Ex: - Construct a DFA accepting all strings over {a/b} ending in ab.

Stop - per require two parsition for accepting the string ab. It

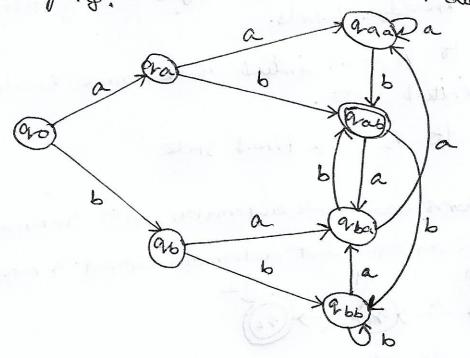
the symbol b is processed after an or ba, then also nee

end in ab. So, we can have states for lengthboring

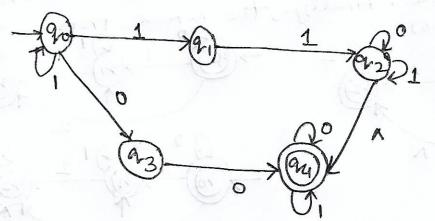
be final state in our DFA. Keeping these in mind, her

described by fio.

HS Densition diagram is



* N-MFA: Transition System for a Nondeterministic automator



* Conversion of A-NFA into NFA. It is Possible to

Convert a Densition System with 1 - moves into an Equiralent Transition 845ton veithout A-onores, see Shell give a simple method of doing it with the keep of an example

Suppose we want to seplace a n-move from vertex VI to voiting 12. Then we proceed as follows:

Step 1 find all the edges starting from 12

Step 2 Dupticate all trese edges starting form VI, without Changing the edge labels.

Steps: - It vi is as initial state, make v2 culso as Initial State.

Step 4! - 16 V2 is a final State

Example: Consider a finte centomator, with 1-noves, given in figure obtain on equivolent automator without A moves,



Sol" - her first-cleminate tre 1-more foroso goto 9, to set fig@, 9 is made an initial state. Then we eliminate the A move from no to 92 in fig @ to set fig (b). AS 92 in a final state, 90 is also made a final state. Finally, the some from anti- orz is Climinated in fig (b).

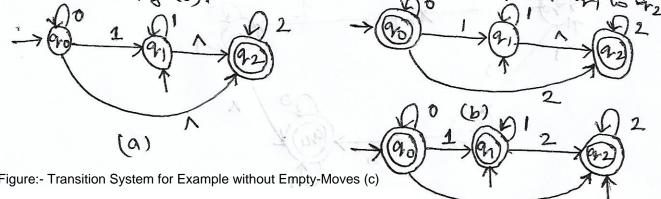


Figure:- Transition System for Example without Empty-Moves (c

Minimization of FINITE Automata: > Here, we construct
an automator with the number of states equivalent
to a given Automator H.

Definition: Two states q, and 22 are equivalent (denoted by (91=92) if bots S(21, x) and S(22, x) are final states, or bots of them are non final states for all. $x \in \mathbb{Z}^*$

As it is difficult to construct $S(\alpha_1, \kappa)$ and $S(\alpha_2, \kappa)$ for all $\kappa \in \mathbb{Z}^*$ (there are an infinite number of Ships in \mathbb{Z}^* , here one more definition.

Definition: > two states 9, and or are k-equivalent (K 7,0) if both S(9, x) and S(9, x) are final states or both room final states for all ships x of length Kor less. In lauticular, any two final states are o-equivalent and any two montional states are also o-equivalent.

We Mention some of the Properties of these Selections.

Property 1:- The Relations we have defined, i.e. equivalence and x-equivalence are equivalence Relations, i.e. They are Reflexive, symmetric and Transitive.

Property 2:- nel hone to pulitions of 9 in two disjoint class/set. These faulitions can be denoted by a and to, respectively. The elevents of the are K-equivalence classes.

Property 3:- It an and on are k-Equivalent for all K7,0, Then
trey are equivalent.

Property 4: - if 2, and 22 are (KH). equivalent, then trey are equivalent.

