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Greg Byrd, Lynn Byrd and Chris Pearce

Cambridge Checkpoint

Mathematics

Coursebook

9

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Greg Byrd, Lynn Byrd and Chris Pearce

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Mathematics

Coursebook

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Contents



Introduction	5	6 Planning and collecting data	55
Acknowledgements	6	6.1 Identifying data	56
1 Integers, powers and roots	7	6.2 Types of data	58
1.1 Directed numbers	8	6.3 Designing data-collection sheets	59
1.2 Square roots and cube roots	10	6.4 Collecting data	61
1.3 Indices	11	End-of-unit review	63
1.4 Working with indices	12	7 Fractions	64
End-of-unit review	14	7.1 Writing a fraction in its simplest form	65
2 Sequences and functions	15	7.2 Adding and subtracting fractions	66
2.1 Generating sequences	16	7.3 Multiplying fractions	68
2.2 Finding the n th term	18	7.4 Dividing fractions	70
2.3 Finding the inverse of a function	20	7.5 Working with fractions mentally	72
End-of-unit review	22	End-of-unit review	74
3 Place value, ordering and rounding	23	8 Constructions and Pythagoras' theorem	75
3.1 Multiplying and dividing decimals mentally	24	8.1 Constructing perpendicular lines	76
3.2 Multiplying and dividing by powers of 10	26	8.2 Inscribing shapes in circles	78
3.3 Rounding	28	8.3 Using Pythagoras' theorem	81
3.4 Order of operations	30	End-of-unit review	83
End-of-unit review	32	9 Expressions and formulae	84
4 Length, mass, capacity and time	33	9.1 Simplifying algebraic expressions	85
4.1 Solving problems involving measurements	34	9.2 Constructing algebraic expressions	86
4.2 Solving problems involving average speed	36	9.3 Substituting into expressions	88
4.3 Using compound measures	38	9.4 Deriving and using formulae	89
End-of-unit review	40	9.5 Factorising	91
5 Shapes	41	9.6 Adding and subtracting algebraic fractions	92
5.1 Regular polygons	42	9.7 Expanding the product of two linear expressions	94
5.2 More polygons	44	End-of-unit review	96
5.3 Solving angle problems	45	10 Processing and presenting data	97
5.4 Isometric drawings	48	10.1 Calculating statistics	98
5.5 Plans and elevations	50	10.2 Using statistics	100
5.6 Symmetry in three-dimensional shapes	52	End-of-unit review	102
End-of-unit review	54		

Contents

11 Percentages	103	16 Probability	151
11.1 Using mental methods	104	16.1 Calculating probabilities	152
11.2 Comparing different quantities	105	16.2 Sample space diagrams	153
11.3 Percentage changes	106	16.3 Using relative frequency	155
11.4 Practical examples	107	End-of-unit review	157
End-of-unit review	109		
12 Tessellations, transformations and loci	110	17 Bearings and scale drawings	158
12.1 Tessellating shapes	111	17.1 Using bearings	159
12.2 Solving transformation problems	113	17.2 Making scale drawings	162
12.3 Transforming shapes	116	End-of-unit review	164
12.4 Enlarging shapes	119		
12.5 Drawing a locus	121	18 Graphs	165
End-of-unit review	123	18.1 Gradient of a graph	166
		18.2 The graph of $y = mx + c$	168
13 Equations and inequalities	124	18.3 Drawing graphs	169
13.1 Solving linear equations	125	18.4 Simultaneous equations	171
13.2 Solving problems	127	18.5 Direct proportion	173
13.3 Simultaneous equations 1	128	18.6 Practical graphs	174
13.4 Simultaneous equations 2	129	End-of-unit review	176
13.5 Trial and improvement	130		
13.6 Inequalities	132	19 Interpreting and discussing results	177
End-of-unit review	134	19.1 Interpreting and drawing frequency diagrams	178
		19.2 Interpreting and drawing line graphs	180
14 Ratio and proportion	135	19.3 Interpreting and drawing scatter graphs	182
14.1 Comparing and using ratios	136	19.4 Interpreting and drawing stem-and-leaf diagrams	184
14.2 Solving problems	138	19.5 Comparing distributions and drawing conclusions	186
End-of-unit review	140	End-of-unit review	189
		End-of-year review	190
15 Area, perimeter and volume	141	Glossary and index	194
15.1 Converting units of area and volume	142		
15.2 Using hectares	144		
15.3 Solving circle problems	145		
15.4 Calculating with prisms and cylinders	147		
End-of-unit review	150		

