

Universidade Federal do Rio Grande do Norte  
Instituto Metr pole Digital  
**IMD0601 - Bioestat stica**

# Dados normais

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## Baixe a aula (e os arquivos)

- Para aqueles que não clonaram o repositório:

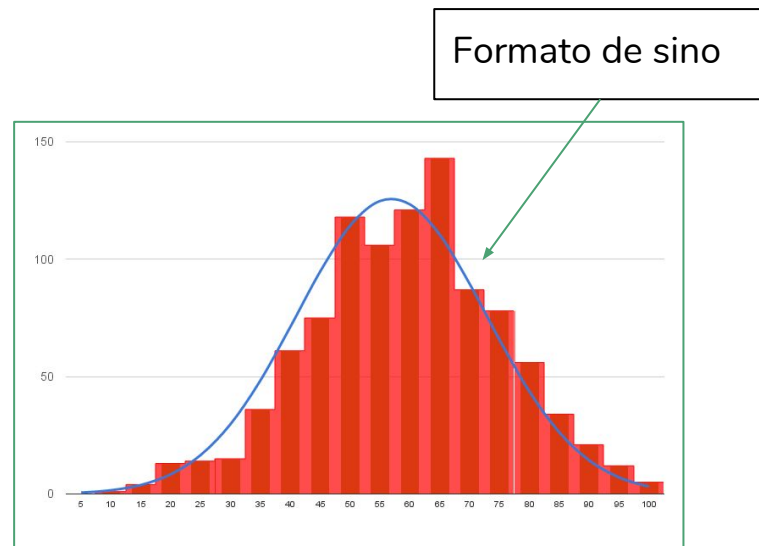
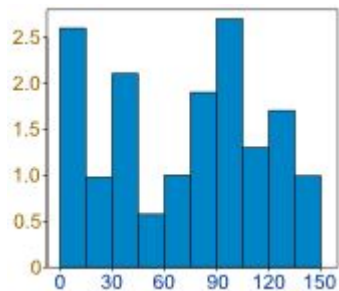
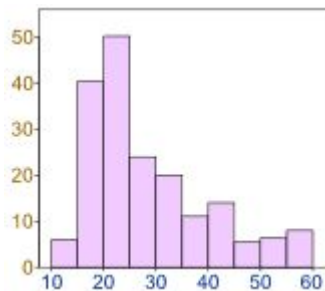
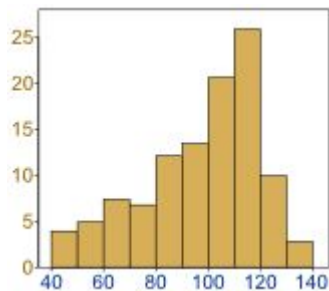
```
> git clone https://github.com/tetsufmbio/IMD0601.git
```

- Para aqueles que já tem o repositório local:

```
> cd /path/to/IMD0601
```

```
> git pull
```

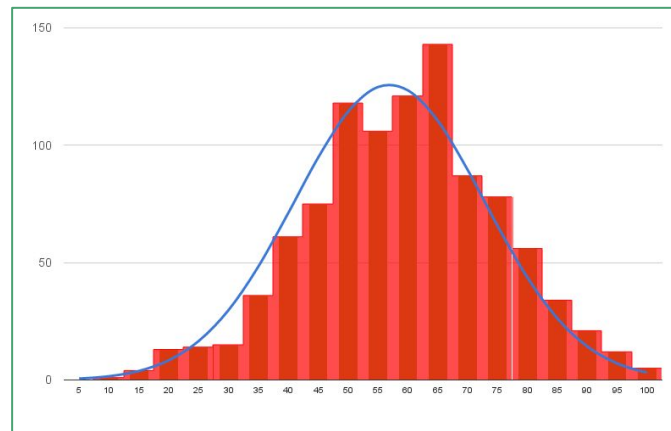
# Distribuição dos dados



Dados com Distribuição Normal

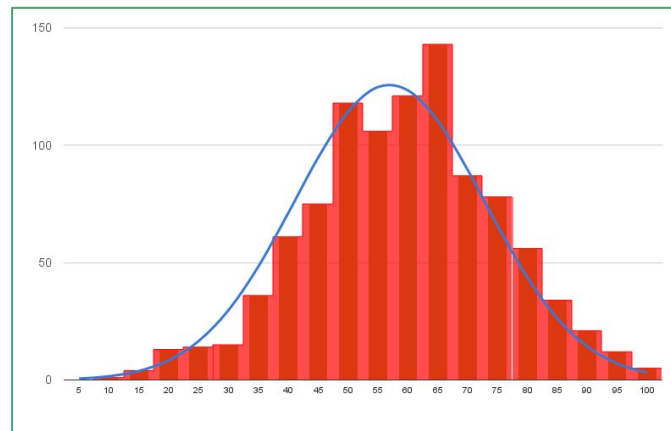
# Exemplos de dados normais

- Altura das pessoas;
- Notas de prova;
- Duração da gravidez;
- Salário;
- Tamanho de peças produzidas em uma fábrica;
- etc...

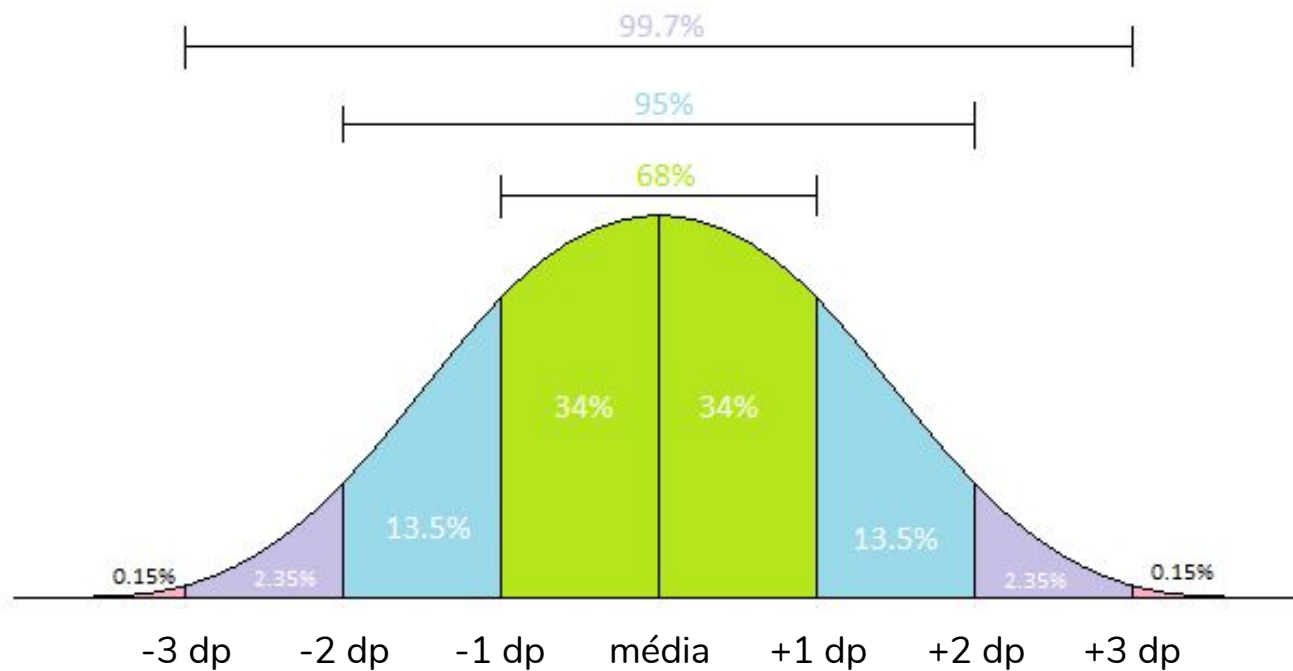


# Propriedades de uma distribuição normal

- Formato de sino;
- Simétrico;
- Média = Mediana = Moda;
- Regra do desvio padrão.



