Model Checking for ARMv8

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1 Introduction and Motivation

In the paper [1], the authors demonstrated a general scheme by which one could ascertain decidability for a wide range of memory models, which resulted in acknowledgement of the undecidability for a wide range of memory models, including AArch64. This called for an efficient under-approximation to the model, and accordingly an efficient model checking scheme which can use it. While existing models such as Herd [2] and the Flat [3] model do a good job of expressing the memory model, neither is well suited to a model checking approach. This is primarily because the former is in the form of predicates over allowed abstractions which is not easily extended to operational semantics, while the latter is not expressed in a formal notation and also does not include many oft-used instructions such as load and store exclusives. Motivated by recent approaches to using context-bounding as an efficient under-approximation to reachability, such as for POWER [4], we make the following contributions in this document: 1) We simplify the above two models into a form directly usable for the purposes of model checking, and prove it's equivalence to the herd model; and 2) We develop an under-approximation scheme to check reachability by bounding the number of contexts of execution, in the spirit of the work first championed by Lal and Reps [5]. We demonstrate that it is feasible to check moderately complex multithreaded programs running under power in acceptable amounts of time, opening the door to further optimizations. We open source our code so that others can build upon it.

2 Syntax for programs (simpler version)

We use the following syntax for the program.

```
\begin{array}{lll} Prog ::= & \mathrm{vars:} & x^* \\ & \mathrm{procs:} & p^* \end{array} p ::= & \mathrm{regs:} & \$r^* \\ & i ::= l : \$ \\ & i ::= l : \$ \\ & \$ ::= & x \leftarrow exp \\ & & \|\$r \leftarrow x \\ & & \|\$r \leftarrow exp \\ & & \| \mathrm{if} & exp & \mathrm{then} & i^* & \mathrm{else} & i^* \\ & & & \| \mathrm{while} & exp & \mathrm{do} & i^* \\ & & & \| \mathrm{assume} & exp \\ & & \| \mathrm{assert} & exp \\ & & \| \mathrm{term} \end{array}
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A program Prog first declares a set \mathcal{X} of (shared) variables followed by the code of a set \mathcal{P} of processes. Each process in turn declares a set of registers \$r and it's code in the form of a sequence of instructions denoted by i^* . Each such instruction consists of a label l and a statement s. A write instruction has a statement of the form $x \leftarrow exp$ where $x \in \mathcal{X}$ is a variable and exp is an expression. In all the above rules, exp is an expression containing only constants and registers, and no shared variables. A read instruction in a process $p \in \mathcal{P}$ is a statement of the form $\$r \leftarrow x$, where \$r is a register in p and $x \in \mathcal{X}$ is a variable. An assign instruction in a process $p \in \mathcal{P}$ has the form $\$r \leftarrow exp$, where \$r is a register and exp is an expression. Conditional, iterative, assume and assert instructions, collectively called aci instructions describe the rest of the instructions. The special instruction term is a syntactic sugar to mark the end of the code for the process.

3 Definitions for the rules

We first define a few helper functions:

- We refer to the statement corresponding to an instruction i by the function stmt(i).
- For a write instruction i whose statement is of the form $x \leftarrow exp$, or a read instruction i whose statement is of the form $\$r \leftarrow x$, we define $\mathsf{var}(i) := x$ to be the variable corresponding to the instruction. For all other types of instructions we define $\mathsf{var}(i) = \bot$.
- For a instruction i which is of one of the following forms: a write instruction with $\mathsf{stmt}(i) = \$r \leftarrow exp$, an assign instruction with $\$r \leftarrow exp$, an aci instruction with either $\mathsf{stmt}(i) = \mathsf{if}\ exp\ \mathsf{then}\ i^*\ \mathsf{else}\ i^*\ \mathsf{or}\ \mathsf{stmt}(i) = \mathsf{while}\ exp\ \mathsf{do}\ i^*, \mathsf{or}\ \mathsf{stmt}(i) = \mathsf{assume}\ exp, \mathsf{or}\ \mathsf{stmt}(i) = \mathsf{assert}\ exp, \mathsf{we}\ \mathsf{define}\ \mathsf{the}\ \mathsf{expression}\ \mathsf{occuring}\ \mathsf{in}\ \mathsf{the}\ \mathsf{statement}\ \mathsf{as}\ \mathsf{exp}(i) := exp.$ For all other types of instructions we define $\mathsf{exp}(i) := \bot$.
- For an instruction instance i belonging to the process p, we define proc(i) := p. Further, we denote the set of instructions of process p by \mathcal{J}_p . Also, we denote the statement at which process p begins execution (i.e. the first instruction of the process), by i_p^{init} .
- For an instruction instance $i \in \mathcal{J}_p$, we denote by $\mathsf{next}(i)$ the set of instructions that could immediately follow i in program order. In particular, for an ACI instruction i, we denote the set of instructions that could follow i upon evaluation of $\mathsf{exp}(i)$ to True, as $\mathsf{Tnext}(i)$, and the set of those that could follow on its evaluation to False as $\mathsf{Fnext}(i)$.
- We define the closest write $CW(\mathfrak{c}, \mathfrak{e}) := \mathfrak{e}'$ where \mathfrak{e}' is the unique event such that (here and in the rest of the document, an *event* is a single execution instance of an instruction),
 - 1. $e' \in \mathbb{E}_p^W$ (\mathbb{E}_p^W denotes the set of write events as defined below),
 - 2. $e' \prec_{poloc} e$ (The poloc program order \prec_{poloc} will be defined below),
 - 3. there is no event e'' such that $e'' \in \mathbb{E}_p^W$ and $e' \prec_{poloc} e'' \prec_{poloc} e$.

If no such events exists, we write $CW(e) := \bot$.

• We define by $\mathcal{R}(i)$ the set of registers appearing in $\exp(i)$. In the special case that $\exp(i) = \bot$, we write $\mathcal{R}(i) := \emptyset$.

We define a configuration $\mathbb C$ as the tuple $\langle \mathbb E, \prec, \text{ins}, \text{status}, \text{rf}, \text{Prop} \rangle$. Here, $\mathbb E \in \mathcal E$ is the set of events that have been created up to that point in the program. For any process p, we denote by $\mathbb E_p$ the events of process p that have been created so far. By $\mathbb E^W$ we denote the subset of $\mathbb E$ containing precisely the write events. We similarly define $\mathbb E^R$, $\mathbb E^{ACI}$ and so on. The program order relation $\prec \subseteq \mathbb E \times \mathbb E$ is an irreflexive partial order that describes for each process $p \in \mathcal P$ the order in which events are fetched from the code of p. Note that $e_1 \not\prec e_2$ if $\mathsf{proc}(e_1) \not= \mathsf{proc}(e_2)$, i.e. if they belong to different processes, and \prec is a total order on each of the $\mathbb E_p$ individually. The function $\mathsf{status} : \mathbb E \mapsto \{\mathsf{fetch}, \mathsf{init}, \mathsf{com}\}$ defines the current status of each event, which is one of fetched, initialized, and committed. The function $\mathsf{Prop} : \mathcal X \mapsto \mathbb E^W \cup \mathcal E^{\mathsf{init}}$ defines for each variable that has been propagated to the main memory. The function $\mathsf{rf} : \mathbb E^R \mapsto \mathbb E^W \cup \mathcal E^{\mathsf{init}}$ defines for each read event e the event e0 from which e1 gets its value. We introduce a number of dependency relations to help us frame the rules. The e1 from e2 from e3 is such that e1 e3 is such that e1 e3 if and only if e1 e2 and e3 if e4 var(e1). Further, we define the data dependency order e4 such that e1 e3 if

- $e_1 \in \mathbb{E}^R \cup \mathbb{E}^A$, i.e. e_1 is a read or assign event.
- $e_2 \in \mathbb{E}^W \cup \mathbb{E}^A \cup \mathbb{E}^{ACI}$, i.e. e_2 is a write, assign or ACI event.
- $e_1 \prec e_2$
- $stmt(ins(e_1))$ is of the form $\$r \leftarrow x$ or $\$r \leftarrow exp$,
- $\$r \in \mathcal{R}(\mathsf{ins}(e_2))$
- There is no event $e_3 \in \mathbb{E}^R \cup \mathbb{E}^A$ such that $e_1 \prec e_3 \prec e_2$ is of the form $r \leftarrow y$ or $r \leftarrow exp'$. That is, we want that e_1 be responsible for "supplying" the data to e_2 .

Finally, we define the control dependency \prec_{ctrl} as $e_1 \prec_{\mathsf{ctrl}} e_2$ if $e_1 \in \mathbb{E}^{ACI}$ and $e_1 \prec e_2$. We also define the transition relation as a relation $\longrightarrow \subseteq \mathbb{C} \times \mathcal{P} \times \mathbb{C}$. For configurations $e_1, e_2 \in \mathbb{C}$ and a process $p \in \mathcal{P}$, we write $e_1 \xrightarrow{p} e_2$ to denote that $\langle e_1, p, e_2 \rangle \in \longrightarrow$.

4 Helper predicates for next section

Predicate	Definition	Meaning
$\mathbf{e} \in \mathbb{E}^W:$ $ComCnd(\mathbf{c},\mathbf{e})$	$\begin{array}{c} \forall e' \in \mathbb{E} : \\ ((e' \prec_{\texttt{data}} e) \lor (e' \prec_{\texttt{ctrl}} e) \lor (e' \prec_{\texttt{poloc}} e)) \\ \Longrightarrow \\ (\texttt{status}(e') = \texttt{com}) \end{array}$	All events preceeding e in \prec_{data} , \prec_{ctrl} or \prec_{poloc} have already been committed.
$\mathbf{e} \in \mathbb{E}^R \cup \mathbb{E}^A:$ RdAssignComCnd (\mathbf{c},\mathbf{e})	$\begin{array}{c} \forall \mathtt{e}' \in \mathbb{E} : \\ (\mathtt{e}' \prec_{\mathtt{data}} \mathtt{e}) \\ \Longrightarrow \\ (\mathtt{status}(\mathtt{e}') = \mathtt{com}) \end{array}$	All events preceeding e in \prec_{data} , have already been committed.
$\mathtt{e} \in \mathbb{E}^W$: InitCnd(\mathtt{c},\mathtt{e})	$\begin{array}{c} \forall \mathbf{e}' \in \mathbb{E}^R \cup \mathbb{E}^A : \\ (\mathbf{e}' \prec_{\mathtt{data}} \mathbf{e}) \\ \Longrightarrow \\ ((\mathtt{status}(\mathbf{e}') = \mathtt{init}) \vee (\mathtt{status}(\mathbf{e}') = \mathtt{com})) \end{array}$	All instructions on which e is data-dependent on have already been initialized.
$\mathtt{e} \in \mathbb{E}^{\mathtt{ACI}}:$ $ValidCnd(\mathtt{c},\mathtt{e})$	$ \forall \mathbf{e}' \in \mathbb{E}^{ACI} : \\ ((\mathbf{e} \prec \mathbf{e}') \land (\nexists \mathbf{e}'' \in \mathbb{E} : \mathbf{e} \prec \mathbf{e}'' \prec \mathbf{e}')) \\ \Longrightarrow \\ (((Val(\mathbf{c}, \mathbf{e}) = true) \land (ins(\mathbf{e}') = Tnext(ins(\mathbf{e})))) \\ \lor \\ ((Val(\mathbf{c}, \mathbf{e}) = false) \land (ins(\mathbf{e}') = Fnext(ins(\mathbf{e}))))) $	The instruction that was fetched right after the ACI instruction was consistent with its truth value.

5 Rules without synchronization instructions

In each of these rules, $c \equiv \langle E, \prec, ins, status, rf, Prop \rangle$ denotes the "current" configuration, and the rule describes one possible way in which this configuration may evolve.

$$\frac{e \notin \mathbb{E}, \quad \prec' = \prec \cup \{\langle e', e \rangle | e' \in \mathbb{E}\}, \quad i \in \operatorname{MaxI}(c, p)}{\operatorname{c}^p } \operatorname{Fetch}$$

$$\frac{e \in \mathbb{E}_p^R, \quad \operatorname{status}(e) = \operatorname{fetch}, \quad CW(c, e) = e', \quad \operatorname{status}(e') = \operatorname{com}, \quad \operatorname{RdAssignComCnd}(c, e)}{\operatorname{c}^p } \operatorname{ComReadFromLocal}$$

$$\frac{e \in \mathbb{E}_p^R, \quad \operatorname{status}(e) = \operatorname{fetch}, \quad CW(c, e) = e', \quad \operatorname{status}(e') = \operatorname{com}, \quad \operatorname{RdAssignComCnd}(c, e)}{\operatorname{c}^p } \operatorname{ComReadFromLocal}$$

$$\frac{e \in \mathbb{E}_p^R, \quad \operatorname{status}(e) = \operatorname{fetch}, \quad (CW(c, e) = \bot) \lor (CW(c, e) = e' \land \operatorname{status}(e') = \operatorname{com}), \quad \operatorname{RdAssignComCnd}(c, e)}{\operatorname{c}^p } \operatorname{ComReadFromProp}$$

$$\frac{e \in \mathbb{E}_p^W, \quad \operatorname{status}(e) \in \operatorname{fetch}, \quad \operatorname{InitCnd}(c, e)}{\operatorname{c}^p } \operatorname{InitWrite}$$

$$\frac{e \in \mathbb{E}_p^W, \quad \operatorname{status}(e) = \operatorname{fetch}, \quad \operatorname{InitCnd}(c, e)}{\operatorname{c}^p } \operatorname{InitWrite}$$

$$\frac{e \in \mathbb{E}_p^W, \quad \operatorname{status}(e) = \operatorname{init}, \quad \operatorname{ComCnd}(c, e)}{\operatorname{c}^p } \operatorname{ComWrite}$$

$$\frac{e \in \mathbb{E}_p^A, \quad \operatorname{status}(e) = \operatorname{init}, \quad \operatorname{RdAssignComCnd}(c, e)}{\operatorname{c}^p } \operatorname{ComWrite}$$

$$\frac{e \in \mathbb{E}_p^A, \quad \operatorname{status}(e) = \operatorname{init}, \quad \operatorname{RdAssignComCnd}(c, e)}{\operatorname{c}^p } \operatorname{ComAssign}$$

$$\frac{e \in \mathbb{E}_p^A, \quad \operatorname{status}(e) = \operatorname{init}, \quad \operatorname{RdAssignComCnd}(c, e)}{\operatorname{c}^p } \operatorname{ComAssign}$$

$$\frac{e \in \mathbb{E}_p^{A, I}, \quad \operatorname{status}(e) = \operatorname{fetch}, \quad \operatorname{ComCnd}(c, e), \quad \operatorname{ValidCnd}(c, e)}{\operatorname{c}^p } \operatorname{ComAcI}$$

The rule Fetch chooses the next instruction to be executed from the code of a process $p \in \mathcal{P}$. To do this it should be able to select the next instruction i given the configuration c. To do this, we define the function $\mathsf{MaxI}(c,p)$ to be the set of instructions that can (intuitively) follow the current one. Formally,

- If $\mathbb{E}_p = \emptyset$, then we define $\operatorname{MaxI}(\mathbb{C},p) := \{i_p^{init}\}$, i.e. the first instruction to be fetched by p is i_p^{init} .
- If $\mathbb{E}_p \neq \emptyset$ let $\mathbb{e}' \in \mathbb{E}_p$ be the maximal event in \mathbb{E}_p w.r.t \prec in the configuration \mathbb{c} . Define $\mathsf{MaxI}(\mathbb{c},p) := \mathsf{next}(\mathsf{ins}(\mathbb{e}'))$

The remaining rules can be explained as follows:

• Once a read instruction is fetched, it can be satisfied by reading from either the latest po-previous write instruction (from the same process) that has not yet been propagated to memory, or can be satisfied by reading the value from memory if no such instruction exists. The rule ComReadFromLocal captures the former case, while the rule ComReadFromProp captures the latter. In both cases, we update the status of e to show that it has been 'committed', and update rf to indicate the instruction that satisfied it.

- A write instruction can be initialized if all events it is data-dependent on have been initialized. This rule is captured in the form of InitWrite. At this point events of the same thread can read from this write.
- Once all po-previous instructions on which e depends in some way (via a data, control or poloc dependency) have been committed (i.e. been propagated to memory), an initialized read can be propagated to memory and be committed. At this point events from all threads can read from this write. This forms ComWrite.
- The rules for an assign event are similar to that of a read event.
- An ACI event undergoes only one state transition after being fetched, i.e. being committed. However, such an event can be committed if and only if it is *valid*, i.e., e.g. the predicted branch turns out to be correct, or a loop is entered, etc. Of course, along with this it must satisfy the ComCnd which says that all events that e depends upon must have already been committed. This is captured as the rule ComACI.

6 Syntax for programs (complete version)

We introduce a number of instructions resembling those that are used in the AArch64. We explain them in the next section.