Introduction

Welcome to Cambridge Checkpoint Mathematics stage 9

The *Cambridge Checkpoint Mathematics* course covers the Cambridge Secondary 1 mathematics framework and is divided into three stages: 7, 8 and 9. This book covers all you need to know for stage 9.

There are two more books in the series to cover stages 7 and 8. Together they will give you a firm foundation in mathematics.

At the end of the year, your teacher may ask you to take a **Progression test** to find out how well you have done. This book will help you to learn how to apply your mathematical knowledge and to do well in the test.

The curriculum is presented in six content areas:

- Number
- Measures
- Geometry
- Algebra
- Handling data
- Problem solving.

This book has 19 units, each related to one of the first five content areas. Problem solving is included in all units. There are no clear dividing lines between the five areas of mathematics; skills learned in one unit are often used in other units.

Each unit starts with an introduction, with **key words** listed in a blue box. This will prepare you for what you will learn in the unit. At the end of each unit is a **summary** box, to remind you what you've learned.

Each unit is divided into several topics. Each topic has an introduction explaining the topic content, usually with worked examples. Helpful hints are given in blue rounded boxes. At the end of each topic there is an exercise. Each unit ends with a review exercise. The questions in the exercises encourage you to apply your mathematical knowledge and develop your understanding of the subject.

As well as learning mathematical skills you need to learn when and how to use them. One of the most important mathematical skills you must learn is how to solve problems.



When you see this symbol, it means that the question will help you to develop your problem-solving skills.

During your course, you will learn a lot of facts, information and techniques. You will start to think like a mathematician. You will discuss ideas and methods with other students as well as your teacher. These discussions are an important part of developing your mathematical skills and understanding.

Look out for these students, who will be asking questions, making suggestions and taking part in the activities throughout the units.





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1 Integers, powers and roots



Mathematics is about finding patterns.

How did you first learn to add and multiply negative integers?

Perhaps you started with an addition table or a multiplication table for positive integers and then extended it. The patterns in the tables help you to do this.

Key words

Make sure you learn and understand these key words:

power
index (indices)

+	3	2	1	0	-1	-2	-3
3	6	5	4	3	2	1	0
2	5	4	3	2	1	0	-1
1	4	3	2	1	0	-1	-2
0	3	2	1	0	-1	-2	-3
-1	2	1	0	-1	-2	-3	-4
-2	1	0	-1	-2	-3	-4	-5
-3	0	-1	-2	-3	-4	-5	-6

This shows

$$1 + -3 = -2.$$

You can also subtract.

$$-2 - 1 = -3 \text{ and}$$

$$-2 - -3 = 1.$$

×	3	2	1	0	-1	-2	-3
3	9	6	3	0	-3	-6	-9
2	6	4	2	0	-2	-4	-6
1	3	2	1	0	-1	-2	-3
0	0	0	0	0	0	0	0
-1	-3	-2	-1	0	1	2	3
-2	-6	-4	-2	0	2	4	6
-3	-9	-6	-3	0	3	6	9

This shows

$$2 \times -3 = -6.$$

You can also divide.

$$-6 \div 2 = -3 \text{ and}$$

$$-6 \div -3 = 2.$$

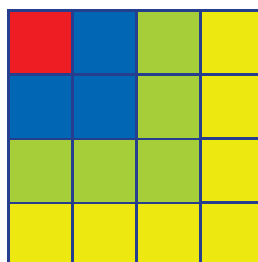
Square numbers show a visual pattern.

$$1 + 3 = 4 = 2^2$$

$$1 + 3 + 5 = 9 = 3^2$$

$$1 + 3 + 5 + 7 = 16 = 4^2$$

Can you continue this pattern?