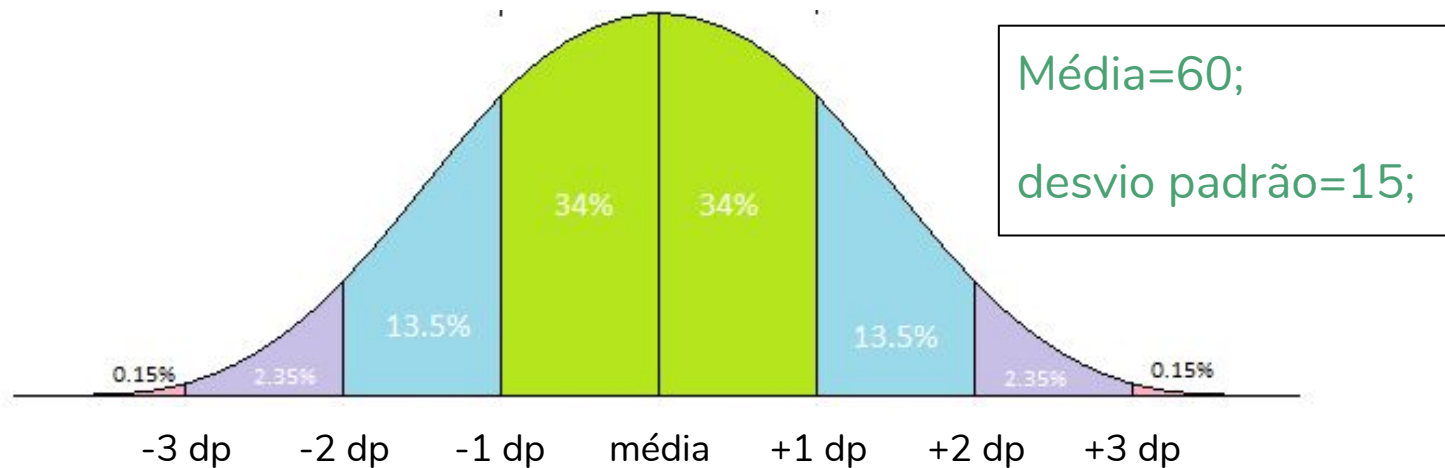
# Regra do desvio padrão



# Regra do desvio padrão

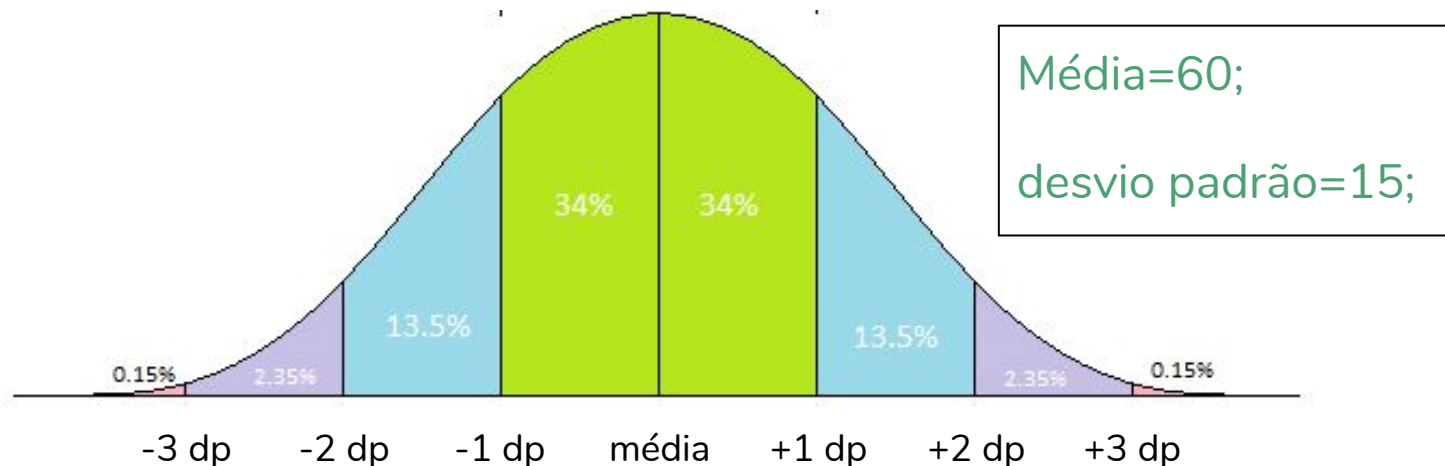
Tirei nota 75. Quantos alunos tiraram uma nota menor que a minha? 84%

Quantos tiraram uma nota acima que a minha? 16%



# Regra do desvio padrão

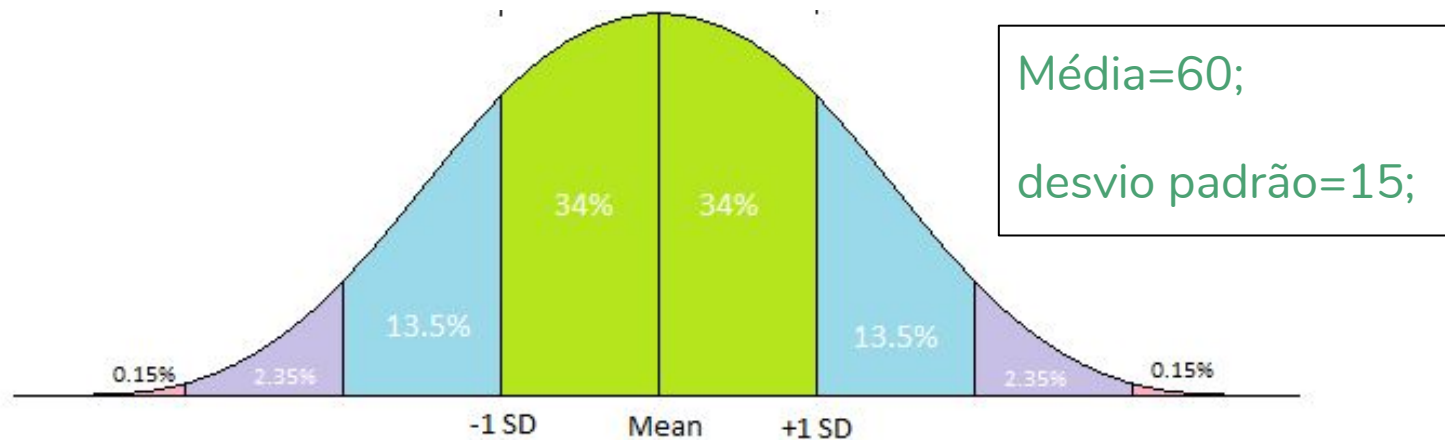
Quero estar entre os 5% dos alunos que tiraram a maior nota. Que nota eu devo tirar? Resposta: 90





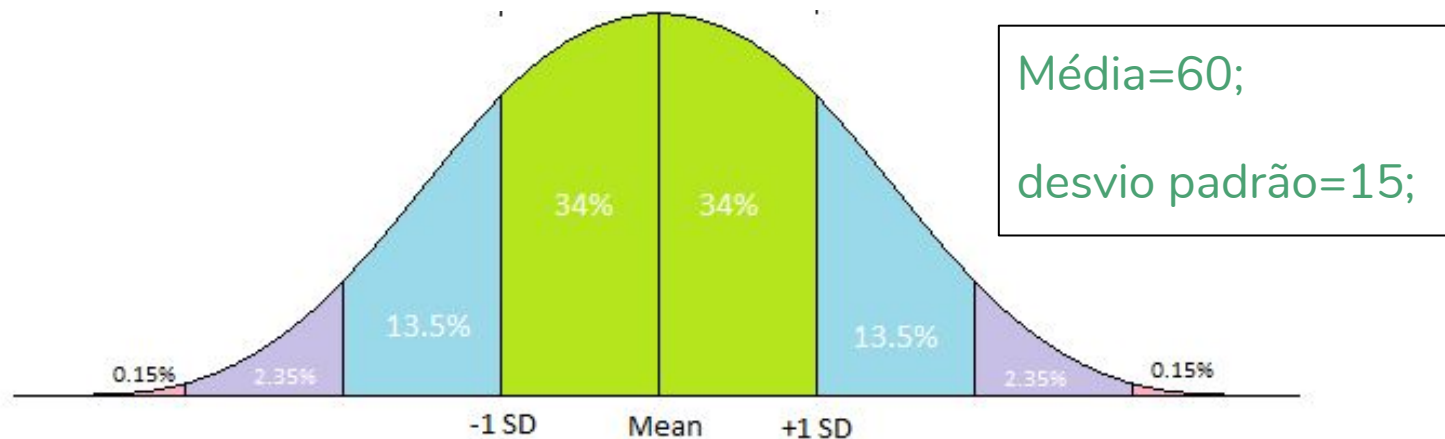
# Regra do desvio padrão

Se eu tirei 80, quantos alunos ficaram abaixo da minha nota?