```
Proq ::= procs: p^*
  p ::= regs: \$r^*
           instrs: i
        i ::= l : s
               r \leftarrow exp
s ::=
             |\mathsf{LD} \ \$r' \leftarrow [\$r]
             |\mathsf{ST}| \$r' \leftarrow \$r
             |LDA \$r' \leftarrow [\$r]
             |STL [\$r'] \leftarrow \$r
             |LDX \$r' \leftarrow [\$r]
            |\text{STX }\$r'', \ [\$r'] \leftarrow \$r
             |LDAX \$r' \leftarrow [\$r]
             |STLX \$r'', [\$r'] \leftarrow \$r
             |if exp then i^* else i^*
             while exp do i^*
             assume exp
             |assert exp|
             dmb.ld
             dmb.st
             dmb.sy
             isb
            lterm
```

We comment about a few things here: the first thing to notice is that we have removed variables, and instead introduced addressed memory: the latter is exactly the same as the former, with the added complexity that there can now be address dependencies between instructions, which did not exist for variables. We refer to all kinds of loads collectively as "reads", and all kinds of stores collectively as "writes". Second, the assign instruction is closer to a read than it is a write: the primary reason is that it writes to registers and not memory (and thus it's side effects affect the former). In fact, an assign may be represented as a store to a "private" variable followed by a load from it, hence it is in a sense a compound instruction. However, since it does not directly interface with the memory at all, any run is indistinguishable from another wherein an assign is initialized or committed at a different time, as long as the read-from relations to and from it are preserved. Hence, we do not include the assign statement in the statement of the predicates. Third, for simplicity we assume that the addresses of loads and stores are registers, and not expressions of registers. The reason for this is that one, exactly the same rules given in the next-to-next section apply if we use expressions instead, and this, two, we can simply assume that we assign the expression to a reserved register and use it as the address immediately after (this is the same under this model).

7 Definitions and Helper predicates for next section

Along with the usual load/store and read/write operations, we also introduce three "special" types of loads and stores. First, a load or a store can be exclusive. The significance of a load exclusive that loads from an address and a store exclusive that writes back to that address is that the store succeeds if and only if no other event (from any process) has written to that address since the load exclusive. Also, corresponding to whether the store exclusive succeeded or not, the success value is written to a specified register. Note that such a primitive may be used to implement, e.g. locks or CAS instructions. There are also load-acquire and store-release instructions. These are special in that it is forbidden for any instruction that appears po-after the load-acquire to be reordered with it. Similarly, it is forbidden for any instruction that appears po-before the store-release to be reordered with it. In effect, the combination of a load-acquire and store-release serves like a dmb.sy. Finally there are LDAX and STLX instructions which are simply the combination of both the acquire/release and exclusive type of instructions, i.e. they provide the strictest guarantees. One point to observe here is that by nature of its definition the exclusive versions of stores are multi-copy atomic: every process (including the local one) sees the write at the same time; consequently we can consider it to have only a commit rule (since the init rules were meant to portray the period where effects were visible only to the local process).

We also introduce a few more helpful definitions. For any event e, RegWritten(e) is the register that e writes to, or \bot if there is no such register. This is non-bot for read, exclusive store and assign events. Further, for an assign event e of the form r0 we define as OpRegs(e) to be the set of registers appearing in exp.

It is also worth pointing out that any kind of read has only a commit rule: since the point of local and global visibility for a read is same, we can assume that the init and commit point are the same; consequently we let them directly commit after being fetched. This applies to all four kinds of reads.

Since we now have address dependencies, we note that at any point in an execution, for an event e, $\mathsf{addr}(e)$ may not be defined, which we write as $\mathsf{addr}(e) = \top$. Then, for two events $e_1 \prec e_2$, if $\mathsf{addr}(e_1) = \top$, it is possible that upon resolution, we get later that $e_1 \prec_{\mathsf{poloc}} e_2$. Subsequently, we include in poloc -dependencies all event pairs (e_1, e_2) such that $\mathsf{addr}(e_1) = \top$. Coming to the barriers, there are four types: three are $\mathsf{dmb.ld,dmb.st}$ and $\mathsf{dmb.sy}$. The ld variant stops the reordering of (local) load instructions (and variants therof, including "reads" from a variable) with it, while the st variant does that with stores and writes. The sy variant does both. The isb instruction is a bit different: all we need is that when it is committed, all $\mathsf{po-preceeding}$ events have their addresses (to which they write or from which they read) fully determined, i.e. any instruction that they are $\mathsf{addr-dependent}$ on must have been initialized (or committed).

We introduce events corresponding to these new instructions: we retain our nomenclature of their partition, with the corresponding \mathbb{E}^{name} being the subset of \mathbb{E} corresponding to name type of instructions. We should also revise our definition of CW. The events that can now write to a memory location are stores and store releases. Note however that Store Releases will write the success/failure indicator bit (0 is success) into a register (called r above), hence we need to consider them for the definition of r0 as well. Thus, our definition of r0 is revised to be the following: for reads and loads r0 equal defined to the po-latest store/write or variant therof that is poloc-before the store release. Note that this works even if that instruction is exclusive, because since a store exclusive has only a commit rule, that any read that is poloc after it has to wait for it to commit; by which time due to the rule, all events po-before the SRel are committed as well. Hence, the effects of the SRel are already well defined and visible to all processes. We also comment that we refer to both the old type of reads as well as the normal load instructions as "reads", and the old type of writes as well as plain stores as "writes".

Since we need to be able to determine if an intervening write overwrote the value written by an exclusive load, we introduce into our concept of a configuration a mapping function $Mark : \mathcal{X} \mapsto \mathcal{P} \cup \{\bot\}$. Here \mathcal{X} includes addressable memory locations instead of variables as it did before: both are the same, except that variables do not have address dependencies. Accordingly, we also reuse the function var to return the address of a load/store event. The idea is that any exclusive load "marks" the memory location with its originating process, while all other store based instructions simply overwrite the marker with \bot to record that the location is dirty.

We also make the following note: that the orders \prec_{data} and \prec_{addr} exclude the success-value write-to-registers by exclusive stores. This is because the herd model does not consider these to be coherence-relate. It can be microarchitecturally understood as thus: the processor assumes the store will succeed and proceeds with everything; if it fails the dependent instructions are squashed. Thus the future instructions may see the success value before the exclusive store is committed. There is one more note of importance: the *Fetch* rule is purely cosmetic: it is more intuitive to present a Fetch rule so as to encapsulate the out-of-order execution, however it could simply be merged with the init/commit rules. Subsequently, our code-to-code translation scheme (presented later) does not make use of the fetch rule (i.e. incorporates it as a part of the other rules).

We next define a bunch of predicates which will prove to be useful in stating the transition rules.

Predicate	Definition	Meaning
${\mathfrak e}\in {\mathbb E}:$ AllDmbLds $({\mathfrak c},{\mathfrak e})$	$\forall \mathtt{e}' \in \mathbb{E}^{\mathtt{DmbLd}} : \\ ((\mathtt{e}' \prec \mathtt{e}) \implies \mathtt{status}(\mathtt{e}') = \mathtt{com}))$	All po-previous dmb.ld's have been committed.
${\mathfrak e}\in {\mathbb E}$: AllDmbSts $({\mathfrak c},{\mathfrak e})$	$\forall e' \in \mathbb{E}^{DmbSt} : \\ ((e' \prec e) \implies status(e') = com))$	All po-previous dmb.st's have been committed.

$\mathtt{e} \in \mathbb{E}$: AllDmbSys (\mathtt{c},\mathtt{e})	$\forall e' \in \mathbb{E}^{\mathrm{DmbSy}} : \\ ((e' \prec e) \implies \mathrm{status}(e') = \mathrm{com}))$	All po-previous dmb.sy's have been committed.
$\mathbf{e} \in \mathbb{E}^{STL} \cup \mathbb{E}^{STLX} \cup \mathbb{E}^{DmbSt} :$ $AllWrites(\mathbf{c}, \mathbf{e})$	$\forall e' \in \mathbb{E}^{ST} \cup \mathbb{E}^{STL} \cup \mathbb{E}^{STX} \cup \mathbb{E}^{STLX} : \\ ((e' \prec e) \implies status(e') = com))$	All po-previous write-variants have been committed.
$\mathbf{e} \in \mathbb{E}^{STL} \cup \mathbb{E}^{STLX} \cup \mathbb{E}^{DmbLd} :$ $AllReads(\mathbf{c},\mathbf{e})$	$\forall \texttt{e}' \in \mathbb{E}^{\texttt{LD}} \cup \mathbb{E}^{\texttt{LDA}} \cup \mathbb{E}^{\texttt{LDX}} \cup \mathbb{E}^{\texttt{LDAX}} : \\ ((\texttt{e}' \prec \texttt{e}) \implies status(\texttt{e}') = com))$	All po-previous read-variants have been committed.
$\mathtt{e} \in \mathbb{E}$: AllSyncs (\mathtt{c},\mathtt{e})	$\forall e' \in \mathbb{E}^{DmbSy} \cup \mathbb{E}^{Isb} : $ $((e' \prec e) \implies status(e') = com))$	All po-previous dmb.sy's and isb's have been committed.
$\mathbf{e} \in \mathbb{E}^{ extsf{LDA}} \cup \mathbb{E}^{ extsf{LDAX}}:$ AllSRels (\mathbf{e},\mathbf{e})	$\forall \mathbf{e} \in \mathbb{E}^{STL} \cup \mathbb{E}^{STLX} : \\ ((\mathbf{e}' \prec \mathbf{e}) \implies status(\mathbf{e}') = com))$	All po-previous Store-Releases have been committed.
$\mathbf{e} \in \mathbb{E}^{ST} \cup \mathbb{E}^{STX}$: AllLAcqs (\mathbf{c}, \mathbf{e})	$\forall \mathtt{e}' \in \mathbb{E}^{\mathtt{LDA}} \cup \mathbb{E}^{\mathtt{LDAX}} : \\ ((\mathtt{e}' \prec \mathtt{e}) \implies \mathtt{status}(\mathtt{e}') = \mathtt{com}))$	All po-previous Load-Acquires have been committed.
$\mathbf{e} \in \mathbb{E}^{STL} \cup \mathbb{E}^{STLX}:$ $AllMem(\mathbf{e},\mathbf{e})$	${\tt AllWrites}({\tt c},{\tt e}) \land {\tt AllReads}({\tt c},{\tt e})$	All po-previous events that access memory have been committed.
$\mathtt{e} \in \mathbb{E}$: AllBarriers (\mathtt{c},\mathtt{e})	$AllDmbLds(\mathbb{c},\mathbb{e}) \land AllDmbSts(\mathbb{c},\mathbb{e}) \land AllSyncs(\mathbb{c},\mathbb{e})$	All po-previous barriers have been committed.
$\mathbf{e} \in \mathbb{E}^{ST} \cup \mathbb{E}^{STL}$: $InitCnd(\mathbf{c}, \mathbf{e})$	$\begin{array}{c} \forall e' \in \mathbb{E} : \\ (e' \prec_{\text{data}} e) \lor (e' \prec_{\text{addr}} e) \\ \Longrightarrow \\ (\text{status}(e') = \text{com})) \end{array}$	All events on which e is dependent on have already been committed.
$\mathbf{e} \in \mathbb{E}^{Isb} \cup \mathbb{E}^{ST} \cup \mathbb{E}^{STL} \ \cup \mathbb{E}^{STX} \cup \mathbb{E}^{STLX} : \ AddrCnd(\mathbf{c}, \mathbf{e})$	$\begin{split} \forall \mathbf{e}' \in \mathbb{E}^{\mathrm{LD}} \cup \mathbb{E}^{A} \cup \mathbb{E}^{\mathrm{LDA}} \cup \mathbb{E}^{\mathrm{LDX}} \cup \mathbb{E}^{\mathrm{LDAX}}, \mathbf{e}'' \in \mathbb{E} : \\ (\mathbf{e}' \prec_{\mathrm{addr}} \mathbf{e}'') \wedge (\mathbf{e}'' \prec_{\mathrm{po}} \mathbf{e}) \\ &\Longrightarrow \\ ((\mathrm{status}(\mathbf{e}') = \mathrm{init}) \vee (\mathrm{status}(\mathbf{e}') = \mathrm{com})) \end{split}$	All events po-before e have fully defined memory footprints.
$\mathtt{e} \in \mathbb{E}$: IsWrite(\mathtt{e})	$\mathbf{e} \in \mathbb{E}^{ST} \vee \mathbf{e} \in \mathbb{E}^{STL}$ $\forall \mathbf{e} \in \mathbb{E}^{STX} \vee \mathbf{e} \in \mathbb{E}^{STLX}$	Event e is a write.
$\mathtt{e} \in \mathbb{E}$: IsSync(\mathtt{e})	$e \in \mathbb{E}^{DmbSy} \lor e \in \mathbb{E}^{Isb}$	Event e is a dmb.sy or isb.
$\mathtt{e} \in \mathbb{E}$: $ComCnd(\mathtt{c},\mathtt{e})$	$\forall e' \in \mathbb{E} : \\ (((e' \prec_{\mathtt{data}} e) \lor (e' \prec_{\mathtt{ctrl}} e \land \\ (\mathtt{IsWrite}(e) \lor \mathtt{IsSync}(e))) \lor \\ (e' \prec_{\mathtt{poloc}} e) \lor (e' \prec_{\mathtt{addr}} e)) \Longrightarrow \\ (\mathtt{status}(e') = \mathtt{com}))$	All events preceding e in \prec_{data} , \prec_{addr} , \prec_{poloc} and if e is a write or a barrier, in \prec_{ctrl} , have already been committed.
$\mathtt{e} \in \mathbb{E}$: $RdComCnd(\mathtt{c},\mathtt{e})$	$\begin{array}{c} \forall \texttt{e}' \in \mathbb{E} : \\ ((\texttt{e}' \prec_{\texttt{data}} \texttt{e}) \lor (\texttt{e}' \prec_{\texttt{addr}} \texttt{e}) \Longrightarrow \\ (\texttt{status}(\texttt{e}') = \texttt{com}) \\ \land (\texttt{e} \in \mathbb{E}^{\texttt{LDX}} \cup \mathbb{E}^{\texttt{LDAX}}) \Longrightarrow \\ \forall \texttt{e}' \in \mathbb{E}^{\texttt{STX}} \cup \mathbb{E}^{\texttt{STLX}}.(\texttt{status}(\texttt{e}) \neq \texttt{init}) \end{array}$	All events on which e is dependent on have already been initialized. Further no prior store-exclusive is in it's init-stage (to avoid spurious successes of ST(L)X's).
$\mathfrak{e} \in \mathbb{E}^{A}:$ AssignComCnd $(\mathfrak{c},\mathfrak{e})$	$\forall \mathtt{e}' \in \mathbb{E} : \\ ((\mathtt{e}' \prec \mathtt{e}) \land (RegWritten(\mathtt{e}') \in OpRegs(\mathtt{e})) \land \\ \not \exists \mathtt{e}'' s.t. ((\mathtt{e}' \prec \mathtt{e}'' \prec \mathtt{e}) \land \\ (RegWritten(\mathtt{e}') = RegWritten(\mathtt{e}''))) \\ \Longrightarrow (status(\mathtt{e}') = com)$	The closest events writing to any register that e reads from have all been committed.
$\mathbf{e} \in \mathbb{E}^{\mathtt{LD}} \cup \mathbb{E}^{\mathtt{LDA}} \cup \mathbb{E}^{\mathtt{LDX}} \cup \mathbb{E}^{\mathtt{LDAX}}:$ $ReadFromNewEvent(\mathbf{c},\mathbf{e})$	$\exists e' \in \mathbb{E}^{LD} \cup \mathbb{E}^{LDA} \cup \mathbb{E}^{LDX} \cup \mathbb{E}^{LDAX} :$ $(e' \prec e) \land (rf(e') \neq rf(e)) \land$ $(\forall e' \in \mathbb{E}^{LD} \cup \mathbb{E}^{LDA} \cup \mathbb{E}^{LDX} \cup \mathbb{E}^{LDAX}.$ $e'' \prec e \implies e'' \prec e')$	The closest read event reading from the same location does so from a different event than that of e.

$\mathbf{e} \in \mathbb{E}^{\mathrm{LD}} \cup \mathbb{E}^{\mathrm{LDA}} \cup \mathbb{E}^{\mathrm{LDX}} \cup \mathbb{E}^{\mathrm{LDAX}}:$ $ReadExtComCnd(\mathbf{c},\mathbf{e})$	$\begin{array}{c} \forall \texttt{e}' \in \mathbb{E}^{\texttt{LD}} \cup \mathbb{E}^{\texttt{LDA}} \cup \mathbb{E}^{\texttt{LDX}} \cup \mathbb{E}^{\texttt{LDAX}} : \\ \text{ReadFromNewEvent}(\texttt{c},\texttt{e}) \implies \\ \text{status}(\texttt{e}') = \texttt{com} \end{array}$	The coherence order of $\mathfrak e$ w.r.t previous reads is maintained.
$\mathbf{e} \in \mathbb{E}^{\mathtt{LDA}} \cup \mathbb{E}^{\mathtt{LDAX}}:$ AcquireComCnd(\mathbf{c}, \mathbf{e})	$ \begin{array}{c} \forall e' \in \mathbb{E}^{ST} \cup \mathbb{E}^{STL} \cup \mathbb{E}^{STX} \cup \mathbb{E}^{STLX} : \\ (e' \in \mathbb{E}^{STX} \cup \mathbb{E}^{STLX}) \vee (\exists e'' \in \mathbb{E}^{LDX} \cup \mathbb{E}^{LDAX}. \\ \forall e''' \in \mathbb{E}^{STX} \cup \mathbb{E}^{STLX}.e''' \prec e' \implies e''' \prec e'') \\ \Longrightarrow (status(e') = com) \end{array} $	All write events part of or sandwiched between a load exclusive-store exclusive pair have already been committed.
$\mathbf{e} \in \mathbb{E}^{STX} \cup \mathbb{E}^{STLX}$: $SuccessCnd(\mathbf{c},\mathbf{e})$	$\operatorname{mark}(\mathbf{e}) = \operatorname{proc}(\mathbf{e})$	There has been no write to a location by any event after the po-closest load-exclusive by the same process.

8 Rules with synchronization conditions

For each of the rules below, c is the configuration before the rule, and is of the form $\langle \mathbb{E}, \prec, \text{ins}, \text{status}, \text{rf}, \text{Prop}, \text{Mark} \rangle$. The rules describe one possible way in which this configuration may evolve. The initial configuration is $\langle \emptyset, \emptyset, \lambda i.\emptyset, \lambda i.$

