation='sigmoid'))
```

#### Multi-Class Classification

```
>>> from keras.layers import Dropout
>>> model.add(Dense(512,activation='relu',input_shape=(784,)))
>>> model.add(Dropout(0.2))
>>> model.add(Dense(512,activation='relu'))
>>> model.add(Dropout(0.2))
>>> model.add(Dense(10,activation='softmax'))
```

#### Regression

```
>>> model.add(Dense(64,activation='relu',input_dim=train_data.shape[1]))
>>> model.add(Dense(1))
```

### Convolutional Neural Network (CNN)

```
>>> from keras.layers import Activation,Conv2D,MaxPooling2D,Flatten
>>> model2.add(Conv2D(32,(3,3),padding='same',input_shape=x_train.shape[1:]))
>>> model2.add(Activation('relu'))
>>> model2.add(Conv2D(32,(3,3)))
>>> model2.add(Activation('relu'))
>>> model2.add(MaxPooling2D(pool_size=(2,2)))
>>> model2.add(Dropout(0.25))
>>> model2.add(Conv2D(64,(3,3),padding='same'))
>>> model2.add(Activation('relu'))
>>> model2.add(Conv2D(64,(3,3)))
>>> model2.add(Activation('relu'))
>>> model2.add(MaxPooling2D(pool_size=(2,2)))
>>> model2.add(Dropout(0.25))
>>> model2.add(Flatten())
>>> model2.add(Dense(512))
>>> model2.add(Activation('relu'))
>>> model2.add(Dropout(0.5))
>>> model2.add(Dense(num_classes))
>>> model2.add(Activation('softmax'))
```

### Recurrent Neural Network (RNN)

```
>>> from keras.layers import Embedding,LSTM
>>> model3.add(Embedding(20000,128))
>>> model3.add(LSTM(128,dropout=0.2,recurrent_dropout=0.2))
>>> model3.add(Dense(1,activation='sigmoid'))
```

## Inspect Model

```
>>> model.output_shape
>>> model.summary()
>>> model.get_config()
>>> model.get_weights()
```

**Model output shape**  
**Model summary representation**  
**Model configuration**  
**List all weight tensors in the model**

## Prediction

```
>>> model3.predict(x_test4, batch_size=32)
>>> model3.predict_classes(x_test4,batch_size=32)
```

## Model Training

```
>>> model3.fit(x_train4,
    y_train4,
    batch_size=32,
    epochs=15,
    verbose=1,
    validation_data=(x_test4,y_test4))
```

## Evaluate Your Model's Performance

```
>>> score = model3.evaluate(x_test,
    y_test,
    batch_size=32)
```

## Model Fine-tuning

### Optimization Parameters

```
>>> from keras.optimizers import RMSprop
>>> opt = RMSprop(lr=0.0001, decay=1e-6)
>>> model2.compile(loss='categorical_crossentropy',
    optimizer=opt,
    metrics=[accuracy])
```

### Early Stopping

```
>>> from keras.callbacks import EarlyStopping
>>> early_stopping_monitor = EarlyStopping(patience=2)
>>> model3.fit(x_train4,
    y_train4,
    batch_size=32,
    epochs=15,
    validation_data=(x_test4,y_test4),
    callbacks=[early_stopping_monitor])
```

## Compile Model

### MLP: Binary Classification

```
>>> model.compile(optimizer='adam',
    loss='binary_crossentropy',
    metrics=[accuracy])
```

### MLP: Multi-Class Classification

```
>>> model.compile(optimizer='rmsprop',
    loss='categorical_crossentropy',
    metrics=[accuracy])
```

### MLP: Regression

```
>>> model.compile(optimizer='rmsprop',
    loss='mse',
    metrics=[mae])
```

## Recurrent Neural Network

```
>>> model3.compile(loss='binary_crossentropy',
    optimizer='adam',
    metrics=[accuracy])
```

## Save/ Reload Models

```
>>> from keras.models import load_model
>>> model3.save('model.h5')
>>> my_model = load_model('my_model.h5')
```

## Preprocessing

### Sequence Padding

```
>>> from keras.preprocessing import sequence
>>> x_train4 = sequence.pad_sequences(x_train4,maxlen=80)
>>> x_test4 = sequence.pad_sequences(x_test4,maxlen=80)
```

### One-Hot Encoding

```
>>> from keras.utils import to_categorical
>>> Y_train = to_categorical(y_train, num_classes)
>>> Y_test = to_categorical(y_test, num_classes)
>>> Y_train3 = to_categorical(y_train3, num_classes)
>>> Y_test3 = to_categorical(y_test3, num_classes)
```

### Train and Test Sets

```
>>> from sklearn.model_selection import train_test_split
>>> X_train5,X_test5,y_train5,y_test5 = train_test_split(X,
    y,
    test_size=0.33,
    random_state=42)
```

### Standardization/Normalization

```
>>> from sklearn.preprocessing import StandardScaler
>>> scaler = StandardScaler().fit(x_train2)
>>> standardized_X = scaler.transform(x_train2)
>>> standardized_X_test = scaler.transform(x_test2)
```

# Pandas Basics

## Cheat Sheet

BecomingHuman.AI



Use the following import convention: >>> import pandas as pd

The Pandas library is built on NumPy and provides easy-to-use data structures and data analysis tools for the Python programming language.

### Pandas Data Structures

#### Series

A one-dimensional labeled array capable of holding any data type

```
>>> s = pd.Series([3, -5, 7, 4], index=['a', 'b', 'c', 'd'])
```

#### Data Frame

A two-dimensional labeled data structure with columns of potentially different types

```
>>> data = {'Country': ['Belgium', 'India', 'Brazil'],
   ...: 'Capital': ['Brussels', 'New Delhi', 'Brasilia'],
   ...: 'Population': [11190846, 1303171035, 207847528]}
>>> df = pd.DataFrame(data,
   ...: columns=['Country', 'Capital', 'Population'])
```

### Dropping

```
>>> s.drop(['a', 'c'])
>>> df.drop('Country', axis=1)
```

Drop values from rows (axis=0)  
Drop values from columns(axis=1)

### Sort & Rank

```
>>> df.sort_index()
>>> df.sort_values(by='Country')
>>> df.rank()
```

Sort by labels along an axis  
Sort by the values along an axis  
Assign ranks to entries

### Retrieving Series/ DataFrame Information

```
>>> df.shape
>>> df.index
>>> df.columns
>>> df.info()
>>> df.count()
```

(rows,columns)  
Describe index  
Describe DataFrame columns  
Info on DataFrame  
Number of non-NA values

### Summary

```
>>> df.sum()
>>> df.cumsum()
>>> df.min()/df.max()
>>> df.idxmin()/df.idxmax()
>>> df.describe()
>>> df.mean()
>>> df.median()
```

Sum of values  
Cummulative sum of values  
Minimum/maximum values  
Minimum/Maximum index value  
Summary statistics  
Mean of values  
Median of values

### Selection

Also see NumPy Arrays

#### Getting

```
>>> s[b]
>>> df[1:]
>>> df[['Country', 'Population']]
1  India    New Delhi  1303171035
2  Brazil   Brasilia  207847528
```

Get one element

Get subset of a DataFrame

#### Selecting, Boolean Indexing & Setting

##### By Position

```
>>> df.loc[[0],[0]]
>>> df.loc[[0],['Country']]
>>> df.at[0,'Country']
```

Select single value by row & column

##### By Label

```
>>> df.loc[[0], 'Belgium']
>>> df.at[0, 'Country']
```

Select single value by row & column labels

##### By Label/Position