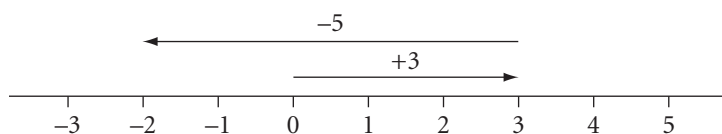


1.1 Directed numbers

Directed numbers have direction; they can be positive or negative. Directed numbers can be integers (whole numbers) or they can be decimal numbers.

Here is a quick reminder of some important things to remember when you add, subtract, multiply and divide integers. These methods can also be used with any directed numbers.

What is $3 + -5$?



Think of a number line. Start at 0. Moving 3 to the right, then 5 to the left is the same as moving 2 to the left.

Or you can change it to a subtraction: $3 + -5 = 3 - 5$.

Either way, the answer is -2 .

What about $3 - -5$?

Perhaps the easiest way is to add the inverse.

$$3 - -5 = 3 + 5 = 8$$

What about multiplication?

$$3 \times 5 = 15 \quad 3 \times -5 = -15 \quad -3 \times 5 = -15 \quad -3 \times -5 = 15$$

Multiply the corresponding positive numbers and decide whether the answer is positive or negative.

Division is similar.

$$15 \div 3 = 5 \quad -15 \div 3 = -5 \quad -15 \div -3 = 5 \quad 15 \div -3 = -5$$

These are the methods for integers.

You can use exactly the same methods for any directed numbers, even if they are not integers.

add negative \rightarrow subtract positive
subtract negative \rightarrow add positive

Remember for multiplication and division:
same signs \rightarrow positive answer
different signs \rightarrow negative answer

Worked example 1.1

Complete these calculations. **a** $3.5 + -4.1$ **b** $3.5 - -2.8$ **c** 6.3×-3 **d** $-7.5 \div -2.5$

- | | |
|---|--|
| <p>a $3.5 - 4.1 = -0.6$</p> <p>b $3.5 + 2.8 = 6.3$</p> <p>c $6.3 \times -3 = -18.9$</p> <p>d $-7.5 \div -2.5 = 3$</p> | <p>You could draw a number line but it is easier to subtract the inverse (which is 4.1). Change the subtraction to an addition. Add the inverse of -2.8 which is 2.8.</p> <p>First multiply 6.3 by 3. The answer must be negative because 6.3 and -3 have opposite signs.</p> <p>$7.5 \div 2.5 = 3$. The answer is positive because -7.5 and -2.5 have the same sign.</p> |
|---|--|

Exercise 1.1

Do not use a calculator in this exercise.

1 Work these out.

- a** $5 + -3$ **b** $5 + -0.3$ **c** $-5 + -0.3$ **d** $-0.5 + 0.3$ **e** $0.5 + -3$

2 Work these out.

- a** $2.8 + -1.3$ **b** $0.6 + -4.1$ **c** $-5.8 + 0.3$ **d** $-0.7 + 6.2$ **e** $-2.25 + -0.12$

3 Work these out.

a $7 - -4$ **b** $-7 - 0.4$ **c** $-0.4 - -7$ **d** $-0.4 - 0.7$ **e** $-4 - -0.7$

4 Work these out.

a $2.8 - -1.3$ **b** $0.6 - -4.1$ **c** $-5.8 - 0.3$ **d** $-0.7 - 6.2$ **e** $-2.25 - -0.12$



5 The midday temperature, in Celsius degrees ($^{\circ}\text{C}$), on four successive days is 1.5, -2.6 , -3.4 and 0.5. Calculate the mean temperature.

