

① Find the conductivity and resistivity of an intrinsic semiconductor at temperature of  $300^\circ\text{K}$ . It is given that

$$n_i = 2.5 \times 10^{13} / \text{cm}^3$$

$$\mu_n = 3800 \text{ cm}^2/\text{V}\cdot\text{s}$$

$$\mu_p = 1800 \text{ cm}^2/\text{V}\cdot\text{s}$$

$$q = 1.6 \times 10^{-19} \text{ C}$$

sol<sup>n</sup>

$$\sigma_i = n_i e (\mu_e + \mu_h)$$

$$= 2.5 \times 10^{13} \times 1.6 \times 10^{-19} (3800 + 1800)$$

$$= 0.0224 \text{ S/cm.}$$

intrinsic resistivity

$$\rho_i = \frac{1}{\sigma_i} = \frac{1}{0.0224} = 44.64 \text{ } \Omega\text{-cm.}$$

② The intrinsic resistivity of germanium at  $300^\circ\text{K}$  is  $0.47 \Omega\text{-m}$ . The electron mobility at  $300^\circ\text{K}$  in germanium is  $0.39 \text{ m}^2/\text{V}\cdot\text{s}$ . The hole mobility  $\mu_h$  at  $300^\circ\text{K}$  in germanium is  $0.19 \text{ m}^2/\text{V}\cdot\text{s}$ . ~~The data~~ Calculate the density of electrons in the intrinsic material. Also calculate the drift velocity of holes and electrons for an electric field ( $E = 10^4 \text{ V/m}$ ).

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$$\text{intrinsic resistivity } (\rho_i) = 0.47 \Omega\text{-m}$$

$$\text{intrinsic conductivity } (\sigma_i) = \frac{1}{\rho_i}$$

$$= \frac{1}{0.47} = 2.12766 \text{ S/m}$$

$$\mu_e = 0.39 \text{ m}^2/\text{V}\cdot\text{s}$$

$$\mu_h = 0.19 \text{ m}^2/\text{V}\cdot\text{s}$$

$$e = 1.6 \times 10^{-19} \text{ C}$$

$$\sigma_i = n_i e (\mu_e + \mu_h)$$

$$n_i = \frac{\sigma_i}{e (\mu_e + \mu_h)}$$

$$= \frac{2.12766}{1.6 \times 10^{-19} (0.39 + 0.19)}$$

$$\boxed{n_i = 2.293 \times 10^{19} / \text{m}^3} \text{ ANS}$$

$$E = 10^4 \text{ V/m}$$

$$v_n = \mu_e E = 0.39 \times 10^4$$

$$\boxed{v_n = 3900 \text{ m/s}} \text{ ANS}$$

~~$$v_n = 0.39 \times 10^4$$~~

$$v_h = \mu_h E = 0.19 \times 10^4$$

$$\boxed{v_h = 1900 \text{ m/s}} \text{ ANS}$$

③ The intrinsic carrier concentration for silicon at room temp. is  $1.5 \times 10^{10} / \text{cm}^3$ . If the mobility of electrons and holes are  $1300 \text{ cm}^2/\text{V-s}$  and  $450 \text{ cm}^2/\text{V-s}$  respectively. What is the conductivity of silicon (intrinsic) at  $300^\circ\text{K}$ ? If silicon is doped with  $10^{18}$  boron atoms per cc, what is its conductivity.

$$\begin{aligned} n_i &= 1.5 \times 10^{10} / \text{cm}^3 \\ \mu_h &= 450 \text{ cm}^2/\text{V-s} \\ \mu_e &= 1300 \text{ cm}^2/\text{V-s} \\ \sigma_i &= n_i e (\mu_e + \mu_h) \\ &= 1.5 \times 10^{10} \times 1.6 \times 10^{-19} (1300 + 450) \\ \sigma_i &= 4.2 \times 10^{-6} \text{ S/cm.} \quad \text{Ans.} \end{aligned}$$

After Doping

$$\begin{aligned} N_A &= 10^{18} / \text{cm}^3 \\ \sigma_p &= N_A e \mu_h \\ &= 10^{18} \times 1.6 \times 10^{-19} \times 450 \\ \sigma_p &= 72 \text{ S/cm.} \quad \text{Ans.} \end{aligned}$$

