

Pseudocode: Left and Right Algorithm

Begin print_disks()

For i=0 to 2*n

If disks[i] = 1

Print "d" (1)

Else if disks[i] = 0

Print "l" (1)

End print_disks()

Start main()

8 { (4) ← Initialize n, k, i, q
(2) ← Initialize m=0, temp=0
(1) ← Initialize array disks
(1) ← Read in a number, n

(1) ← Set disks array of n = to new array of n*2

For i=0 to n

disks[2 * i] = 1 → (1)

disks[2 * i + 1] = 0 → (1)

(1) ← Print_disks() } 6n + 3

For k = 0 to n

For q = 0 to 2*n

If disks[q] = 1 → (1)

Else

If (q != 0) and (disks[q - 1] = 1)

temp = disks[q] → (1)

disks[q] = disks[q - 1] → (1)

disks[q - 1] = temp; → (1)

m++ → (1)

(1) ← print_disks() } 6n + 3

(1) ← print number of swap, m

(1) ← delete array disks

$$\sum_{i=0}^{2n} 3 = \frac{(2n-0+1)}{1} 3 = (2n+1) 3 = 6n + 3$$

$$\sum_{i=0}^n 2 = \frac{(n-0+1)}{1} 2 = (n+1) 2 = 2n + 2$$

$$\sum_{k=0}^n \sum_{q=0}^{2n} 8 \Rightarrow \sum_{q=0}^{2n} 8 = (2n-0+1) 8 = (2n+1) 8 = 16n + 8$$

$$\sum_{k=0}^n 16n + 8 = \sum_{k=0}^n 16n + \sum_{k=0}^n 8$$

$$\sum_{k=0}^n 16n = 16 \sum_{k=0}^n n = 16 \frac{n(n+1)}{2}$$

$$16 \sum_{k=0}^n n = \frac{16n(n+1)}{2}$$

$$\sum_{k=0}^n 8 = (n-0+1) 8 = 8n + 8$$

$$8 \left(\frac{n(n+1)}{2} \right) + 8n + 8 = 8n^2 + 8n + 8n + 8 = 8n^2 + 16n + 8$$

$$8n^2 + 16n + 8$$

$$= 8 + 1 + (2n+2) + 1 + (6n+3) + (8n^2+16n+8) + (1) + (6n+3) + 1 + 1 =$$

$$= 8n^2 + 30n + 29$$

$$= 8n^2 + 30n + 29 \in O(n^2)$$

$$\lim_{n \rightarrow \infty} \frac{8n^2 + 30n + 29}{n^2} = \lim_{n \rightarrow \infty} \frac{8n^2}{n^2} = 8 \geq 0.$$

Pseudocode: Lawnmower Algorithm

Begin print_disks()

For i=0 to 2*n

If disks[i] = 1

Print "d" (1)

Else if disks[i] = 0

Print "l" (1)

End print_disks()

Start main ()

8 { (4) ← Initialize n, l, k, j
(2) ← Initialize m=0, temp=0
(1) ← Initialize array disks
(1) ← Read a number, n

(1) ← Set disks array of n = to new array of n*2

For i=0 to n

disks[2 * i] = 1 → (1)

disks[2 * i + 1] = 0 → (1)

(1) ← Print_disks() (6n+3)

For k=0 to n/2+1

For j=0 to n*2-1

3 + max(4,0) { if (disks[j] = 1) and (disks[j] != disks[j+1])
3+4=7 { temp = disks[j]; → (1)
disks[j] = disks[j+1] → (1)
disks[j+1] = temp → (1)
m++ → (1)

for q = n*2-1 to n-3

if (disks[q] = 1)

else if (disks[q] != 1) and (disks[q] != disks[q-1])

temp = disks[q] → (1)

disks[q] = disks[q-1] → (1)

disks[q-1] = temp → (1)

m++ → (1)

(1) ← print_disks() (6n+3)

(1) ← print number of swap, m

(1) ← delete array disks

Should be: $(n+4)(-4n-4) = -4n^2 - 16n - 4n - 16 = -4n^2 - 20n - 16$

$= \underline{8} + \underline{1} + \underline{(2n+2)} + \underline{11(6n+3)} + \underline{(7n^2+28n)} + \underline{(-4n^2-20n-16)} +$
 $\underline{1} + \underline{(6n+3)} + \underline{1} + \underline{1}$

$= 3n^2 + 22n + 5$

$= 3n^2 + 22n + 5 \in \Theta(n^2) = \lim_{n \rightarrow \infty} \frac{3n^2 + 22n + 5}{n^2} = \lim_{n \rightarrow \infty} \frac{3n^2}{n^2} = 3 \geq 0$

$$\sum_{i=0}^{2n} 3 = (2n-0+1)3 = 6n+3$$

$$\left. \begin{array}{l} 1 + \max(1,2) \\ 1+2=3 \end{array} \right\}$$

$$\left. \begin{array}{l} 1 + \max(0,1) \\ 1+1=2 \end{array} \right\}$$

$$\sum_{i=0}^n 2 = (n-0+1)2 = 2n+2$$

$$\sum_{k=0}^{\frac{n}{2}+1} \sum_{j=0}^{2n-1} 7 \Rightarrow (2n-1-0+1)7 = 14n$$

$$\sum_{k=0}^{\frac{n}{2}+1} 14n = \left(\frac{n}{2}+1-0+1\right)(14n)$$

$$\left(\frac{n}{2} + \frac{4}{2}\right)(14n) = \left(\frac{n+4}{2}\right)(14n)$$

$$7n^2 + 28n$$

$$\sum_{k=0}^{\frac{n}{2}+1} \sum_{q=2n-1}^{n-3} 8 \Rightarrow ((n-3)-(2n-1)+1)8$$

$$(n-3-2n+1+1)8 = (-n-1)8 = -8n-8$$

$$\sum_{k=0}^{\frac{n}{2}+1} -8n-8 \Rightarrow \left(\frac{n}{2}+1-0+1\right)(-8n-8)$$

$$\left(\frac{n+4}{2}\right)(-8n-8) = \left(\frac{n+4}{2}\right)(-2)(4n+4) = (-)(n+4)(4n+4)$$

$$(-)(4n^2-12n+16) = 4n^2+12n-16$$

CPSC 335-03 - Programming Assignment #1

The alternating disks problem: left-to-right algorithm

Enter the number of single color disks (light or dark)

4

Initial configuration

List of disks

d l d l d l d l

After moving darker ones to the right

List of disks

l l l l d d d d

Number of swaps is 10

Press any key to continue . . .

CPSC 335-x - Programming Assignment #1

The alternating disks problem: lawnmower algorithm

Enter the number of single color disks (light or dark)

3

Initial configuration

List of disks

d l d l d l

After moving darker ones to the right

List of disks

l l l d d d

Number of swaps is 6

Press any key to continue . . .