```
\frac{\mathbb{e} \in \mathbb{E}_p, \quad \prec' = \prec \cup \{\langle \mathbb{e}', \mathbb{e} \rangle | \mathbb{e}' \in \mathbb{E}_p\}, \quad i \in \mathsf{MaxI}(\mathbb{c}, p)}{\mathbb{c} \xrightarrow{p} \langle \mathbb{E} \cup \mathbb{e}, \prec', \mathsf{ins}[\mathbb{e} \leftarrow i], \mathsf{status}[\mathbb{e} \leftarrow \mathsf{fetch}], \mathsf{rf}, \mathsf{Prop}, \mathsf{Mark} \rangle} \mathsf{Fetch}
                                                                                                                                            \mathbf{e} \in \mathbb{E}_p^{\mathrm{LD}}, \quad \mathsf{status}(\mathbf{e}) = \mathsf{fetch}, \quad \mathsf{AllSyncs}(\mathbb{c}, \mathbf{e}), \quad \mathsf{RdComCnd}(\mathbb{c}, \mathbf{e}), \\ \\ \mathsf{AllDmbLds}(\mathbb{c}, \mathbf{e}), \quad \mathsf{AllLacqs}(\mathbb{c}, \mathbf{e}), \quad \mathbf{e}' = CW(\mathbb{c}, \mathbf{e}), \quad \mathsf{status}(\mathbf{e}') = \mathsf{init} \\ \mathsf{ComLDFromLocal}
                                                                                                                                                                                                          \mathbb{C} \xrightarrow{p} \langle \mathbb{E}, \prec, \text{ins}, \text{status}[\mathbb{e} \leftarrow \text{com}], \text{rf}[\mathbb{e} \leftarrow \mathbb{e}'], \text{Prop}, \text{Mark} \rangle
                                                                \mathbf{e} \in \mathbb{E}_p^{\mathrm{LD}}, \quad \mathsf{status}(\mathbf{e}) = \mathsf{fetch}, \quad \mathsf{AllSyncs}(\mathbf{c}, \mathbf{e}), \quad \mathsf{AllDmbLds}(\mathbf{c}, \mathbf{e}), \quad \mathsf{ReadExtComCnd}(\mathbf{c}, \mathbf{e}), \\ \quad \underline{\mathsf{AllLacqs}}(\mathbf{c}, \mathbf{e}), \quad (CW(\mathbf{c}, \mathbf{e}) = \bot) \vee (CW(\mathbf{c}, \mathbf{e}) = \mathbf{e}' \wedge \mathsf{status}(\mathbf{e}') = \mathsf{com}), \quad \mathsf{RdComCnd}(\mathbf{c}, \mathbf{e}) \\ \quad \underline{\mathsf{ComLDFromProp}}(\mathbf{c}, \mathbf{e}), \quad \underline{\mathsf{ComLDFromProp}}(\mathbf{c}, \mathbf{e}), \quad \underline{\mathsf{ComLDFromProp}}(\mathbf{c}, \mathbf{e}))
                                                                                                                                                              \mathbb{C} \xrightarrow{p} \langle \mathbb{E}, \prec, \mathsf{ins}, \mathsf{status}[\mathbb{e} \leftarrow \mathsf{com}], \mathsf{rf}[\mathbb{e} \leftarrow \mathsf{Prop}(\mathsf{Var}(\mathbb{c}, \mathbb{e}))], \mathsf{Prop}, \mathsf{Mark} \rangle
                                                                                                                                             \mathbf{e} \in \mathbb{E}_p^{\mathrm{LDX}}, \quad \mathrm{status}(\mathbf{e}) = \mathrm{fetch}, \quad \mathrm{AllSyncs}(\mathbf{c}, \mathbf{e}), \quad \mathrm{RdComCnd}(\mathbf{c}, \mathbf{e}),
                                                                                                                                 \frac{\mathsf{AllDmbLds}(\mathbb{c},\mathbb{e}), \quad \mathsf{AllLacqs}(\mathbb{c},\mathbb{e}), \quad \mathbb{e}' = CW(\mathbb{c},\mathbb{e}), \quad \mathsf{status}(\mathbb{e}') = \mathsf{init}}{\mathbb{c} \xrightarrow{p} \langle \mathbb{E}, \prec, \mathsf{ins}, \mathsf{status}[\mathbb{e} \leftarrow \mathsf{com}], \mathsf{rf}[\mathbb{e} \leftarrow \mathbb{e}'], \mathsf{Prop}, \mathsf{Mark}[\mathsf{var}(\mathbb{e}) \leftarrow \mathsf{proc}(\mathbb{e})] \rangle} \mathsf{ComLDXFromLocal}}
                                                             \textbf{e} \in \mathbb{E}_{p}^{\text{LDX}}, \quad \text{status}(\textbf{e}) = \text{fetch}, \quad \text{AllSyncs}(\textbf{c},\textbf{e}), \quad \text{AllDmbLds}(\textbf{c},\textbf{e}), \quad \text{ReadExtComCnd}(\textbf{c},\textbf{e}),
                                                                            \frac{\mathsf{AllLacqs}(\mathtt{c},\mathtt{e}), \quad (CW(\mathtt{c},\mathtt{e}) = \bot) \vee (CW(\mathtt{c},\mathtt{e}) = \mathtt{e}' \wedge \mathsf{status}(\mathtt{e}') = \mathsf{com}), \quad \mathsf{RdComCnd}(\mathtt{c},\mathtt{e})}{\mathtt{c} \xrightarrow{p} \langle \mathbb{E}, \prec, \mathsf{ins}, \mathsf{status}[\mathtt{e} \leftarrow \mathsf{com}], \mathsf{rf}[\mathtt{e} \leftarrow \mathsf{Prop}(\mathsf{Var}(\mathtt{c},\mathtt{e}))], \mathsf{Prop}, \mathsf{Mark}[\mathsf{var}(\mathtt{e}) \leftarrow \mathsf{proc}(\mathtt{e})] \rangle} \mathsf{ComLDXFromProp}(\mathtt{c},\mathtt{e})
                                                                   \mathbb{e} \in \mathbb{E}_n^{\text{LDA}}, \quad \text{status}(\mathbb{e}) = \text{fetch}, \quad \text{AllSyncs}(\mathbb{c},\mathbb{e}), \quad \text{AllSRels}(\mathbb{c},\mathbb{e}), \quad \text{AcquireComCnd}(\mathbb{c},\mathbb{e}),
                                                                        \frac{\mathsf{AllDmbLds}(\mathbb{c},\mathbb{e}), \quad \mathsf{AllLacqs}(\mathbb{c},\mathbb{e}), \quad \mathbb{e}' = CW(\mathbb{c},\mathbb{e}), \quad \mathsf{status}(\mathbb{e}') = \mathsf{init}, \quad \mathsf{RdComCnd}(\mathbb{c},\mathbb{e})}{\mathbb{c} \stackrel{p}{\longrightarrow} \langle \mathbb{E}, \prec, \mathsf{ins}, \mathsf{status}[\mathbb{e} \leftarrow \mathsf{com}], \mathsf{rf}[\mathbb{e} \leftarrow \mathbb{e}'], \mathsf{Prop}, \mathsf{Mark} \rangle} \mathsf{ComLDAFromLocal}
   \mathbb{e} \in \mathbb{E}_p^{\text{LDA}}, \quad \text{status}(\mathbb{e}) = \text{fetch}, \quad \text{AllSyncs}(\mathbb{c},\mathbb{e}), \quad \text{AllLacqs}(\mathbb{c},\mathbb{e}), \quad \text{RdComCnd}(\mathbb{c},\mathbb{e}), \quad \text{ReadExtComCnd}(\mathbb{c},\mathbb{e}),
  \mathsf{AllDmbLds}(\mathbb{c},\mathbb{e}), \quad \mathsf{AllSRels}(\mathbb{c},\mathbb{e}), \quad \mathsf{Acqui} \underbrace{\mathsf{reComCnd}(\mathbb{c},\mathbb{e}), \quad (CW(\mathbb{c},\mathbb{e}) = \bot) \vee (CW(\mathbb{c},\mathbb{e}) = \mathbb{e}' \wedge \mathsf{status}(\mathbb{e}') = \mathsf{com})}_{\mathsf{ComLDAFromProp}} \mathsf{ComLDAFromProp}(\mathbb{c},\mathbb{e}) = \mathbb{c}' \wedge \mathsf{status}(\mathbb{c}') = \mathsf{com})
                                                                                                                                                                  \mathbb{C} \xrightarrow{p} \langle \mathbb{E}, \prec, \text{ins}, \text{status}[e \leftarrow \text{com}], \text{rf}[e \leftarrow \text{Prop}(\text{Var}(\mathbb{c}, e))], \text{Prop}, \text{Mark} \rangle
                                                             \mathbf{e} \in \mathbb{E}_p^{\mathrm{LDAX}}, \quad \mathsf{status}(\mathbf{e}) = \mathsf{fetch}, \quad \mathsf{AllSyncs}(\mathbf{c}, \mathbf{e}), \quad \mathsf{AllSRels}(\mathbf{c}, \mathbf{e}), \quad \mathsf{AcquireComCnd}(\mathbf{c}, \mathbf{e}), \\ \\ \underline{\mathsf{AllDmbLds}}(\mathbf{c}, \mathbf{e}), \quad \mathsf{AllLacqs}(\mathbf{c}, \mathbf{e}), \quad \mathbf{e}' = CW(\mathbf{c}, \mathbf{e}), \quad \mathsf{status}(\mathbf{e}') = \mathsf{init}, \quad \mathsf{RdComCnd}(\mathbf{c}, \mathbf{e}) \\ \underline{\mathsf{ComLDAXFromLocal}}(\mathbf{c}, \mathbf{e}), \quad \underline{\mathsf{ComLDAXFromLocal}}(\mathbf{c}, \mathbf{e}), \quad \underline{\mathsf{ComLDAXFromLocal}}(\mathbf{c}, \mathbf{e}), \\ \underline{\mathsf{ComLDAX
                                                                                                                           \mathbb{C} \xrightarrow{p} \langle \mathbb{E}, \prec, \text{ins, status}[e \leftarrow \text{com}], \text{rf}[e \leftarrow e'], \text{Prop, Mark}[\text{var}(e) \leftarrow \text{proc}(e)] \rangle
\textbf{e} \in \mathbb{E}_p^{\texttt{LDAX}}, \quad \texttt{status}(\textbf{e}) = \texttt{fetch}, \quad \texttt{AllSyncs}(\textbf{c},\textbf{e}), \quad \texttt{AllLacqs}(\textbf{c},\textbf{e}), \quad \texttt{RdComCnd}(\textbf{c},\textbf{e}), \quad \texttt{ReadExtComCnd}(\textbf{c},\textbf{e}),
  \mathsf{AllDmbLds}(\mathbb{c},\mathbb{e}), \quad \mathsf{AllSRels}(\mathbb{c},\mathbb{e}), \quad \mathsf{AcquireComCnd}(\mathbb{c},\mathbb{e}), \quad (CW(\mathbb{c},\mathbb{e}) = \bot) \lor (CW(\mathbb{c},\mathbb{e}) = \mathbb{e}' \land \mathsf{status}(\mathbb{e}') = \mathsf{com}) \\ \mathsf{ComLDAXFromProp}(\mathbb{c},\mathbb{e}) = \mathbb{c}' \land \mathsf{status}(\mathbb{e}') = \mathbb{c}' \land \mathsf{status}(\mathbb{e}') = \mathsf{com}) \\ \mathsf{ComLDAXFromProp}(\mathbb{c},\mathbb{e}) = \mathbb{c}' \land \mathsf{status}(\mathbb{e}') = \mathbb{c}' \land \mathsf{status}(\mathbb{e}') = \mathsf{com}) \\ \mathsf{ComLDAXFromProp}(\mathbb{c},\mathbb{e}) = \mathbb{c}' \land \mathsf{status}(\mathbb{e}') = \mathbb{c}' \land \mathsf{status}(\mathbb
                                                                                                  \mathbb{C} \xrightarrow{p} \langle \mathbb{E}, \prec, \mathsf{ins}, \mathsf{status}[\mathbb{e} \leftarrow \mathsf{com}], \mathsf{rf}[\mathbb{e} \leftarrow \mathsf{Prop}(\mathsf{Var}(\mathbb{c}, \mathbb{e}))], \mathsf{Prop}, \mathsf{Mark}[\mathsf{var}(\mathbb{e}) \leftarrow \mathsf{proc}(\mathbb{e})] \rangle
                                                                                                                                                                                    \frac{\mathbb{e} \in \mathbb{E}_p^{\mathrm{STL}} \cup \mathbb{E}_p^{\mathrm{STL}} \cup \mathbb{E}_p^{\mathrm{STLX}}, \quad \mathrm{status}(\mathbb{e}) = \mathrm{fetch}, \quad \mathrm{InitCnd}(\mathbb{c}, \mathbb{e}),}{\mathbb{c} \xrightarrow{p} \langle \mathbb{E}, \prec, \mathrm{ins}, \mathrm{status}[\mathbb{e} \leftarrow \mathrm{init}], \mathrm{rf}, \mathrm{Prop}, \mathrm{Mark} \rangle} \mathrm{InitWrite}
                                                                                                                                                                                                        \frac{\mathbb{e} \in \mathbb{E}_p^{\text{STX}} \cup \mathbb{E}_p^{\text{STLX}}, \quad \text{status}(\mathbb{e}) = \text{fetch}}{\mathbb{c} \xrightarrow{p} \left\langle \mathbb{E}, \prec, \text{ins}, \text{status}[\mathbb{e} \leftarrow \text{com}], \text{rf}, \text{Prop}, \text{Mark} \right\rangle} \text{ComFailExclusiveWrite}
```

