# Simulation study, misspecification

### Tetiana Gorbach

## Contents

```
Simulation results
                                                         1
 load("../results/sim study misspecification res2023 08 09 19 32 22.Rdata")
sim.results <- as.data.frame(output[[1]])</pre>
Transform to a long format:
sim.results.long <- sim.results %>%
 gather(method, ate.est, BD: BD FD TD, factor_key = TRUE) %>%
 mutate(
  `estimated ACE - true ACE` = ate.est - ate,
  method = factor(method, levels = c("FD", "FD TD", "BD", "BD TD", "TD", "BD FD TD")),
  misspecification = factor(misspecification,
   levels = c("Z", "C, A, Y", "C, Z", "A, Y"),
   labels = c("1. p(Z|A)", "2. All except p(Z|A)", "3. p(C), p(Z|A)", "4. p(A|C), E(Y|Z,C)")
 )
```

#### Simulation results

Boxplots of estimates per model misspecification and estimation method:

```
cbbPalette <- c("#E69F00", "#D55E00", "#56B4E9", "#0072B2", "#009E73", "#000000", "#FF0000FF")
# colorblind-friendly palette
names(cbbPalette) <- levels(sim.results.long$method)

p <- sim.results.long %>%
    ggplot(aes(x = misspecification, y = `estimated ACE - true ACE`, fill = method)) +
    geom_boxplot() +
    scale_fill_manual(values = alpha(cbbPalette, .7)) +
    xlab("Model misspecification") +
    theme_bw() +
    theme(
        text = element_text(size = 6),
        axis.title = element_text(size = 8),
        strip.text = element_text(size = 8)
    ) +
    theme(
```

```
legend.key.size = unit(2, "line"),
   legend.position = "bottom",
   legend.title = element_blank()
  guides(fill = guide_legend(nrow = 1))
pdf("Figure_sim_study2.pdf", height = 4, width = 6)
dev.off()
## pdf
##
BIAS and MSE
sim.results.long <- sim.results.long %>%
  mutate(method = factor(method,
                         levels = c("BD", "FD", "TD", "BD TD", "FD TD", "BD FD TD")))
# changing order of the levels for tables
s2 <- simsum(
 data = sim.results.long, estvarname = "ate.est", true = "ate",
 methodvar = "method", by = "misspecification",
 x = T
)
## 'ref' method was not specified, BD set as the reference
result.bias.se.mse <- summary(s2, digits = 3, ci.level = 0.95,
                              stats = c("bias", "empse", "mse"))$summ %>%
  mutate(estim = paste0(format(round(est, digits = 4), nsmall = 3), "(",
                        format(round(mcse, digits = 3), nsmall = 3), ")")) %>%
  select(stat, estim, misspecification, method) %>%
  spread(method, estim)
result.bias.se.mse
##
       stat
               misspecification
                                             BD
                       1. p(Z|A) -0.0006(0.001) -0.0004(0.001) -0.0006(0.000)
## 1
      bias
## 2
      bias 2. All except p(Z|A) = 0.3659(0.001) -0.0012(0.002) -0.0012(0.001)
                3. p(C), p(Z|A) -0.0006(0.001) -0.0004(0.001) -0.0006(0.000)
## 3
      bias
## 4
      bias 4. p(A|C), E(Y|Z,C) -0.0006(0.001) -0.0008(0.001) -0.0012(0.001)
## 5
                       1. p(Z|A) 0.0172(0.000) 0.0164(0.000) 0.0153(0.000)
      empse
## 6
      empse 2. All except p(Z|A) 0.0180(0.000) 0.0558(0.001) 0.0472(0.001)
## 7
      empse
                3. p(C), p(Z|A) 0.0172(0.000) 0.0164(0.000)
                                                                0.0153(0.000)
## 8
      empse 4. p(A|C), E(Y|Z,C)
                                 0.0171(0.000) 0.0212(0.000)
                                                                0.0472(0.001)
                       1. p(Z|A) 0.0003(0.000) 0.0003(0.000)
## 9
                                                                0.0002(0.000)
       mse
## 10
       mse 2. All except p(Z|A) = 0.1342(0.000) = 0.0031(0.000)
                                                                0.0022(0.000)
                3. p(C), p(Z|A) 0.0003(0.000) 0.0003(0.000)
## 11
                                                                0.0002(0.000)