④ Find the conductivity of intrinsic germanium at  $300^\circ\text{K}$ . If donor type impurity is added to the extent of 1 impurity atom in  $10^7$  germanium atoms, find the conductivity. Given that

$$\begin{aligned} n_i &= 2.5 \times 10^{13} / \text{cm}^3 \\ \mu_h &= 1800 \text{ cm}^2/\text{V-s} \\ \mu_e &= 3800 \text{ cm}^2/\text{V-s} \\ \text{Concentration of Ge atoms} &= 4.41 \times 10^{22} / \text{cm}^3 \end{aligned}$$

$$\begin{aligned} \sigma_p &= n_i e (\mu_e + \mu_h) \\ &= 2.5 \times 10^{13} \times 1.6 \times 10^{-19} (3800 + 1800) \\ \sigma_p &= 0.0224 \text{ S/cm.} \quad \text{Ans.} \end{aligned}$$

$$\text{No. of Ge atoms/cm}^3 = 4.41 \times 10^{22} / \text{cm}^3$$

$$N_D = \frac{4.41 \times 10^{22}}{10^7} = 4.41 \times 10^{15} / \text{cm}^3$$

Concentration of electrons.

$$n \approx N_D = 4.41 \times 10^{15} / \text{cm}^3$$

$$p = \frac{n_i^2}{N_D} = \frac{(2.5 \times 10^{13})^2}{4.41 \times 10^{15}}$$

$$p = 1.417 \times 10^{11} / \text{cm}^3$$

$$\sigma_e = e N_D \mu_e$$

$$= 1.6 \times 10^{-19} \times 4.41 \times 10^{15} \times 3800$$

$$\sigma_e = 2.68 \text{ S/cm.} \quad \text{Ans.}$$

(5)

A pd (Potential difference) of 10V is applied longitudinally to a rectangular specimen of intrinsic Ge of length 25 mm, width 4 mm and thickness 1.5 mm. Determine at room temp.

- (i) electron and hole drift velocities -  
 (ii) the conductivity of intrinsic germanium if intrinsic carrier density is  $2.5 \times 10^{19} / \text{m}^3$

(iii) Total current.

Given:  $\mu_e = 0.38 \text{ m}^2/\text{Vs}$ ,  $\mu_h = 0.18 \text{ m}^2/\text{Vs}$

Sol (i)  $E = V/l = \frac{10}{0.025}$   
 $= 400 \text{ V/m}$

$$v_e = \mu_e \times E = 0.38 \times 400$$

$$\boxed{v_e = 152 \text{ m/s}} \quad \text{Ans}$$

$$v_h = \mu_h \times E = 0.18 \times 400$$

$$\boxed{v_h = 72 \text{ m/s}} \quad \text{Ans}$$

(ii)  $\sigma_i = n_i e (\mu_e + \mu_h)$

$$= 2.5 \times 10^{19} \times 1.6 \times 10^{-19} (0.38 + 0.18)$$

$$\boxed{\sigma_i = 2.24 \text{ S/m}} \quad \text{Ans}$$

(iii)  $I = \sigma_i E a$

$$= 2.24 \times 400 \times 4 \times 10^{-3} \times 1.5 \times 10^{-3}$$

$$\boxed{I = 5.376 \text{ mA}} \quad \text{Ans}$$



Tutorial - 1

- ① In a certain copper conductor, the current density is  $2.4 \text{ A/mm}^2$  and electron density is  $5 \times 10^{28}$  free electrons per  $\text{m}^3$  of the copper. Determine the drift velocity of the electrons.

Sol<sup>n</sup>

$$J = 2.4 \text{ A/mm}^2 = 2.4 \times 10^6 \text{ A/m}^2$$

$$n = 5 \times 10^{28}$$

$$(\text{charge on electron}) q = 1.6 \times 10^{-19} \text{ C}$$

$$J = n q v$$

$$v = \frac{J}{nq} = \frac{2.4 \times 10^6}{1.6 \times 10^{-19} \times 5 \times 10^{28}} = 0.3 \times 10^{-3} \text{ m/s} \quad \underline{\text{Ans}}$$

- ② A conductor material has a free electron density of  $10^{24}$  electrons per  $\text{m}^3$ . When a voltage is applied, a constant drift velocity of  $1.5 \times 10^{-2} \text{ m/s}$  is attained by the electron. If the cross-sectional area of the material is  $1 \text{ cm}^2$  calculate the magnitude of current. ~~charge~~