6 Find the missing numbers.

a $\square + 4 = 1.5$ **b** $\square + -6.3 = -5.9$ **c** $4.3 + \square = -2.1$ **d** $12.5 + \square = 3.5$

7 Find the missing numbers.

a $\square - 3.5 = -11.6$ **b** $\square - -2.1 = 4.1$ **c** $\square - 8.2 = 7.2$ **d** $\square - -8.2 = 7.2$



8 Copy and complete this addition table.

+	-3.4	-1.2
5.1		
	-4.7	



9 Use the information in the box to work these out.

a -2.3×-9.6 **b** $-22.08 \div 2.3$ **c** $22.08 \div -9.6$
d -4.6×-9.6 **e** $-11.04 \div -2.3$

$2.3 \times 9.6 = 22.08$

10 Work these out.

a 2.7×-3 **b** $2.7 \div -3$ **c** -1.2×-1.2 **d** -3.25×-4 **e** $17.5 \div -2.5$



11 Copy and complete this multiplication table.

\times	3.2	-0.6
-1.5		
		1.5

12 Complete these calculations.

a -2×-3 **b** $(-2 \times -3) \times -4$ **c** $(-3 \times 4) \div -8$



13 Use the values given in the box to work out the value of each expression.

a $p - q$ **b** $(p + q) \times r$
c $(q + r) \times p$ **d** $(r - q) \div (q - p)$

$p = -4.5$ $q = 5.5$ $r = -7.5$

14 Here is a multiplication table.

Use the table to calculate these.

a $(-2.4)^2$ **b** $13.44 \div -4.6$
c $-16.1 \div -3.5$ **d** $-84 \div 2.4$

\times	2.4	3.5	4.6
2.4	5.76	8.4	13.44
3.5	8.4	12.25	16.1
4.6	13.44	16.1	21.16

15 p and q are numbers, $p + q = 1$ and $pq = -20$. What are the values of p and q ?

1.2 Square roots and cube roots

You should be able to recognise:

- the squares of whole numbers up to 20×20 and their corresponding square roots
- the cubes of whole numbers up to $5 \times 5 \times 5$ and their corresponding cube roots.

Only squares or cubes of integers have integer square roots or cube roots.

You can use a calculator to find square roots and cube roots, but you can estimate them without one.

Worked example 1.1

Estimate each root, to the nearest whole number. **a** $\sqrt{295}$ **b** $\sqrt[3]{60}$

a $17^2 = 289$ and $18^2 = 324$

$\sqrt{295}$ is 17 to the nearest whole number.

295 is between 289 and 324 so $\sqrt{295}$ is between 17 and 18.

It will be a bit larger than 17.

b $3^3 = 27$ and $4^3 = 64$

$\sqrt[3]{60}$ is 4, to the nearest whole number.

60 is between 27 and 64 so $\sqrt[3]{60}$ is between 3 and 4.

It will be a bit less than 4. A calculator gives 3.91 to 2 d.p.

Exercise 1.2

Do not use a calculator in this exercise, unless you are told to.

1 Read the statement on the right. Write a similar statement for each root.

a $\sqrt{20}$ **b** $\sqrt{248}$ **c** $\sqrt{314}$ **d** $\sqrt{83.5}$ **e** $\sqrt{157}$

$2 < \sqrt{8} < 3$

2 Explain why $\sqrt[3]{305}$ is between 6 and 7.

3 Estimate each root, to the nearest whole number.

a $\sqrt{171}$ **b** $\sqrt{35}$ **c** $\sqrt{407}$ **d** $\sqrt{26.3}$ **e** $\sqrt{292}$

4 Read the statement on the right. Write a similar statement for each root.

a $\sqrt[3]{100}$ **b** $\sqrt[3]{222}$ **c** $\sqrt[3]{825}$ **d** $\sqrt[3]{326}$ **e** $\sqrt[3]{58.8}$

$10 < \sqrt[3]{1200} < 11$

5 What Ahmad says is not correct.

a Show that $\sqrt{160}$ is between 12 and 13.

b Write down the number of which 40 is square root.



$\sqrt{16} = 4$ so $\sqrt{160} = 40$.

6 **a** Find $\sqrt{1225}$. **b** Estimate $\sqrt[3]{1225}$ to the nearest whole number.