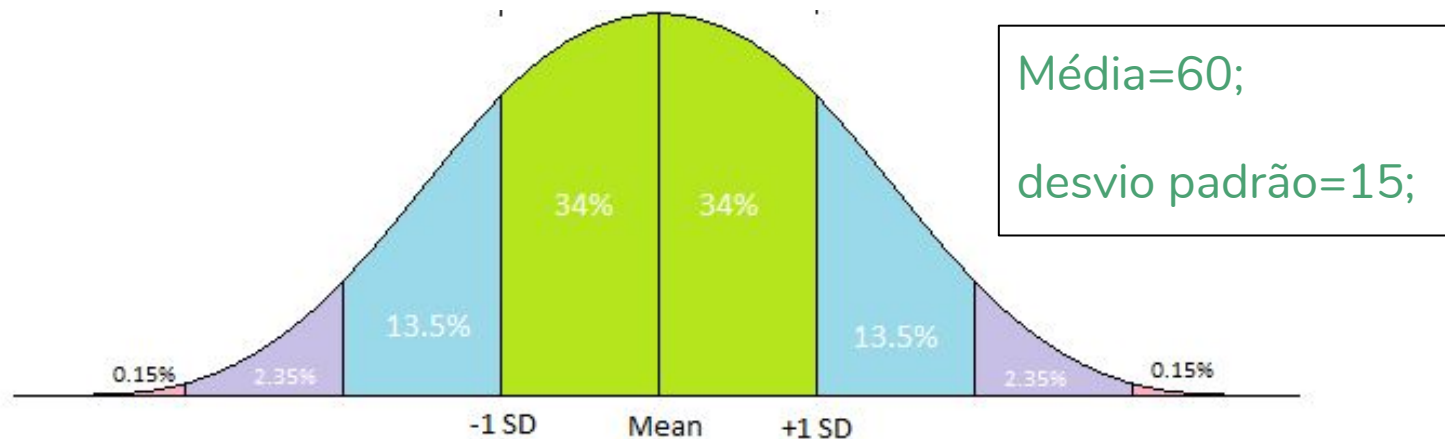


# Função da distribuição normal

$$F(x) = \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$$



Se eu tirei 80, quantos desvios padrão estou da média?

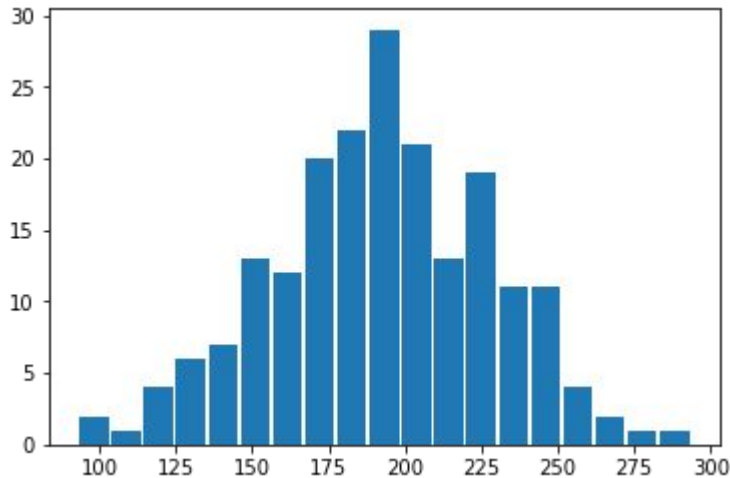


# Z-score

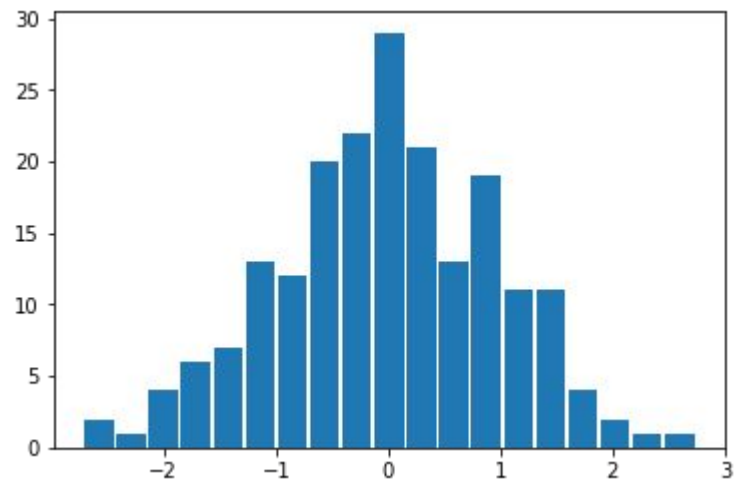
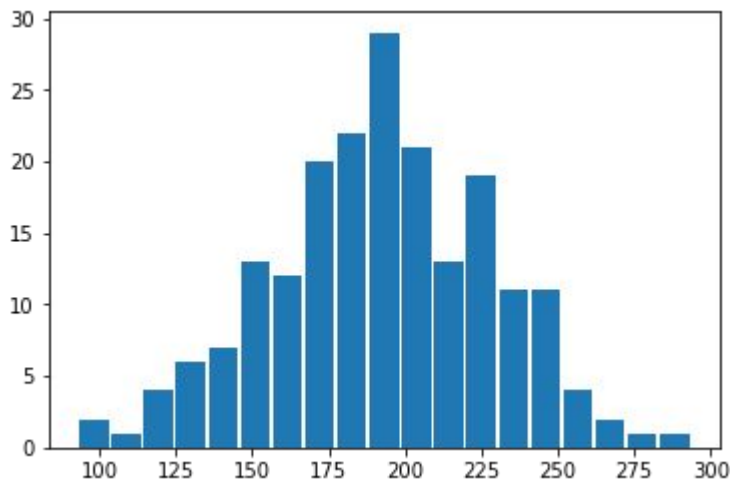
Z-score → unidades de desvio padrão de um determinado valor em um conjunto de dados de média  $\mu$  e desvio padrão  $\sigma$ .

$$z = \frac{x - \mu}{\sigma}$$

O que acontece se eu aplicar o z-score em todo dado...?



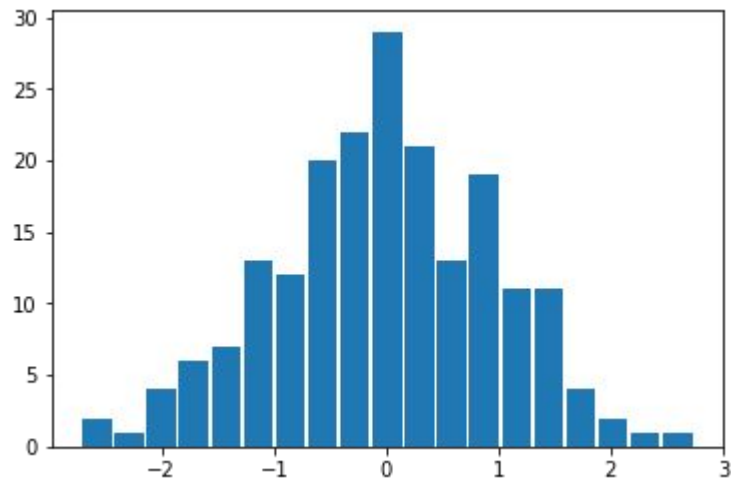
O que acontece se eu aplicar o z-score em todo dado...?



Qual é a média e o desvio padrão dos dados transformados em z-score?

$$\mu = 0$$

$$\sigma = 1$$



# Quando os dados são transformados em z-score...

Eles se transformam em um conjunto de dados de:

- $\mu = 0$
- $\sigma = 1$

Transformar os dados em Z-score é uma forma de padronizar (normalizar) os dados;

Gera uma distribuição normal padrão.



