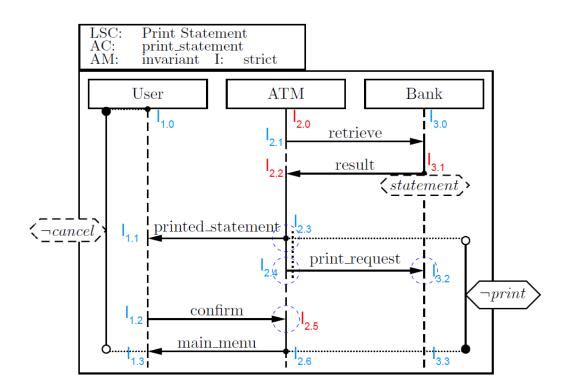
Solutions for Excercise sheet 4

Exercise 1 – LCS Syntax and Semantics

(i) LCS:



- a) $\mathcal{L} = \{l_{1.0}, l_{1.1}, l_{1.2}, l_{1.3}, l_{2.0}, l_{2.1}, l_{2.2}, l_{2.3}, l_{2.4}, l_{2.5}, l_{2.6}, l_{3.0}, l_{3.1}, l_{3.2}, l_{3.3}\}$
- b) $\mathcal{I} = \{\{l_{1.0}, l_{1.1}, l_{1.2}, l_{1.3}\}, \{l_{2.0}, l_{2.1}, l_{2.2}, l_{2.3}, l_{2.4}, l_{2.5}, l_{2.6}\}, \{l_{3.0}, l_{3.1}, l_{3.2}, l_{3.3}\}\}$
- c) $l_{2.4} \sim l_{3.3}, l_{2.3} \leq l_{2.5}, l_{2.4} \leq l_{2.5}$
- d) Msg: $\{(l_{2.1}, retrieve, l_{3.1})\}$
- e) Inv: $\{l_{1.0}, \bullet, \neg cancel, l_{1.3}, \circ\}$
- f) Cond: $\{(\{l_{3,2}\}, statement)\}$

```
(ii) c_1 = \{l_{1.0}, l_{2.0}, l_{3.0}\}

c_2 = c_1 \cup \{l_{2.1}, l_{3.1}\}

c_3 = c_2 \cup \{l_{2.2}, l_{3.2}\}

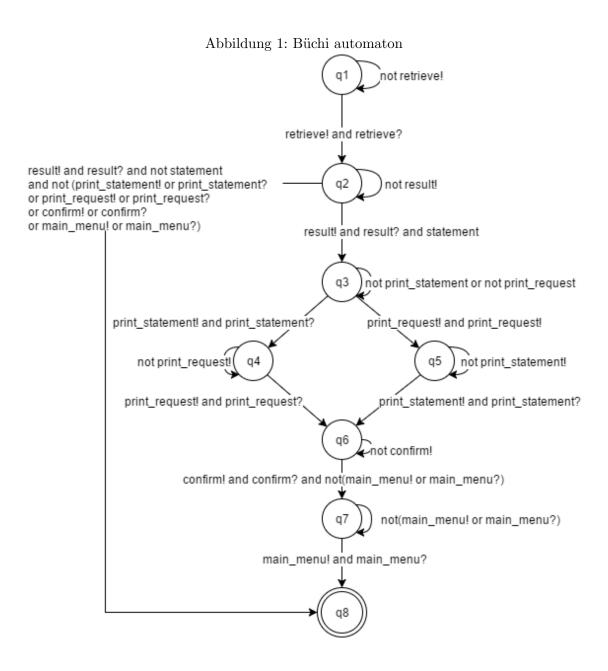
c_4 = c_3 \cup \{l_{2.3}, l_{1.1}\}

c_5 = c_3 \cup \{l_{2.4}, l_{3.3}\}

c_6 = c_3 \cup \{l_{2.3}, l_{1.1}, l_{2.4}, l_{3.3}\}

c_7 = c_6 \cup \{l_{1.2}, l_{2.5}\}

c_8 = c_7 \cup \{l_{2.6}, l_{1.3}\}
```

