

	MODULE <i>Helper</i>	
<p>EXTENDS <i>Naturals, TLC</i></p> <p>VARIABLES <i>pick</i></p> <p>$Range(T) \triangleq \{\langle T[x], x \rangle : x \in \text{DOMAIN } T\}$</p> <p>$Pick(S) \triangleq \text{CHOOSE } s \in S : \text{TRUE}$</p> <p>RECURSIVE $SetReduce(-, -, -)$</p> <p>$SetReduce(Op(-, -), S, value) \triangleq$</p> <p style="padding-left: 20px;">IF $S = \{\}$ THEN $value$</p> <p style="padding-left: 20px;">ELSE LET $s \triangleq Pick(S)$</p> <p style="padding-left: 40px;">IN</p> <p style="padding-left: 40px;">IF $Op(s[1], value) = Op(value, s[1])$</p> <p style="padding-left: 60px;">THEN $SetReduce(Op, S \setminus \{s\}, Op(s[1], value))$</p> <p style="padding-left: 60px;">ELSE $Assert(\text{FALSE}, \text{"error"})$</p> <p>$Sum(S) \triangleq \text{LET } _op(a, b) \triangleq a + b$</p> <p style="padding-left: 20px;">IN $SetReduce(_op, S, 0)$</p>		