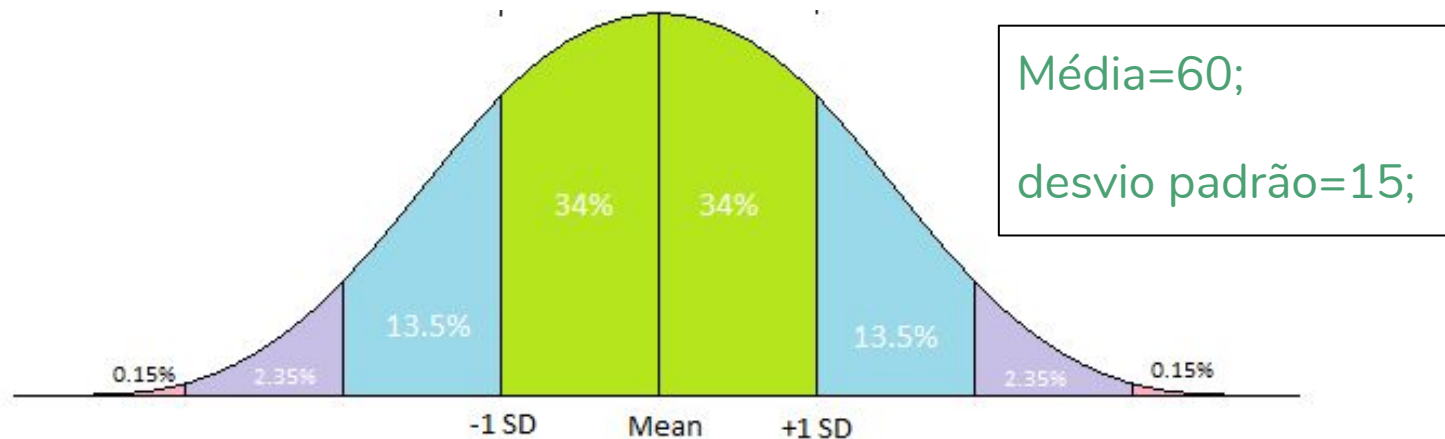
A normal distribution curve is shown. A vertical line is drawn from the x-axis to the curve at a point labeled  $z$ . The area under the curve to the left of this line is shaded gray, representing the cumulative probability  $P(Z \leq z)$ .

$$= \frac{1}{\sqrt{2\pi}} e^{-\frac{1}{2}(z)^2} \quad -\infty \leq z \leq \infty$$