```
>>> df.ix[2]
>>> df.ix[2, 'Country']
>>> df.ix[2, 'Population']
>>> df.ix[[0], 'Capital']
>>> df.ix[[0], 'Brussels']
>>> df.ix[[0], 'New Delhi']
>>> df.ix[[0], 'Brasilia']
>>> df.ix[[0], 'Brazil']
```

Select single row of subset of rows

##### Select a single column of subset of columns

```
>>> df.ix[[0], 'Capital']
>>> df.ix[[0], 'Brussels']
>>> df.ix[[0], 'New Delhi']
```

Select rows and columns

##### Boolean Indexing

```
>>> s[s > 1]
>>> s[(s < -1) | (s > 2)]
>>> df[df['Population'] > 1200000000]
```

Series s where value is not > 1

s where value is <-1 or > 2

Use filter to adjust DataFrame

##### Setting

```
>>> s['a'] = 6
```

Set index a of Series s to 6

### Asking For Help

```
>>> help(pd.Series.loc)
```

### Applying Functions

```
>>> f = lambda x: x**2
>>> df.apply(f)
>>> df.applymap(f)
```

Apply function

Apply function element-wise

### Data Alignment

#### Internal Data Alignment

NA values are introduced in the indices that don't overlap:

```
>>> s3 = pd.Series([7, -2, 3], index=['a', 'c', 'd'])
>>> s = s3
a 10.0
b NaN
c 5.0
d 7.0
```

#### Arithmetic Operations with Fill Methods

You can also do the internal data alignment yourself with the help of the fill methods:

```
>>> s.add(s3, fill_value=0)
a 10.0
b -5.0
c 5.0
d 7.0
>>> s.sub(s3, fill_value=2)
>>> s.div(s3, fill_value=4)
```

### I/O

#### Read and Write to CSV

```
>>> pd.read_csv('file.csv', header=None, nrows=5)
>>> df.to_csv('myDataFrame.csv')
```

#### Read and Write to Excel

```
>>> pd.read_excel('file.xlsx')
>>> pd.to_excel('dir/myDataFrame.xlsx', sheet_name='Sheet1')
```

#### Read multiple sheets from the same file

```
>>> xls = pd.ExcelFile('file.xls')
>>> df = pd.read_excel(xls, 'Sheet1')
```

#### Read and Write to SQL Query or Database Table

```
>>> from sqlalchemy import create_engine
>>> engine = create_engine('sqlite:///memory:')
>>> pd.read_sql('SELECT * FROM my_table', engine)
>>> pd.read_sql_table('my_table', engine)
>>> pd.read_sql_query('SELECT * FROM my_table', engine)
```

read\_sql() is a convenience wrapper around read\_sql\_table() and read\_sql\_query()

```
>>> pd.to_sql('myDf', engine)
```

# Pandas Cheat Sheet

BecomingHuman.AI



## Pandas Data Structures

### Pivot

```
>>> df3 = df2.pivot(index='Date',
                   columns='Type',
                   values='Value')
```

	Date	Type	Value
0	2016-03-01	a	11.432
1	2016-03-02	b	13.031
2	2016-03-01	c	20.784
3	2016-03-03	a	99.906
4	2016-03-02	a	1.303
5	2016-03-03	c	20.784

Spread rows into columns



Type	a	b	c
Date			
2016-03-01	11.432		
2016-03-02		13.031	
2016-03-03			20.784

### Pivot Table

```
>>> df4 = pd.pivot_table(df2,
                        values='Value',
                        index='Date',
                        columns='Type')
```

	0	1
1	5	0.233482
2	4	0.184713
3	3	0.433522

Unstacked

Spread rows into columns



1	5	0	0.233482
2	4	0	0.184713
3	3	0	0.433522
4	3	1	0.429401

Stacked

### Melt

```
>>> pd.melt(df2,
            id_vars=['Date'],
            value_vars=['Type', 'Value'],
            value_name='Observations')
```

	Date	Type	Value
0	2016-03-01	a	11.432
1	2016-03-02	b	13.031
2	2016-03-01	c	20.784
3	2016-03-03	a	99.906
4	2016-03-02	a	1.303
5	2016-03-03	c	20.784

Gather columns into rows



	Date	Variables	Observations
0	2016-03-01	Type	a
1	2016-03-02	Type	b
2	2016-03-01	Type	c
3	2016-03-03	Type	a
4	2016-03-02	Type	a
5	2016-03-03	Type	c
6	2016-03-01	Value	11.432
7	2016-03-02	Value	13.031
8	2016-03-01	Value	20.784
9	2016-03-03	Value	99.906
10	2016-03-02	Value	1.303
11	2016-03-03	Value	20.784

## Advanced Indexing

Also see NumPy Arrays

### Selecting

```
>>> df3.loc[:,(df3>1).any()]
>>> df3.loc[:,(df3>1).all()]
>>> df3.loc[:,df3.isnull().any()]
>>> df3.loc[:,df3.notnull().all()]
```

### Indexing With isin

```
>>> df[(df.Country.isin(df2.Type))]
>>> df3.filter(items=["a","b"])
>>> df.select(lambda x: not x%5)
```

### Where

```
>>> s.where(s > 0)
```

### Query

```
>>> df6.query('second > first')
```

## Setting/Resetting Index

```
>>> df.set_index('Country')
>>> df4 = df.reset_index()
>>> df = df.rename(index=str,
                  columns={"Country":'cntry',
                           "Capital":'cptl',
                           "Population":'plpn'})
```

Select cols with any vals >1

Select cols with vals > 1

Select cols with NaN

Select cols without NaN

Find same elements

Filter on values

Select specific elements

Subset the data

Query DataFrame

Set the index

Reset the index

Rename DataFrame

## Reindexing

```
>>> s2 = s.reindex(['a','c','d','b'])
```

### Forward Filling

```
>>> df.reindex(range(4),
               method='ffill')
```

Country Capital Population  
0 Belgium Brussels 11190846  
1 India New Delhi 1303171035  
2 Brazil Brasilia 207847528  
3 Brazil Brasilia 207847528

### Forward Filling

```
>>> s3 = s.reindex(range(5),
                   method='bfill')
```

0 3  
1 3  
2 3  
3 3  
4 3

## MultiIndexing

```
>>> arrays = [np.array([1,2,3]),
             np.array([5,4,3])]
>>> df5 = pd.DataFrame(np.random.rand(3, 2), index=arrays)
>>> tuples = list(zip(*arrays))
>>> index = pd.MultiIndex.from_tuples(tuples,
                                      names=['first', 'second'])
>>> df6 = pd.DataFrame(np.random.rand(3, 2), index=index)
>>> df2.set_index(['Date', 'Type'])
```

Return unique values

Check duplicates

Drop duplicates

Drop duplicates

## Duplicate Data

```
>>> s3.unique()
>>> df2.duplicated('Type')
>>> df2.drop_duplicates('Type', keep='last')
>>> df.index.duplicated()
```

## Grouping Data

### Aggregation

```
>>> df2.groupby(by=['Date','Type']).mean()
>>> df4.groupby(level=0).sum()
>>> df4.groupby(level=0).agg(lambda x:sum(x)/len(x); 'b': np.sum)
```

### Transformation

```
>>> customSum = lambda x: (x+x%2)
>>> df4.groupby(level=0).transform(customSum)
```

Drop NaN value

Fill NaN values with a predetermined value

Replace values with others

## Missing Data

```
>>> df.dropna()
>>> df3.fillna(df3.mean())
>>> df2.replace("a", "f")
```

## Combining Data

X1	X2
a	11.432
b	1.303
c	99.906

X1	X2	X3
a	11.432	20.784
b	NaN	NaN
c	99.906	NaN

### Pivot

```
>>> pd.merge(data1,
             data2,
             how='left',
             on=X1')
```

X1	X2	X3
a	11.432	20.784
b	1.303	NaN
c	99.906	NaN