$35^2 = 1225$

7 Show that $\sqrt[3]{125}$ is less than half of $\sqrt{125}$.

8 Use a calculator to find these square roots and cube roots.

a $\sqrt{625}$ **b** $\sqrt{20.25}$ **c** $\sqrt{46.24}$ **d** $\sqrt[3]{1728}$ **e** $\sqrt[3]{6.859}$

9 Use a calculator to find these square roots and cube roots. Round your answers to 2 d.p.

a $\sqrt{55}$ **b** $\sqrt{108}$ **c** $\sqrt[3]{200}$ **d** $\sqrt[3]{629}$ **e** $\sqrt[3]{10\,000}$

1.3 Indices

This table shows powers of 3. Look at the patterns in the table.

Power	3^{-4}	3^{-3}	3^{-2}	3^{-1}	3^0	3^1	3^2	3^3	3^4	3^5
Value	$\frac{1}{81}$	$\frac{1}{27}$	$\frac{1}{9}$	$\frac{1}{3}$	1	3	9	27	81	243

3^4 is 3 to the **power** 4.

4 is called the **index**.

The plural of index is **indices**.

Negative powers of any positive integer are fractions. Here are some more examples.

$$2^4 = 2 \times 2 \times 2 \times 2 = 16 \quad 2^{-4} = \frac{1}{16} \quad 7^3 = 7 \times 7 \times 7 = 343 \quad 7^{-3} = \frac{1}{343}$$

Any positive integer to the power 0 is 1. $2^0 = 1$ $7^0 = 1$ $12^0 = 1$

Worked example 1.3

Write these as fractions.

a 2^{-6}

b 6^{-2}

a $2^{-6} = \frac{1}{2^6} = \frac{1}{64}$ $2^6 = 2 \times 2 \times 2 \times 2 \times 2 \times 2 = 64$

b $6^{-2} = \frac{1}{6^2} = \frac{1}{36}$ $6^2 = 36$

Exercise 1.3

1 Write each number as a fraction. **a** 5^{-1} **b** 5^{-2} **c** 5^{-3} **d** 5^{-4}

2 Write each number as a fraction or as an integer.

a 7^2

b 7^{-2}

c 7^{-1}

d 7^0

e 7^3

3 Write each number as a fraction.

a 4^{-1}

b 10^{-2}

c 2^{-3}

d 12^{-1}

e 15^{-2}

f 20^{-2}

4 a Simplify each number.

i 2^0

ii 5^0

iii 10^0

iv 20^0

b Write the results in part **a** as a generalised rule.

5 Write each expression as a single number.

a $2^0 + 2^{-1} + 2^{-2}$

b $3^2 + 3 + 3^0 + 3^{-1}$

c $5 - 5^0 - 5^{-1}$

6 Write each number as a decimal.

a 5^{-1}

b 5^{-2}

c 10^{-1}

d 10^{-2}

e 10^{-3}

7 Write each number as a power of 2.

a 8

b $\frac{1}{2}$

c $\frac{1}{4}$

d $\frac{1}{16}$

e 1

8 $2^{10} = 1024$. In computing this is called 1K. Write each of these as a power of 2.

a 2K

b 0.5K

c $\frac{1}{1K}$

1.4 Working with indices

You can write the numbers in the boxes as powers.

Look at the indices. $2 + 3 = 5$ and $5 + 3 = 8$.

$$9 \times 27 = 243$$

$$32 \times 8 = 256$$

$$3^2 \times 3^3 = 3^5$$

$$2^5 \times 2^3 = 2^8$$

This is an example of a general result.

To multiply powers of a number, add the indices. $A^m \times A^n = A^{m+n}$

$$9 \times 9 = 81 \quad \Rightarrow \quad 3^2 \times 3^2 = 3^4 \quad 2 + 2 = 4$$

$$4 \times 8 = 32 \quad \Rightarrow \quad 2^2 \times 2^3 = 2^5 \quad 2 + 3 = 5$$

The multiplications above can be written as divisions.

You can write the numbers as powers.

Again, look at the indices. $5 - 3 = 2$ and $8 - 3 = 5$.

