

**Binomial Distribution:** Used when finding probability of event that has multiple choices (Ex: Five children chosen out of ten).

$$\binom{n}{x} (p)^x (1-p)^{n-x}$$

In which p is probability, x is total population, n is the number of items chosen.

Expected Value:  $np$

Variance:  $\sigma^2 = np(1-p)$

**Hypergeometric Distribution** Used when replacement isn't in place (When the probability changes after selecting an option).

$$P = \frac{\binom{K}{k} \binom{N-K}{n-k}}{\binom{N}{n}} \quad \text{N=population size, K=Successes in population, n=number of draws, k=observed successes}$$

successes

$$E(X) = n \frac{M}{N}$$

$$V(x) = \frac{N-n}{N-1} np(1-p)$$

**Negative Binomial Distribution** Used when determining time or other quantifier before event occurs.

$$P(X) = \binom{x+r-1}{r-1} p^r (1-p)^x$$

$$E(X) = \frac{r(1-p)}{p}$$

$$V(X) = \frac{r(1-p)}{p^2}$$

**Poisson Distribution** Use when given the average amount of an event.

$$p.m.f. = \frac{e^{-\lambda} \lambda^x}{x!}$$

$$E(x) = \lambda$$

$$V(x) = \lambda$$

**If-then** Represented as  $P(A|B)$ , meaning Probability of A given B. Probability equals  $P(A|B) = \frac{P(A \cap B)}{P(B)}$ .

If  $P(A)P(B) = P(A \cap B)$ , then  $P(A)$  and  $P(B)$  are independent, otherwise they are dependent.

Baye's Theorem:

$$P(A_j|B) = \frac{P(A_j \cap B)}{P(B)} = \frac{P(B|A_j)P(A_j)}{\sum_{i=1}^k P(B|A_i)P(A_i)} \quad i \in \mathbb{N}$$