       mse
## 12
           4. p(A|C), E(Y|Z,C) 0.0003(0.000) 0.0005(0.000)
                                                                0.0022(0.000)
##
              BD TD
                              FD TD
                                          BD FD TD
## 1 -0.0006(0.000) -0.0005(0.000) -0.0005(0.000)
## 2 -0.0480(0.000) -0.0012(0.001) -0.0480(0.000)
     -0.0006(0.000) -0.0919(0.000) -0.0919(0.000)
## 4 -0.0480(0.000) -0.0012(0.001) -0.0480(0.000)
## 5 0.0153(0.000) 0.0150(0.000) 0.0150(0.000)
```

# Scaled empirical variance vs bounds

```
result.sc.emp.var <- sim.results.long %>%
  group_by(misspecification, method) %>%
  summarise(sc.emp.var = var(sqrt(sample.size) * ate.est)) %>%
  ungroup() %>%
  mutate(mc.se.of.sc.emp.var = sqrt(2 * sc.emp.var^2 / number.of.replicates)) %>%
  mutate(estim = paste0(format(round(sc.emp.var, digits = 4), nsmall = 3), "(",
                        format(round(mc.se.of.sc.emp.var, digits = 3), nsmall = 3), ")")) %>%
  select(misspecification, method, estim) %>%
  spread(method, estim) %>%
  add_column(stat = "ScEmpSE^2", .before = "misspecification") %>%
  add row(tibble row(
   stat = "Bound", misspecification = "",
   BD = as.character(round(output[[2]]["bound.BD"], digits = 3)),
   FD = as.character(round(output[[2]]["bound.FD"], digits = 3)),
   TD = as.character(round(output[[2]]["bound.TD"], digits = 3)),
    `BD TD` = as.character(round(output[[2]]["bound.BDTD"], digits = 3)),
   'FD TD' = as.character(round(output[[2]]["bound.FDTD"], digits = 3)),
    `BD FD TD` = as.character(round(output[[2]]["bound.BDFDTD"], digits = 3))
## `summarise()` has grouped output by 'misspecification'. You can override using
## the `.groups` argument.
result.sc.emp.var
## # A tibble: 5 x 8
##
                                                            `BD TD` `FD TD` BD FD~1
     stat
              misspecification
                                      RD
                                                FD
                                                      TD
##
     <chr>>
               <chr>>
                                      <chr>
                                                <chr> <chr> <chr>
                                                                    <chr>
                                                                             <chr>>
## 1 ScEmpSE^2 "1. p(Z|A)"
                                      " 14.800~ " 13~ " 11~ " 11.7~ " 11.2~ " 11.2~
## 2 ScEmpSE^2 "2. All except p(Z|A)" " 16.141~ "155~ "111~ " 10.8~ "111.4~ " 10.8~
## 3 ScEmpSE^2 "3. p(C), p(Z|A)"
                                      " 14.800~ " 13~ " 11~ " 11.7~ " 10.5~ " 10.5~
## 4 ScEmpSE^2 "4. p(A|C), E(Y|Z,C)"
                                     " 14.558~ " 22~ "111~ " 10.8~ "111.4~ " 10.8~
## 5 Bound
                                      "14.765" "22.~ "18.~ "11.86~ "17.99~ "11.15"
## # ... with abbreviated variable name 1: `BD FD TD`
```

## Printing for LaTeX

```
## % latex table generated in R 4.2.1 by xtable 1.8-4 package
## % Thu Aug 10 10:47:22 2023
## \begin{table}[ht]
## \centering
## \begin{tabular}{rrrrrrr}
##
     \hline
## stat & misspecification & BD & FD & TD & BD TD & FD TD \\
     \hline
##
## Bias & 1. p(Z$|$A) & -0.0006(0.001) & -0.0004(0.001) & -0.0006(0.000) & -0.0006(0.000) & -0.0006(0.000)
     Bias & 2. All except p(Z$|$A) & 0.3659(0.001) & -0.0012(0.002) & -0.0012(0.001) & -0.0480(0.000)
##
##
     Bias & 3. p(C), p(Z$|$A) & -0.0006(0.001) & -0.0004(0.001) & -0.0006(0.000) & -0.0006(0.000) & -0.0006(0.000)
##
     Bias & 4. p(A$|$C), E(Y$|$Z,C) & -0.0006(0.001) & -0.0008(0.001) & -0.0012(0.001) & -0.0480(0.000)
##
     EmpSE & 1. p(Z$|$A) & 0.0172(0.000) & 0.0164(0.000) & 0.0153(0.000) & 0.0153(0.000) & 0.0150(