```
>>> pd.merge(data1,
             data2,
             how='right',
             on=X1')
```

X1	X2	X3
a	11.432	20.784
b	1.303	NaN
d	NaN	NaN

```
>>> pd.merge(data1,
             data2,
             how='inner',
             on=X1')
```

X1	X2	X3
a	11.432	20.784
b	1.303	NaN

### Join

```
>>> data1.join(data2, how='right')
```

### Concatenate

#### Vertical

```
>>> s.append(s2)
```

#### Horizontal/Vertical

```
>>> pd.concat([s,s2],axis=1,keys=[One,Two])
>>> pd.concat([data1, data2],axis=1,join='inner')
```

## Dates

```
>>> df2['Date']= pd.to_datetime(df2['Date'])
>>> df2['Date']= pd.date_range('2000-1-1', periods=6,
                               freq='M')
>>> dates = [datetime(2012,5,1), datetime(2012,5,2)]
>>> index = pd.DatetimeIndex(dates)
>>> index = pd.date_range(datetime(2012,2,1), end, freq='BM')
```

## Visualization

```
>>> import matplotlib.pyplot as plt
>>> s.plot()
>>> plt.show()
```

```
>>> df2.plot()
>>> plt.show()
```

# Data Wrangling with pandas Cheat Sheet

BecomingHuman.AI

## Syntax Creating DataFrames

	a	b	c
1	4	7	10
2	5	8	11
3	6	9	12

```
df = pd.DataFrame(
    {'a': [4, 5, 6],
     'b': [7, 8, 9],
     'c': [10, 11, 12]},
    index=[1, 2, 3])
Specify values for each column.
```

```
df = pd.DataFrame(
    [[4, 7, 10],
     [5, 8, 11],
     [6, 9, 12]],
    index=[1, 2, 3],
    columns=['a', 'b', 'c'])
Specify values for each row.
```

	a		b	c
n	v			
d	1	4	7	10
e	2	5	8	11
	2	6	9	12

```
df = pd.DataFrame(
    {'a': [4, 5, 6],
     'b': [7, 8, 9],
     'c': [10, 11, 12]},
    index=pd.MultiIndex.from_tuples(
        [('d',1),('d',2),('e',2)],
        names=['n','v']))
Create DataFrame with a MultiIndex
```

## Method Chaining

Most pandas methods return a DataFrame so that another pandas method can be applied to the result. This improves readability of code.

```
df = (pd.melt(df)
      .rename(columns={'variable': 'var',
                      'value': 'val'})
      .query('val >= 200'))
```

## Windows

```
df.expanding()
Return an Expanding object allowing summary functions to be applied cumulatively.
```

```
df.rolling(n)
Return a Rolling object allowing summary functions to be applied to windows of length n.
```

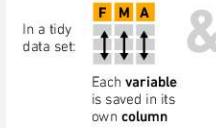
## Windows

```
df.plot.hist()
Histogram for each column
```

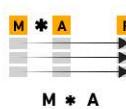


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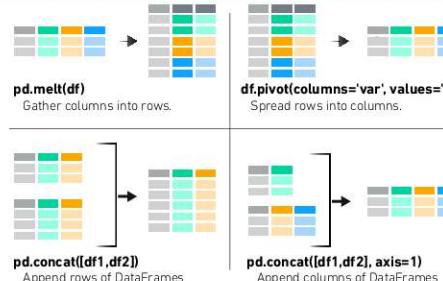
## Tidy Data A foundation for wrangling in pandas



Tidy data complements pandas's vectorized operations. pandas will automatically preserve observations as you manipulate variables. No other format works as intuitively with pandas



## Reshaping Data Change the layout of a data set



```
df.sort_values('mpg')
Order rows by values of a column (low to high).

df.sort_values('mpg', ascending=False)
Order rows by values of a column (high to low).

df.rename(columns = {'y': 'year'})
Rename the columns of a DataFrame

df.sort_index()
Sort the index of a DataFrame

df.reset_index()
Reset index of DataFrame to row numbers, moving index to columns.

df.drop(columns=['Length','Height'])
Drop columns from DataFrame
```

## Subset Observations (Rows)

```
df[df.Length > 7]
Extract rows that meet logical criteria.

df.drop_duplicates()
Remove duplicate rows (only considers columns).

df.head(n)
Select first n rows.

df.tail(n)
Select last n rows.
```

**Logic in Python (and pandas)**

<	Less than	is	Not equal to
>	Greater than	df.column.isin(values)	Group membership
==	Equal to	pd.isnull(obj)	Is NaN
<=	Less than or equal to	pd.notnull(obj)	Is not NaN
>=	Greater than or equal to	&,  , ~, ^, df.any(), df.all()	Logical and, or, not, xor, any, all

## Subset Variables (Columns)

```
df[['width','length','species']]
Select multiple columns with specific names.

df['width'] or df.width
Select single column with specific name.

df.filter(regex='regex')
Select columns whose name matches regular expression regex.
```

**Logic in Python (and pandas)**

'\.'	Matches strings containing a period .
'Length\$'	Matches strings ending with the 'Length' suffix.
'^Species\$'	Matches strings beginning with 'Species'.
'x1 1-S'	Matches strings beginning with 'x1' and ending with 1,2,3,4,5.
'[^Species]'	Matches strings except the string 'Species'.

df.loc[:, 'x2':'x4']
Select all columns between x2 and x4 (inclusive).

df.loc[:,[1,2,5]]
Select columns in positions 1, 2 and 5 (first column is 0).

df.loc[df['a'] > 10, ['a','c']]
Select rows meeting logical condition, and only the specific columns.

## Windows

df.groupby(by='col')
Return a GroupBy object, grouped by values in column named 'col'.

df.groupby(level='ind')
Return a GroupBy object, grouped by values in index level named 'ind'.

All of the summary functions listed above can be applied to a group.

Additional GroupBy functions:

**size()** Size of each group.

**agg(function)** Aggregate group using function.

The examples below can also be applied to groups. In this case, the function is applied on a per-group basis, and the returned vectors are of the length of the original DataFrame.

```
shift(1)
Copy with values shifted by 1.

rank(method='dense')
Ranks with no gaps.

rank(method='min')
Ranks. Ties get min rank.

rank(pct=True)
Ranks rescaled to interval [0, 1].
```

## Summarise Data

```
df['w'].value_counts()
Count number of rows with each unique value of variable
```

```
len(df)
# of rows in DataFrame.
```

```
df['w'].unique()
# of distinct values in a column.
```

```
df.describe()
Basic descriptive statistics for each column (or GroupBy)
```



pandas provides a large set of **summary functions** that operate on different kinds of pandas objects (DataFrame columns, Series, GroupBy, Expanding and Rolling (see below)) and produce single values for each of the groups. When applied to a DataFrame, the result is returned as a pandas Series for each column. Examples:

sum()	Sum values of each object.	min()	Minimum value in each object.
count()	Count non-NA/null values of each object.	max()	Maximum value in each object.
median()	Median value of each object.	mean()	Mean value of each object.
quantile(q=0.25,0.75)	Quantiles of each object.	var()	Variance of each object.
apply(function)	Apply function to each object	std()	Standard deviation of each object.

## Handling Missing Data

```
df.dropna()
Drop rows with any column having NA/null data.
```

```
df.fillna(value)

