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Mealy and Moose Machine

* An Automaton in which the output depends only on The Import is called an automaton without a Memory. An

* Antomaton in venich The output depends on The states as well, is called authoration with a finite Memory.

* An automator in which The operful depends only on The states of the machine is called a Moore machine.

* An automatom in which The output depends on The state as well as on The 11P at any Instance of time is called a Mealy machine.

Meety machine: The value of the output function z(t) in The most general case is a function of the Present State q(t) and the present input x(t), i.e.

$z(t) = \lambda(2(t), x(t))$

model is usually called the mealy marine.

Moore machine: It The output function z(t) depends only on the present state and is independent of the Current input, The output hundrin oney be written as $Z(t) = \lambda(q(t))$

This sest hicked wooder is called the moose machine. It is more convenient to use moore nearline is automate theory.

Definations:

Moose Machine: -> A Moose madrice is a six taple

 $(Q, \Xi, \Delta, S, \lambda, 90)$, where

& is a finite set of states;

E is The lapant applaced

D is The output alphabet

S in The Transition function Exainto Q;

A is the output function mapping Quito D;

To jes the initial state.

Mealy machine !-A Mealy machine is a six type

(Q, E, D, S, 1, 20), wehere all The symbol except 1 Thank the same Meaning as in the Morse machine.

) is the output function majoring EXQ into D For Example, Table 1 describes a Moose machine. The initial State go is marked with an arrow. The table defines Sand). Table: - A Moose madire

Present state	Next 5	State 8	ontact
	9=0	a = 1	À
→ 90	93	21	0
9,	a	22	1
92	92	023	0
0/3	02	20	b

For The IMPLE String 0111, The pareition of states is given by go -> orz -> oro -> or, -> orz. The output string is 00010. For The Input string 1, The output is 1(90) 25.

Transition Table 2 describes a Healy machine. 3

A Mealy machine

Present state		Next	State	
	a	-0	And Markey	9=1
	state	ontput	State	output
<i>→</i> 91	23	0	92	0
92	a,	1	ny	0
9-3	or2		or	1
94	Orze	alone 1 1x 3	ar3	0

Note: -> for The Input String 0011, The Transition of states is given by $q_1 \rightarrow q_3 \rightarrow q_2 \rightarrow q_4 \rightarrow q_3$, and The output String is 0100.

In this case of a Mealy martine, we get an output only on the application of an what symbol. So For the light shing Λ , the output is only Λ . It may be observed that in the case of a moose martine, we get $\lambda(90)$ for the input string Λ .

- * For a Moose machine if The Input String is of length on, the output String is of length on+1. The first output is $\Lambda(90)$ for all output strings.
- * In The case at am early machine if The light string is of length on, The output string is also af the Same lengths.

* Procedure for Transforming A Mealy machine into a moose maeline ? >

we develop preedule for parstorning a realy machine isto a Moose machine and vice-rease so that for a given input Shing the output Strings we The Same (except for The first good) inabots The machines.

Example: - Consider the Healy Machine described by The trunsition table given by Pollaring table. Construct a Mouse machine which is equivalent to The Mealy machine

Present state		Mext state		J. T.	E.
A SEED OF THE	State	a=0	Input	t a=1	
-> a1	orz .	DO	9-2	0	-
02	21	1	94	0	
oz	92	- P. 1-7-1 - 3	ay	1	
ay	By	1 70 000	Az	0	\sim

Sol":- At The first stage we develop the procedule so trait both mactives accept exactly the same set of input sequences, he look into the rext state Column for any state, say ai, and determine the monder of deflerent outputs associated with ai in that Column.

in give that it for entering and a set of the

af Such states being equal to the number of different outputs associated with 9i. For Example, in this Problem, 9, in associated with one output I and 92 is associated with two different outputs of and 1. Significally, 973 and 974 are associated with the outputs of and 0, 1, sespectively. So, we split one into 920 and 971. Similarly, 974 is split into ergo and 941. Now table above.

Can be Recombinated for the rew states as given by followip table.

State table for Example:

Present State	<u>.</u>	Next 8	Hate	
	1 >	5 Put a =0	infact	9=1
of seconds a	State	output	State	output
-> 9 ₁	23	0	920	0
920	ap,	1	940	б
021	eri		940	0
93	921	Car make the	21	1
040	041	1	93	
941	241		or3	0

The Pair of states and ontents in the rest state Column Can be searranged as given by task following task.

Present State	Me	xt state	output
	9=0	a=1	when the state of the
->91	orz.	920	1
920	an	940	O
821	21	240	1
93	921	21	0
940	Sul	az	O
941	241	orz	1

table "above" gives the Moose machine. Here we observe that the initial State on is ansociated with I. This means that with what I have set an output of I, if The machine starts at stale on. Thus this machine accepts a zero length sequence (null sequence) which is not accepted by the Mealy machine.

response at a Moose machine to input A, or we must add a new string state 90, whose state parsitions are identical with those of 9, but nevose output is 0. So, table "above" is parsporred to table "below"

Present state	rest s	tate	(
	920	a = 1	output
→ 90	93	920	0
an an	93	920	1
920	n	240	0
921	21	340	1
23	021	orl	0
ayo	041	93	D
241	erns	nz	1 - 125 -

from the foregoing Proceedure it is clear that if ree have an in-output, on- State marly machine, the Corresponding on-output moore markine has no more them man +1 states.

