

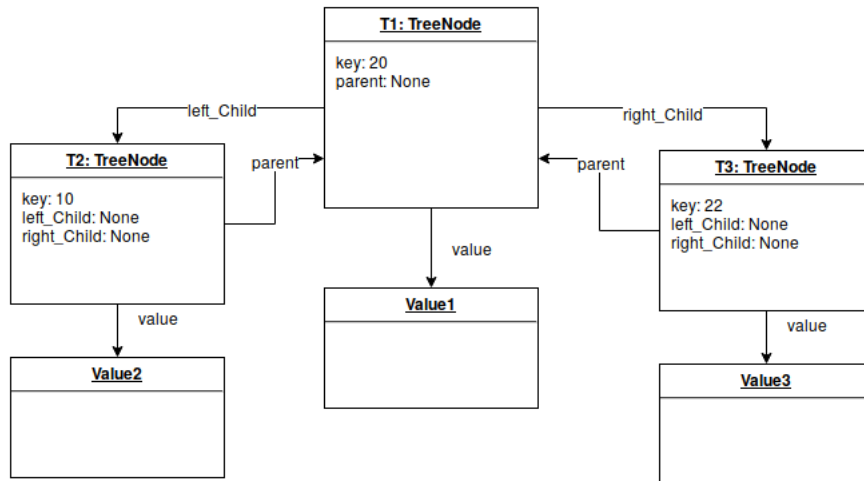
## Solutions for Exercise sheet 2

### Exercise 1 – OCL

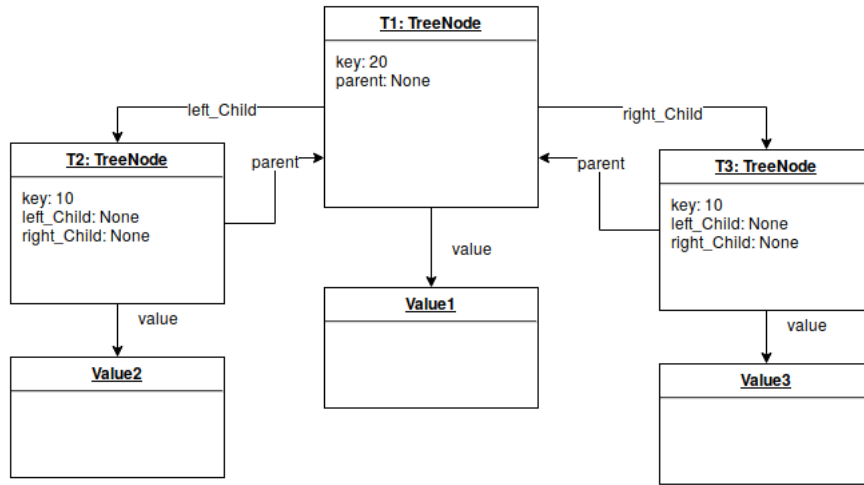
i  $\mathcal{S} = (\{Int\}, TreeNode, Object, \{key : Int, left\_Child : TreeNode, right\_Child : TreeNode, parent : TreeNode, value : Object\}, \{TreeNode \mapsto \{key, left\_Child, right\_Child, parent, value\}, \{\}, \{TreeNode \mapsto \emptyset, Object \mapsto \{\}\})$   
 $\mathcal{D}(Int) = Z, \mathcal{D}(TreeNode) = \{T1, T2, T3, \dots\}, \mathcal{D}(Object) = \{O1, O2, O3, \dots\}$

a)

$\sigma_1 = \{T_1 \mapsto \{key \mapsto 20, left\_Child \mapsto \{T_2\}, right\_Child \mapsto \{T_3\}, parent \mapsto \emptyset, value \mapsto O_1\}$   
 $T_2 \mapsto \{key \mapsto 10, left\_Child \mapsto \emptyset, right\_Child \mapsto \emptyset, parent \mapsto \{T_1\}, value \mapsto O_2\}$   
 $T_3 \mapsto \{key \mapsto 20, left\_Child \mapsto \emptyset, right\_Child \mapsto \emptyset, parent \mapsto \{T_1\}, value \mapsto O_3\}$   
 $O_1 \mapsto \{\}$   
 $O_2 \mapsto \{\}$   
 $O_3 \mapsto \{\}$   
 $\}$



The system state  $\sigma_1$  evaluates to true because  $key(left\_Child(T_1)) \leq key(T_1) \leq key(right\_Child(T_1))$

$$\begin{aligned}\sigma_2 = & \{T_1 \mapsto \{key \mapsto 20, left\_Child \mapsto \{T_2\}, right\_Child \mapsto \{T_3\}, parent \mapsto \emptyset, value \mapsto O_1\} \\ & T_2 \mapsto \{key \mapsto 10, left\_Child \mapsto \emptyset, right\_Child \mapsto \emptyset, parent \mapsto \{T_1\}, value \mapsto O_2\} \\ & T_3 \mapsto \{key \mapsto 10, left\_Child \mapsto \emptyset, right\_Child \mapsto \emptyset, parent \mapsto \{T_1\}, value \mapsto O_3\} \\ & O_1 \mapsto \{\} \\ & O_2 \mapsto \{\} \\ & O_3 \mapsto \{\} \\ & \}\end{aligned}$$