```
\mathbf{e} \in \mathbb{E}_p^{\mathrm{ST}}, \quad \mathrm{status}(\mathbf{e}) = \mathrm{init}, \quad \mathrm{ComCnd}(\mathbf{c}, \mathbf{e}), \quad \mathrm{AddrCnd}(\mathbf{c}, \mathbf{e}),
             \mathsf{AllSyncs}(\mathbb{C},\mathbb{e}), \quad \mathsf{AllSyncs}(\mathbb{C},\mathbb{e}), \quad \mathsf{AllDmbLds}(\mathbb{C},\mathbb{e}), \quad \mathsf{AllLAcqs}(\mathbb{C},\mathbb{e}), \quad \mathsf{AllDmbSts}(\mathbb{C},\mathbb{e}) \\ \mathsf{ComST}(\mathbb{C},\mathbb{e}), \quad \mathsf{AllDmbSts}(\mathbb{C},\mathbb{e}), \quad \mathsf{AllDmbSts}(\mathbb{C},\mathbb{e}), \quad \mathsf{AllDmbSts}(\mathbb{C},\mathbb{e})
                                \boxed{ \texttt{c} \xrightarrow{p} \langle \mathbb{E}, \prec, \texttt{ins}, \texttt{status}[\texttt{e} \leftarrow \texttt{com}], \texttt{rf}, \texttt{Prop}[\texttt{var}(\texttt{e}) \leftarrow \texttt{e}], \texttt{Mark}[\texttt{var}(\texttt{e}) \leftarrow \bot] \rangle}
                                                          e \in \mathbb{E}_n^{\mathsf{STL}}, \quad \mathsf{status}(e) = \mathsf{init}, \quad \mathsf{ComCnd}(e, e), \quad \mathsf{AddrCnd}(e, e),
               \frac{\mathsf{AllSyncs}(\mathbb{c},\mathbb{e}), \quad \mathsf{AllSyncs}(\mathbb{c},\mathbb{e}), \quad \mathsf{AllDmbLds}(\mathbb{c},\mathbb{e}), \quad \mathsf{AllMem}(\mathbb{c},\mathbb{e}), \quad \mathsf{AllDmbSts}(\mathbb{c},\mathbb{e})}{\mathsf{ComSTL}} \\
                             \mathbb{C} \xrightarrow{p} \langle \mathbb{E}, \prec, \text{ins}, \text{status}[\mathbb{e} \leftarrow \text{com}], \text{rf}, \text{Prop}[\text{var}(\mathbb{e}) \leftarrow \mathbb{e}], \text{Mark}[\text{var}(\mathbb{e}) \leftarrow \bot] \rangle
                            \textbf{e} \in \mathbb{E}_p^{\text{STX}}, \quad \text{status}(\textbf{e}) = \text{init}, \quad \text{ComCnd}(\textbf{c},\textbf{e}), \quad \text{AddrCnd}(\textbf{c},\textbf{e}), \quad \text{SuccessCnd}(\textbf{c},\textbf{e}),
\mathsf{AllSyncs}(\mathbb{c},\mathbb{e}), \quad \mathsf{AllSyncs}(\mathbb{c},\mathbb{e}), \quad \mathsf{AllDmbLds}(\mathbb{c},\mathbb{e}), \quad \mathsf{AllLAcqs}(\mathbb{c},\mathbb{e}), \quad \mathsf{AllDmbSts}(\mathbb{c},\mathbb{e}) \\ \mathsf{ComSuccessSTX}
                \mathbb{C} \xrightarrow{p} \langle \mathbb{E}, \prec, \text{ins}, \text{status}[\mathbb{e} \leftarrow \text{init}], \text{rf}, \text{Prop}[\text{var}(\mathbb{e}) \leftarrow \mathbb{e}], \text{Mark}[\text{var}(\mathbb{e}) \leftarrow \bot] \rangle
                           e \in \mathbb{E}_n^{\mathsf{STLX}}, \mathsf{status}(e) = \mathsf{init}, \mathsf{ComCnd}(e, e), \mathsf{AddrCnd}(e, e), \mathsf{SuccessCnd}(e, e),
 \mathsf{AllSyncs}(\mathbb{c},\mathbb{e}), \quad \mathsf{AllSyncs}(\mathbb{c},\mathbb{e}), \quad \mathsf{AllDmbLds}(\mathbb{c},\mathbb{e}), \quad \mathsf{AllMem}(\mathbb{c},\mathbb{e}), \quad \mathsf{AllDmbSts}(\mathbb{c},\mathbb{e}) \\ \mathsf{ComSuccessSTLX}
              \mathbb{c} \xrightarrow{p} \langle \mathbb{E}, \prec, \mathsf{ins}, \mathsf{status}[\mathbb{e} \leftarrow \mathsf{init}], \mathsf{rf}, \mathsf{Prop}[\mathsf{var}(\mathbb{e}) \leftarrow \mathbb{e}], \mathsf{Mark}[\mathsf{var}(\mathbb{e}) \leftarrow \bot] \rangle
          \textbf{e} \in \mathbb{E}_n^{\texttt{DmbSy}}, \quad \texttt{status}(\textbf{e}) = \texttt{fetch}, \quad \texttt{ComCnd}(\textbf{e}, \textbf{e}), \quad \texttt{AllMem}(\textbf{e}, \textbf{e}), \quad \texttt{AllBarriers}(\textbf{e}, \textbf{e}) \\ \hline \\ \texttt{ComDmbSy}
                                                                               \mathbb{C} \xrightarrow{p} \langle \mathbb{E}, \text{ins}, \text{status} [\mathbb{e} \leftarrow \text{com}], \text{rf}, \text{Prop} \rangle
                  \frac{\mathbb{e} \in \mathbb{E}_p^{\mathrm{Isb}}, \quad \mathsf{status}(\mathbb{e}) = \mathsf{fetch}, \quad \mathsf{ComCnd}(\mathbb{c}, \mathbb{e}), \quad \mathsf{AddrCnd}(\mathbb{c}, \mathbb{e}), \quad \mathsf{AllDmbSys}(\mathbb{c}, \mathbb{e})}{\mathbb{c} \xrightarrow{p} \langle \mathbb{E}, \mathsf{ins}, \mathsf{status}[\mathbb{e} \leftarrow \mathsf{com}], \mathsf{rf}, \mathsf{Prop} \rangle} \mathsf{ComIsb}
          \textbf{e} \in \mathbb{E}_p^{\texttt{DmbLd}}, \quad \texttt{status}(\textbf{e}) = \texttt{fetch}, \quad \texttt{ComCnd}(\textbf{c},\textbf{e}), \quad \texttt{AllReads}(\textbf{c},\textbf{e}), \quad \texttt{AllDmbSys}(\textbf{c},\textbf{e}) \\ & \\ \texttt{ComDmbLd}
                                                                      \mathbb{C} \xrightarrow{p} \langle \mathbb{E}, \text{ins}, \text{status} | \mathbb{e} \leftarrow \text{com} |, \text{rf}, \text{Prop}, \text{Mark} \rangle
        \textbf{e} \in \mathbb{E}_p^{\texttt{DmbSt}}, \quad \texttt{status}(\textbf{e}) = \texttt{fetch}, \quad \underbrace{\texttt{ComCnd}(\textbf{c}, \textbf{e}), \quad \texttt{AllWrites}(\textbf{c}, \textbf{e}), \quad \texttt{AllDmbSys}(\textbf{c}, \textbf{e})}_{\texttt{ComDmbSt}} \texttt{ComDmbSt}
                                                                      \mathbb{C} \xrightarrow{p} \langle \mathbb{E}, \mathsf{ins}, \mathsf{status}[e \leftarrow \mathsf{com}], \mathsf{rf}, \mathsf{Prop}, \mathsf{Mark} \rangle
                  \textbf{e} \in \underbrace{\mathbb{E}^{\text{ACI}}_p, \quad \text{status}(\textbf{e}) = \text{fetch}, \quad \text{ComCnd}(\textbf{c},\textbf{e}), \quad \text{ValidCnd}(\textbf{c},\textbf{e}), \quad \text{AllSyncs}(\textbf{c},\textbf{e})}_{\text{ComACI}}
                                                                         \mathbb{C} \xrightarrow{p} \langle \mathbb{E}, \text{ins}, \text{status}[e \leftarrow \text{com}], \text{rf}, \text{Prop}, \text{Mark} \rangle
```

We explain the above rules as thus:

- The Fetch rule is the same as before (and is cosmetic as explained above).
- We need the following pre-conditions to hold for committing a non-acquire read (exclusive as well as not) event e (from either local uncommitted events or memory):
 - 1. For all events \mathfrak{C}' that are poloc-predecessors of \mathfrak{C} , \mathfrak{C}' must have been initialized.
 - 2. All dmb.sy, isb and dmb.ld instructions that are po-predecessors of e have been committed.
 - 3. All po-preceding load acquire instructions have been committed.
 - 4. All data and addr dependents have committed.
- The rule for committing an acquire-read (exclusive as well as not) is similar to that above, but with the extra condition that all po-previous Store Releases have been committed. Further, all writes po-before the read that are a part of an LX-SX block should also have been committed.
- One condition required for committing for any kind of write needs that we know the "memory footprint", i.e. address of all po-previous memory access events is known.
- To initialize a (non-exclusive, non-release) write, along with an InitCnd that we had previously (but which also includes address dependencies now), we need the following condition to hold: all po-previous dmb.sy, isb, dmb.ld, dmb.st, and Load Acquire instructions have been committed.
- To initialize a release- but non-exclusive write (STL), instead of just load-acquires, we need *all* po-preceding memory access instructions to have been committed.
- To commit any write, two of the conditions required are ComCnd and AddrCnd. The latter postulates that all po-previous events have well defined memory footprints. However, note that the success-value-writes of exclusive stores to registers are not bound by any addr or data relations.
- The exclusive versions of the two kinds of writes are to be directly committed and failed at any point even before the address has been resolved (this is in fact tested by a litmus test). If instead they are to succeed, they need to go through the regular init and commit steps.
- The condition for committing a non-exclusive write is similar to other writes, with the added condition that checks for success.

- All ACI and barrier instructions have only one transition: from fetch to commit. Across all of them, the ComCnd and ValidCnd are common conditions, as is the condition that all dmb.sy's have been committed (for ACI's and dmb.sy's we also need po-previous isb's to have been committed). Apart from this,
 - 1. For dmb.sy's we need all po-previous memory access instructions to have committed.
 - 2. For isb's we need all po-previous memory access instructions to have fully defined memory footprints.
 - 3. For dmb.ld's we need all po-previous load (read and load acquire) instructions to have been committed.
 - 4. For dmb.st's we need all po-previous stores (write and store release) instructions to have been committed.

Assign instructions. The Herd or the Flat model do not explicitly handle assign instructions. Consider the hypothetical scenario where we assign the value of a register r_1 to a register r_2 . We would then want the latter to be able to init/commit just after but no before the former. Generalizing this to any assign, we postulate that an assign can commit once all of it's operands (unless they are literals) have committed. We also corroborate the validity of this rule via litmus tests. Note that this rule is, in a sense, not a central rule: it is not directly modelled by Herd of Flat, and it's only purpose is to act as a bridge connected many producing LD*'s to an event. Thus, it is, in effect, a syntactic sugar and does not represent a "real" (i.e. interfacing with memory) event.

$$\frac{\mathbb{e} \in \mathbb{E}_p^A, \quad \mathsf{status}(\mathbb{e}) = \mathsf{fetch}, \quad \mathsf{AssignComCnd}(\mathbb{c}, \mathbb{e})}{\mathbb{c} \xrightarrow{p} \langle \mathbb{E}, \prec, \mathsf{ins}, \mathsf{status}[\mathbb{e} \leftarrow \mathsf{com}], \mathsf{rf}, \mathsf{Prop} \rangle} \mathsf{ComAssign}$$

9 Proof of equivalence to the Herd Model

We give here the proof of equivalence of the above model to the Herd model, as found in section B2.3 of the ARM developer manual. There are two main conditions for the equivalence to hold: the internal and the external visibility requirements. We do not take into account tag reads or tag writes since our model does not include them. We use the .cat file available at [6] for our purposes of specification: we note that the requirements are stated as predicates over possible orderings, and are as follows:

```
(* Ordered-before *)
(* Internal visibility requirement *)
                                                    let rec ob = obs; si
let po-loc =
                                                             lob
  let Exp = M \setminus domain(tob) in
                                                             ob; ob
  (po-loc & Exp*Exp) | (po & tlo)
acyclic po-loc | ca | rf as internal
                                                    (* Locally-ordered-before *)
                                                    let rec lob = lws; si
(* External visibility requirement *)
                                                                   dob
irreflexive ob as external
                                                                   aob
                                                                   bob
(* Observed-by *)
                                                                   tob
let obs = rfe | fre | coe
                                                                  lob; lob
```

Above, po-loc, ca and rf stand for meanings consistent with our definitions, and lob stands for "locally-ordered-before". Further, rfe stands for "read-from-external", and so on. The constituents of lob are further elaborated as:

```
(* Local write successor *)
let lws = po-loc; [W]
                                               (* Local read successor *)
                                              let lrs = [W]; (po-loc \setminus (po-loc; [W]; po-loc)); [R]
(*Atomic-ordered-before *)
let aob = rmw
                                               (* Read-modify-write *)
         | [range(rmw)]; lrs; [A | Q]
                                              let rmw = lxsx \mid amo
(* Barrier-ordered-before *)
                                               (* Dependency-ordered-before *)
let bob = po; [dmb.full]; po
                                              let dob = addr \mid data
         | po; ([A]; amo; [L]); po
                                                        | \operatorname{ctrl}; [W]
           [L]; po; [A]
                                                        | (ctrl | (addr; po)); [ISB]; po; [R]
           [R \setminus NoRet]; po; [dmb.ld]; po
                                                        | addr; po; [W]
           [A \mid Q]; po
                                                       | (addr | data); lrs
           [W]\,;\ po\,;\ [dmb.\,st\,]\,;\ po\,;\ [W]
           po; [L]
```

Above, si relates events belonging to the same instruction, and range refers to all the events constituting the rmw block (i.e., the read, the comparison and the write). Also, [A] and [L] refer to acquire and release instructions, respectively.

We further comment that we do not support amo-type instructions for simplicity. However, it is straightforward to extend the model to create rules for amo instruction. We call our model as ARM' and the model presented above as ARM. We wish to show that ARM' \equiv ARM. For this, we prove subsumption in both directions below. Note that we do not consider the tob

condition since we do not support tags in our model. Further, for our purposes rmw is equivalent to a lx+sx pair due to non-existence of amo instructions under our model. We omit assign events in the following proof since the Herd model does not talk about it; however note that since an assign can take any transition once all of it's operands have, adding an assign is simply equivalent to conjunction of multiple data dependencies. As mentioned above, we also verify this through extensive litmus testing.

9.1 All execution traces valid under ARM' are valid under ARM

First consider the internal visibility requirements. Note that due to the rules, read events always read from either the main memory or from the closest po-before write. We also have that writes need all dependents to have been committed before the former are initialized. Consequently, from the above two, the locally observed poloc-order is acyclic. Further, ca simply stems from poloc-order in the case of writes. For rf, note that when a read is committed, it's closest write must have either initialized (if it reads via forwarding) or have been committed (if it reads from main memory). In either case, if the event it reads from belongs to the same thread must have already at least been initialized, preserving the rf order. Thus no cycle may exist among these pairs: hence the internal order is acyclic, as needed.

Next we come to the external visibility constraints. For rfe, note that an event can only read from an event via main memory if the latter has been committed already, preserving rfe. Further, an event cannot read from an event that commits after it, preserving the fre order. In addition, coe is obviously preserved among write-write and read-write pairs since after a write event \mathfrak{e}_1 "overwrites" another write event \mathfrak{e}_2 , no event can read from \mathfrak{e}_2 ever again. Finally, we come to read-read pairs. If two consecutive reads r_1 and r_2 (not separated by a write; otherwise the ordering follows trivially from the read-write-read ordering) read from different events we require their ordering to be consistent with the requirement of coherence. Note that this case cannot arise in the case of forwarding since forwarding will happen from the po-closest write which would be the same for both. In the case of reading from main memory, the ReadExtCnd ensures preservation of coherence order. These imply that the partial order obs is preserved.

Further, from ComCnd we conclude that lws is preserved.

Next we tackle dob. The first line is obviously satisfied since ComCnd/RdComCnd enforces preservation of addr and data dependencies. Further, note that ComCnd also enforces the second line of dob. In addition, the AddrCnd appears in all the write-commit rules and ensures that the fourth line of dob is respected. The third line holds because a) When committing an ISB event, the AddrCnd and ComCnd ensure the first half of the order holds; and b) We require all ISB's to have been committed while committing reads. Note: We require this even for writes, but note that anyway writes have to commit after any event they are dependent on via ctrl or addr; po so this is a redundant clause and causes no extra conditions for writes. For the final line, note that we need reads to commit not before a write whose lrs the read is, is initialized. Further, said write can init only after it's address and data dependents have committed, effectively proving the last line of dob.

In effect, we have proved that dob is preserved under ARM'.

Next we come to aob. Since we do not model amo instructions, we can focus on lx-sx pairs exclusively. The listed condition is the same as our AcquireComCnd, and thus we conclude that the ordering aob is preserved.

Next we come to bob. The first line follows since dmb.sy's require virtually every preceding event (other than assigns) to have committed, and all events require every po-previous dmb.sy to have committed. The second line is not of consequence since we do not model amo instructions. The third follows from the AllSRels predicate appearing in the commit-rules for acquire-loads. The next follows from the predicate AllReads of ComDmbLd and AllDmbLds that appears while committing any read/write event. The line after that is respected since AllLAcqs appears in all read-write events. Similarly, the sixth line too is respected. Finally, the last line follows from the AllMem predicate that appears in the commit-rules for store-releases. This completes bob. We do not model tags and so tob is skipped.

The final line of lob is transitivity which obviously holds here.

Since lws,dob,aob and bob are preserved, so is lob. Further, since obs is also preserved, we conclude that ob is preserved. Hence, we have that $ARM' \subseteq ARM$.

9.2 All execution traces valid under ARM are valid under ARM'

To prove this direction, we must reconstruct all of the rules of our model from the predicates of the Herd model. The Fetch rule is not relevant, since given any run that is valid under ARM, one can imagine an equivalent run under ARM', where every instruction is fetched just before it is initialized (so we only need to prove the validity of other rules).

Consider the ComlDFrom* rules. The AllSyncs predicate is justified by the first line of bob and the third line of dob. The AllDmbLds is justified by the fourth line of bob. Further, the AllLacqs predicate is justified by the fifth line of bob. Then, the condition that the closest read has been at least initialized is derived from the local visibility condition on ca. Further, RdComCnd has two parts: addr and data. Both are justified using the first line of dob. Finally, the rule ReadExtCnd can be derived from the external visibility order - coherence, on reads.

Next, in the ComlDAFrom* rules, the only extra predicates are AllSRels and AcquireComCnd. The former is justified using the third line of bob. The latter follows from the definition in the second line of aob.

For ComLDXFrom* and ComLDAX* rules, the same arguments hold as above since they are functionally identical to the above two, and only differ in the update of the "mark" attribute.

The rule InitCnd in InitWrite follows from the internal visibility condition, for the following reason: if writes could initialize

before a read event that supplies, e.g. their data is committed, then we could have a scenario where this same read event reads-from that write, violating the acyclicity of local visibility. The AllSyncs, AllDmbLds and AllLacqs for committing writes are explained as for reads. The AllDmbSts predicate follows from the sixth line of bob. Also, the part of ComCnd about ACI events is due to the second line of dob.

The only extra predicate in the case of ComSTL is AllMem (which subsumes AllLacqs). This is justified by referring to the last line of bob.

Further, the AddrCnd is a consequence of the fourth line of dob. The ComCnd is as before, with the poloc order added in to respect the ca order (coe as appears in obs).

For failing of exclusive writes, there are in fact no rules: they can fail even before any of their addresses are resolved, as mentioned before; consistent with our rule. This is further elaborated upon in a hand-crafted litmus test which is a part of our litmus suite. Lastly, if they succeed, they have the very same conditions as other stores. The onyl extra condition is the SuccessCnd, which is justified since it ensures that the write did in fact succeed. Note that, we could initialize an exclusive write expecting it to succeed and never be able to proceed with committing due to the violation of SuccessCnd: this does not emulate a real system but leads to a deadlock which does not affect reachability.

For the ComDmb* rules, the respective lines of bob are enough justification. Further, for dmb.sy's and isb's, the first line of bob and the third line of dob imply the commit of ACI instructions as well.

Thus, we have that $ARM \subseteq ARM'$.

Combining this with the result of the previous subsection, we conclude that

$$ARM' \equiv ARM$$

10 Context Bound Model Checking for ARM

In the spirit of Context Bound Model Checking, we propose a code-to-code translation from source code written under the ARMv8 model to one that runs under Sequential Consistency (SC), but with a bound on the maximum number of contexts of execution. Here, we define a context as a stretch of execution (across time) in which only one process is active. Thus, inside a single context, the program behaves exactly like SC to the executing process (and the other processes are not executing). This context-bound reduction was first pioneered by Lal and Reps [5], and we adapt their approach (with the required changes) to fit the ARMv8 model. In particular, our code guesses the global state (the state of the main memory) at all context switches. Then, our code simulates, for each process, the contexts in which it is active, starting from the respective guessed global states. In the end, we verify, that for each context k, the process active in context k transforms the global state from that guessed at the end of context k-1 to that guessed at the end of context k. The advantage of this approach over naive simulation is that it avoids having to deal with cross-products of local spaces, and hence avoids the exponential blowup associated with it. As an end result, we have code that when run under SC successfully simulates all possible runs under the ARM v8 memory model that incur at most k context switches. That is, Context Bound Model Checking is an efficient under-approximation to state reachability. Since it has been demonstrated before that most bugs are (as a general rule of thumb) reachable in a small number of context switches, our approach is an effective means of tackling the undecidability of the ARM v8 memory model.

We first demonstrate the above method on the simple model introduced at the beginning of the document, and then proceed to adapt it to the whole model.

11 Code-to-code translation for reduction to SC (for the simple model)

For the sake of performing context-bound model checking, we next define the scheme for the code-to-code translation.

11.1 Scheme for the first part of model (without synchronization instructions)

Our translation scheme translates a program Prog into a program $Prog^{\clubsuit}$ using the map function $\llbracket \cdot \rrbracket_K$. Let \mathcal{P} and \mathcal{X} be the set of processes and shared variables in our program. Then, the map $\llbracket \cdot \rrbracket_K$ replaces the variables of Prog by $|\mathcal{P}| \cdot K$ copies of the set \mathcal{X} , along with a finite set of finite data structures defined below. Below, the function gen takes in a finite set and returns a randomly chosen element of the set.

$$\begin{split} \llbracket Prog \rrbracket_K & \stackrel{\text{def}}{=} \text{ vars: } x^* \ \langle \text{addvars} \rangle_K \\ & \text{procs: } (\llbracket p \rrbracket_K)^* \ \langle \text{initProc} \rangle_K \ \langle \text{verProc} \rangle_K \\ & \llbracket p \rrbracket_K \stackrel{\text{def}}{=} \text{regs: } \$r^* \\ & \text{instrs: } (\llbracket i \rrbracket_K^p)^* \\ & \llbracket i \rrbracket_K^p \stackrel{\text{def}}{=} l : \ \llbracket \mathbf{s} \rrbracket_K^p \\ & \llbracket x \leftarrow exp \rrbracket_K^p \stackrel{\text{def}}{=} \llbracket x \leftarrow exp \rrbracket_K^{\mathbf{p}, \text{Write}} \end{split}$$

$$\llbracket \$r \leftarrow x \rrbracket_K^p \overset{\text{def}}{=} \llbracket \$r \leftarrow x \rrbracket_K^{p, \text{Read}} \\ \llbracket \$r \leftarrow exp \rrbracket_K^p \overset{\text{def}}{=} \llbracket \$r \leftarrow exp \rrbracket_K^{p, \text{Assign}} \\ \llbracket \text{if } exp \text{ then } i^* \text{ else } i^* \rrbracket_K^p \overset{\text{def}}{=} \text{if } exp \text{ then } (\llbracket i \rrbracket_K^p)^* \text{ else } (\llbracket i \rrbracket_K^p)^*; \ \langle \text{control} \rangle_K^p \\ \llbracket \text{while } exp \text{ do } i^* \rrbracket_K^p \overset{\text{def}}{=} \text{while } exp \text{ do } (\llbracket i \rrbracket_K^p)^*; \ \langle \text{control} \rangle_K^p \\ \llbracket \text{assume } exp \rrbracket_K^p \overset{\text{def}}{=} \text{assume } exp; \ \langle \text{control} \rangle_K^p \\ \llbracket \text{assert } exp \rrbracket_K^p \overset{\text{def}}{=} \text{assert } exp; \ \langle \text{control} \rangle_K^p \\ \llbracket \text{term} \rrbracket_K^p \overset{\text{def}}{=} \text{term} \\ \langle \text{addvars} \rangle_K \overset{\text{def}}{=} \mu(|\mathcal{X}|, K), \mu^{init}(|\mathcal{X}|, K), \nu(|\mathcal{P}|, |\mathcal{X}|), \\ \mathsf{cR}(|\mathcal{P}|, |\mathcal{X}|), \\ \mathsf{iW}(|\mathcal{P}|, |\mathcal{X}|), \mathsf{cW}(|\mathcal{P}|, |\mathcal{X}|), \\ \mathsf{cReg}(|\mathcal{P}|, |\mathcal{R}|), \\ \mathsf{ctrl}(|\mathcal{P}|), \mathsf{active}(K) \\ \mathsf{assume}(cnt \leq K) \\ \langle \mathsf{control} \rangle_K^p \overset{\text{def}}{=} \mathsf{ctrl}(p) \leftarrow \mathsf{ctrl}(p) + \mathsf{gen}(0, \cdots, K-1); \\ \mathsf{assume}(\mathsf{ctrl}(p) \leq K) \\ \end{cases}$$

11.2 Data Structures (for the model without synchronization)

We denote by \mathcal{D} the domain of all possible values of expressions and variables. Our simulation maintains, as described above, a finite set of finite data structures. We explain each in turn. First, for each context k, we store the ID of the active process p in the context k, using the mapping $\operatorname{active}:[1,\cdots,K]\mapsto \mathcal{P}$. The mapping $\mu^{init}:\mathcal{X}\times[1,\cdots,K]\mapsto \mathcal{D}$ maintains, for each variable x and context k the last value of the variable x that has been propagated to memory by any process u the beginning of context k. We also define the mapping $\mu:\mathcal{X}\times[1,\cdots,K]\mapsto \mathcal{D}$ as the counterpart of the above mapping that actually changes (gets updated) through the course of context k, i.e. at any given point in time covered by context k, $\mu(x,k)$ gives the latest value of variable x propagated to memory until that point. Further, the mapping $\nu:\mathcal{P}\times\mathcal{X}\mapsto \mathcal{D}$ denotes for each process p and variable x the latest value that has been written to x by p. We also maintain the maps

$$\begin{split} \mathrm{iW} : \mathcal{P} \times \mathcal{X} &\mapsto [1, \cdots, K] \\ \mathrm{cW} : \mathcal{P} \times \mathcal{X} &\mapsto [1, \cdots, K] \\ \mathrm{cR} : \mathcal{P} \times \mathcal{X} &\mapsto [1, \cdots, K] \end{split}$$

The first map indicates, for each process p and variable x, the latest context in which a write on x has been initialized by p. Similarly, the second one indicates for each such pair the latest context in which a write was committed by p. Similarly, we define cR for committing reads.

Since registers are shared among all processes, we need to define special mappings for them. Thus we define $\operatorname{cReg}: \mathcal{P} \times \mathcal{R} \mapsto [1,\cdots,K]$ captures for each register r the committing context of the latest read or assign event loading a value to r. We also extend this to expressions, by defining $\operatorname{cReg}(p,exp) = \max\{\operatorname{cReg}(p,r) | r \in \mathcal{R}(exp)\}$. Finally, the mapping $\operatorname{ctrl}: \mathcal{P} \mapsto [1,\cdots,K]$ gives for each process p the committing context of the latest aci event in p. The variable cnt tracks the current context.

The function gen is assumed to return, given a set S, a random element of S.

11.3 The initializing process

We next present the algorithm $\langle initProc \rangle_K$.

$\overline{\mathbf{Algorithm}}$ 1: Algorithm $\langle \mathsf{initProc} \rangle_K$.