Sol<sup>n</sup>

$$n = 10^{24}$$

$$q = 1.6 \times 10^{-19} \text{ C}$$

$$v = 1.5 \times 10^{-2} \text{ m/s} = 0.015 \text{ m/s}$$

$$a = 1 \text{ cm}^2 = 1 \times 10^{-4} \text{ m}^2$$

$$\dots \text{magnitude of } (I) = q n v a = 1.6 \times 10^{-19} \times 10^{24} \times 0.015 \times 1 \times 10^{-4}$$

$$= 0.24 \text{ A} \quad \underline{\text{Ans}}$$

$$J = n q v = n e v$$

$$I = n e v A$$

$$\begin{aligned} I &= \frac{N q v}{L A} \\ I &= n q v \\ J &= \sigma E \\ &= \sigma E a \\ &= n q v a \end{aligned}$$

$$n q \mu E$$

- ③. A specimen of germanium at  $300^{\circ}\text{K}$  for which the density of carriers is  $2.5 \times 10^{13}$  per  $\text{cm}^3$ , is doped with impurity atoms such that there is one impurity atom for  $10^6$  germanium atoms. All the impurity atoms may be assumed ionized. The conductivity of doped material is  $25.64 \text{ S/cm}$ . Carrier mobility for germanium at  $300^{\circ}\text{K}$  is  $3600 \text{ cm}^2/\text{V-s}$ . For the doped material, find the electron and hole density.

Sol<sup>n</sup>

$$\sigma = 25.64 \text{ S/cm}$$

$$\text{charge on electron } (q) = 1.602 \times 10^{-19} \text{ C.}$$

$$\text{mobility } \mu_e = 3600 \text{ cm}^2/\text{V-s}$$

$$\sigma_n = nq\mu_e = N_D q \mu_e \quad \text{--- ①}$$

$$N_D = \frac{\sigma_n}{q\mu_e} = \frac{25.64}{1.602 \times 10^{-19} \times 3600}$$

$$= 4.45 \times 10^{16} / \text{cm}^3$$

(i) Concentration of electron  $n \approx N_D = 4.45 \times 10^{16} / \text{cm}^3$

(ii) Concentration of hole,  $p = \frac{n_i^2}{n} = \frac{(2.5 \times 10^{13})^2}{4.45 \times 10^{16}}$

$$= 1.4 \times 10^{10} / \text{cm}^3$$

Ans



④ A donor type impurity is added to the extent of 1 atom per  $10^6$  atoms of an intrinsic semiconductor (Silicon). Calculate

- (i) Resulting donor atom concentration
- (ii) Resulting mobile electron concentration
- (iii) Resulting hole concentration.
- (iv) Conductivity of doped silicon sample.
- (v) If silicon bar is 0.5 cm long, cross-section area of  $(50 \times 10^{-4})^2 \text{ cm}^2$ . Find its resistivity.

Concentration of silicon atoms =  $5 \times 10^{22} \text{ cm}^{-3}$

and  $n_i = 1.45 \times 10^{10} \text{ cm}^{-3}$   
and silicon  $\mu_e = 1300 \text{ cm}^2/\text{V-s}$

Sol<sup>n</sup>

(i)  $N_D = (\text{no. of silicon atom } \text{cm}^{-3}) \times (\text{donor impurity})$

$$= 5 \times 10^{22} \times \frac{1}{10^6} = 5 \times 10^{16} / \text{cm}^3 \quad \underline{\text{ANS}}$$

(ii) Mobile electron concentration  $n \approx N_D = 5 \times 10^{16} / \text{cm}^3 \quad \underline{\text{ANS}}$

(iii) Hole concentration  $p = \frac{n_i^2}{N_D} = \frac{(1.45 \times 10^{10})^2}{5 \times 10^{16}} = 4.205 \times 10^3 \text{ per cm}^3 \quad \underline{\text{ANS}}$

(iv) Conductivity of doped silicon

$$\sigma = nq\mu_e = 5 \times 10^{16} \times 1.602 \times 10^{-19} \times 1300 = 10.413 \text{ S/cm} \quad \underline{\text{ANS}}$$

(v) Resistivity  $\rho = \frac{1}{\sigma} = \frac{1}{10.413} = 0.096 \text{ } \Omega \cdot \text{cm}.$

Resistance of given semiconductor

$$R = \frac{\rho l}{a} = \frac{0.096 \times 0.5}{(50 \times 10^{-4})^2} = 1920 \text{ } \Omega \quad \underline{\text{ANS}}$$