This shows that:

$$243 \div 27 = 9$$

$$256 \div 8 = 32$$

$$3^5 \div 3^3 = 3^2$$

$$2^8 \div 2^3 = 2^5$$

To divide powers of a number, subtract the indices. $A^m \div A^n = A^{m-n}$

$$27 \div 3 = 9 \quad \Rightarrow \quad 3^3 \div 3^1 = 3^2 \quad 3 - 1 = 2$$

$$4 \div 8 = \frac{1}{2} \quad \Rightarrow \quad 2^2 \div 2^3 = 2^{-1} \quad 2 - 3 = -1$$

Worked example 1.4

- a** Write each expression as a power of 5. **i** $5^2 \times 5^3$ **ii** $5^2 \div 5^3$
b Check your answers by writing the numbers as decimals.

- a** **i** $5^2 \times 5^3 = 5^{2+3} = 5^5$ $2 + 3 = 5$
ii $5^2 \div 5^3 = 5^{2-3} = 5^{-1} = \frac{1}{5}$ $2 - 3 = -1$
b **i** $25 \times 125 = 3125$ 3125 is 5^5
ii $25 \div 125 = \frac{1}{5} = 0.2$

Exercise 1.4

- Simplify each expression. Write your answers in index form.
 - $5^2 \times 5^3$
 - $6^4 \times 6^3$
 - $10^4 \times 10^2$
 - $a^2 \times a^2 \times a^3$
 - $4^5 \times 4$
- Simplify each expression. Leave your answers in index form where appropriate.
 - $2^5 \times 2^3$
 - $8^2 \times 8^4$
 - $a^3 \times a^2$
 - $2^3 \times 2^3$
 - $b^3 \times b^4$
- Simplify each expression.
 - $3^5 \div 3^2$
 - $k^4 \div k^3$
 - $10^6 \div 10^4$
 - $5^2 \div 5^4$
 - $7 \div 7^1$
- Simplify each expression.
 - $2^2 \div 2^2$
 - $2^2 \div 2^3$
 - $2^2 \div 2^4$
 - $2^4 \div 2^2$
 - $2^4 \div 2^6$

5 Write each expression as a power or fraction.

a $8^3 \times 8^4$

b $5^2 \times 5$

c $4^2 \times 4^4$

d $9^2 \div 9^3$

e $12^2 \div 12^4$



6 Find the value of N in each part.

a $10^2 \times 10^N = 10^4$

b $10^2 \div 10^N = 10$

c $10^2 \times 10^N = 10^7$

d $10^2 \div 10^N = 10^{-1}$



7 This table shows values of powers of 7.

Use the table to find the value of:

a 49×2401

b $16\,807 \div 343$

c 343^2

7^1	7^2	7^3	7^4	7^5	7^6
7	49	343	2401	16 807	117 649

8 **a** Write the numbers in the box as powers of 4. Check that the division rule for indices is correct.

$1024 \div 16 = 64$

b Write the numbers as powers of 2 and check that the division rule for indices is correct.

9 **a** Write 9 and 243 as powers of 3.

b Use your answers to part **a** to find, as powers of 3: **i** 9×243 **ii** $9 \div 243$.

10 Simplify each fraction.

a $\frac{2^3 \times 2^4}{2^5}$

b $\frac{a^3 \times a^2}{a^2}$

c $\frac{d^3 \times d}{d^1}$

d $\frac{10^6 \times 10^4}{10^2 \times 10^3}$

11 **a** Write each of these as a power of 2.

i $(2^2)^2$

ii $(2^2)^3$

iii $(2^4)^2$

iv $(2^4)^3$

v $(2^2)^4$

b What can you say about $(2^m)^n$ if m and n are positive integers?



