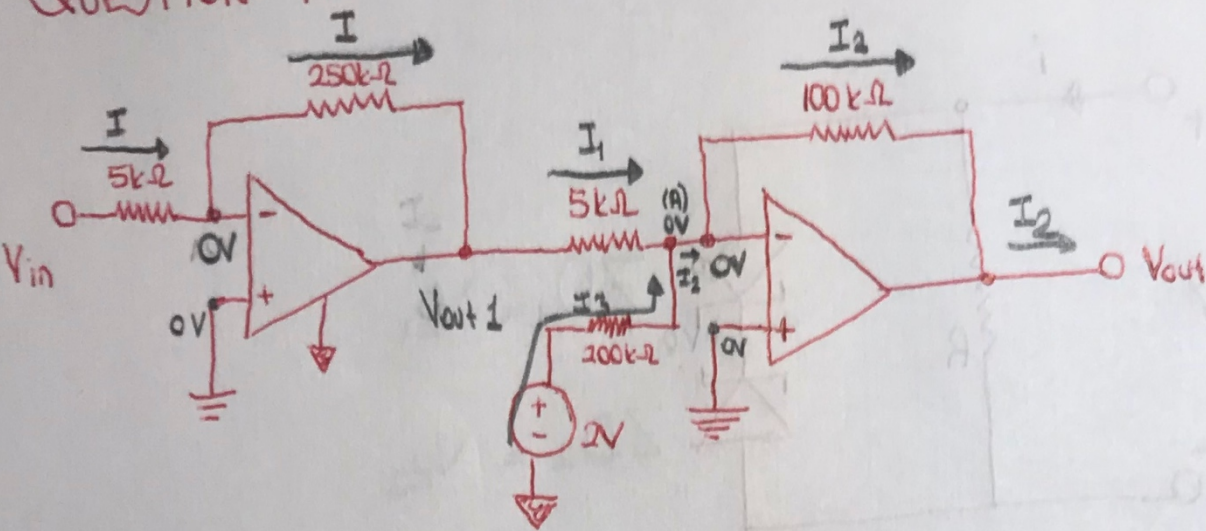


## QUESTION 1:



$V_{out} = ?$

$$V_{out1} = -V_{in} \cdot \frac{250}{5} = -50 \cdot V_{in}$$

$I_1 + I_2 - I_3 = 0 \rightarrow$  KCL at point A.

$$\frac{V_{out1} - 0V}{5k\Omega} + \frac{2V - 0V}{200k\Omega} - \frac{0V - V_{out}}{100k\Omega} = 0$$

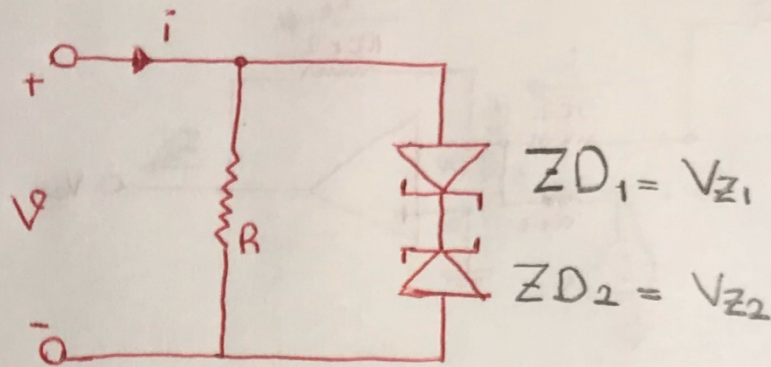
$$\frac{-50V_{in}}{5k\Omega} + \frac{2V}{200k\Omega} + \frac{V_{out}}{100k\Omega} = 0 \Rightarrow \frac{V_{out}}{100k\Omega} = \frac{10V_{in}}{1k\Omega} - \frac{1V}{100k\Omega}$$