Proceedings for transforming a Mealy marriage into a Moode marriage into a Moode marriage into a marriage into a

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Procedure for Dansproning a Moose Machine into a Mealy

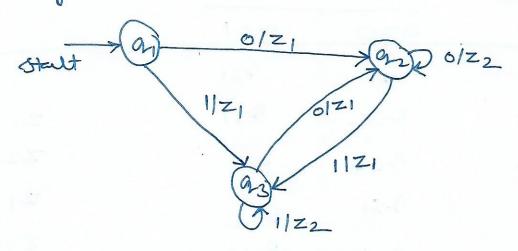
Gre modify the acceptability of Input String by a Moore machine by reglecting the lesponse of the moore machine to input n. Lee thus define that Mealy machine M and Moore Machine M' are equivalent if for all input strings w, bZM(w) = ZM'(w), before b is the art put of the Moore machine for its initial state. He give the following herult: let M= (B, E, D, 8, p), 90) be a Moore machine. Then The following Procedure may be adopted to Consmut an equivalent Mealy machine M2.

Construction: — (i) we have to define the output function i' for the Mealy machine as a function of the present state and the Imput symbol. we define it by

1'(9,a)= >(&(9,a)) For all states gand

(ii) The pansition function is the same as that all

Example? — Consider a Mealy machine represented by Fig. Construct a Moose machine equivalent to This Mealy machine.



Mealy madrice of Ex. Sol? - Let us convert pensition diagram into pensition taske Danstion taske to Ex.

Present state		plext stat	te .	
	920		Q=	
	State	ontput	Stale	output
->91	orz	2	ans a	21
92	92	Z	23	Z
93	92	7	93	Z 2

for the given problem: or, is not associated with city output; or in associated with two different authors zy and zz; org is associated with two different states outputs zy and zz. Thus we must split or into organd organists. Outputs zy and zz, sespectively and organish zy and zz, sespectively.

Following table Shows The Transition of Mosse machine For Example.

reart	stale	1 27 1 2007	output
a=0	0=1		
921	931	fr.	
922	931		21
922	931		22
921	233		21
221	2-32		22
	a=0 921 922 922 921	921 931 922 931 921 932	a=0 $a=1$ $a=0$ $a=1$ $a=1$ $a=1$ $a=2$ $a=3$ $a=2$ $a=3$

figure gives The Transition diagrams of The lequised moose machine

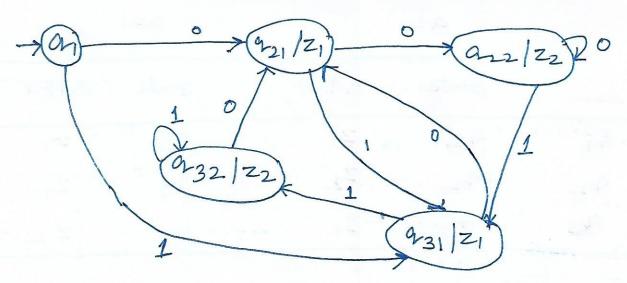


fig: - Moose Machine of Ex.

Ex: - Construct a Mealy Machine which is equirelent to the Moose machine given by table ziren below

Present State	M	ext state	ontput
	9=0	a=1	
→90	orz	91	0
9,	27	92	me day mitie
92	92	9-3	Laste of the cores
ind": - hee muss	93	20	D

sol?: - he must follow The leverse Procedure of converting a mealy meetine into a moose machine. In The Case of the Moose machine, for every 11P symbol we form the Pair Consisting of the Lext state and the corresponding output and reconstruct the table for the Mealy Machine.

For Example, the state or and or, in the next state Column should be associated with ontput o and 1, sexutively The Transition table for the Mealy machine is

Present		Next state	and the state	
State	a	20 0	0	1=1
1	State	ontput	State	ontput
-> 90	or3	0	Qr.	
91	81	7 34 5216	92	21 3/1-3/1-
92	a-2	0	93	0
ar3	93	0	go	0

Note: - her can beduce the number of states in any onodel by worsidering states with Identical parintions. it Two states have identical Transitions (ie the souls Corresponding to trese two states are Identical), then we can delete one of Them.

Example: - Consider the Moose Machine described by the parsition table Firen by table "belod" construct The Coresponding Mealy machine.

sesent state	ple	XX State	ontput
	a=0	a =1	
→ 9 ₁	ar 1	92	0
9-2	a,	23	0
23	91	23	

Solution: > Le construct Tre Transition table as in in follois
table by association the output with The parsitions. In table below, The sous consponding to 92 and 93 are Identical. So nee can delete one af The Two states, i.e or or or 3. we delete or 3.

Presentotate		plent s	tate	. We de
	9=		a=	-1
	State	ortput	eact.	ortput
-s ori	or 1	0	an.	0.444
a ₂	91	OATO	23	1
45			013	1

The table rext to it; gives The seconsmitted table.

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Present State	reext state			
	9:0		a=1	
	State	ontput	State	ontput
->91	21	O	92	0
92	21	0	22	1

in the above table, we have deleted the 93- sow and le-