12 In computing, $1\text{K} = 2^{10} = 1024$. Write each of these in K.

a 2^{12}

b 2^{15}

c 2^{20}

d 2^7



13 Find the value of n in each equation.

a $3^n \times 3^2 = 81$

b $5^n \times 25 = 625$

c $2^n \div 2 = 8$

d $n^2 \times n = 216$

Summary

You should now know that:

- ★ You can add, subtract, multiply or divide directed numbers in the same way as integers.
- ★ Using inverses can simplify calculations with directed numbers.
- ★ Only square numbers or cube numbers have square roots or cube roots that are integers.
- ★ $A^0 = 1$ if A is a positive integer.
- ★ $A^{-n} = \frac{1}{A^n}$ if A and n are positive integers.
- ★ $A^m \times A^n = A^{m+n}$
- ★ $A^m \div A^n = A^{m-n}$



You should be able to:

- ★ Add, subtract, multiply and divide directed numbers.
- ★ Estimate square roots and cube roots.
- ★ Use positive, negative and zero indices.
- ★ Use the index laws for multiplication and division of positive integer powers.
- ★ Use the rules of arithmetic and inverse operations to simplify calculations.
- ★ Calculate accurately, choosing operations and mental or written methods appropriate to the number and context.
- ★ Manipulate numbers and apply routine algorithms.

End-of-unit review

1 Complete these additions.

a $-3 + 6$ **b** $12 + -14.5$ **c** $-3.5 + -5.7$ **d** $-3.6 + 2.8 + -1.3$

2 Subtract.

a $12 - -4$ **b** $-6.4 - 8.3$ **c** $3.7 - -8.3$ **d** $-5.1 - -5.2$

3 $2.5 \times 4.5 = 11.25$. Use this to find the value of each expression.

a -2.5×-4.5 **b** $-11.25 \div -4.5$ **c** -4.5×1.25

4 Solve these equations.

a $x + 17.8 = 14.2$ **b** $y - 3.4 = -9.7$ **c** $3y + -4.9 = 2.6$

5 Look at the statement in the box. Write a similar statement for each number.

a $\sqrt{111}$ **b** $\sqrt{333}$ **c** $\sqrt{111}$ **d** $\sqrt[3]{333}$

$$4 < \sqrt{19} < 5$$

6 **a** Estimate $\sqrt{200}$ to the nearest whole number.

b Estimate $\sqrt[3]{200}$ to the nearest whole number.

7 Choose the number that is closest to $\sqrt{250}$.

14.9 15.1 15.4 15.8 16.2

8 Choose the number that is closest to $\sqrt[3]{550}$.

7.6 7.8 8.2 8.5 8.8

9 Show that $\sqrt{1000}$ is more than three times $\sqrt[3]{1000}$.

10 Write each of these numbers as a decimal.

a 2^{-1} **b** 4^{-1} **c** 2^{-2} **d** 5^{-2}

11 Write each number as a fraction.

a 3^{-2} **b** 2^{-3} **c** 6^{-1} **d** 12^{-2}

12 Write each expression as a single number.

a $2^2 + 2^0 + 2^{-2}$ **b** $10^{-1} + 10^0 + 10^3$

13 Write each number as a power of 10.

a 100 **b** 1000 **c** 0.01 **d** 0.001 **e** 1

14 Write each expression as a single power.

a $9^2 \times 9^3$ **b** 8×8^2 **c** $7^5 \div 7^2$ **d** $a \div a^3$ **e** $n^1 \div n^2$



15 Simplify each expression.

a $2^4 \div 2^5$ **b** $15^0 \times 15^2$ **c** $20^5 \div 20^3$ **d** $5^2 \div (5^3 \times 5^1)$

16 Write each expression as a power of a .

a $a^2 \times a^4$ **b** $a^2 \div a^4$ **c** $a^2 \times a^0$ **d** $a^1 \times a^4$ **e** $a^2 \div a^4$



17 Simplify each expression.

a $\frac{4^2 \times 4^4}{4^3}$ **b** $\frac{a^2}{a^3 \times a}$ **c** $\frac{n^2 \times n^1}{n^2}$

18 Find the value of n in each of these equations.

a $4^n = 1$ **b** $5^n = 0.2$ **c** $n \times n^2 = 343$ **d** $2^4 \div 2^n = 4$