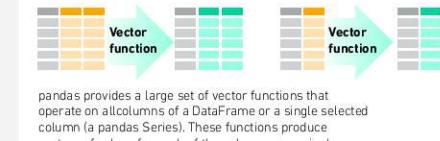
```

## Make New Columns



```
df['Volume'] = df.Length*df.Height*df.Depth
Add single column.
```

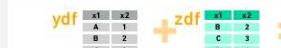
```
pd.qcut(df.col, n, labels=False)
Bin column into n buckets.
```



pandas provides a large set of vector functions that operate on all columns of a DataFrame or a single selected column (a pandas Series). These functions produce vectors of values for each of the columns, or a single Series for the individual Series. Examples:

max(axis=1)	Element-wise max.	min(axis=1)	Element-wise min.
clip(lower=-10,upper=10)	Trim values at input thresholds	abs()	Absolute value.

## Combine Data Sets



### Set Operations

```
pd.merge(ydf, zdf)
Rows that appear in both ydf and zdf (Intersection).
```

```
pd.merge(ydf, zdf, how='outer')
Rows that appear in either or both ydf and zdf (Union).
```

```
pd.merge(ydf, zdf, how='outer',
         indicator=True,
         query('_merge == "left_only"'))
drop(columns=['_merge'])
```

Rows that appear in ydf but not zdf (Sedtfdf)



**Standard Joins**

x1	x2	x3	pd.merge(adf, bdf,
A	1	T	how='left', on='x1')
B	2	F	Join matching rows from bdf to adf.
C	3	NAN	

```
pd.merge(adf, bdf,
         how='right', on='x1')
Join matching rows from adf to bdf.
```

x1	x2	x3	pd.merge(adf, bdf,
A	1	T	how='inner', on='x1')
B	2	F	Join data. Retain only rows in both sets.
D	NAN	T	

```
pd.merge(adf, bdf,
         how='outer', on='x1')
Join data. Retain all values, all rows.
```

### Filtering Joins

x1	x2	x3	adf[adf.x1.isin(bdf.x1)]
A	1	T	All rows in adf that have a match in bdf.
B	2	F	
C	3	NAN	

```
adf[~adf.x1.isin(bdf.x1)]
All rows in adf that do not have a match in bdf
```

# Data Wrangling with dplyr and tidyr

## Cheat Sheet

BecomingHuman.AI

### Syntax Helpful conventions for wrangling

`dplyr::tbl_df(iris)`

Converts data to `tbl` class. `tbl`'s are easier to examine than data frames. R displays only the data that fits onscreen

Source: local data frame [150 x 5]

	Sepal.Length	Sepal.Width	Petal.Length	Petal.Width
1	5.1	3.5	1.4	0.2
2	4.9	3.0	1.4	0.2
3	4.7	3.2	1.3	0.2
4	4.6	3.1	1.5	0.2
5	5.0	3.6	1.4	0.2
..	..	..	..	..
Variables not shown:	Petal.Width (dbl), Species (fctr)			

`dplyr::glimpse(iris)`

Information dense summary of `tbl` data.

`utils::View(iris)`

View data set in spreadsheet-like display (note capital V)

	Sepal.Length	Sepal.Width	Petal.Length	Petal.Width	Species
1	5.1	3.5	1.4	0.2	setosa
2	4.9	3.0	1.4	0.2	setosa
3	4.7	3.2	1.3	0.2	setosa
4	4.6	3.1	1.5	0.2	setosa
5	5.0	3.6	1.4	0.2	setosa
6	5.4	3.9	1.7	0.4	setosa
7	4.6	3.4	1.4	0.3	setosa
8	5.0	3.4	1.5	0.2	setosa

`dplyr::%>%`

Passes object on left hand side as first argument (or . argument) of function on righthand side.

`x %>% f(y)` is the same as `f(x, y)`

`y %>% f(x, z)` is the same as `f(y, x, z)`

"Piping" with `%>%` makes code more readable, e.g.

`iris %>%`

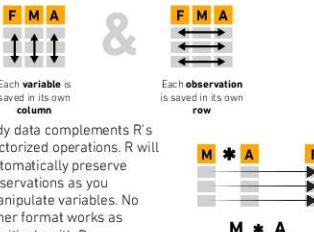
`group_by(Species) %>%`

`summarise(avg = mean(Sepal.Width)) %>%`

`arrange(avg)`

### Tidy Data A foundation for wrangling in R

In a tidy data set:



### Reshaping Data Change the layout of a data set



`tidyR::gather(cases, "year", "n", 2:4)`  
Gather columns into rows.



`tidyR::spread(pollution, size, amount)`  
Spread rows into columns.

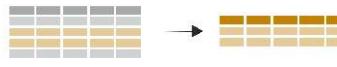


`tidyR::separate(storms, date, c("y", "m", "d"))`  
separate(storms, date, c("y", "m", "d"))



`tidyR::unite(data, col, ..., sep)`  
Unite several columns into one.

### Subset Observations (Rows)



`dplyr::filter(iris, Sepal.Length > 7)`  
Extract rows that meet logical criteria.

`dplyr::distinct(iris)`  
Remove duplicate rows.

`dplyr::sample_frac(iris, 0.5, replace = TRUE)`  
Randomly select fraction of rows.

`dplyr::sample_n(iris, 10, replace = TRUE)`  
Randomly select n rows.

`dplyr::slice(iris, 10:15)`  
Select rows by position.

`dplyr::top_n(storms, 2, date)`  
Select and order top n entries (by group if grouped data).

Logic in R - ?	Comparison, ?base	?-logic
<	is <	Not less than
>	is >	Not greater than
==	is ==	Group membership
==>	is .na	is NA
==<	is .na	is not NA
	is .any.all	Boolean operators

`select(iris, contains("x"))`  
Select columns whose name contains a character string.  
`select(iris, ends_with("Length"))`  
Select columns whose name ends with a character string.  
`select(iris, everything())`  
Select every column.  
`select(iris, matches("L"))`  
Select columns whose name matches a regular expression.  
`select(iris, num_range("x", 1:5))`  
Select columns named x1, x2, x3, x4, x5.  
`select(iris, one_of(c("Species", "Genus")))`  
Select columns whose names are in a group of names.  
`select(iris, starts_with("Sepal"))`  
Select columns whose name starts with a character string.  
`select(iris, Sepal.Length:Petal.Width)`  
Select all columns between Sepal.Length and Petal.Width (inclusive).  
`select(iris, -Species)`  
Select all columns except Species.

### Group Data

`dplyr::group_by(iris, Species)`  
Group data into rows with the same value of Species.  
`dplyr::ungroup(iris)`  
Remove grouping information from data frame.

`iris %>% group_by(Species) %>% summarise(...)`  
Compute separate summary row for each group.

`iris %>% group_by(Species) %>% mutate(...)`  
Compute new variables by group.



### Summarise Data



`dplyr::summarise(iris, avg = mean(Sepal.Length))`  
Summarise data into single row of values.

`dplyr::summarise_each(iris, funs(mean))`  
Apply summary function to each column.

`dplyr::count(iris, Species, wt = Sepal.Length)`  
Count number of rows with each unique value of variable (with or without weights).

summary function

Summarise uses **summary functions**, functions that take a vector of values and return a single value, such as:

min	Minimum value in a vector.
max	Last value of a vector.
mean	Maximum value in a vector.
nth	Nth value of a vector.
dplyr::min_rank	Median value of a vector.
# of values in a vector.	Ranks with no gaps.
dplyr::percent_rank	# of distinct values in a vector.
dplyr::n_distinct	Ranks rescaled to [0, 1].
var	Variance of a vector.
sd	Standard deviation of a vector.

### Make New Variables



`dplyr::mutate(iris, sepal = Sepal.Length + Sepal.Width)`  
Compute and append one or more new columns.

`dplyr::mutate_each(iris, funs(min_rank))`  
Apply window function to each column.

`dplyr::transmute(iris, sepal = Sepal.Length + Sepal.Width)`  
Compute one or more new columns. Drop original columns



window function

Mutate uses **window functions**, functions that take a vector of values and return another vector of values, such as:

dplyr::lead	Cumulative all
Copy with values shifted by 1.	<code>dplyr::cumall</code>
Copy with values lagged by 1.	<code>dplyr::cumany</code>
Copy with values lagged by n.	<code>dplyr::cummean</code>
Ranks with no gaps.	<code>dplyr::cumsum</code>
Ranks. Ties get min rank.	<code>dplyr::cummax</code>
Ranks rescaled to [0, 1].	<code>dplyr::cummin</code>
Ranks. Ties get to first value.	<code>dplyr::cumprod</code>
Bin vector into n buckets.	<code>dplyr::max</code>
Are values between a and b?	<code>dplyr::percentile</code>
Bin data. Retain only rows in both sets.	<code>dplyr::pmax</code>
Cumulative distribution.	<code>dplyr::min</code>

### Combine Data Sets



### Mutating Joins

`dplyr::left_join(a, b, by = "x1")`  
Join matching rows from b to a.

`dplyr::right_join(a, b, by = "x1")`  
Join matching rows from a to b.

`dplyr::inner_join(a, b, by = "x1")`  
Join data. Retain only rows in both sets.

`dplyr::full_join(a, b, by = "x1")`  
Join data. Retain all values, all rows.

`dplyr::semi_join(a, b, by = "x1")`  
All rows in a that have a match in b.

`dplyr::anti_join(a, b, by = "x1")`  
All rows in a that do not have a match in b.

### Set Operations

`dplyr::intersect(y, z)`  
Rows that appear in both y and z.

`dplyr::union(y, z)`  
Rows that appear in either or both y and z.

`dplyr::setdiff(y, z)`  
Rows that appear in y but not z.

`dplyr::bind_rows(y, z)`  
Append z to y as new rows.

`dplyr::bind_cols(y, z)`  
Append z to y as new columns.

`dplyr::bind_rows(y, z)`  
Caution: matches rows by position.

### Binding

`dplyr::bind_rows(y, z)`  
Append z to y as new rows.

`dplyr::bind_cols(y, z)`  
Append z to y as new columns.

The SciPy library is one of the core packages for scientific computing that provides mathematical algorithms and convenience functions built on the NumPy extension of Python.

# Scipy Linear Algebra Cheat Sheet

## BecomingHuman.AI



### Interacting With NumPy

[Also see NumPy](#)

