# Xylophone Project

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#### Abstract

This document describes the building of an electromechanical xylophone. Copper  $\,$ 

# 1 Introduction

## 2 Pipes

#### 2.1 Materials

We use copper pipes as vibrating elements. The main reasons being copper is simple to work with, easily found in local stores and cheap.





#### 2.2 Computing pipe length

The length depends on 3 factors:

- the required frequency,
- the vibrating element shape,
- the sound propagation speed in the medium.

According to [wiki\_acous\_reson], the formula for a cylinder is:

$$f = \frac{nv}{2(l+0.8d)}$$

where:

- f the frequency in hz,
- n an integer (1, 2, 3 ...),
- v the speed of sound in medium in  $ms^{-1}$ ,
- l the length in mm,
- d the cylinder diameter in mm.

However, we found an apparently better formula in [tamhigh\_xylo] which accounts for the pipe radius of gyration. The nth transveral frequency is given by:

$$f_n = \frac{\pi vk}{8l^2} m^2$$

where:

- $f_n$  the frequency in hz,
- v the speed of sound in medium in  $ms^{-1}$ ,
- k the gyration of radius,
- l the length in mm,
- $\bullet$  m a value such that:
  - -m = 3.0112 when n = 1,
  - m = 5 when n = 2,
  - m = 7 when n = 3,
  - -m = 2(n+1) otherwise.

For a cylinder, the gyration of radius is:

$$k = \frac{1}{2}\sqrt{i^2 + o^2}$$

where:

- i the inner diameter in mm,
- o the outter diameter in mm.

The copper sound propagation speed is:

$$3700ms^{-1}$$

Since we want the whole device small, we keep the pipe as short as possible. However, we want to build it using relatively inaccurate drilling and cutting tools. Thus, we ended up choosing the 8th frequency mode, which results in the folloing table:

frequency (hz)	length (mm)	first node (mm)	second node (mm)
2093.000000	0.141960	0.031799	0.110161
2349.313067	0.133993	0.030014	0.103978
2637.014757	0.126472	0.028330	0.098142
2793.819815	0.122872	0.027523	0.095349
3135.956712	0.115976	0.025979	0.089997
3519.992394	0.109466	0.024520	0.084946
3951.057873	0.103322	0.023144	0.080178
4186.010000	0.100381	0.022485	0.077896

### 2.3 Cutting the pipes

The easiest and most accurate way to cut the pipe is by using a pipe cutter:



pipe cutter

We found experimentally that we must add roughly 1.5mm to the previously computed length. This is due to the transversal holes and the vibration effects when the pipe is finally mounted. By the way, it is always better to have a longuer pipe, since we can reduce it with a lime for tuning until it reaches the correct frequency.

## 3 Assembling

### 3.1 Drilling the base

Drill the pipe transversal holes before drilling the base holes. Once this is done, mark the base to prepare the drilling. It helps correcting small errors made while percing he pipe holes.

## 3.2 Mounting the pipes





# 4 Bill of materials

reference	reseller	description	quantity	price (euros)
copper pipe				

## 5 References

- $\bullet \ \ wiki\_acous\_reson: \ http://en.wikipedia.org/wiki/Acoustic\_resonance$
- $\bullet \ tamhigh\_xylo: \ staff.tamhigh.org/lapp/xylophone.pdf \\$