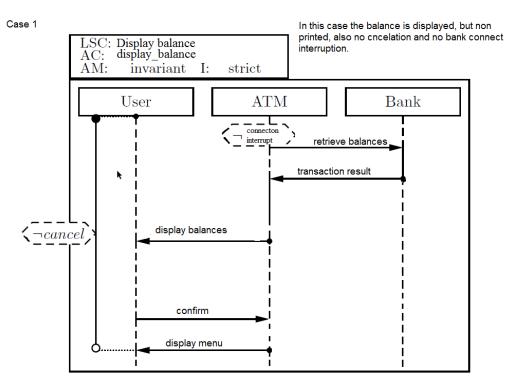


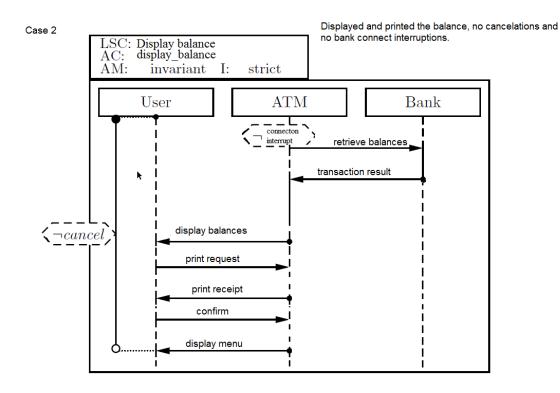
Seite 2

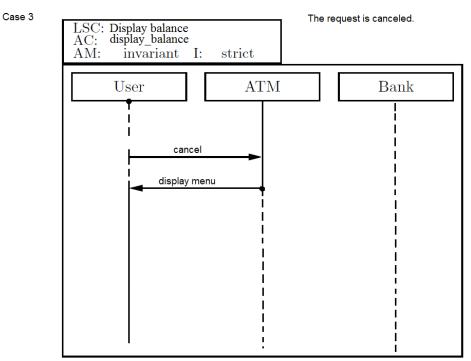
(iii) Strictness conditions omitted for readability.

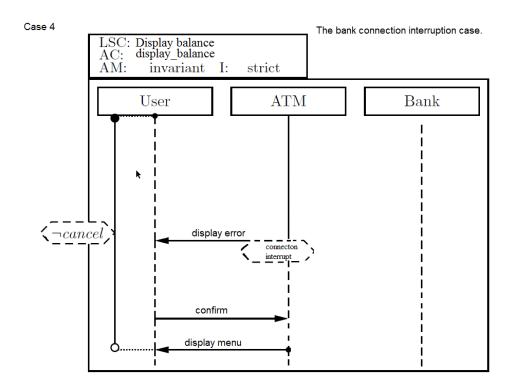
- a) $\pi_{accept} = c_1 \xrightarrow{retrieve! \land retrieve?} c_2 \xrightarrow{result! \land result? \land statement} c_3 \xrightarrow{print-request! \land print-request?} c_6 \xrightarrow{confirm! \land confirm?} c_7 \xrightarrow{main-menu! \land main-menu?} c_8$
- b) $\pi_{exit} = c_1 \xrightarrow{retrieve! \land retrieve?} c_2 \xrightarrow{result! \land result? \land \neg statement} c_8$
- c) $\pi_{violate} = c_1 \xrightarrow{retrieve! \land retrieve?} c_2 \xrightarrow{result! \land result? \land statement} c_3 \xrightarrow{print-request! \land print-request? \land print} illegal$

Exercise 2









Exercise 3

```
 \begin{split} & \text{i} \ \mathscr{S} = \{\mathscr{T}, \mathscr{C}, V, atr, F, mth\} \text{ mit} \\ & \mathscr{T} = \{int\} \\ & \mathscr{C} = \{TreeNode, Object\} \\ & V = \{key: int, leftChild: TreeNode, rightChild: TreeNode, parent: TreeNode, value: Object\} \\ & atr = \{TreeNode \mapsto \{key, leftChild, rightChild, parent, value\}, Object \mapsto \emptyset\} \\ & F = \{\emptyset\} \\ & mth = \{TreeNode \mapsto \emptyset, Object \mapsto \emptyset\} \end{aligned}
```