```
>>> import numpy as np
>>> a = np.array([1,2,3])
>>> b = np.array([(1+5j),2,(3j),(4j),5j,6j]))
>>> c = np.array([(1,5,2,3),(4,5,6)],[(3,2,1),(4,5,6)])
```

#### Index Tricks

>>> np.mgrid[0:5:0.5]	Create a dense meshgrid
>>> np.ogrid[0:2:0.2]	Create an open meshgrid
>>> np.r_[3,0]*5:-1:10j]	Stack arrays vertically (row-wise)
>>> np.c_[b,c]	Create stacked column-wise arrays

#### Shape Manipulation

>>> np.transpose(b)	Permute array dimensions
>>> b.flatten()	Flatten the array
>>> np.hstack((b,c))	Stack arrays horizontally (column-wise)
>>> np.vstack((a,b))	Stack arrays vertically (row-wise)
>>> np.hsplit(c,2)	Split the array horizontally at the 2nd index
>>> np.vsplit(d,2)	Split the array vertically at the 2nd index

#### Polynomials

```
>>> from numpy import poly1d
>>> p = poly1d([3,4,5])
```

Create a polynomial object

#### Vectorizing Functions

```
>>> def myfunc(a):
    if a < 0:
        return a**2
    else:
        return a/2
>>> np.vectorize(myfunc)
```

Vectorize functions

#### Type Handling

>>> np.real(b)	Return the real part of the array elements
>>> np.imag(b)>>>	Return the imaginary part of the array elements
np.real_if_close(a,c,tol=1000)	Return a real array if complex parts close to 0
>>> np.cast['f'](np.pi)	Cast object to a data type

#### Other Useful Functions

>>> np.angle(b,deg=True)	Return the angle of the complex argument
>>> g = np.linspace(0,np.pi,num=5)	Create an array of evenly spaced values (number of samples)
>>> g [3:] += np.pi	
>>> np.unwrap(g)	Unwrap
>>> np.logspace(0,10,3)	Create an array of evenly spaced values (log scale)
>>> np.select([c<4],[c*2])	Return values from a list of arrays depending on conditions
>>> misc.factorial(a)	Factorial
>>> misc.comb(10,3,exact=True)	Combine N things taken at k time
>>> misc.central_diff_weights(3)	Weights for N-point central derivative
>>> misc.derivative(myfunc,1.0)	Find the n-th derivative of a function at a point

### Linear Algebra

[Also see NumPy](#)

You'll use the linalg and sparse modules. Note that scipy.linalg contains and expands on numpy.linalg

>>> from scipy import linalg, sparse

#### Creating Matrices

```
>>> A = np.matrix(np.random.random((2,2)))
>>> B = np.asmatrix(b)
>>> C = np.mat(np.random.random((10,5)))
>>> D = np.mat([[3,4], [5,6]])
```

#### Basic Matrix Routines

##### Inverse

```
>>> A.I
```

Inverse

##### Transposition

```
>>> A.T
```

Transpose matrix

##### Trace

```
>>> np.trace(A)
```

Trace

##### Norm

```
>>> linalg.norm(A)
```

Frobenius norm

```
>>> linalg.norm(A)
```

L1 norm (max column sum)

```
>>> linalg.norm(A,np.inf)
```

L inf norm (max row sum)

##### Rank

```
>>> np.linalg.matrix_rank(C)
```

Matrix rank

##### Determinant

```
>>> linalg.det(A)
```

Determinant

##### Solving linear problems

```
>>> linalg.solve(A,b)
```

Solver for dense matrices

```
>>> E = np.mat(a).T
```

Solver for dense matrices

```
>>> linalg.lstsq(F,E)
```

Least-squares solution to linear matrix

##### Generalized inverse

```
>>> linalg.pinv(C)
```

Compute the pseudo-inverse of a matrix (least-squares solver)

```
>>> linalg.pinv2(C)
```

Compute the pseudo-inverse of a matrix (SVD)

#### Creating Matrices

```
>>> F = np.eye(3,k=1)
```

Create a 2X2 identity matrix

```
>>> G = np.mat(np.identity(2))
```

Create a 2x2 identity matrix

```
>>> C[C > 0.5] = 0
```

```
>>> H = sparse.csr_matrix(C)
```

Compressed Sparse Row matrix

```
>>> I = sparse.csc_matrix(D)
```

Compressed Sparse Column matrix

```
>>> J = sparse.dok_matrix(A)
```

Dictionary Of Keys matrix

```
>>> E.todense()
```

Sparse matrix to full matrix

```
>>> sparse.isspmatrix_csc(A)
```

Identify sparse matrix

#### Matrix Functions

##### Addition

```
>>> np.add(A,D)
```

Addition

##### Subtraction

```
>>> np.subtract(A,D)
```

Subtraction

##### Division

```
>>> np.divide(A,D)
```

Division

##### Multiplication

```
>>> A @ D
```

Multiplication operator (Python 3)

```
>>> np.multiply(D,A)
```

Multiplication

```
>>> np.dot(A,D)
```

Dot product

```
>>> np.vdot(A,D)
```

Vector dot product

```
>>> np.inner(A,D)
```

Inner product

```
>>> np.outer(A,D)
```

Outer product

```
>>> np.tensordot(A,D)
```

Tensor dot product

```
>>> np.kron(A,D)
```

Kronecker product

**Exponential Functions**

```
>>> linalg.expm(A)
```

Matrix exponential

```
>>> linalg.expm2(A)
```

Matrix exponential (Taylor Series)