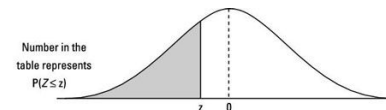
| Z    | 0.00   | 0.01   | 0.02   | 0.03   | 0.04   | 0.05   | 0.06   | 0.07   | 0.08   | 0.09   |
|------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| -3.4 | 0.0003 | 0.0003 | 0.0003 | 0.0003 | 0.0003 | 0.0003 | 0.0003 | 0.0003 | 0.0003 | 0.0002 |
| -3.3 | 0.0005 | 0.0005 | 0.0005 | 0.0004 | 0.0004 | 0.0004 | 0.0004 | 0.0004 | 0.0004 | 0.0003 |
| -3.2 | 0.0007 | 0.0007 | 0.0006 | 0.0006 | 0.0006 | 0.0006 | 0.0006 | 0.0005 | 0.0005 | 0.0005 |
| -3.1 | 0.0010 | 0.0010 | 0.0009 | 0.0009 | 0.0009 | 0.0009 | 0.0009 | 0.0008 | 0.0008 | 0.0008 |
| -3.0 | 0.0013 | 0.0013 | 0.0013 | 0.0012 | 0.0012 | 0.0011 | 0.0011 | 0.0011 | 0.0010 | 0.0010 |
| -2.9 | 0.0019 | 0.0018 | 0.0018 | 0.0017 | 0.0016 | 0.0016 | 0.0015 | 0.0015 | 0.0014 | 0.0014 |
| -2.8 | 0.0026 | 0.0025 | 0.0024 | 0.0023 | 0.0023 | 0.0022 | 0.0021 | 0.0021 | 0.0020 | 0.0019 |
| -2.7 | 0.0035 | 0.0034 | 0.0033 | 0.0032 | 0.0031 | 0.0030 | 0.0029 | 0.0028 | 0.0027 | 0.0026 |
| -2.6 | 0.0047 | 0.0046 | 0.0044 | 0.0043 | 0.0042 | 0.0041 | 0.0040 | 0.0039 | 0.0037 | 0.0036 |
| -2.5 | 0.0062 | 0.0060 | 0.0059 | 0.0057 | 0.0055 | 0.0054 | 0.0052 | 0.0051 | 0.0049 | 0.0048 |
| -2.4 | 0.0082 | 0.0080 | 0.0078 | 0.0075 | 0.0073 | 0.0071 | 0.0069 | 0.0068 | 0.0066 | 0.0064 |
| -2.3 | 0.0107 | 0.0104 | 0.0102 | 0.0099 | 0.0096 | 0.0094 | 0.0091 | 0.0089 | 0.0087 | 0.0084 |
| -2.2 | 0.0139 | 0.0136 | 0.0132 | 0.0129 | 0.0125 | 0.0122 | 0.0119 | 0.0116 | 0.0113 | 0.0110 |
| -2.1 | 0.0179 | 0.0174 | 0.0170 | 0.0166 | 0.0162 | 0.0158 | 0.0154 | 0.0150 | 0.0146 | 0.0143 |
| -2.0 | 0.0227 | 0.0221 | 0.0217 | 0.0212 | 0.0207 | 0.0203 | 0.0198 | 0.0194 | 0.0189 | 0.0185 |
| -1.9 | 0.0281 | 0.0271 | 0.0274 | 0.0268 | 0.0262 | 0.0256 | 0.0250 | 0.0244 | 0.0239 | 0.0233 |
| -1.8 | 0.0359 | 0.0351 | 0.0344 | 0.0336 | 0.0329 | 0.0322 | 0.0314 | 0.0307 | 0.0301 | 0.0294 |
| -1.7 | 0.0446 | 0.0436 | 0.0427 | 0.0418 | 0.0409 | 0.0401 | 0.0392 | 0.0384 | 0.0375 | 0.0367 |
| -1.6 | 0.0548 | 0.0537 | 0.0526 | 0.0516 | 0.0505 | 0.0495 | 0.0485 | 0.0475 | 0.0465 | 0.0455 |
| -1.5 | 0.0663 | 0.0651 | 0.0639 | 0.0628 | 0.0616 | 0.0604 | 0.0591 | 0.0579 | 0.0567 | 0.0555 |
| -1.4 | 0.0808 | 0.0793 | 0.0778 | 0.0764 | 0.0749 | 0.0735 | 0.0721 | 0.0708 | 0.0694 | 0.0681 |
| -1.3 | 0.0968 | 0.0951 | 0.0934 | 0.0918 | 0.0901 | 0.0885 | 0.0869 | 0.0853 | 0.0838 | 0.0823 |
| -1.2 | 0.1151 | 0.1131 | 0.1112 | 0.1093 | 0.1075 | 0.1056 | 0.1038 | 0.1020 | 0.1003 | 0.0985 |
| -1.1 | 0.1357 | 0.1335 | 0.1314 | 0.1292 | 0.1271 | 0.1249 | 0.1230 | 0.1210 | 0.1190 | 0.1170 |
| -1.0 | 0.1587 | 0.1562 | 0.1538 | 0.1515 | 0.1492 | 0.1469 | 0.1446 | 0.1423 | 0.1401 | 0.1379 |
| -0.9 | 0.1841 | 0.1814 | 0.1787 | 0.1758 | 0.1729 | 0.1699 | 0.1668 | 0.1635 | 0.1601 | 0.1567 |
| -0.8 | 0.2119 | 0.2090 | 0.2061 | 0.2033 | 0.2005 | 0.1977 | 0.1949 | 0.1922 | 0.1894 | 0.1867 |
| -0.7 | 0.2420 | 0.2389 | 0.2358 | 0.2327 | 0.2296 | 0.2266 | 0.2236 | 0.2206 | 0.2177 | 0.2148 |
| -0.6 | 0.2743 | 0.2709 | 0.2676 | 0.2643 | 0.2611 | 0.2578 | 0.2546 | 0.2514 | 0.2483 | 0.2451 |
| -0.5 | 0.3085 | 0.3045 | 0.3015 | 0.2981 | 0.2946 | 0.2912 | 0.2877 | 0.2843 | 0.2810 | 0.2776 |
| -0.4 | 0.3446 | 0.3397 | 0.3356 | 0.3314 | 0.3270 | 0.3226 | 0.3181 | 0.3136 | 0.3091 | 0.3045 |
| -0.3 | 0.3821 | 0.3763 | 0.3715 | 0.3707 | 0.3669 | 0.3632 | 0.3594 | 0.3557 | 0.3520 | 0.3483 |
| -0.2 | 0.4207 | 0.4168 | 0.4129 | 0.4090 | 0.4052 | 0.4013 | 0.3974 | 0.3936 | 0.3897 | 0.3859 |
| -0.1 | 0.4602 | 0.4562 | 0.4522 | 0.4483 | 0.4443 | 0.4404 | 0.4364 | 0.4325 | 0.4286 | 0.4247 |
| 0.0  | 0.5000 | 0.5000 | 0.4920 | 0.4880 | 0.4840 | 0.4801 | 0.4761 | 0.4721 | 0.4681 | 0.4641 |
| 0.1  | 0.5400 | 0.5359 | 0.5319 | 0.5278 | 0.5237 | 0.5197 | 0.5156 | 0.5115 | 0.5074 | 0.5033 |
| 0.2  | 0.5808 | 0.5758 | 0.5717 | 0.5675 | 0.5634 | 0.5593 | 0.5552 | 0.5511 | 0.5470 | 0.5429 |
| 0.3  | 0.6224 | 0.6164 | 0.6122 | 0.6079 | 0.6037 | 0.5995 | 0.5953 | 0.5911 | 0.5869 | 0.5827 |
| 0.4  | 0.6647 | 0.6577 | 0.6534 | 0.6491 | 0.6447 | 0.6404 | 0.6360 | 0.6317 | 0.6273 | 0.6229 |
| 0.5  | 0.7076 | 0.7006 | 0.6962 | 0.6918 | 0.6874 | 0.6830 | 0.6786 | 0.6742 | 0.6697 | 0.6653 |
| 0.6  | 0.7513 | 0.7442 | 0.7397 | 0.7352 | 0.7307 | 0.7262 | 0.7217 | 0.7172 | 0.7127 | 0.7082 |
| 0.7  | 0.7958 | 0.7887 | 0.7841 | 0.7795 | 0.7749 | 0.7703 | 0.7657 | 0.7611 | 0.7565 | 0.7519 |
| 0.8  | 0.8411 | 0.8340 | 0.8293 | 0.8246 | 0.8199 | 0.8152 | 0.8105 | 0.8058 | 0.8011 | 0.7964 |
| 0.9  | 0.8870 | 0.8799 | 0.8751 | 0.8703 | 0.8655 | 0.8607 | 0.8559 | 0.8511 | 0.8463 | 0.8415 |
| 1.0  | 0.9334 | 0.9263 | 0.9214 | 0.9165 | 0.9116 | 0.9067 | 0.9018 | 0.8969 | 0.8920 | 0.8871 |
| 1.1  | 0.9801 | 0.9730 | 0.9680 | 0.9630 | 0.9580 | 0.9530 | 0.9480 | 0.9430 | 0.9380 | 0.9330 |
| 1.2  | 1.0274 | 1.0203 | 1.0152 | 1.0102 | 1.0051 | 1.0000 | 0.9949 | 0.9898 | 0.9847 | 0.9796 |
| 1.3  | 1.0754 | 1.0683 | 1.0631 | 1.0580 | 1.0528 | 1.0477 | 1.0425 | 1.0374 | 1.0322 | 1.0270 |
| 1.4  | 1.1240 | 1.1169 | 1.1116 | 1.1064 | 1.1011 | 1.0958 | 1.0905 | 1.0852 | 1.0799 | 1.0746 |