```
1 for p \in \mathcal{P} \land x \in \mathcal{X} do
           iR(p,x) \leftarrow 1;
 2
           iW(p,x) \leftarrow 1;
 3
           \mathsf{cR}(p,x) \leftarrow 1;
 4
           \nu(p,x) \leftarrow 0;
 5
           \mu(p, x, 1) \leftarrow 0;
 6
           for k \in [2, \cdots, K] do
                 \mu^{init}(x,k) \leftarrow \text{gen}(\mathcal{D});
 8
                \mu(x,k) \leftarrow \mu^{init}(p,x,k);
 9
           end
10
11 end
12 for p \in \mathcal{P} do
          \mathsf{ctrl}(p) \leftarrow 1;
13
14 end
15 for \$r \in \mathcal{R} do
           \mathsf{cReg}(p,\$r) \leftarrow 1;
17 end
18 for k \in [1, \dots, K] do
           active(k) \leftarrow gen([1, \cdots, K]);
20 end
21 cnt \leftarrow 1;
```

The initial process's job is to initialize all the data structures. We assume that in the beginning all variables are assigned the value 0. If needed we can replace this by a symbolic variable depicting all possible values. The structures which record contexts are all initialized to 1, since that is the earliest context possible. We also assign to each context a randomly chosen active process.

11.4 Write instructions

```
Algorithm 2: [x \leftarrow exp]_K^{p,\text{Write}}
```

```
Algorithm 2: \llbracket x \leftarrow exp \rrbracket_K

1 //\text{Guess}
2 \mathrm{iW}(p,x) \leftarrow \mathrm{gen}([1,\cdots,K]);
3 \mathrm{old\text{-}cW} \leftarrow \mathrm{cW}(p,x);
4 \mathrm{cW}(p,x) \leftarrow \mathrm{gen}([1,\cdots,K]);
5 //\mathrm{Check}
6 \mathrm{assume}(\mathrm{active}(\mathrm{iW}(p,x)) = p);
7 \mathrm{assume}(\mathrm{iW}(p,x) \geq \mathrm{cReg}(p,exp));
8 \mathrm{assume}(\mathrm{cW}(p,x) \geq \mathrm{iW}(p,x));
9 \mathrm{assume}(\mathrm{active}(\mathrm{cW}(p,x)) = p);
10 \mathrm{assume}(\mathrm{cW}(p,x) \geq \mathrm{max}(\mathrm{old\text{-}cW},\mathrm{cR}(p,x),\mathrm{ctrl}(p));
11 //\mathrm{Update}
12 \mu(x,\mathrm{cW}(p,x)) \leftarrow exp;
13 \nu(p,x) \leftarrow exp;
```

The above listing shows how write instructions are handled. First, we guess the contexts in which the write will be initialized and committed respectively. Next, we perform a set of sanity checks to ensure that the write conforms to the rule InitWrite: line 7 ensures that p is the active process in that context. We then make sure that InitCnd is satisfied in line 8. Further, the write must be initialized before committed, as expressed in line 9. Finally, we must ensure that the write is committed not before any poloc-preceding write or read, and also not before any po-previous aci instruction or before any instruction which supplies the data for this write. That is expressed in line 10. Then, we update the new values of the global values of x in the respective context, and the latest local value of x.

11.5 Read Instructions

```
Algorithm 3: [\$r \leftarrow x]_K^{p,\text{Read}}

1 //Guess

2 cR(p,x) \leftarrow gen([1,\cdots,K]);

3 cReg(p,\$r) \leftarrow cR(p,x);

4 //Check

5 assume(active(cR(p,x)) = p);

6 assume(cR(p,x) \ge iW(p,x));

7 //Update

8 if iR(p,x) < cW(p,x) then

9 | \$r \leftarrow \nu(p,x);

10 else

11 | \$r \leftarrow \mu(x,iR(p,x));

12 end
```

As for writes, we start by guessing the context in which the read is committed. We then perform some sanity checks in the lines 5-6, which we explain next. Line 5 ensures that p is the active process during the commit of the read. Line 6 ensures that the read is committed only after the closest po-before write is; this is needed due to the model. If the read is initialized before the closest po-before write (say w) is committed, then we must follow the rule ComReadFromLocal, as dictated by line 9. Otherwise, the global memory is at least as up-to-date, and we must use the rule ComReadFromProp to read from it. This is captured by the update of rule 11.

11.6 Assign Instructions

```
Algorithm 4: [\$r \leftarrow exp]_K^{p, Assign}

1 //Guess

2 \mathsf{cReg}(p,\$r) \leftarrow \mathsf{gen}([1,\cdots,K]);

3 //Check

4 for \$r' \in \mathcal{R}(exp) do

5 | \mathsf{assume}(\mathsf{cReg}(p,\$r) \ge \mathsf{cReg}(p,\$r'));

6 end

7 //Update

8 \$r \leftarrow exp;
```

We first guess the committing context of the assign statement. We then check that it commits no earlier than any of the events that supply it with the operand values, in line 5. The update step is simple: we just record the new value of the register range register

11.7 Verifying process

```
Algorithm 5: \langle \text{verProc} \rangle_K.

1 for p \in \mathcal{P} \land x \in \mathcal{X} \land k \in [1, \cdots, K-1] do

2 | assume(\mu(p, x, k) = \mu^{init}(p, x, k+1));

3 end

4 if l is reachable then

5 | error;

6 end
```

The verifying process simply makes sure that the modifications to global state by a process in a context leaves it exactly in the state that the process of the next context finds it. If this is satisfied, then the execution is valid and the *error* state is reachable if and only if a bad state can be reached in this reduced SC program.

12 Code-to-code translation for reduction to SC (for the complete model)

12.1 Scheme for the complete model

Our translation scheme translates a program Prog into a program $Prog^{\clubsuit}$ using the map function $\llbracket \cdot \rrbracket_K$. Let \mathcal{P} and \mathcal{X} be the set of processes and shared memory locations in our program. Then, the map $\llbracket \cdot \rrbracket_K$ replaces the memory of Prog by $|\mathcal{P}| \cdot K$ copies of the set \mathcal{X} , along with a finite set of finite data structures defined below. Below, the function gen takes in a finite set S and returns a randomly chosen element of S.

```
 [\![ Prog ]\!]_K \stackrel{\text{def}}{=} \langle \mathsf{addvars} \rangle_K \\ \mathsf{procs} \colon ([\![ p ]\!]_K)^* \ \langle \mathsf{initProc} \rangle_K \ \langle \mathsf{verProc} \rangle_K 
                                                                                                [\![p]\!]_K \stackrel{\mathrm{def}}{=} \underset{\mathrm{instrs:}}{\operatorname{regs:}} \ \$r^* \\ \text{instrs:} \ ([\![i]\!]_K^p)^*
                                                                                                        [i]_K^p \stackrel{\mathrm{def}}{=} l : [s]_K^p
                                                                          [\![\$r \leftarrow exp]\!]_K^p \overset{\mathrm{def}}{=} [\![\$r \leftarrow exp]\!]_K^{\mathrm{p,Assign}}
                                                                   \llbracket \texttt{LD} \ \$r' \leftarrow \llbracket \$r \rrbracket \rrbracket_K^p \overset{\text{def}}{=} \llbracket \texttt{LD} \ \$r' \leftarrow \llbracket \$r \rrbracket \rrbracket_K^{p, \mathsf{LD}}
                                                                  [\![\mathsf{ST}\ [\$r'] \leftarrow \$r]\!]_K^p \stackrel{\text{def}}{=} [\![\mathsf{ST}\ [\$r'] \leftarrow \$r]\!]_K^{\mathsf{p,ST}}
                                                             \llbracket \texttt{LDA} \ \$r' \leftarrow [\$r] \rrbracket_K^p \overset{\text{def}}{=} \llbracket \texttt{LDA} \ \$r' \leftarrow [\$r] \rrbracket_K^{\texttt{p,LDA}}
                                                             [\![\mathsf{STL}\ [\$r'] \leftarrow \$r]\!]_K^p \overset{\mathrm{def}}{=} [\![\![\mathsf{STL}\ [\$r'] \leftarrow \$r]\!]_K^{\mathsf{p,STL}}
                                                             [\![\operatorname{LDX} \ \$r' \leftarrow [\$r]]\!]_K^p \overset{\mathrm{def}}{=} [\![\operatorname{LDX} \ \$r' \leftarrow [\$r]]\!]_K^{\mathsf{p,LDX}}
                                             [\![\mathsf{STX} \ \$r'', \ [\$r'] \leftarrow \$r]\!]_K^p \overset{\text{def}}{=} [\![\mathsf{STX} \ \$r'', \ [\$r'] \leftarrow \$r]\!]_K^{\mathsf{p,STX}}
                                                [\![ \texttt{LDAX} \ \$r'', \ \$r' \leftarrow [\$r] ]\!]_{\scriptscriptstyle K}^{p} \overset{\text{def}}{=} [\![ \texttt{LDAX} \ \$r' \leftarrow [\$r] ]\!]_{\scriptscriptstyle K'}^{\mathsf{p,LDAX}}
                                                [\![\mathtt{STLX}\ [\$r'] \leftarrow \$r]\!]_K^p \overset{\mathrm{def}}{=} [\![\mathtt{STLX}\ \$r'',\ [\$r'] \leftarrow \$r]\!]_K^{\mathsf{p,STLX}}
[\![ \text{if } exp \text{ then } i^* \text{ else } i^*]\!]_K^p \overset{\text{def}}{=} \text{if } exp \text{ then } ([\![i]\!]_K^p)^* \text{ else } ([\![i]\!]_K^p)^*; \text{ } \langle \text{control} \rangle_K^p 
                                 [\![ \text{while } exp \text{ do } i^*]\!]_K^p \overset{\text{def}}{=} \text{while } exp \text{ do } ([\![i]\!]_K^p)^*; \text{ } \langle \text{control} \rangle_K^p
                                                           [assume exp]_{K}^{p} \stackrel{\text{def}}{=} \operatorname{assume} \ exp; \ \langle \operatorname{control} \rangle_{K}^{p}
                                                            \| \mathsf{assert} \ exp \|_K^p \overset{\mathrm{def}}{=} \mathsf{assert} \ exp; \ \langle \mathsf{control} \rangle_K^p 
                                                            [\![\mathsf{acquire}\ \$\mathsf{r} \leftarrow [exp]]\!] \stackrel{\mathrm{def}}{=} [\![\![\$r \leftarrow [exp]]\!]_K^{\mathsf{p,LAcq}}
                                                  [\![ \mathtt{release} \ [ \mathtt{exp'} ] \leftarrow exp ]\!]_K^p \overset{\mathrm{def}}{=} [\![ exp' ] \leftarrow exp ]\!]_K^{\mathtt{p,SRel}}
                                                                                    [\![\mathsf{dmb.ld}]\!]_K^p \overset{\mathrm{def}}{=} [\![\mathsf{dmb.ld}]\!]_K^{\mathsf{p,DmbLd}}
                                                                                    [\![\mathsf{dmb.st}]\!]_K^p \overset{\mathrm{def}}{=} [\![\mathsf{dmb.st}]\!]_K^{\mathsf{p,DmbSt}}
                                                                                    [\operatorname{dmb.sy}]_{K}^{p} \stackrel{\operatorname{def}}{=} [\operatorname{dmb.sy}]_{K}^{p,\operatorname{DmbSy}}
                                                                                                 [\![\mathrm{isb}]\!]_K^p \overset{\mathrm{def}}{=} [\![\mathrm{isb}]\!]_K^{\mathrm{p,isb}}
                                                                                                       [\![\operatorname{term}]\!]_K^p \stackrel{\mathrm{def}}{=} \operatorname{term}
                                                                   \langle \operatorname{addvars} \rangle_K \stackrel{\operatorname{def}}{=} \mu(|\mathcal{X}|,K), \mu^{init}(|\mathcal{X}|,K),
                                                                                               pW(|\mathcal{P}|, |\mathcal{X}|), \nu(|\mathcal{P}|, |\mathcal{X}|),
                                                                            \delta(|\mathcal{X}|, K), \delta^{init}(|\mathcal{X}|, K), \text{nW}(|\mathcal{X}|, K),
                                                                                              cR(|\mathcal{P}|, |\mathcal{X}|), cX(|\mathcal{P}|, |\mathcal{X}|)
                                                                                              iW(|\mathcal{P}|, |\mathcal{X}|), cW(|\mathcal{P}|, |\mathcal{X}|),
                                                                                                              cReg(|\mathcal{P}|, |\mathcal{R}|),
                                                                                                                 cL(|\mathcal{P}|, |\mathcal{R}|),
                                                                                              iS(|\mathcal{P}|, |\mathcal{X}|), cS(|\mathcal{P}|, |\mathcal{X}|),
                                                                                       cDY(|\mathcal{P}|), cDL(|\mathcal{P}|), cDS(|\mathcal{P}|), cISB(|\mathcal{P}|),
                                                                                      \operatorname{ctrl}(|\mathcal{P}|), \operatorname{cAddr}(|\mathcal{P}|), \operatorname{active}(K), \operatorname{cnt}
                                                              \langle \operatorname{activeCnt} \rangle_K^p \overset{\mathrm{def}}{=} \operatorname{assume}(\operatorname{active}(\operatorname{cnt}) = p)
                                                  \langle \mathsf{closeCnt} \rangle_K^p \overset{\text{def}}{=} cnt \leftarrow cnt + \mathsf{gen}([0, \cdots, K-1]); \\ \mathsf{assume}(cnt \leq K)
                                         \langle \texttt{control} \rangle_K^p \overset{\text{def}}{=} \texttt{ctrl}(p) \leftarrow \texttt{ctrl}(p) + \texttt{gen}(0, \cdots, K-1); \\ \texttt{assume}(\texttt{ctrl}(p) \leq K)
```

12.2 Additional data structures for the complete model

We use all of the data structures described in the section of the simple model, with a few minor changes. One, the set \mathcal{X} now refers to the set of shared memory locations instead of shared variables. Further, functions such as cR are updated by all four types of reads, and similar conditions hold for the other three analogous functions. Since some predicates in this model are over just load-acquires or store-releases, we also define the predicates:

$$\begin{split} \operatorname{cL}: \mathcal{P} \times \mathcal{R} &\mapsto [1, \cdots, K] \\ \operatorname{is}: \mathcal{P} \times \mathcal{X} &\mapsto [1, \cdots, K] \\ \operatorname{cS}: \mathcal{P} \times \mathcal{X} &\mapsto [1, \cdots, K] \\ \operatorname{cX}: \mathcal{P} \times \mathcal{X} &\mapsto [1, \cdots, K] \\ \operatorname{pW}: \mathcal{P} \times \mathcal{X} &\mapsto \mathbb{N} \\ \operatorname{nW}: \mathcal{X} \times [1, \cdots, K] &\mapsto \mathbb{N} \\ \operatorname{cDY}: \mathcal{P} &\mapsto [1, \cdots, K] \\ \operatorname{cISB}: \mathcal{P} &\mapsto [1, \cdots, K] \\ \operatorname{cDS}: \mathcal{P} &\mapsto [1, \cdots, K] \\ \operatorname{cDL}: \mathcal{P} &\mapsto [1, \cdots, K] \end{split}$$

The first four describe, for each process-register or process-variable pair, the initializing and committing contexts of the latest STL or instruction that loads to, and the latest SRel instruction that stores from that register/to that variable. There is however one change that we must keep in mind: now the set \mathcal{X} consists of addressable memory regions (as opposed to variables). Also note that since exclusive stores directly commit, we use their committing context to also update iW, since later instructions need them to be "at least" initialized, and so we need these two functions to take into account their committing (it's as if they initialized and spontaneously committed). Also, noting that the predicates on LAcq or SRel that appear in our rules, such as AlllAcqs, are not about those to a particular variable but over all of them, it will be helpful to define for $p \in \mathcal{P}$:

$$\mathrm{iS}(p) = \max_{x \in \mathcal{X}} \mathrm{iS}(p,x)$$

We similarly define cL(p) and cS(p). The last four are the analogues for the four types of barrier instructions respectively: dmb.sy, dmb.st, dmb.ld and isb.

We shall also need to track the tags of memory locations. To this end, we introduce two new data structures, δ^{init} : $\mathcal{X} \times [2, \cdots, K] \mapsto \mathcal{P} \cup \{\bot\}$, and $\delta : \mathcal{X} \times [1, \cdots, K] \mapsto \mathcal{P} \cup \{\bot\}$. These give the value of the tag of a memory location in a particular context: the first at the beginning of the context, and the second at any given moment in time (i.e. it gets updated as more and more transitions are taken in the corresponding context). During implementation, we can use, e.g., 0 to represent \bot . Three other structures are introduced. The mapping cX gives, for each process and address, the latest committing event of a write that is in-between a load exclusive-store exclusive pair event that to that address. Then, we have nW, which for each global address maintains a counter that is incremented every time a write event is propagated to it. We track this counter separately for each context, and ensure consistency across contexts using assume statements. Further, pW records for each address the latest value of nW that was seen by a read event propagated to memory. These two structures will be used to ensure coherence for reads.

With these structures defined, we now elaborate upon the components of the code-to-code translation above. Below, when we refer to a register in the pseudo-code, such as r, we are actually referring to the *value* stored in the register. Thus, for example, $\mathsf{cW}(p, [r])$ refers to the context of latest write-commit that writes to the location whose address is given by the then-present-value in r.

Finally, we need to track, for the sake of isb and write events, the latest committing context of any instruction that supplies addr-data to a read or write: this is because when an isb is committed we need all po-preceding instructions to have well defined memory footprints. So, we define

$$\mathsf{cAddr}: \mathcal{P} \mapsto [1, \cdots, K]$$

which gives for each process P, the maximum initializing context of an instruction that supplies the address to another instruction seen so far.

Algorithm 6: Algorithm $\langle \text{initProc} \rangle_K$.

