

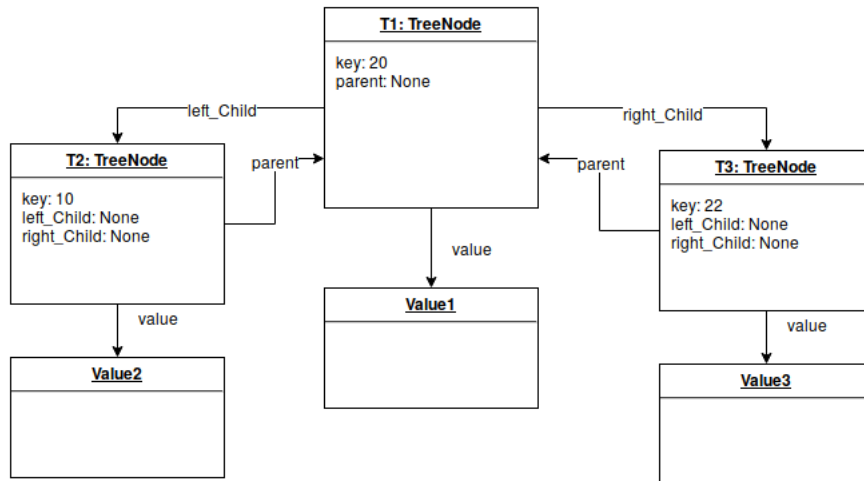
Solutions for Exercise sheet 2

Exercise 1 – OCL

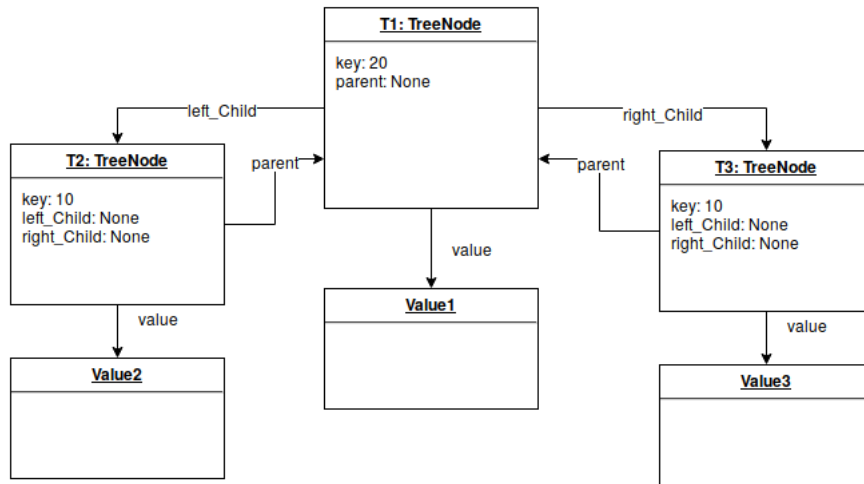
i $\mathcal{S} = (\{Int\}, \{TreeNode, Object\}, \{key : Int, left_Child : TreeNode, right_Child : TreeNode, parent : TreeNode, value : Object\}, \{TreeNode \mapsto \{key, left_Child, right_Child, parent\}, \{Object \mapsto \{key, left_Child, right_Child, parent\}\}, \{\}, \{TreeNode \mapsto \emptyset, Object \mapsto \{\}\})$
 $\mathcal{D}(Int) = \mathbb{Z}, \mathcal{D}(TreeNode) = \{T1, T2, T3, \dots\}, \mathcal{D}(Object) = \{O1, O2, O3, \dots\}$

a)

$\sigma_1 = \{T_1 \mapsto \{key \mapsto 20, left_Child \mapsto \{T_2\}, right_Child \mapsto \{T_3\}, parent \mapsto \emptyset, value \mapsto O_1\}$
 $T_2 \mapsto \{key \mapsto 10, left_Child \mapsto \emptyset, right_Child \mapsto \emptyset, parent \mapsto \{T_1\}, value \mapsto O_2\}$
 $T_3 \mapsto \{key \mapsto 20, left_Child \mapsto \emptyset, right_Child \mapsto \emptyset, parent \mapsto \{T_1\}, value \mapsto O_3\}$
 $O_1 \mapsto \{\}$
 $O_2 \mapsto \{\}$
 $O_3 \mapsto \{\}$
 $\}$



The system state σ_1 evaluates to true because $key(left_Child(T_1)) \leq key(T_1) \leq key(right_Child(T_1))$

$$\begin{aligned}\sigma_2 = & \{T_1 \mapsto \{key \mapsto 20, left_Child \mapsto \{T_2\}, right_Child \mapsto \{T_3\}, parent \mapsto \emptyset, value \mapsto O_1\} \\ & T_2 \mapsto \{key \mapsto 10, left_Child \mapsto \emptyset, right_Child \mapsto \emptyset, parent \mapsto \{T_1\}, value \mapsto O_2\} \\ & T_3 \mapsto \{key \mapsto 10, left_Child \mapsto \emptyset, right_Child \mapsto \emptyset, parent \mapsto \{T_1\}, value \mapsto O_3\} \\ & O_1 \mapsto \{\} \\ & O_2 \mapsto \{\} \\ & O_3 \mapsto \{\} \\ & \}\end{aligned}$$


The system state σ_2 evaluates to false because
 $key(left_Child(T_1)) < key(right_Child(T_1)) = key(T_1)$

$$\sigma_3 = \{\}$$

The system state σ_3 evaluates to \perp because there are no Instances of `TreeNode` and the formula can not be evaluated to true or false.