##
     EmpSE & 2. All except p(Z$|$A) & 0.0180(0.000) & 0.0558(0.001) & 0.0472(0.001) & 0.0147(0.000)
##
     EmpSE & 3. p(C), p(Z$|$A) & 0.0172(0.000) & 0.0164(0.000) & 0.0153(0.000) & 0.0153(0.000) & 0
##
     EmpSE & 4. p(A$|$C), E(Y$|$Z,C) & 0.0171(0.000) & 0.0212(0.000) & 0.0472(0.001) & 0.0147(0.000
##
     MSE & 1. p(Z$|$A) & 0.0003(0.000) & 0.0003(0.000) & 0.0002(0.000) & 0.0002(0.000) & 0.0002(0.000)
##
     MSE & 2. All except p(Z$|$A) & 0.1342(0.000) & 0.0031(0.000) & 0.0022(0.000) & 0.0025(0.000) &
##
    MSE & 3. p(C), p(Z$|$A) & 0.0003(0.000) & 0.0003(0.000) & 0.0002(0.000) & 0.0002(0.000) & 0.0
##
    MSE & 4. p(A$|$C), E(Y$|$Z,C) & 0.0003(0.000) & 0.0005(0.000) & 0.0022(0.000) & 0.0025(0.000)
##
    ScEmpVar & 1. p(Z$|$A) & 14.8007(0.662) & 13.4974(0.604) & 11.7573(0.526) & 11.7573(0.526) &
     ScEmpVar & 2. All except p(Z$|$A) & 16.1414(0.722) & 155.8208(6.969) & 111.4742(4.985) & 10.8023
##
     ScEmpVar & 3. p(C), p(Z$|$A) & 14.8007(0.662) & 13.4974(0.604) & 11.7573(0.526) & 11.7573(0.52
##
     ScEmpVar & 4. p(A$|$C), E(Y$|$Z,C) & 14.5580(0.651) & 22.5721(1.009) & 111.4742(4.985) & 10.802
##
     Bound & & 14.765 & 22.5 & 18.71 & 11.864 & 17.995 & 11.15 \\
##
##
      \hline
## \end{tabular}
## \end{table}
rbind(result.bias.se.mse, result.sc.emp.var)%>%
       mutate(stat = recode(stat, "bias" ="Bias", "empse" = "EmpSE", "mse" = "MSE", "ScEmpSE^2" = "Sc
##
          stat
                   misspecification
                                                 BD
## 1
                                     -0.0006(0.001)
                                                     -0.0004(0.001)
         Bias
                          1. p(Z|A)
## 2
         Bias 2. All except p(Z|A)
                                      0.3659(0.001)
                                                    -0.0012(0.002)
## 3
         Bias
                    3. p(C), p(Z|A)
                                     -0.0006(0.001)
                                                    -0.0004(0.001)
               4. p(A|C), E(Y|Z,C)
                                     -0.0006(0.001)
                                                    -0.0008(0.001)
## 4
         Bias
## 5
         EmpSE
                          1. p(Z|A)
                                      0.0172(0.000)
                                                      0.0164(0.000)
## 6
         EmpSE 2. All except p(Z|A)
                                      0.0180(0.000)
                                                      0.0558(0.001)
## 7
         EmpSE
                    3. p(C), p(Z|A)
                                      0.0172(0.000)
                                                      0.0164(0.000)
## 8
         EmpSE
               4. p(A|C), E(Y|Z,C)
                                      0.0171(0.000)
                                                      0.0212(0.000)
## 9
          MSE
                                      0.0003(0.000)
                          1. p(Z|A)
                                                      0.0003(0.000)
## 10
          MSE 2. All except p(Z|A)
                                      0.1342(0.000)
                                                      0.0031(0.000)
## 11
          MSE
                    3. p(C), p(Z|A)
                                      0.0003(0.000)
                                                      0.0003(0.000)
## 12
          MSE
               4. p(A|C), E(Y|Z,C)
                                      0.0003(0.000)
                                                      0.0005(0.000)
## 13 ScEmpVar
                          1. p(Z|A)
                                     14.8007(0.662)
                                                     13.4974(0.604)
## 14 ScEmpVar 2. All except p(Z|A)
                                     16.1414(0.722) 155.8208(6.969)