```
1 for p \in \mathcal{P} do
           for x \in \mathcal{X} do
  \mathbf{2}
                  iR(p,x) \leftarrow 1;
  3
                  \mathsf{cR}(p,x) \leftarrow 1;
                  iW(p,x) \leftarrow 1;
  5
                  cW(p,x) \leftarrow 1;
  6
                  pW(p,x) \leftarrow 1;
                  iS(p, x) \leftarrow 1;
  8
                  \mathsf{cS}(p,x) \leftarrow 1;
  9
                  \mathsf{cX}(p,x) \leftarrow 1;
10
                  \nu(p,x) \leftarrow 0;
11
           end
12
           for r \in \mathcal{R} do
13
14
                  \mathsf{cL}(p,r) \leftarrow 1;
                  \mathsf{cReg}(p,\$r) \leftarrow 1;
15
16
           end
           \mathsf{ctrl}(p) \leftarrow 1;
17
           \mathsf{cAddr}(p) \leftarrow 1;
18
           cDY(p) \leftarrow 1;
19
           cISB(p) \leftarrow 1;
20
           cDS(p) \leftarrow 1;
21
           cDL(p) \leftarrow 1;
22
23 end
24 for k \in [1, \dots, K] do
           active(k) \leftarrow gen(\mathcal{P});
25
           if k \neq 1 then
26
27
                  for x \in \mathcal{X} do
                        \mu^{init}(x,k) \leftarrow \bot;
28
                        \delta^{init}(x,k) \leftarrow \bot;
29
                        \mathrm{nW}^{init}(x,k) \leftarrow 1;
30
                        \mu(x,k) \leftarrow \mu^{init}(x,k);
31
                        \delta(x,k) \leftarrow \delta^{init}(x,k);
32
                        \mathrm{nW}(x,k) \leftarrow \mathrm{nW}^{init}(x,k);
33
                  end
34
35
           else
                  for x \in \mathcal{X} do
36
                        \mu(x,k) \leftarrow \bot;
37
                        \delta(x,k) \leftarrow \bot;
38
                        nW(x,k) \leftarrow 1;
39
                  end
40
           end
41
42 end
```

The algorithm is largely similar to before. We add statements that initialize the values of the new structures defined above to their respective initial values.

Implementation detail. In case certain registers and/or memory contents are to be set to initial values, the statements for doing so are added at the end of initProc as well. Further, we can use -1 as a representative for \bot in the implementation.

12.4 Write Statements

First we show the algorithm for ST statements.

Algorithm 7: $[\![\mathtt{ST}\ [\$r'] \leftarrow \$r]\!]_K^{p,\mathtt{ST}}$

```
1 //Guess
 2 iW(p, [\$r']) \leftarrow gen([1, \cdots, K]);
 3 old-cW \leftarrow cW(p, [\$r']);
 4 cW(p, [\$r']) \leftarrow gen([1, \cdots, K]);
 5 // The below line is present only if in the code, this write
    // is in between a LDX/LDAX-STX/STLX pair.
 7 cX(p, [\$r']) \leftarrow cW(p, [\$r']);
 8 //Check
 9 assume(active(iW(p,[$r'])) = p);
\mathbf{10} \ \operatorname{assume}(\mathrm{iW}(p,[\$r']) \geq \max(\mathrm{cReg}(p,\$r'),\mathrm{cReg}(p,\$r)));
11 for r \in \mathcal{R} do
          \operatorname{assume}(\operatorname{cW}(p, [\$r']) \ge \operatorname{cL}(p, \$r));
13 end
14 assume(active(cW(p, [$r'])) = p);
15 assume(cW(p,[$r']) \geq iW(p,[$r']));
16 assume(cW(p,[\$r']) \geq max(cDY(p), cISB(p)));
    \operatorname{assume}(\operatorname{cW}(p, [\$r']) \ge \max(\operatorname{cDS}(p), \operatorname{cDL}(p)));
    \operatorname{assume}(\operatorname{cW}(p, [\$r']) \ge \max(\operatorname{old-cW}, \operatorname{cR}(p, [\$r'])));
    assume(cW(p, [\$r']) \ge max(cAddr(p), ctrl(p));
21 \mathsf{cAddr}(p) \leftarrow \mathsf{max}(\mathsf{cAddr}(p), \mathsf{cReg}(p, \$r'));
    \mu([\$r'], \mathsf{cW}(p, [\$r'])) \leftarrow \$r;
22
23 \nu(p, [\$r']) \leftarrow \$r;
24 \delta([\$r'], \mathsf{cW}(p, [\$r'])) \leftarrow \bot;
25 \mathsf{nW}([\$r'], \mathsf{cW}(p, [\$r'])) \leftarrow \mathsf{nW}([\$r'], \mathsf{cW}(p, [\$r'])) + 1;
```

We first guess the initializing and committing contexts of the ST in lines 1-3. We also update cX if the write happens to be in a load exclusive-store exclusive block. Then, we run it through a bunch of sanity checks. At lines 9 and 14 we check that the process p is active during init and commit, respectively. Then we need that the two register values are ready, i.e. the events providing them have been committed, at the moment when the event is initialized: this is expressed by line 10. Line 15 posits that the instruction is committed no sooner than it is initialized, and lines 16 and 17 ensure that all po-preceeding barriers are committed. We also need all po-previous load-acquires to have been committed no later than this write is: that is checked in line 12. We then ensure the in-order commit of poloc-related instructions by comparing with old-cW and cR(...) in line 14 18. Finally, line 19 checks that 1) any po-preceding ACI instruction has been committed, and 2) all po-previous memory-access instructions have fully determined addresses ("memory footprints"). Once all the checks pass, we update the respective data structures in lines 21 through 25.

We next present the other three types of writes. Since the changes are minor, we only highlight the differences in text.

Algorithm 8: $[STL \ [\$r'] \leftarrow \$r]_{K}^{p,STL}$

```
1 //Guess
  2 iW(p, [\$r']) \leftarrow gen([1, \cdots, K]);
  \mathbf{3} old-cW \leftarrow cW(p, [\$r']);
  4 cW(p, [\$r']) \leftarrow gen([1, \cdots, K]);
  _{5} // The below line is present only if in the code, this write
  6 // is in between a LDX/LDAX-STX/STLX pair.
  7 cX(p, [\$r']) \leftarrow cW(p, [\$r']);
  8 iS(p, [\$r']) \leftarrow iW(p, [\$r']);
  9 cS(p, [\$r']) \leftarrow cW(p, [\$r']);
10 //Check
\mathbf{11} \ \mathsf{assume}(\mathsf{active}(\mathsf{iW}(p,[\$r'])) = p);
12 assume(iW(p, [\$r']) \ge \max(cReg(p, \$r), cReg(p, \$r'));
13 for \$x \in \mathcal{X} do
           \operatorname{assume}(\operatorname{cW}(p, [\$r']) \ge \max(\operatorname{cR}(p, x), \operatorname{cW}(p, x)));
14
15 end
16 assume(active(cW(p, [\$r'])) = p);
17 assume(cW(p, [$r']) \geq iW(p, [$r']));
     \operatorname{assume}(\operatorname{cW}(p,[\$r']) \geq \max(\operatorname{cDY}(p),\operatorname{cISB}(p)));
18
     \operatorname{assume}(\operatorname{cW}(p,[\$r']) \geq \max(\operatorname{cDS}(p),\operatorname{cDL}(p)));
     \operatorname{assume}(\operatorname{cW}(p,[\$r']) \geq \max(\operatorname{old-cW},\operatorname{cR}(p,[\$r'])));
21 assume(cW(p,[r']) \geq max(cAddr(p), ctrl(p));
22 //Update
23 \operatorname{cAddr}(p) \leftarrow \max(\operatorname{cAddr}(p), \operatorname{cReg}(p, \$r'));
24 \mu([\$r'], \mathsf{cW}(p, [\$r'])) \leftarrow \$r;
25 \nu(p, [\$r']) \leftarrow \$r;
26 \delta([\$r'], \mathsf{cW}(p, [\$r'])) \leftarrow \bot;
27 \mathsf{nW}([\$r'], \mathsf{cW}(p, [\$r'])) \leftarrow \mathsf{nW}([\$r'], \mathsf{cW}(p, [\$r'])) + 1;
```

The difference of this from the previous listing is only that instead of just load-acquires, we need all memory-access instructions that precede this one in program order to have been committed: this change results in line 14.

Algorithm 9: $[STX \ \$r'', \ [\$r'] \leftarrow \$r]_K^{p,STX}$

```
1 //Guess
 2 old-cW \leftarrow cW(p, [\$r']);
 \mathbf{3} \text{ new-iW} \leftarrow \text{gen}([1, \cdots, K]);
 4 new-cW \leftarrow gen([1, \cdots, K]);
 5 if \delta([\$r'], \textit{new-cW}) = p then
           //Check
  6
          assume(active(new-iW) = p);
  7
          assume(new-iW \ge max(cReg(p, \$r), cReg(p, \$r'));
  8
          for r \in \mathcal{R} do
10
            new-cW \geq cL(p, \$r);
          end
11
          assume(active(new-cW) = p);
12
          assume(new-cW \geq max(cDY(p), cISB(p)));
13
          assume(new-cW \ge max(cDS(p), cDL(p)));
14
          \mathsf{assume}(\mathsf{new\text{-}cW} \geq \mathsf{max}(\mathsf{old\text{-}cW}, \mathsf{cR}(p, [\$r']));
15
          assume(new-cW \ge max(cAddr(p), ctrl(p));
16
17
          \mathsf{cAddr}(p) \leftarrow \mathsf{max}(\mathsf{cAddr}(p), \mathsf{cReg}(p, \$r'));
18
          \mu([\$r'], \mathsf{new-cW}) \leftarrow \$r;
19
          \nu(p, [\$r']) \leftarrow \$r;
20
21
          \mathsf{nW}([\$r'], \mathsf{new-cW}) \leftarrow \mathsf{nW}([\$r'], \mathsf{new-cW}) + 1;
          \delta([\$r'], \mathsf{new-cW}) \leftarrow \bot;
22
          r'' \leftarrow 0;
23
          iW(p, [\$r']) \leftarrow cW(p, [\$r']);
\mathbf{24}
          cW(p, [\$r']) \leftarrow new-cW;
25
          \mathsf{cX}(p, [\$r']) \leftarrow \mathsf{new-cW};
26
27 else
          r'' \leftarrow 1;
28
29 end
30 \mathsf{cReg}(p,\$r'') \leftarrow 1;
```

This listing is still very similar to the first one: the difference is that all checks and changes (except those to r'' and cAddr) are predicated on the "success" of the store-exclusive instruction. One interesting point is that a store exclusive can fail even before it's addres is determined.

The same difference applied to the second listing leads to the one below.

Algorithm 10: $[STLX \ \$r'', \ [\$r'] \leftarrow \$r]_K^{p,STLX}$

```
1 //Guess
 2 old-cW \leftarrow cW(p, [\$r']);
 \mathbf{3} \text{ new-iW} \leftarrow \text{gen}([1,\cdots,K]);
  4 new-cW \leftarrow gen([1, \cdots, K]);
  5 if \delta([\$r'], \textit{new-cW}) = p then
          //Check
  6
          assume(active(new-iW) = p);
  7
          assume(new-iW \ge \max(cReg(p,\$r),cReg(p,\$r'));
  8
          for \$x \in \mathcal{X} do
           assume(new-cW \geq max(cR(p, x), cW(p, x));
10
          end
11
          assume(active(new-cW) = p);
12
          assume(new-cW \geq max(cDY(p), cISB(p)));
13
          assume(new-cW \geq max(cDS(p), cDL(p)));
14
          assume(new-cW \geq max(old-cW, cR(p, [\$r']));
15
          assume(new-cW \ge max(cAddr(p), ctrl(p));
16
          //Update
17
          \mathsf{cAddr}(p) \leftarrow \mathsf{max}(\mathsf{cAddr}(p), \mathsf{cReg}(p, \$r'));
18
          \mu([\$r'], \texttt{new-cW}) \leftarrow \$r;
19
          \nu(p, [\$r']) \leftarrow \$r;
20
          \mathsf{nW}([\$r'], \mathsf{new-cW}) \leftarrow \mathsf{nW}([\$r'], \mathsf{new-cW}) + 1;
21
          \delta([\$r'], \mathsf{new-cW}) \leftarrow \bot;
22
          r'' \leftarrow 0;
23
          iW(p, [\$r']) \leftarrow cW(p, [\$r']);
24
          cW(p, [\$r']) \leftarrow new-cW;
25
          \mathsf{cX}(p, [\$r']) \leftarrow \mathsf{new-cW};
26
27 else
          r'' \leftarrow 1;
28
29 end
30 \mathsf{cReg}(p,\$r'') \leftarrow 1;
```

Implementation detail. For write (and read) instructions with offsets, we reserve a private register. We first assign the sum of the base and offset to this private register followed by one of the above listings, in order to replicate the effect of a write-to-offset style instruction. This preserves correctness since, for an assign instruction, the only condition is that it is not initialized(committed) before any of its operands are initialized(committed): hence, every execution trace valid without this hack still remains so.

12.5 Assign Instructions