| 1.5  | 1.1732 | 1.1660 | 1.1606 | 1.1553 | 1.1500 | 1.1446 | 1.1392 | 1.1338 | 1.1284 | 1.1229 |
| 1.6  | 1.2230 | 1.2157 | 1.2102 | 1.2048 | 1.1993 | 1.1938 | 1.1883 | 1.1828 | 1.1772 | 1.1717 |
| 1.7  | 1.2734 | 1.2660 | 1.2604 | 1.2549 | 1.2493 | 1.2437 | 1.2381 | 1.2325 | 1.2268 | 1.2212 |
| 1.8  | 1.3244 | 1.3169 | 1.3112 | 1.3056 | 1.3000 | 1.2943 | 1.2886 | 1.2829 | 1.2772 | 1.2715 |
| 1.9  | 1.3760 | 1.3684 | 1.3626 | 1.3569 | 1.3511 | 1.3453 | 1.3395 | 1.3337 | 1.3278 | 1.3219 |
| 2.0  | 1.4282 | 1.4205 | 1.4146 | 1.4088 | 1.4029 | 1.3970 | 1.3911 | 1.3852 | 1.3792 | 1.3732 |
| 2.1  | 1.4810 | 1.4732 | 1.4672 | 1.4613 | 1.4553 | 1.4493 | 1.4433 | 1.4373 | 1.4312 | 1.4252 |
| 2.2  | 1.5344 | 1.5265 | 1.5204 | 1.5144 | 1.5083 | 1.5022 | 1.4961 | 1.4900 | 1.4838 | 1.4777 |
| 2.3  | 1.5884 | 1.5804 | 1.5742 | 1.5681 | 1.5619 | 1.5557 | 1.5495 | 1.5433 | 1.5371 | 1.5309 |
| 2.4  | 1.6430 | 1.6349 | 1.6286 | 1.6224 | 1.6161 | 1.6098 | 1.6035 | 1.5972 | 1.5908 | 1.5845 |
| 2.5  | 1.6981 | 1.6899 | 1.6835 | 1.6772 | 1.6708 | 1.6644 | 1.6580 | 1.6515 | 1.6451 | 1.6386 |
| 2.6  | 1.7538 | 1.7455 | 1.7390 | 1.7325 | 1.7260 | 1.7195 | 1.7130 | 1.7064 | 1.6998 | 1.6932 |
| 2.7  | 1.8100 | 1.8016 | 1.7950 | 1.7884 | 1.7818 | 1.7752 | 1.7686 | 1.7619 | 1.7553 | 1.7486 |
| 2.8  | 1.8667 | 1.8582 | 1.8515 | 1.8448 | 1.8381 | 1.8314 | 1.8247 | 1.8179 | 1.8112 | 1.8044 |
| 2.9  | 1.9239 | 1.9153 | 1.9085 | 1.9017 | 1.8949 | 1.8881 | 1.8813 | 1.8744 | 1.8676 | 1.8607 |
| 3.0  | 1.9816 | 1.9729 | 1.9660 | 1.9591 | 1.9522 | 1.9453 | 1.9384 | 1.9314 | 1.9245 | 1.9175 |
| 3.1  | 2.0398 | 2.0310 | 2.0240 | 2.0170 | 2.0100 | 2.0030 | 1.9960 | 1.9890 | 1.9820 | 1.9750 |
| 3.2  | 2.0984 | 2.0895 | 2.0824 | 2.0753 | 2.0682 | 2.0611 | 2.0540 | 2.0469 | 2.0398 | 2.0327 |
| 3.3  | 2.1574 | 2.1484 | 2.1412 | 2.1341 | 2.1270 | 2.1198 | 2.1127 | 2.1055 | 2.0984 | 2.0912 |
| 3.4  | 2.2168 | 2.2077 | 2.2004 | 2.1932 | 2.1860 | 2.1788 | 2.1715 | 2.1643 | 2.1570 | 2.1497 |
| 3.5  | 2.2766 | 2.2674 | 2.2600 | 2.2527 | 2.2454 | 2.2381 | 2.2308 | 2.2234 | 2.2161 | 2.2087 |
| 3.6  | 2.3368 | 2.3275 | 2.3200 | 2.3126 | 2.3052 | 2.2978 | 2.2903 | 2.2828 | 2.2753 | 2.2678 |
| 3.7  | 2.3973 | 2.3879 | 2.3803 | 2.3728 | 2.3653 | 2.3577 | 2.3501 | 2.3425 | 2.3349 | 2.3273 |
| 3.8  | 2.4582 | 2.4487 | 2.4410 | 2.4334 | 2.4258 | 2.4181 | 2.4104 | 2.4027 | 2.3950 | 2.3873 |
| 3.9  | 2.5194 | 2.5098 | 2.5020 | 2.4943 | 2.4866 | 2.4788 | 2.4711 | 2.4633 | 2.4555 | 2.4477 |
| 4.0  | 2.5809 | 2.5712 | 2.5633 | 2.5555 | 2.5476 | 2.5397 | 2.5318 | 2.5239 | 2.5159 | 2.5079 |
| 4.1  | 2.6427 | 2.6329 | 2.6249 | 2.6169 | 2.6089 | 2.6008 | 2.5927 | 2.5846 | 2.5765 | 2.5684 |
| 4.2  | 2.7048 | 2.6949 | 2.6868 | 2.6787 | 2.6705 | 2.6623 | 2.6541 | 2.6459 | 2.6376 | 2.6294 |
| 4.3  | 2.7671 | 2.7571 | 2.7489 | 2.7406 | 2.7323 | 2.7240 | 2.7157 | 2.7073 | 2.6989 | 2.6905 |
| 4.4  | 2.8296 | 2.8195 | 2.8112 | 2.8028 | 2.7944 | 2.7860 | 2.7775 | 2.7690 | 2.7605 | 2.7520 |
| 4.5  | 2.8923 | 2.8821 | 2.8737 | 2.8652 | 2.8567 | 2.8481 | 2.8396 | 2.8310 | 2.8224 | 2.8138 |
| 4.6  | 2.9552 | 2.9449 | 2.9363 | 2.9277 | 2.9190 | 2.9103 | 2.9016 | 2.8929 | 2.8841 | 2.8754 |
| 4.7  | 3.0183 | 3.0079 | 2.9991 | 2.9903 | 2.9815 | 2.9727 | 2.9638 | 2.9549 | 2.9460 | 2.9371 |
| 4.8  | 3.0816 | 3.0711 | 3.0621 | 3.0531 | 3.0441 | 3.0351 | 3.0261 | 3.0170 | 3.0079 | 2.9988 |
| 4.9  | 3.1451 | 3.1345 | 3.1253 | 3.1161 | 3.1069 | 3.0976 | 3.0883 | 3.0790 | 3.0696 | 3.0603 |
| 5.0  | 3.2087 | 3.1980 | 3.1886 | 3.1792 | 3.1698 | 3.1603 | 3.1508 | 3.1413 | 3.1317 | 3.1222 |
| 5.1  | 3.2725 | 3.2617 | 3.2522 | 3.2426 | 3.2330 | 3.2234 | 3.2137 | 3.2041 | 3.1944 | 3.1848 |
| 5.2  | 3.3364 | 3.3255 | 3.3159 | 3.3062 | 3.2965 | 3.2868 | 3.2770 | 3.2673 | 3.2575 | 3.2478 |
| 5.3  | 3.4005 | 3.3895 | 3.3800 | 3.3702 | 3.3604 | 3.3506 | 3.3407 | 3.3308 | 3.3209 | 3.3110 |
| 5.4  | 3.4647 | 3.4536 | 3.4440 | 3.4342 | 3.4243 | 3.4144 | 3.4045 | 3.3945 | 3.3845 | 3.3745 |
| 5.5  | 3.5290 | 3.5178 | 3.5081 | 3.4982 | 3.4882 | 3.4782 | 3.4682 | 3.4581 | 3.4480 | 3.4379 |
| 5.6  | 3.5934 | 3.5821 | 3.5723 | 3.5623 | 3.5522 | 3.5421 | 3.5320 | 3.5219 | 3.5117 | 3.5015 |
| 5.7  | 3.6579 | 3.6465 | 3.6366 | 3.6265 | 3.6163 | 3.6061 | 3.5959 | 3.5856 | 3.5754 | 3.5651 |
| 5.8  | 3.7225 | 3.7110 | 3.7010 | 3.6908 | 3.6805 | 3.6702 | 3.6599 | 3.6495 | 3.6391 | 3.6287 |
| 5.9  | 3.7872 | 3.7756 | 3.7655 | 3.7552 | 3.7448 | 3.7344 | 3.7240 | 3.7135 | 3.7030 | 3.6925 |
| 6.0  | 3.8520 | 3.8403 | 3.8301 | 3.8196 | 3.8091 | 3.7985 | 3.7879 | 3.7773 | 3.7667 | 3.7561 |
| 6.1  | 3.9169 | 3.9051 | 3.8948 | 3.8842 | 3.8736 | 3.8629 | 3.8522 | 3.8415 | 3.8308 | 3.8201 |
| 6.2  | 3.9819 | 3.9699 | 3.9595 | 3.9488 | 3.9380 | 3.9272 | 3.9164 | 3.9055 | 3.8946 | 3.8837 |
| 6.3  | 4.0470 | 4.0349 | 4.0244 | 4.0136 | 4.0027 | 3.9918 | 3.9808 | 3.9698 | 3.9588 | 3.9477 |
| 6.4  | 4.1122 | 4.0999 | 4.0893 | 4.0784 | 4.0674 | 4.0563 | 4.0452 | 4.0341 | 4.0230 | 4.0118 |
| 6.5  | 4.1775 | 4.1651 | 4.1544 | 4.1434 | 4.1323 | 4.1211 | 4.1099 | 4.0986 | 4.0873 | 4.0759 |
| 6.6  | 4.2428 | 4.2303 | 4.2195 | 4.2084 | 4.1972 | 4.1859 | 4.174  |        |        |        |