```
>>> linalg.expm3(D)
```

Matrix exponential (eigenvalue decomposition)

##### Logarithm Function

```
>>> linalg.logm(A)
```

Matrix logarithm

##### Trigonometric Functions

```
>>> linalg.sinm(D)
```

Matrix sine

```
>>> linalg.cosm(D)
```

Matrix cosine

```
>>> linalg.tanm(A)
```

Matrix tangent

##### Hyperbolic Trigonometric Functions

```
>>> linalg.sinhm(D)
```

Hyperbolic matrix sine

```
>>> linalg.coshm(D)
```

Hyperbolic matrix cosine

```
>>> linalg.tanhm(A)
```

Hyperbolic matrix tangent

##### Matrix Sign Function

```
>>> np.signm(A)
```

Matrix sign function

##### Matrix Square Root

```
>>> linalg.sqrtm(A)
```

Matrix square root

##### Arbitrary Functions

```
>>> linalg.fmm(A, lambda x: x*x)
```

Evaluate matrix function

#### Sparse Matrix Routines

##### Inverse

```
>>> sparse.linalg.inv(l)
```

Inverse

##### Norm

```
>>> sparse.linalg.norm(l)
```

Norm

##### Solving linear problems

```
>>> sparse.linalg.spsolve(H,I)
```

Solver for sparse matrices

#### Sparse Matrix Functions

```
>>> sparse.linalg.expm(l)
```

Sparse matrix exponential

#### Decompositions

##### Eigenvalues and Eigenvectors

```
>>> la, v = linalg.eig(A)
```

Solve ordinary or generalized eigenvalue problem for square matrix

>>> l, l2 = la

First eigenvector

>>> v[:,1]

Second eigenvector

```
>>> linalg.eigvals(A)
```

Unpack eigenvalues

##### Singular Value Decomposition

```
>>> U,S,Vh = linalg.svd(B)
```

Singular Value Decomposition (SVD)

>>> M,N = B.shape

Construct sigma matrix in SVD

##### LU Decomposition

```
>>> P,L,U = linalg.lu(C)
```

LU Decomposition

#### Sparse Matrix Decompositions

##### Eigenvalues and eigenvectors

```
>>> la, v = sparse.linalg.eigs(F,1)
```

SVD

```
>>> sparse.linalg.svds(H, 2)
```

#### Asking For Help

>>> help(scipy.linalg.diagsvd)

>>> np.info(np.matrix)

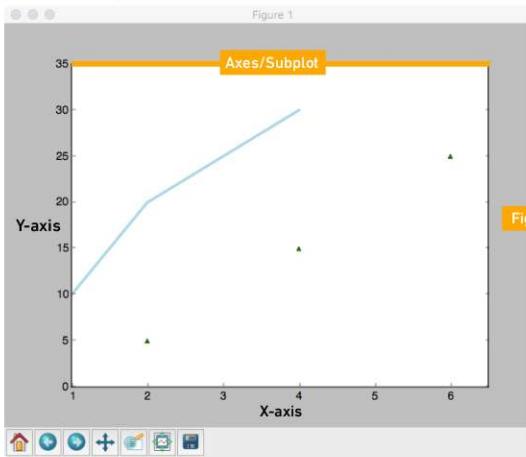
Matplotlib is a Python 2D plotting library which produces publication-quality figures in a variety of hardcopy formats and interactive environments across platforms.

# Matplotlib Cheat Sheet

BecomingHuman.AI

## Anatomy & Workflow

### Plot Anatomy



### Workflow

- |                        |                          |
|------------------------|--------------------------|
| <b>01</b> Prepare data | <b>04</b> Customize plot |
| <b>02</b> Create plot  | <b>05</b> Save plot      |
| <b>03</b> Plot         | <b>06</b> Show plot      |

```
>>> import matplotlib.pyplot as plt
step 1
>>> x = [1,2,3,4]
>>> y = [10,20,25,30]
step 2
>>> fig = plt.figure()
step 3
>>> ax = fig.add_subplot(111)
step 4
>>> ax.plot(x,y, color='lightblue', linewidth=3)
>>> ax.scatter([2,4,6], [5,15,25], color='darkgreen', marker='^')
step 5
>>> ax.set_xlim(1, 6.5)
>>> plt.savefig('foo.png')
>>> plt.show()
```

## Prepare The Data

Also see [Lists & NumPy](#)

### Index Tricks

```
>>> import numpy as np
>>> x = np.linspace(0, 10, 100)
>>> y = np.cos(x)
>>> z = np.sin(x)
```

### 2D Data or Images

```
>>> data = 2 * np.random.random((10, 10))
>>> data2 = 3 * np.random.random((10, 10))
>>> Y, X = np.mgrid[-3:3:100j, -3:3:100j]
>>> U = -1 - X**2 + Y
>>> V = 1 + X - Y**2
>>> from matplotlib.cbook import get_sample_data
>>> img = np.load(get_sample_data('axes_grid/bivariate_normal.npy'))
```

## Create Plot

```
>>> import matplotlib.pyplot as plt
```

### Figure

```
>>> fig = plt.figure()
>>> fig2 = plt.figure(figsize=plt.figaspect(2.0))
```

### Axes

All plotting is done with respect to an Axes. In most cases, a subplot will fit your needs. A subplot is an axes on a grid system.

```
>>> fig.add_axes()
>>> ax1 = fig.add_subplot(221) #row-col-num
>>> ax3 = fig.add_subplot(212)
>>> fig3, axes = plt.subplots(nrows=2, ncols=2)
>>> fig4, axes2 = plt.subplots(ncols=3)
```

## Plotting Routines

### 1D Data

```
>>> lines = ax.plot(x,y) Draw points with lines or markers connecting them
>>> ax.scatter(x,y) Draw unconnected points, scaled or colored
>>> axes[0,0].bar([1,2,3],[3,4,5]) Plot vertical rectangles (constant width)
>>> axes[1,0].barh([0.5,1,2.5],[0,1,2]) Plot horizontal rectangles (constant height)
>>> axes[1,1].axhline(0.45) Draw a horizontal line across axes
>>> axes[0,1].axvline(0.65) Draw a vertical line across axes
>>> ax.fill([x,y],color='blue') Draw filled polygons
>>> ax.fill_between(x,y,color='yellow') Fill between y-values and 0
```

## Customize Plot

### Colors, Color Bars & Color Maps

```
>>> plt.plot(x, x, x**2, x, x**3)
>>> ax.plot(x, y, alpha = 0.4)
>>> ax.plot(x, y, c='k')
>>> fig.colorbar(im, orientation='horizontal')
>>> im = ax.imshow(img, cmap='seismic')
```

### Markers

```
>>> fig, ax = plt.subplots()
>>> ax.scatter(x,y,marker='.')
>>> ax.plot(x,y,marker='o')
```

### Linestyles

```
>>> plt.plot(x,y,linewidth=4.0)
>>> plt.plot(y,ls='solid')
>>> plt.plot(x,ls='--')
>>> plt.plot(x,y,'-.',x**2,y**2,'-')
>>> plt.setp(lines,color='r',linewidth=4.0)
```

### Text & Annotations

```
>>> ax.text(1,-2.1, 'Example Graph', style='italic')
>>> ax.annotate("Sine", xy=(8, 0),
    xycoords='data',
    xytext=(10.5, 0),
    textcoords='data',
    arrowprops=dict(arrowstyle="->",
    connectionstyle="arc3"))
```

### MathText