## 15 ScEmpVar
                    3. p(C), p(Z|A)
                                     14.8007(0.662)
                                                     13.4974(0.604)
## 16 ScEmpVar
               4. p(A|C), E(Y|Z,C)
                                     14.5580(0.651)
                                                     22.5721(1.009)
## 17
         Bound
                                             14.765
                                                               22.5
##
                                BD TD
                                                FD TD
                                                             BD FD TD
## 1
      -0.0006(0.000)
                      -0.0006(0.000)
                                       -0.0005(0.000)
                                                       -0.0005(0.000)
## 2
      -0.0012(0.001)
                       -0.0480(0.000)
                                       -0.0012(0.001)
                                                       -0.0480(0.000)
## 3
      -0.0006(0.000)
                      -0.0006(0.000)
                                      -0.0919(0.000)
                                                       -0.0919(0.000)
## 4
      -0.0012(0.001) -0.0480(0.000) -0.0012(0.001)
                                                      -0.0480(0.000)
```

```
## 5
        0.0153(0.000)
                         0.0153(0.000)
                                         0.0150(0.000)
                                                          0.0150(0.000)
## 6
        0.0472(0.001)
                         0.0147(0.000)
                                         0.0472(0.001)
                                                          0.0147(0.000)
## 7
        0.0153(0.000)
                         0.0153(0.000)
                                         0.0145(0.000)
                                                          0.0145(0.000)
## 8
        0.0472(0.001)
                         0.0147(0.000)
                                         0.0472(0.001)
                                                          0.0147(0.000)
## 9
        0.0002(0.000)
                         0.0002(0.000)
                                         0.0002(0.000)
                                                          0.0002(0.000)
## 10
        0.0022(0.000)
                         0.0025(0.000)
                                         0.0022(0.000)
                                                          0.0025(0.000)
## 11
        0.0002(0.000)
                         0.0002(0.000)
                                         0.0086(0.000)
                                                          0.0086(0.000)
## 12
        0.0022(0.000)
                         0.0025(0.000)
                                         0.0022(0.000)
                                                          0.0025(0.000)
## 13
       11.7573(0.526)
                        11.7573(0.526)
                                        11.2103(0.501)
                                                         11.2103(0.501)
## 14 111.4742(4.985)
                        10.8023(0.483) 111.4742(4.985)
                                                         10.8023(0.483)
       11.7573(0.526)
                        11.7573(0.526)
                                       10.5289(0.471)
                                                         10.5289(0.471)
## 16 111.4742(4.985)
                        10.8023(0.483) 111.4742(4.985)
                                                         10.8023(0.483)
## 17
                18.71
                                11.864
                                                17.995
                                                                  11.15
```