# Voltando a questão

Se eu tirei 80, quantos alunos ficaram abaixo da minha nota?



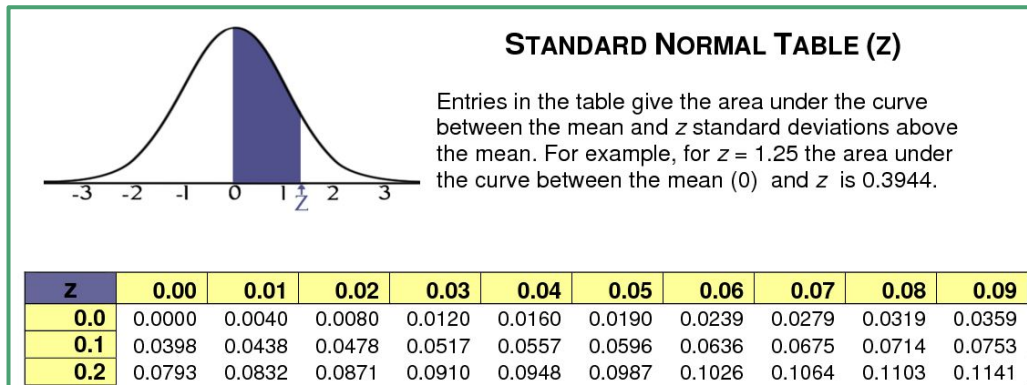
# Diferentes tabelas de z-score



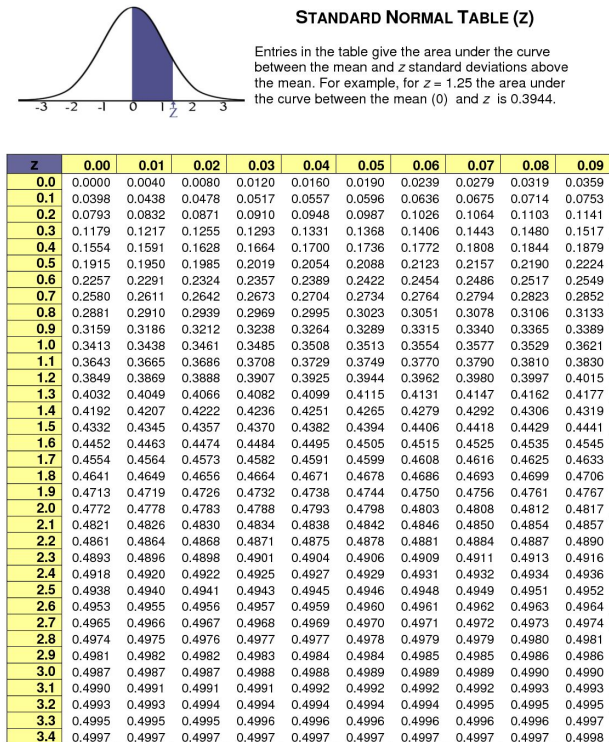
| <b>-0.5</b> | .1841 | .1814 | .1786 | .1762 | .1738 | .1711 | .1685 | .1660 | .1633 | .1611 |
|-------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| <b>-0.8</b> | .2119 | .2090 | .2061 | .2033 | .2005 | .1977 | .1949 | .1922 | .1894 | .1867 |
| <b>-0.7</b> | .2420 | .2389 | .2358 | .2327 | .2296 | .2266 | .2236 | .2206 | .2177 | .2148 |
| <b>-0.6</b> | .2743 | .2709 | .2676 | .2643 | .2611 | .2578 | .2546 | .2514 | .2483 | .2451 |
| <b>-0.5</b> | .3085 | .3050 | .3015 | .2981 | .2946 | .2912 | .2877 | .2843 | .2810 | .2776 |
| <b>-0.4</b> | .3446 | .3409 | .3372 | .3336 | .3300 | .3264 | .3228 | .3192 | .3156 | .3121 |
| <b>-0.3</b> | .3821 | .3783 | .3745 | .3707 | .3669 | .3632 | .3594 | .3557 | .3520 | .3483 |
| <b>-0.2</b> | .4207 | .4168 | .4129 | .4090 | .4052 | .4013 | .3974 | .3936 | .3897 | .3859 |
| <b>-0.1</b> | .4602 | .4562 | .4522 | .4483 | .4443 | .4404 | .4364 | .4325 | .4286 | .4247 |
| <b>-0.0</b> | .5000 | .4960 | .4920 | .4880 | .4840 | .4801 | .4761 | .4721 | .4681 | .4641 |

| <b>z</b> | <b>0.00</b> | <b>0.01</b> | <b>0.02</b> | <b>0.03</b> | <b>0.04</b> | <b>0.05</b> | <b>0.06</b> | <b>0.07</b> | <b>0.08</b> | <b>0.09</b> |
|----------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|
| -3.6     | .0002       | .0002       | .0001       | .0001       | .0001       | .0001       | .0001       | .0001       | .0001       | .0001       |
| -3.5     | .0002       | .0002       | .0002       | .0002       | .0002       | .0002       | .0002       | .0002       | .0002       | .0002       |
| -3.4     | .0003       | .0003       | .0003       | .0003       | .0003       | .0003       | .0003       | .0003       | .0003       | .0002       |
| -3.3     | .0005       | .0005       | .0005       | .0004       | .0004       | .0004       | .0004       | .0004       | .0004       | .0003       |
| -3.2     | .0007       | .0007       | .0006       | .0006       | .0006       | .0006       | .0006       | .0005       | .0005       | .0005       |
| -3.1     | .0010       | .0009       | .0009       | .0009       | .0008       | .0008       | .0008       | .0008       | .0007       | .0007       |
| -3.0     | .0013       | .0013       | .0013       | .0012       | .0012       | .0011       | .0011       | .0011       | .0010       | .0010       |
| -2.9     | .0019       | .0018       | .0018       | .0017       | .0016       | .0016       | .0015       | .0015       | .0014       | .0014       |
| -2.8     | .0026       | .0025       | .0024       | .0023       | .0023       | .0022       | .0021       | .0021       | .0020       | .0019       |
| -2.7     | .0035       | .0034       | .0033       | .0032       | .0031       | .0030       | .0029       | .0028       | .0027       | .0026       |
| -2.6     | .0047       | .0045       | .0044       | .0043       | .0041       | .0040       | .0039       | .0038       | .0037       | .0036       |
| -2.5     | .0062       | .0060       | .0059       | .0057       | .0055       | .0054       | .0052       | .0051       | .0049       | .0048       |
| -2.4     | .0082       | .0080       | .0078       | .0075       | .0073       | .0071       | .0069       | .0068       | .0066       | .0064       |
| -2.3     | .0107       | .0104       | .0102       | .0099       | .0096       | .0094       | .0091       | .0089       | .0087       | .0084       |
| -2.2     | .0139       | .0136       | .0132       | .0129       | .0125       | .0122       | .0119       | .0116       | .0113       | .0110       |
| -2.1     | .0179       | .0174       | .0170       | .0166       | .0162       | .0158       | .0154       | .0150       | .0146       | .0143       |
| -2.0     | .0228       | .0222       | .0217       | .0212       | .0207       | .0202       | .0197       | .0192       | .0188       | .0183       |
| -1.9     | .0287       | .0281       | .0274       | .0268       | .0262       | .0256       | .0250       | .0244       | .0239       | .0233       |
| -1.8     | .0359       | .0351       | .0344       | .0336       | .0329       | .0322       | .0314       | .0307       | .0301       | .0294       |
| -1.7     | .0446       | .0436       | .0427       | .0418       | .0409       | .0401       | .0392       | .0384       | .0375       | .0367       |
| -1.6     | .0548       | .0537       | .0526       | .0516       | .0505       | .0495       | .0485       | .0475       | .0465       | .0455       |
| -1.5     | .0668       | .0655       | .0643       | .0630       | .0618       | .0606       | .0594       | .0582       | .0571       | .0559       |
| -1.4     | .0808       | .0793       | .0778       | .0764       | .0749       | .0735       | .0721       | .0708       | .0694       | .0681       |
| -1.3     | .0968       | .0951       | .0934       | .0918       | .0901       | .0885       | .0869       | .0853       | .0838       | .0823       |
| -1.2     | .1151       | .1131       | .1112       | .1093       | .1075       | .1056       | .1038       | .1020       | .1003       | .0985       |
| -1.1     | .1357       | .1335       | .1314       | .1292       | .1271       | .1251       | .1230       | .1210       | .1190       | .1170       |
| -1.0     | .1587       | .1562       | .1539       | .1515       | .1492       | .1469       | .1446       | .1423       | .1401       | .1379       |
| -0.9     | .1841       | .1814       | .1788       | .1762       | .1736       | .1711       | .1685       | .1660       | .1635       | .1611       |
| -0.8     | .2119       | .2090       | .2061       | .2033       | .2005       | .1977       | .1949       | .1922       | .1894       | .1867       |
| -0.7     | .2420       | .2389       | .2358       | .2327       | .2296       | .2266       | .2236       | .2206       | .2177       | .2148       |
| -0.6     | .2743       | .2709       | .2676       | .2643       | .2611       | .2578       | .2546       | .2514       | .2483       | .2451       |
| -0.5     | .3085       | .3050       | .3015       | .2981       | .2946       | .2912       | .2877       | .2843       | .2810       | .2776       |
| -0.4     | .3446       | .3409       | .3372       | .3336       | .3300       | .3264       | .3228       | .3192       | .3156       | .3121       |
| -0.3     | .3821       | .3783       | .3745       | .3707       | .3669       | .3632       | .3594       | .3557       | .3520       | .3483       |
| -0.2     | .4207       | .4168       | .4129       | .4090       | .4052       | .4013       | .3974       | .3936       | .3897       | .3859       |
| -0.1     | .4602       | .4562       | .4522       | .4483       | .4443       | .4404       | .4364       | .4325       | .4286       | .4247       |
| -0.0     | .5000       | .4960       | .4920       | .4880       | .4840       | .4801       | .4761       | .4721       | .4681       | .4641       |

# Diferentes tabelas de z-score



■ ■ ■

[illegible]