So  $V_{out} = 1000V_{in} - 1$



## QUESTION 2:

TEVFİK ÖZEL  
15060082

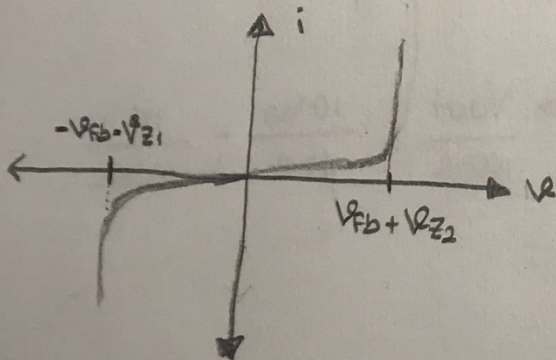


Find nonlinear i-v characteristic of circuit

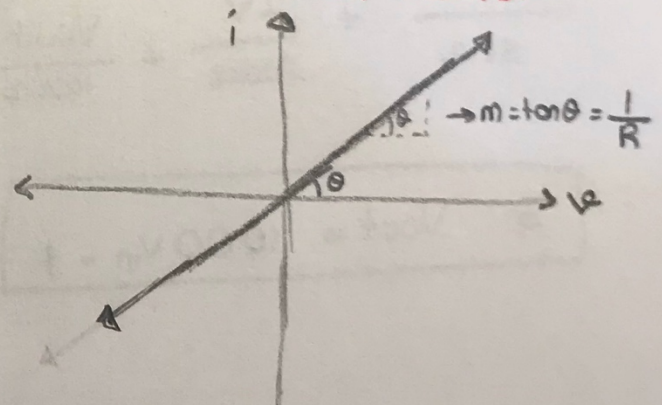
If  $V > 0$ , first Zener diode is forward biased and second Zener diode is reverse biased. So until  $V < V_{fb} + V_{z2}$  there won't be current. And after that point Zener diodes will act like voltage regulator.

If  $V < 0$ , first Zener diode is reverse biased and second Zener diode is forward biased. So until  $V > -V_{fb} - V_{z1}$  there won't be current. After that point Zener diodes will act like voltage regulator.

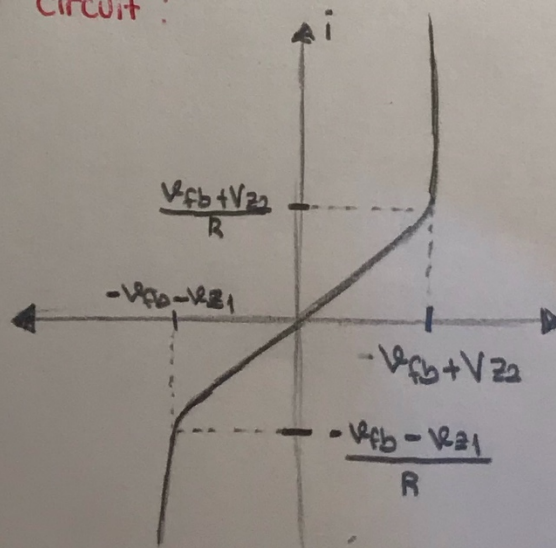
i-v characteristic of Zener diodes:



i-v characteristic of resistor

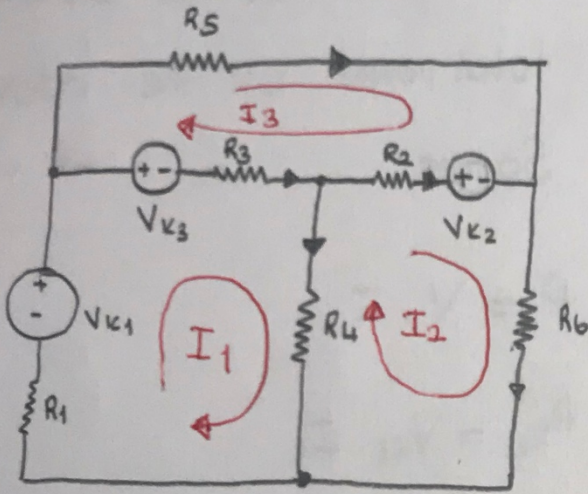


i-v characteristic of circuit:





QUESTION 3:



KVL at MESH 1:  $I_1 R_1 - V_{k1} + V_{k3} + (I_1 - I_3) R_3 + (I_1 - I_2) R_4 = 0$  ①

KVL at MESH 2:  $I_2 R_6 + (I_2 - I_1) R_4 + (I_2 - I_3) R_2 + V_{k2} = 0$  ②

KVL at MESH 3:  $I_3 R_5 - V_{k2} + (I_3 - I_2) R_2 + (I_3 - I_1) R_3 - V_{k3} = 0$  ③

From Eq ①:  $I_1 R_1 + I_1 R_3 - I_3 R_3 + I_1 R_4 - I_2 R_4 - V_{k1} + V_{k3} = 0$