```
>>> plt.title(r'$\sigma_i=15$', fontsize=20)
```

### Vector Fields

```
>>> axes[0,1].arrow(0,0,0.5,0.5) Add an arrow to the axes
>>> axes[1,1].quiver(y,z) Plot a 2D field of arrows
>>> axes[0,1].streamplot(X,Y,U,V) Plot 2D vector fields
```

### Data Distributions

```
>>> ax1.hist(y) Plot a histogram
>>> ax3.boxplot(y) Make a box and whisker plot
>>> ax3.violinplot(z) Make a violin plot
```

```
>>> axes2[0].pcolor(data2) Pseudocolor plot of 2D array
>>> axes2[0].pcolormesh(data) Pseudocolor plot of 2D array
>>> CS = plt.contour(Y,X,U)
>>> axes2[2].contourf(data1) Plot contours
>>> axes2[2].ax.contourf(CS) Plot filled contours
>>> axes2[2].label(CS) Label a contour plot
```

## Limits, Legends & Layouts

### Limits & Autoscaling

```
>>> ax.margins(x=0,y=0.1)
>>> ax.axis('equal')
```

Add padding to a plot  
Set the aspect ratio of the plot to 1  
Set limits for x-and y-axis  
Set limits for x-axis

### Legends

```
>>> ax.set_title('An Example Axes',
    ylabel='Y-Axis',
    xlabel='X-Axis')
>>> ax.legend(loc='best')
```

Set a title and x-and y-axis labels  
No overlapping plot elements

### Ticks

```
>>> ax.xaxis.set_ticks(range(1,5),
    ticklabels=[3,100,-12,'foo'])
    direction='inout',
    length=10)
```

Manually set x-ticks  
Make y-ticks longer and go in and out

### Subplot Spacing

```
>>> fig.subplots_adjust(wspace=0.5,
    hspace=0.3,
    left=0.25,
    right=0.9,
    top=0.9,
    bottom=0.1)
```

fig.tight\_layout()

### Axis Spines

```
>>> ax1.spines['top'].set_visible(False)
>>> ax1.spines['bottom'].set_position(('outward',10))
```

Make the top axis line for a plot invisible  
Move the bottom axis line outward

## Save Plot

### Save figures

```
>>> plt.savefig('foo.png')
```

### Save transparent figures

```
>>> plt.savefig('foo.png', transparent=True)
```

## Show Plot

```
>>> plt.show()
```

## Close & Clear

```
>>> plt.clf()
```

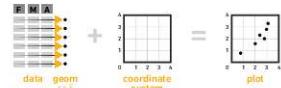
```
>>> plt.cla()
```

```
>>> plt.close()
```

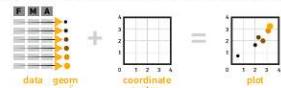
# Data Visualisation with ggplot2 Cheat Sheet

## Basics

ggplot2 is based on the **grammar of graphics**, the idea that you can build every graph from the same few components: a data set, a set of **geoms**—visual marks that represent data points, and a **coordinate system**.



To display data values, map variables in the data set to aesthetic properties of the geom like **size**, **color**, and **x** and **y** locations.

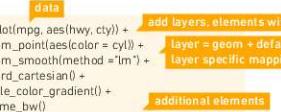


Build a graph with **plot()** or **ggplot()**



**ggplot(aes(x = cty, y = hwy, color = cyl, data = mpg, geom = 'point'))**  
Creates a complete plot with given data, geom, and mappings. Supplies many useful defaults.

**ggplot(data = mpg, aes(x = cty, y = hwy))**  
Begins a plot that you finish by adding layers to. No defaults, but provides more control than **plot()**.

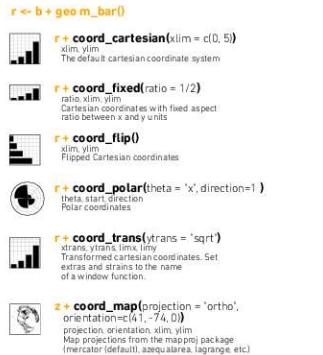


Add a new layer to a plot with a **geom\_()** or **stat\_()** function. Each provides a geom, a set of aesthetic mappings, and a default stat and position adjustment.

**last\_plot()**  
Returns the last plot

**ggsave("plot.png", width = 5, height = 5)**  
Saves last plot as 5" x 5" file named "plot.png" in working directory. Matches file type to file extension.

## Coordinate Systems



## Geoms

Use a geom to represent data points, use the geom's aesthetic properties to represent variables. Each function returns a layer

### One Variable

#### Continuous

```
a <- ggplot(mpg, aes(cty))
  a + geom_area(stat = "bin")
  a + geom_density(kernel = "gaussian")
  a + geom_dotplot()
  a + geom_histogram(binwidth = 5)
  a + geom_rug(sides = "bl")
  a + geom_smooth(method = lm)
  a + geom_text(aes(label = cyl))
  a + geom_step(direction = "hv")
```

#### Discrete

```
b <- ggplot(mpg, aes(fct_l))
  b + geom_bar()
```

## Graphical Primitives

```
c <- ggplot(mpg, aes(lng, lat))
  c + geom_polygon(aes(group = group))
  c + geom_crossbar(fatten = 2)
  d <- ggplot(economics, aes(date, unemploy))
  d + geom_path(lineend = "butt",
    linejoin = "round", linemtire = 1)
  d + geom_ribbon(ymin = unemploy - 900,
    ymax = unemploy + 900, type = "area")
  d + geom_rect(xmin = long, ymin = lat,
    xmax = long + delta_long,
    ymax = lat + delta_lat,
    xmax, ymin, alpha, color, fill, linetype, size)
```

## Three Variables

```
seals <- withheld %>%
  mutate(lat = sqrt(seals$long^2 + delta_lat^2))
m <- ggplot(seals, aes(lat, lon))
  m + geom_contour(aes(z = z))
  m + geom_raster(aes(fill = z), hijust = 0.5,
    vjust = 0.5, interpolate = FALSE)
  m + geom_tile(aes(fill = z))
```

## Faceting

Facets divide a plot into subplots based on the values of one or more discrete variables.

```
t <- ggplot(mpg, aes(cty, hwy)) + geom_point()
  t + facet_grid(~ fl)
  t + facet_grid(year ~ .)
  t + facet_grid(~ fl * year)
  t + facet_wrap(~ fl)
  t + geom_point(position = "jitter")
```

Each position adjustment can be recast as a function with manual **width** and **height** arguments

```
s + geom_bar(position = position_dodge(width = 1))
```

Set scales to let axes limits vary across facets

```
t + facet_grid(~ x, scales = "free")
```

Set **labeler** to adjust facet labels

```
t + facet_grid(~ fl, labeler = label_both)
```

## Two Variables

#### Continuous X, Continuous Y

```
t <- ggplot(movies, aes(year, rating))
  t + geom_blank()
  t + geom_jitter()
  t + geom_point()
  t + geom_hex()
  t + geom_quantile()
  t + geom_rug(sides = "bl")
  t + geom_smooth(method = lm)
  t + geom_line()
  t + geom_step(direction = "hv")
```

#### Discrete X, Continuous Y

```
df <- data.frame(grp = c("A", "B"), fit = 4:5, se = 1:2)
k <- ggplot(df, aes(grp, fit, ymin = fit - se, ymax = fit + se))
  k + geom_bar(stat = "identity")
  k + geom_crossbar(fatten = 2)
  k + geom_boxplot()
  k + geom_errorbar()
  k + geom_dotplot(binaxis = "y",
    stackdir = "center")
  k + geom_linerange()
  k + geom_pointrange()
```

#### Maps