Property 5: - Th= Th+1 for some n. (The denotes The set of equivalence. classes under M. equivalence)

Construction of Minimum Antomation: >

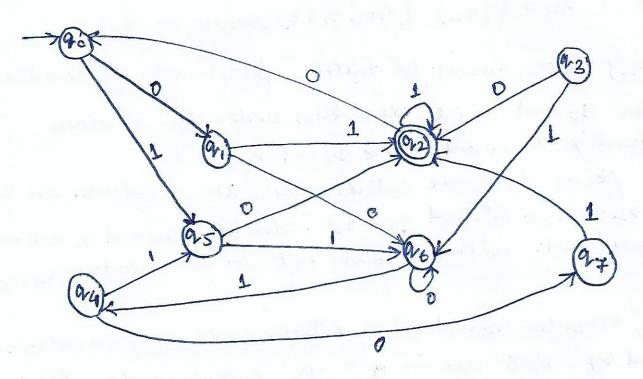
Step 1! (Construction of Xo). By definition of 0- equivalence, To = [0°, 02°] where Q° is The set of all final states and Q2° = Q-Q°.

Step 2! - (Consmetion of XK+1 from XK). Let & K be any susset in XK. if and or are in Dik, They are (K+1)-equivalent provided S(or, a) and 8(or, a) are K-equivalent. Find out wenther S(on)a) and d(or, a) are in the same equivalence dars in XK for every a E Z. It 80, 9, and or are (K+1)-equivalent. In this way, Dik is further devided into (K+1) - equivalence classes. Repeat this for every Dik in XK to Set all The elevents of XK+1.

Step3: + Consmut 2 for on=1,2, -- until To= 20+1.

Step 4: -> (Consmittion of missionum automaton), for the regions minimum state automaton, The states are the equivalence Clarks obtained in step 3. 1.e. The elements of typ. the state table is obtained by replacing a state or by the corresponding equivalence clars [ar].

Ex: - construct a minimum state automator equivalent to the finite automators described by fig



Fig! - Brite autonation

Solution: - It will be easier if we comment the parsition table as snown in this table

Table! - partition table for example / above DFA

State/E	Day of The Control of	1
->90	er,	95
91	ar 6	22
(an)	90	2-2
93	92	96
on	97	95
95	92	96
96	46	ay
az	26	92

By applying step 1, we set $Q_1^\circ = F = \{q_1\}, Q_2^\circ = Q_1^\circ$

The Enzy in To cannot be further fastitioned. so Oi= 2923.

Consider ground on Eq. The entires under the o-column corresponding to go and g, are g, and gro;

they lie in d2°. The entires under the 1-Column are 25 and 92. 926 & and 95 & 92°. Therefore, 90 and 91 are not 1-equivalent. Similarly, 90 is not 1- equivalent to 93,95 and 97.

Now, consider so and sy. The entires under the 0-column are on and st. Bots are in Q2. The entires wrelen the 1-column are are so, so. 80 sy and so are 1-equivalent. similarly soo is 1-equivalent to so. 5 so, say, so, in a subset in 2, 80,

Repeat The Construction by Considering a, and any one after states or 3, 95, 97. Now, or, is not 1-equivalent to 93 or as but 1-equivalent to 97.

Hence, d3'= [91,943. The elements left are in 02 are 93 and 95.

By consider the entires under the o-column and The 1-column, we see that any and as are 1-equivalent, 80 Q'y = 293,253. Therefore,

x= [{923, {90, 94, 963, 24, 473, {23, 25}}

The Jan j is also in 72 as it convot be further partitioned you , The extricts under the 0-column corresponding to go and my are of and 97, and trese lie in the same equivalence class in 2, The entries under the 1-column are 950 95.