The system state  $\sigma_2$  evaluates to false because  
 $key(left\_Child(T_1)) < key(right\_Child(T_1)) = key(T_1)$

$$\sigma_3 = \{\}$$

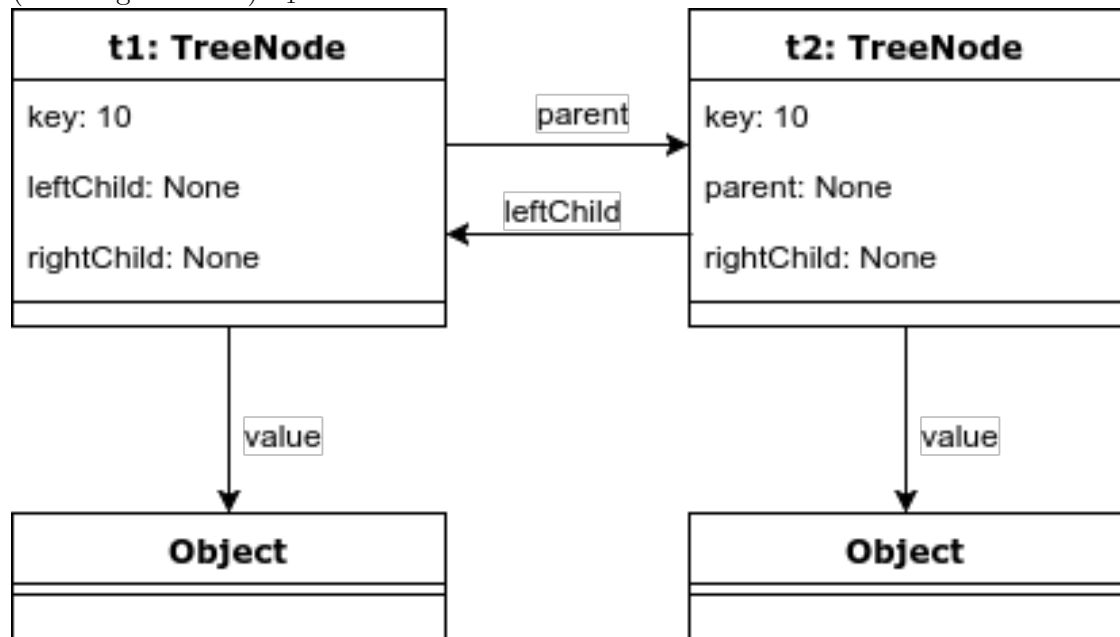
The system state  $\sigma_3$  evaluates to  $\perp$  because there are no Instances of `TreeNode` and the formula can not be evaluated to true or false.

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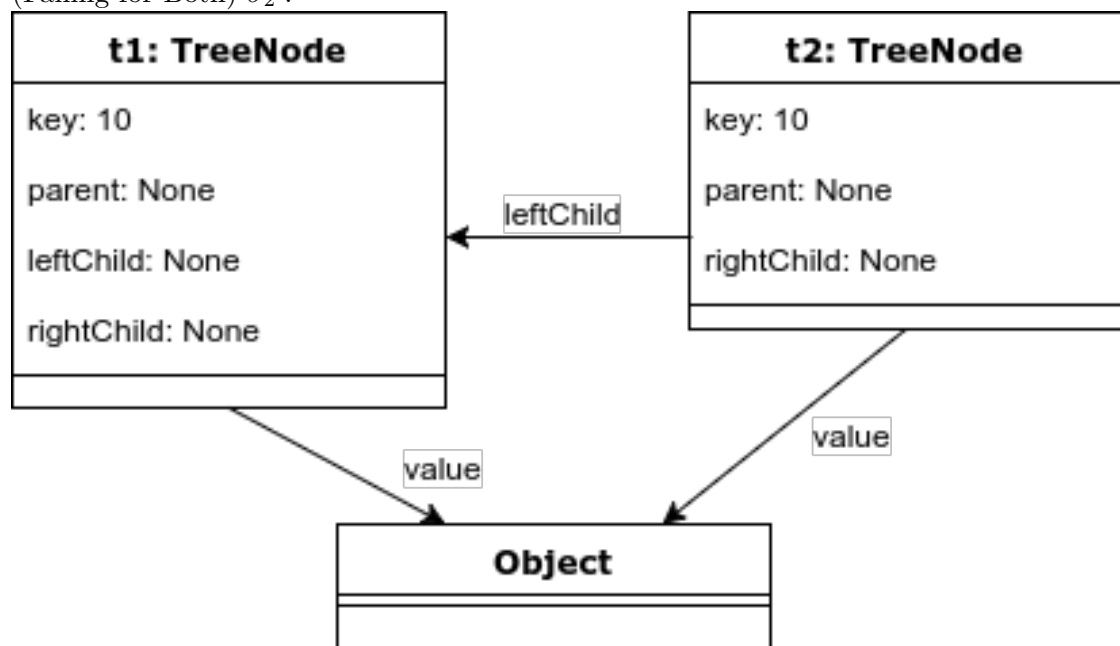
- a)  $\forall o \in allInstancesObject \bullet \forall t_1 \in allInstancesTreeNode \bullet \forall t_2 \in allInstancesTreeNode \bullet (value(t_1) = o \Rightarrow value(t_2) \neq o)$
- b)  $\forall t_1 \in allInstancesTreeNode \bullet \forall t_2 \in allInstancesTreeNode \bullet (t_1 = leftChild(t_2) \Leftrightarrow t_2 = parent(t_1))$

Some System States:

(Working for Both)  $\sigma_1$  :



(Failing for Both)  $\sigma_2$  :



## Exercise 2

Uppaal-checks:

$E_{i\ell}$  worker.BROKEN

(Property is Satisfied)  $E_{ij} (P1.CRITICAL \ \&\& \ P2.CRITICAL)$   
 (Property is Satisfied)

### Exercise 3

$A \parallel \text{not } ((\text{Process}(0).CRITICAL + \text{Process}(1).CRITICAL + \text{Process}(2).CRITICAL + \text{Process}(3).CRITICAL) \geq 1)$   
 (or generally from 0 to n)  
 A and B do not satisfy the Mutual exclusion.