```
Algorithm 11: [\$r \leftarrow exp]_K^{p, \mathsf{Assign}}
```

Assign instructions are simple: the only condition we have on them is that they cannot commit before every one of their operands (which are part of exp) have done so, as expressed in line 5.

12.6 Read Instructions

We show, in order, the listings for LD, LDA, LDX and LDAX respectively.

Algorithm 12: $\llbracket \text{LD } \$r' \leftarrow \llbracket \$r \rrbracket \rrbracket_K^{p,\text{LD}}$

```
1 //Guess
 2 old-cR \leftarrow cR(p, [\$r]);
 3 cR(p, [$r]) ← gen([1,···,K]);
 4 //cReg assigned later since may be needed during check
 5 //Check
 6 assume(active(cR(p,[$r])) = p);
 7 assume(cR(p,[\$r]) \geq iW(p,[\$r]));
 8 assume(cR(p,[\$r]) \geq cReg(p,\$r));
    \operatorname{assume}(\operatorname{cR}(p, [\$r]) \ge \max(\operatorname{cDY}(p), \operatorname{cISB}(p));
    \operatorname{assume}(\operatorname{cR}(p, [\$r]) \ge \operatorname{cDL}(p));
    for r'' \in \mathcal{R} do
          \operatorname{assume}(\operatorname{cR}(p, [\$r]) \ge \operatorname{cL}(p, \$r''));
13 end
14 //Update
15 \mathsf{cReg}(p,\$r') \leftarrow \mathsf{cR}(p,[\$r]);
16 \mathsf{cAddr}(p) \leftarrow \mathsf{max}(\mathsf{cAddr}(p), \mathsf{cReg}(p, \$r));
    if cR(p, [\$r]) < cW(p, [\$r]) then
          \$r' \leftarrow \nu(p, [\$r]);
18
    \mathbf{else}
19
          if pW(p, [\$r]) \neq nW([\$r], cR(p, [\$r])) then
20
               assume(cR(p, [\$r]) \ge old-cR);
21
          \$r' \leftarrow \mu([\$r], \mathsf{cR}(p, [\$r]));
22
          pW(p, [\$r]) \leftarrow nW([\$r], cR(p, [\$r]));
23
24 end
```

The conditions for read instructions, apart from the obvious one about process p being active during commmit, are: 1) we need all dmb.sy's, isb's and dmb.ld's that precede this instruction in program order, to have been committed before it is committed, as lines 9-10 describe. We also need all events supplying the address to have been committed before it, as in line 8. We also require that all poloc-previous writes have initialized, as in line 7. Once the sanity checks are done, we update the required data structures to indicate that the LD instruction has committed. If the load reads from memory, and reads from a different event than the last one that did, we also require it to obey the coherence ordering as in line 21. As noted before, we also have that register writes due to exclusive stores do not impose orderings on future instructions reading the success value, unlike loads. Thus, we set the cReg value to 1, so that any future check will pass (unless it is subsequently overwritten by another event).

We next present the listings for the other three types of reads. The modifications as compared to the above listing are minor and obvious, so we do not elaborate upon them.

Algorithm 13: [LDA $r' \leftarrow [r]$]_K^{p,lda}

```
1 //Guess
 2 cR(p, [\$r]) \leftarrow gen([1, \cdots, K]);
 3 //cReg,cL assigned later since may be needed during check
 4 //Check
 5 assume(active(cR(p,[\$r])) = p);
 6 assume(cR(p, [$r]) \geq iW(p, [$r]));
 7 assume(cR(p,[\$r]) \geq cReg(p,\$r));
 8 assume(cR(p,[\$r]) \geq max(cDY(p), cISB(p));
 9 assume(cR(p,[\$r]) \ge cDL(p));
10 for r'' \in \mathcal{R} do
         assume(cR(p,[\$r]) \ge cL(p,\$r''));
11
12 end
13 for x \in \mathcal{X} do
         \operatorname{assume}(\operatorname{cR}(p, [\$r]) \ge \operatorname{cS}(p, x));
14
15 end
16 //Update
17 \mathsf{cReg}(p,\$r') \leftarrow \mathsf{cR}(p,[\$r]);
18 cL(p, \$r') \leftarrow cR(p, [\$r]);
19 \mathsf{cAddr}(p) \leftarrow \mathsf{max}(\mathsf{cAddr}(p), \mathsf{cReg}(p, \$r));
20 if cR(p, [\$r]) < cW(p, [\$r]) then
21
         \$r' \leftarrow \nu(p, [\$r]);
22 else
         if pW(p, [\$r]) \neq nW([\$r], cR(p, [\$r])) then
23
             assume(cR(p, [\$r]) \ge old-cR);
24
         \$r' \leftarrow \mu([\$r], \mathsf{cR}(p, [\$r]));
25
         pW(p, [\$r]) \leftarrow nW([\$r], cR(p, [\$r]));
26
27 end
```

Algorithm 14: $[LDX \ \$r' \leftarrow [\$r]]_K^{p,LDX}$

```
1 //Guess
  2 cR(p, [\$r]) \leftarrow gen([1, \cdots, K]);
 3 //cReg assigned later since may be needed during check
 4 //Check
 5 assume(active(cR(p,[$r])) = p);
 6 assume(cR(p,[$r]) \geq iW(p,[$r]));
 7 assume(cR(p,[\$r]) \geq cReg(p,\$r));
  8 assume(cR(p,[\$r]) \geq max(cDY(p), cISB(p));
 9 assume(cR(p,[\$r]) \geq cDL(p));
\textbf{10 assume}(\operatorname{cR}(p,[\$r]) \geq \operatorname{cX}(p,[\$r]));
11 for \$r'' \in \mathcal{R} do
          \operatorname{assume}(\operatorname{cR}(p, [\$r]) \ge \operatorname{cL}(p, \$r''));
12
13 end
14 //Update
15 \mathsf{cReg}(p,\$r') \leftarrow \mathsf{cR}(p,[\$r]);
16 \mathsf{cAddr}(p) \leftarrow \mathsf{max}(\mathsf{cAddr}(p), \mathsf{cReg}(p, \$r));
17 if cR(p, [\$r]) < cW(p, [\$r]) then
          \$r' \leftarrow \nu(p, [\$r]);
          \delta([\$r], \mathsf{cW}(p, [\$r])) \leftarrow p;
19
20 else
          if pW(p, [\$r]) \neq nW([\$r], cR(p, [\$r])) then
21
             assume(cR(p, [\$r]) \ge old-cR);
22
          \$r' \leftarrow \mu([\$r], \mathsf{cR}(p, [\$r]));
23
          pW(p, [\$r]) \leftarrow nW([\$r], cR(p, [\$r]));
\mathbf{24}
          \delta([\$r], \mathsf{cR}(p, [\$r])) \leftarrow p;
25
26 end
```

Algorithm 15: $[LDAX \ \$r' \leftarrow [\$r]]_K^{p,LDAX}$

```
1 //Guess
 2 cR(p, [\$r]) \leftarrow gen([1, \cdots, K]);
 3 //cReg,cL assigned later since may be needed during check
 4 //Check
 5 assume(active(cR(p,[\$r])) = p);
 6 assume(cR(p, [$r]) \geq iW(p, [$r]));
 7 assume(cR(p, [$r]) \geq cReg(p, $r));
 8 assume(cR(p,[\$r]) \geq max(cDY(p), cISB(p));
 9 assume(cR(p,[\$r]) \ge cDL(p));
10 assume(cR(p, [$r]) \geq cX(p, [$r]));
11 for r'' \in \mathcal{R} do
         assume(cR(p, [\$r]) \ge cL(p, \$r''));
13 end
14 for x \in \mathcal{X} do
         \operatorname{assume}(\operatorname{cR}(p, [\$r]) \ge \operatorname{cS}(p, x));
15
16 end
17 //Update
18 \mathsf{cReg}(p,\$r') \leftarrow \mathsf{cR}(p,[\$r]);
19 cL(p, \$r') \leftarrow cR(p, [\$r]);
20 \mathsf{cAddr}(p) \leftarrow \mathsf{max}(\mathsf{cAddr}(p), \mathsf{cReg}(p, \$r));
21 if cR(p, [\$r]) < cW(p, [\$r]) then
         \$r' \leftarrow \nu(p, [\$r]);
22
         \delta([\$r], \mathsf{cW}(p, [\$r])) \leftarrow p;
23
24 else
         if pW(p, [\$r]) \neq nW([\$r], cR(p, [\$r])) then
25
             assume(cR(p, [\$r]) \ge old-cR);
26
         \$r' \leftarrow \mu([\$r], \mathsf{cR}(p, [\$r]));
27
         pW(p, [\$r]) \leftarrow nW([\$r], cR(p, [\$r]));
28
         \delta([\$r],\operatorname{cR}(p,[\$r])) \leftarrow p;
29
30 end
```

Implementation detail. The procedure for offset-ed reads is the same as that for offset-ed writes: see the corresponding subsection for details.

12.7 Barrier Instructions

Algorithm 16: $\llbracket dmb.sy \rrbracket_K^{p,DmbSy}$

```
\begin{array}{c} \text{1 } //\mathsf{Guess} \\ \text{2 } \mathsf{old-cDY} \leftarrow \mathsf{cDY}(p); \\ \text{3 } \mathsf{cDY}(p) \leftarrow \mathsf{gen}[1,\cdots,K]; \\ \text{4 } //\mathsf{Check} \\ \text{5 } \mathsf{assume}(\mathsf{cDY}(p) \geq \mathsf{max}(\mathsf{old-cDY},\mathsf{cISB}(p))); \\ \text{6 } \mathsf{assume}(\mathsf{cDY}(p) \geq \mathsf{max}(\mathsf{cDL}(p),\mathsf{cDS}(p))); \\ \text{7 } \mathsf{assume}(\mathsf{cDY}(p) \geq \mathsf{ctrl}(p)); \\ \text{8 } \mathbf{for} \ x \in \mathcal{X} \ \mathbf{do} \\ \text{9 } \left| \begin{array}{c} \mathsf{assume}(\mathsf{cDY}(p) \geq \mathsf{cW}(p,x)); \\ \mathsf{assume}(\mathsf{cDY}(p) \geq \mathsf{cR}(p,x)); \\ \text{10 } \left| \begin{array}{c} \mathsf{assume}(\mathsf{cDY}(p) \geq \mathsf{cR}(p,x)); \\ \end{array} \right. \\ \text{1 } \mathbf{end} \end{array}
```

We first guess the context in which the dmb.sy will be committed, and then run it through some sanity checks. The AllBarriers predicate is spread across lines 5 and 6. The AllMem predicate appears in lines 9-10. Line 7 ensures that all po-previous ACI instructions have been committed.

Next up is the ISB instruction:

Algorithm 17: $[isb]_K^{p,isb}$

```
\begin{array}{l} 1 \ \ //\mathsf{Guess} \\ \mathbf{2} \ \mathsf{cISB}(p) \leftarrow \mathsf{gen}[1,\cdots,K]; \\ \mathbf{3} \ \ //\mathsf{Check} \\ \mathbf{4} \ \mathsf{assume}(\mathsf{cISB}(p) \geq \mathsf{max}(\mathsf{cDY}(p),\mathsf{ctrl}(p))); \\ \mathbf{5} \ \mathsf{assume}(\mathsf{cISB}(p) \geq \mathsf{cAddr}(p)); \end{array}
```

For an ISB instruction, at the time of commit we need that all po-preceding dmb.sy and ACI instructions are committed;

and also that all po-preceding memory access instructions have fully defined addresses: these conditions are a part of lines 4,4 and 5 respectively.

Algorithm 18: $[dmb.ld]_K^{p,DmbLd}$

```
\begin{array}{l} 1 \ \ //\mathsf{Guess} \\ \mathbf{2} \ \mathsf{cDL}(p) \leftarrow \mathsf{gen}[1,\cdots,K]; \\ \mathbf{3} \ \ //\mathsf{Check} \\ \mathbf{4} \ \mathsf{assume}(\mathsf{cDL}(p) \geq \mathsf{cDY}(p)); \\ \mathbf{5} \ \mathbf{for} \ x \in \mathcal{X} \ \mathbf{do} \\ \mathbf{6} \ \ | \ \mathsf{assume}(\mathsf{cDY}(p) \geq \mathsf{cR}(p,x)); \\ \mathbf{7} \ \mathbf{end} \end{array}
```

Again, for a dmb.ld we first guess the committing context for it, in line 2. Then, we run it through the AllDmbSys and AllReads predicates. The first is in line 4, and the second is in line 6.

```
Algorithm 19: [dmb.st]_K^{p,DmbSt}
```

```
\begin{array}{l} 1 \ //\mathsf{Guess} \\ \mathbf{2} \ \mathsf{cDS}(p) \leftarrow \mathsf{gen}[1,\cdots,K]; \\ \mathbf{3} \ //\mathsf{Check} \\ \mathbf{4} \ \mathsf{assume}(\mathsf{cDS}(p) \geq \mathsf{cDY}(p)); \\ \mathbf{5} \ \mathbf{for} \ x \in \mathcal{X} \ \mathbf{do} \\ \mathbf{6} \ \big| \ \mathsf{assume}(\mathsf{cDY}(p) \geq \mathsf{cW}(p,x)); \\ \mathbf{7} \ \mathbf{end} \end{array}
```

12.8 ACI statements

As shown in the translation schemes, the ACI statements themselves are retained as if-then-else C-statements. However, apart from the $\langle control \rangle$, we also need the condition that control(p) is greater than or equal to the committing context of the register it depends on (not committing). Thus, for example, if we have a CBNZ instruction:

```
CBNZ $r, label
```

Then we need that after modification, $\operatorname{ctrl}(p) \ge \operatorname{cReg}(p, \$r)$.

Implementation detail. For instructions such as BEQ which follow a CMP, we do the following: during the CMP we simply assign the two operand-registers to two fixed private registers of the process, and consider BEQ and other such instructions as ACI instructions that use these fixed private registers.

12.9 Verifying process

Algorithm 20: $\langle \text{verProc} \rangle_K$.

```
\begin{array}{ll} \mathbf{1} \ \mathbf{for} \ x \in \mathcal{X} \wedge k \in [1, \cdots, K-1] \ \mathbf{do} \\ \mathbf{2} & | \ \operatorname{assume}(\mu(x,k) = \mu^{init}(x,k+1)); \\ \mathbf{3} & | \ \operatorname{assume}(\delta(x,k) = \delta^{init}(x,k+1)); \\ \mathbf{4} & | \ \operatorname{assume}(\mathsf{nW}(x,k) = \mathsf{nW}^{init}(x,k+1)); \\ \mathbf{5} \ \mathbf{end} \\ \mathbf{6} \ \mathbf{if} \ l \ is \ reachable \ \mathbf{then} \\ \mathbf{7} & | \ error; \\ \mathbf{8} \ \mathbf{end} \end{array}
```

The verifying process is the same as in section 10: it simply ensures that each context leaves the global state in a consistent state for the next one.

Implementation detail. The checking for the final conditions (for which we are to determine reachability) are the contents of line 5.

13 Conclusion

In this document, we first presented an operational semantics-version of the AArch64/ARMv8 memory model which we then showed to accurately mirror the official semantics via both a formal proof and using litmus tests. Then we developed an efficient under-approximation technique to perform model checking for programs under this model, inspired by the context-bounded model checking approach taken by Lal and Reps [5]. Finally, we demonstrated that this approach has acceptable runtimes for use in larger scale projects.

This being a work in progress, in future work, we intend to explore the lazy approach to context bounded model checking and optimize further the runtimes of the model checker.

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