So go and ry are 2 - equivalent. But go and go are not 2-equivalent. Hence, 200,94,963 is lastitized into [90,94] and 1963. On and 27 are 2-equivalent, 93 and 95 are also 2-equivalent. Thus x2= { {223, {90, 243, 2965, 29,9973, 293, 9533. 20 and ay one 3-equivalent. The 9, and 94 are 3- Equivalent. Also 93 and 95 are 3-equivalent. Theelfore,

不多= 11923. 500,943, 1963, 191,943, 123,95分 AS T2=T3, T2 dires us The equivalentel classes, The minimum state autometers is

M'= (Q', \(\gamma\), \(\gamma'\), \(\gamma'\

hebere

96]

Q= [[22], [20,94], [26], [21,27], [23,25]} 20' = [ao, ay], F'= [22]

and 3' is defined by table below State /5 [93,95] [a1,97] (900194) [92] [m] [n, 27] [92) [m/94] [92] [96] [22] [03,25] [90,94] [96]

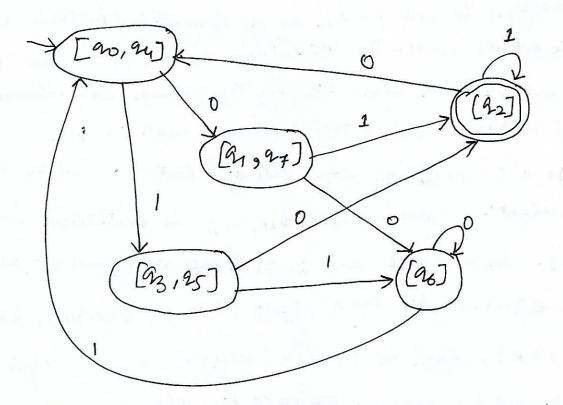


fig: - Minimum state autonator of Example.

EX! - Construct the minimum state automators equivalent to the Transition diagram given by fig.

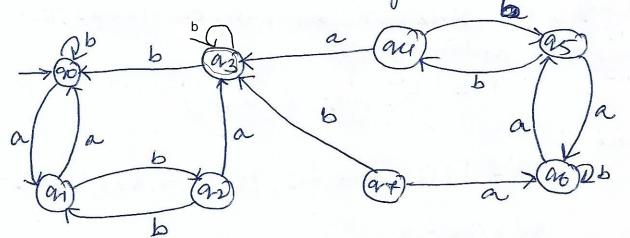


fig:-finte automators of Ex.

Sof? - nee Construct the Transition table as given by Followip Table.

Table: - Densition Table for Ex.

State/2	a	Ь
→90	21	90
an	90	92
92	93	21
(9-3)	arz	90
g _r y	ey3	95
25	016	94
96	as	96
97	96	93

Since There is only one final state 93, 01°= {95}, 02°=0-01°. Hence 12 = 2 {93}, 200, 91 392, 94, 95, 96, 9733. AS 2003 Convot be Partitioned further, 01°= 2923.

Now go is 1-equivalent to an, 95,96, but not to 92,84,90 and some so

Rence, Q's = {ag, qu}. The only element lemaining in Oz' is 27. Thorefore m' = {a7}. Thus,

90 is 2-equivalent to 26 but not to 21 or 25. 80,

022=590,863

As 9, in 2- equivalent to 25,

Q3= 191,953

As 22 in 2-equivalent to ory,

Q42 = 292,943, 052 = 1973

Thus,

T2= 72933, 200,063, 201 3953, (9294), (94)

0,3=[93]

AS goin 3-equivalent to 96,

023= 20,905

As 9 in 3-equivalent to 95

033= 991,953

As 92 in 3-equivaent to my,

043 = [92,94], 053 = 2973

Theeloe, 53= { [23]; 20,50}, 29,25}, 29,24}, [92,94], [94]

AS T3= T2, T2 gives us the equivalent classes, The minimum

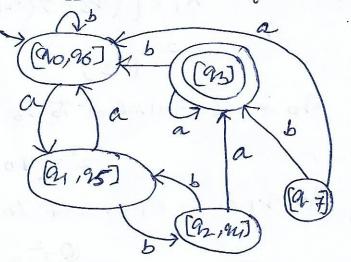
State automator is M'= (0', ja, b', 8', 90', F')

(where Q'= Z[a3], [90,96], [91,95], [92,94], [84]}

% = [90,96], F'=[93] and & indefined in table

State/E	a	b
[90,96]	[21,25]	[90,96]
[04,95]	[00,06]	[22,94]
[22/24]	[az]	[24,25]
[arz]	[c+3]	[90/86]
[at]	(90,96)	[az]
	 	

Fig: - pansition table of Minimum state Autonoton



Minimum state Automaton of Example