$$Tm \otimes \mathbf{P}(n_1 + \cdots + n_m, k) \cdot Tn_1 \otimes \cdots \otimes Tn_m \xrightarrow{\ \ \tau\ \ } Tk$$