```
murder <- data.frame(murder = USAArrests$Murder,
  state = tolower(state.name[USArrests]))
map <- map_data("state")
l <- ggplot(murder, aes(state))
  l + geom_map(aes(map_id = state), map = map) +
    expand_limits(x = map$long, y = map$lat)
  l + geom_point(aes(xmin = long, ymin = lat,
    xmax = long + delta_long,
    ymax = lat + delta_lat),
    xmax, ymin, alpha, color, fill, linetype, size)
```

## Position Adjustments

Position adjustments determine how to arrange geoms that would otherwise occupy the same space

```
s <- ggplot(mpg, aes(fl, fill = drv))
  s + geom_bar(position = "dodge")
  s + geom_bar(position = "fill")
  s + geom_bar(position = "stack")
  t + geom_point(position = "jitter")
```

Each position adjustment can be recast as a function with manual **width** and **height** arguments

```
s + geom_bar(position = position_dodge(width = 1))
```

## Labels

```
t + ggtitle("New Plot Title")
  t + xlab("New X Label")
  t + ylab("New Y Label")
  t + labs(title = "New title", x = "New x", y = "New y")
  All of the above
```

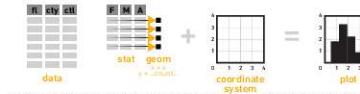
## Legends

```
t + theme(legend.position = "bottom")
  Place legend at "bottom", "left", or "right"
  t + guides(color = "none")
  Set legend type for each aesthetic: color, shape, or none (no legend)
  t + scale_fill_discrete(name = "Title", labels = c("A", "B", "C"))
  Set legendTitle and labels with a scale function
```

## Stats

An alternative way to build a layer

Some plots visualize a **transformation** of the original data set. Use a **stat** to choose a common transformation to visualize, e.g. **a + geom\_bar(stat = "bin")**



Each stat creates additional variables to map aesthetics to. These variables use a common **.name** syntax. stat functions and geom functions both combine a stat with a geom to make a layer, i.e. **stat\_bin geom = bar**) does the same as **geom\_bar(stat = "bin")**

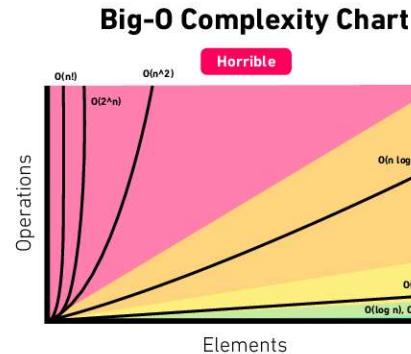


```
a + stat_bin(binwidth = 1, origin = 10)
  x, y, count ... density ... identity
  a + stat_bindot(binwidth = 1, binaxis = "x")
  x, y, I .. count ...
  a + stat_density(adjust = 1, kernel = "gaussian")
  x, y, I .. count ... scaled
```

```
a + stat_bin2d(dens = 30, drop = TRUE)
  x, y, fill ... density ...
  a + stat_binhex(bins = 30)
  x, y, fill ... density ...
  a + stat_density2d(contour = TRUE, n = 100)
  x, y, color ... 1 .. level
```

```
m + stat_contour(aes(z = z))
  x, y, z, order ... level
  m + stat_speke(aes(radius = z, angle = z))
  angle, radius, x, yend = 1 .. xend ... yend ...
  m + stat_summary_hexes(z = 2, bins = 30, fun = mean)
  x, y, I .. density ... count ... n .. wellnveth .. width
```

```
n <- b + geom_bar(aes(fill = fl))
  a + scale_fill_brewer()
  a + scale_fill_gradient()
  a + scale_fill_hex()
  a + scale_fill_hex2()
  a + scale_fill_hex3()
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Data Structure Operation										
	Time Complexity				Space Complexity					
	Average		Worst		Worst		Worst			
	Access	Search	Insertion	Deletion	Access	Search	Insertion	Deletion		
Array	Θ(1)	Θ(n)	Θ(n)	Θ(n)	Θ(1)	Θ(n)	Θ(n)	Θ(n)		
Stack	Θ(n)	Θ(n)	Θ(1)	Θ(1)	Θ(n)	Θ(n)	Θ(1)	Θ(n)		
Queue	Θ(n)	Θ(n)	Θ(1)	Θ(1)	Θ(n)	Θ(n)	Θ(1)	Θ(n)		
Singly-Linked List	Θ(n)	Θ(n)	Θ(1)	Θ(1)	Θ(n)	Θ(n)	Θ(1)	Θ(n)		
Doubly-Linked List	Θ(n)	Θ(n)	Θ(1)	Θ(1)	Θ(n)	Θ(n)	Θ(1)	Θ(n)		
Skip List	Θ(log(n))	Θ(log(n))	Θ(log(n))	Θ(log(n))	Θ(n)	Θ(n)	Θ(n)	Θ(n log(n))		
Hash Table	N/A	Θ(1)	Θ(1)	Θ(1)	N/A	Θ(n)	Θ(n)	Θ(n)		
Binary Search Tree	Θ(log(n))	Θ(log(n))	Θ(log(n))	Θ(log(n))	Θ(n)	Θ(n)	Θ(n)	Θ(n)		
Cartesian Tree	Θ(log(n))	Θ(log(n))	Θ(log(n))	Θ(log(n))	N/A	Θ(n)	Θ(n)	Θ(n)		
B-Tree	N/A	Θ(log(n))	Θ(log(n))	Θ(log(n))	Θ(log(n))	Θ(log(n))	Θ(log(n))	Θ(n)		
Red-Black Tree	Θ(log(n))	Θ(log(n))	Θ(log(n))	Θ(log(n))	Θ(log(n))	Θ(log(n))	Θ(log(n))	Θ(n)		
Splay Tree	N/A	Θ(log(n))	Θ(log(n))	Θ(log(n))	N/A	Θ(log(n))	Θ(log(n))	Θ(n)		
AVL Tree	Θ(log(n))	Θ(log(n))	Θ(log(n))	Θ(log(n))	Θ(log(n))	Θ(log(n))	Θ(log(n))	Θ(n)		
KD Tree	Θ(log(n))	Θ(log(n))	Θ(log(n))	Θ(log(n))	Θ(n)	Θ(n)	Θ(n)	Θ(n)		

Array Sorting Algorithms				
	Time Complexity		Space Complexity	
	Best	Average	Worst	Worst
Quicksort	Ω(n log(n))	Θ(n log(n))	Θ(n^2)	Ο(n log(n))
Mergesort	Ω(n log(n))	Θ(n log(n))	Θ(n log(n))	Ο(n log(n))
Timsort	Ω(n)	Θ(n)	Θ(n log(n))	Ο(n log(n))
Heapsort	Ω(n log(n))	Θ(n log(n))	Θ(n log(n))	Ο(n log(n))
Bubble Sort	Ω(n)	Θ(n)	Θ(n^2)	Ο(n^2)
Insertion Sort	Ω(n)	Θ(n)	Θ(n^2)	Ο(n^2)
Selection Sort	Ω(n^2)	Θ(n^2)	Θ(n^2)	Ο(n^2)
Tree Sort	Ω(n log(n))	Θ(n log(n))	Θ(n^2)	Ο(n log(n))
Shell Sort	Ω(n log(n))	Θ(n(log(n))^2)	Θ(n(log(n))^2)	Ο(n log(n))
Bucket Sort	Ω(n+k)	Θ(n+k)	Θ(n^2)	Ο(n+k)
Radix Sort	Ω(n+k)	Θ(n+k)	Θ(n+k)	Ο(n+k)
Counting Sort	Ω(n+k)	Θ(n+k)	Θ(n+k)	Ο(n+k)
Cubesort	Ω(n)	Θ(n log(n))	Θ(n log(n))	Ο(n log(n))