So  $(R_1 + R_3 + R_4) \cdot I_1 - R_3 \cdot I_3 - R_4 \cdot I_2 = V_{k1} - V_{k3}$

From Eq ②:  $I_2 R_6 + I_2 R_4 - I_1 R_4 + I_2 R_2 - I_3 R_2 + V_{k2} = 0$

So  $-R_4 I_1 - (R_6 + R_4 + R_2) \cdot I_2 + R_2 \cdot I_3 = -V_{k2}$

From Eq ③:  $I_3 R_5 - V_{k2} + I_3 R_2 - I_2 R_2 + I_3 R_3 - I_1 R_3 - V_{k3} = 0$

So  $-I_1 R_3 - I_2 R_2 + (R_3 + R_5 + R_2) I_3 = V_{k3} + V_{k2}$

$$\begin{bmatrix} R_1 + R_3 + R_4 & -R_4 & -R_3 \\ R_4 & -(R_6 + R_4 + R_2) & R_2 \\ -R_3 & -R_2 & R_3 + R_5 + R_2 \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \\ I_3 \end{bmatrix} = \begin{bmatrix} V_{k1} - V_{k3} \\ -V_{k2} \\ V_{k3} + V_{k2} \end{bmatrix}$$



$$I_1 = \frac{\begin{vmatrix} V_{K1} - V_{K3} & -R_4 & -R_3 \\ V_{K2} & -(R_6 + R_4 + R_2) & R_2 \\ V_{K3} + V_{K2} & -R_2 & R_3 + R_5 + R_2 \end{vmatrix}}{\begin{vmatrix} R_1 + R_3 + R_4 & -R_4 & -R_3 \\ R_4 & -(R_6 + R_4 + R_2) & R_2 \\ -R_3 & -R_2 & R_3 + R_5 + R_2 \end{vmatrix}}$$

$$\begin{vmatrix} R_1 + R_3 + R_4 & -R_4 & -R_3 \\ R_4 & -(R_6 + R_4 + R_2) & R_2 \\ -R_3 & -R_2 & R_3 + R_5 + R_2 \end{vmatrix}$$

$$I_2 = \frac{\begin{vmatrix} R_1 + R_3 + R_4 & V_{K1} - V_{K3} & -R_3 \\ R_4 & V_{K2} & R_2 \\ -R_3 & V_{K3} + V_{K2} & R_2 + R_3 + R_5 \end{vmatrix}}{\begin{vmatrix} R_1 + R_3 + R_4 & -R_4 & -R_3 \\ R_4 & -(R_6 + R_4 + R_2) & R_2 \\ -R_3 & -R_2 & R_3 + R_5 + R_2 \end{vmatrix}}$$

$$\begin{vmatrix} R_1 + R_3 + R_4 & -R_4 & -R_3 \\ R_4 & -(R_6 + R_4 + R_2) & R_2 \\ -R_3 & -R_2 & R_3 + R_5 + R_2 \end{vmatrix}$$

$$I_3 = \frac{\begin{vmatrix} R_1 + R_3 + R_4 & -R_4 & V_{K1} - V_{K3} \\ R_4 & -(R_6 + R_4 + R_2) & V_{K2} \\ -R_3 & -R_2 & V_{K3} + V_{K2} \end{vmatrix}}{\begin{vmatrix} R_1 + R_3 + R_4 & -R_4 & -R_3 \\ R_4 & -(R_6 + R_4 + R_2) & R_2 \\ -R_3 & -R_2 & R_3 + R_5 + R_2 \end{vmatrix}}$$

$$\begin{vmatrix} R_1 + R_3 + R_4 & -R_4 & -R_3 \\ R_4 & -(R_6 + R_4 + R_2) & R_2 \\ -R_3 & -R_2 & R_3 + R_5 + R_2 \end{vmatrix}$$

Since we know  $I_1$ ,  $I_2$  and  $I_3$  values we can determine total power of the independent sources.

$$P = V \cdot I$$

$$P_{V_{K1}} = V_{K1} \cdot I_1$$

$$P_{V_{K2}} = V_{K2} \cdot (I_2 - I_3)$$

$$P_{V_{K3}} = V_{K3} \cdot (I_1 - I_3)$$

$$P_{total} = P_{V_{K1}} + P_{V_{K2}} + P_{V_{K3}}$$