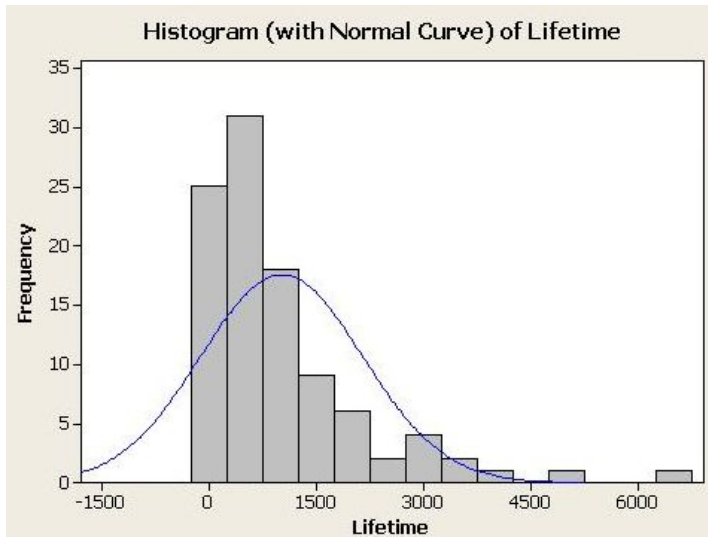
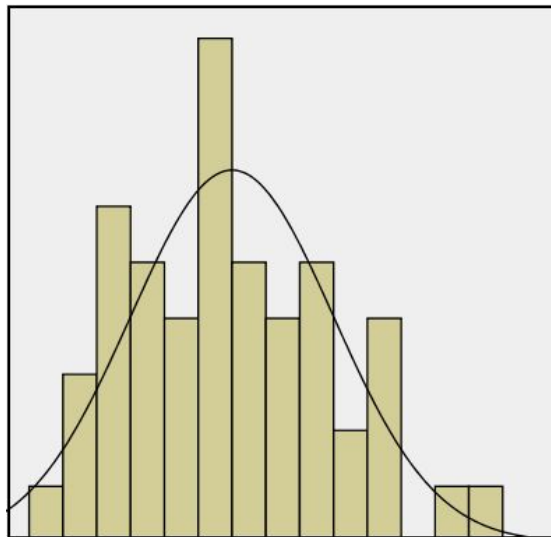
Os valores tabelados do z-score só podem ser utilizados para dados que possuem distribuição normal.

*Como saber se seus dados seguem uma distribuição normal?*

# Como saber se seus dados seguem uma distribuição normal?

Análise visual

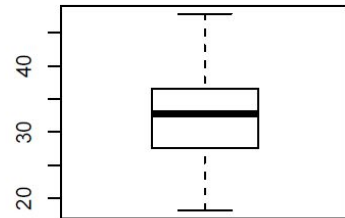
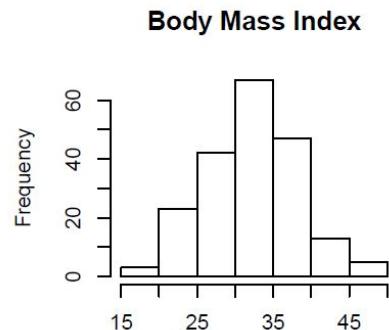
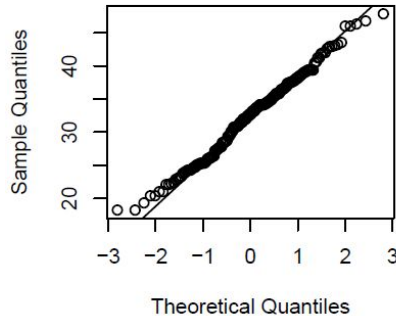
- **Histogramas e a curva normal**



# Como saber se seus dados seguem uma distribuição normal?

## Análise visual

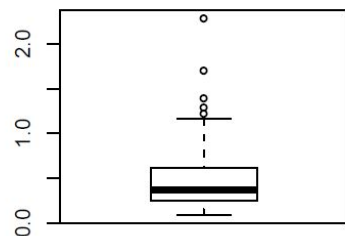
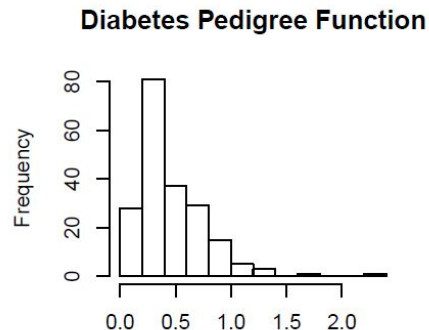
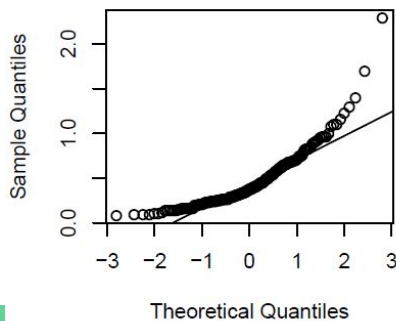
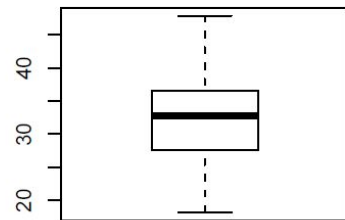
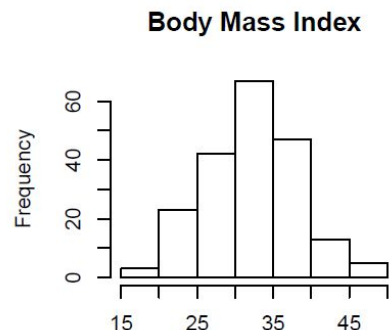
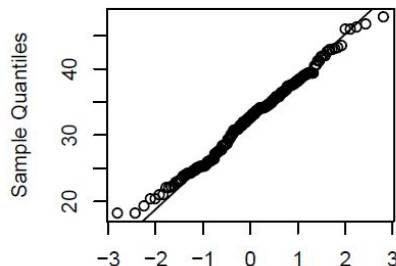
- Histogramas e a curva normal
- **QQ-plot**



# Como saber se seus dados seguem uma distribuição normal?

## Análise visual

- Histogramas e a curva normal
- **QQ-plot**

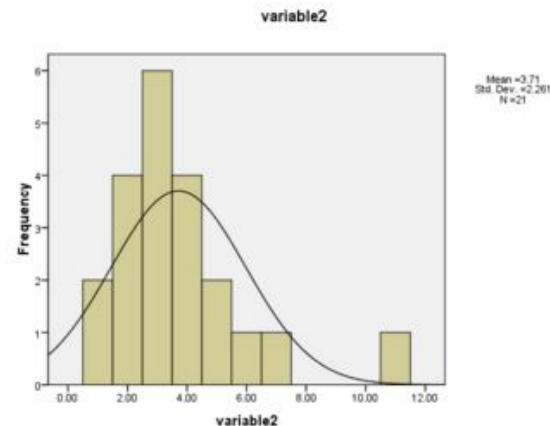
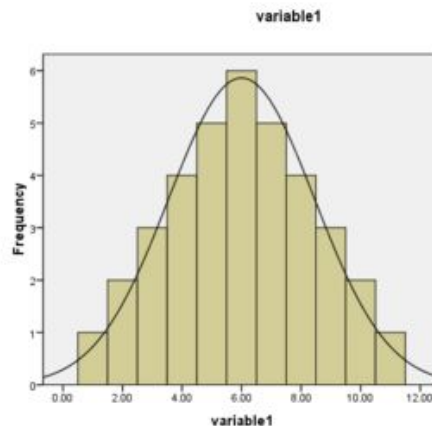




# Como saber se seus dados seguem uma distribuição normal?

Testes estatísticos

- Kolmogorov - Smirnov (K-S)
- Shapiro-Wilk (S-W)



Tests of Normality

|           | Kolmogorov-Smirnov <sup>a</sup> |    |                   | Shapiro-Wilk |    |      |
|-----------|---------------------------------|----|-------------------|--------------|----|------|
|           | Statistic                       | df | Sig.              | Statistic    | df | Sig. |
| variable1 | .083                            | 36 | .200 <sup>*</sup> | .981         | 36 | .782 |
| variable2 | .223                            | 21 | .008              | .805         | 21 | .001 |

a. Lilliefors Significance Correction

\*. This is a lower bound of the true significance.