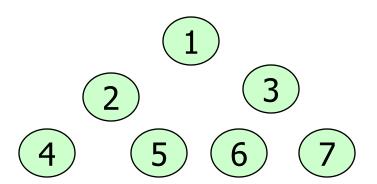
Binary Trees

TreeMap and HashMap

TreeSet and TreeMap were built using binary trees.

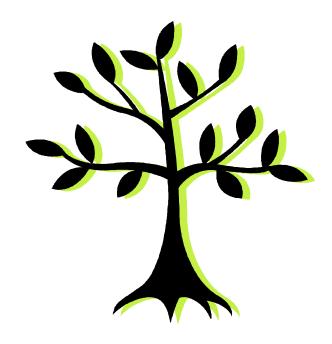


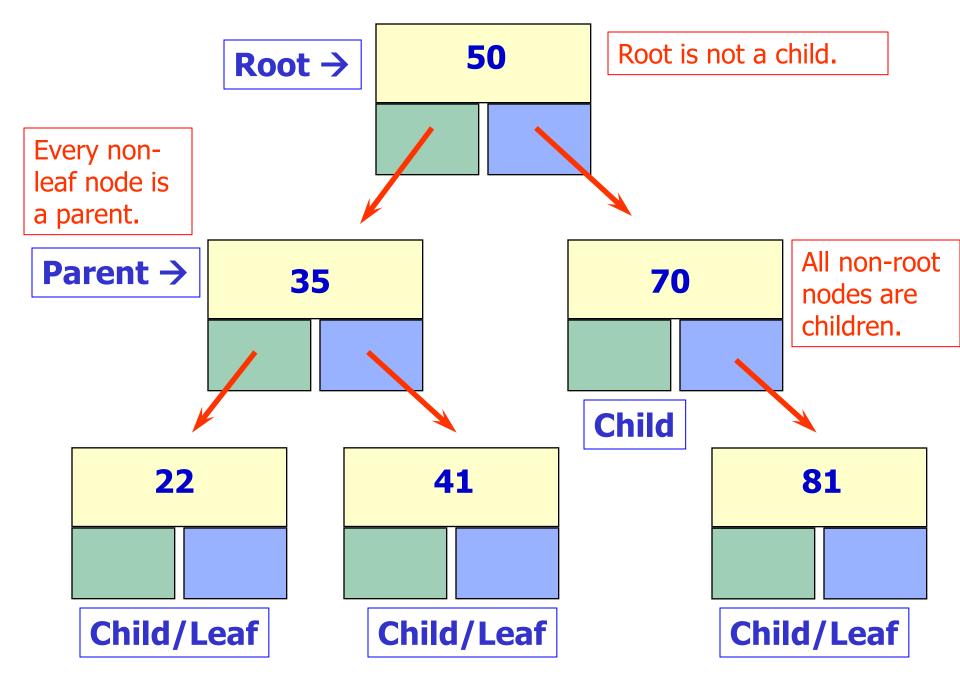


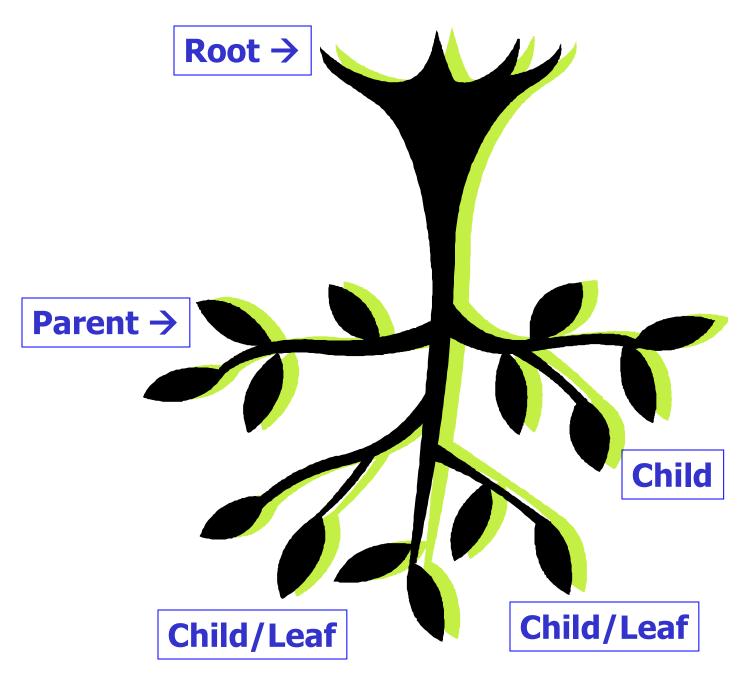
```
Map<Integer,String> map;
map = new TreeMap<Integer,String>();
map.put(1,"one");
map.put(2,"two");
map.put(3,"three");
map.put(4,"four");
map.put(5,"five");
                                         one
map.put(6,"six");
                                         null
map.put(7,"seven");
                                         seven
```

System.out.println(map.get(1)); System.out.println(map.get(13)); System.out.println(map.get(7));

What is a tree?

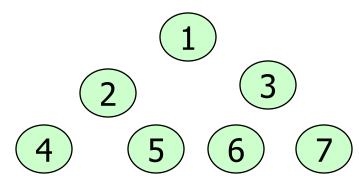






Binary Tree

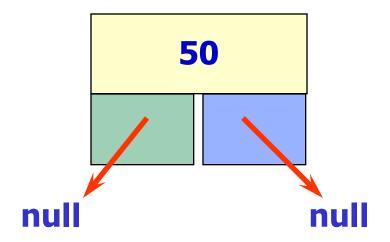
A binary tree is a collection of nodes. Each node has a data value and references to two other nodes. Each node could have a left child and/or a right child.



Simple Node Class

```
public class Node
 private Comparable data;
 private Node left;
 private Node right;
 public Node(Comparable dat, Node Ift, Node rt)
   data=dat;
   left=lft;
   right=rt;
```

A Single Node

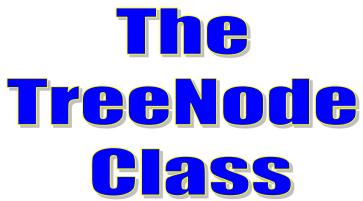


A tree node typically has a data component and a reference to a left child and a reference to a right child.

Treeable Interface

```
public interface Treeable
{
   public Object getValue();
   public Treeable getLeft();
   public Treeable getRight();
   public void setValue(Comparable value);
   public void setLeft(Treeable left);
   public void setRight(Treeable right);
}
```

```
public class TreeNode implements Treeable
 private Comparable treeNodeValue;
 private TreeNode leftTreeNode;
 private TreeNode rightTreeNode;
 public TreeNode( ){
   treeNodeValue = null;
   leftTreeNode = null;
   rightTreeNode = null;
```



public TreeNode(Comparable value, TreeNode left, TreeNode right){

treeNodeValue = value; leftTreeNode = left; rightTreeNode = right;

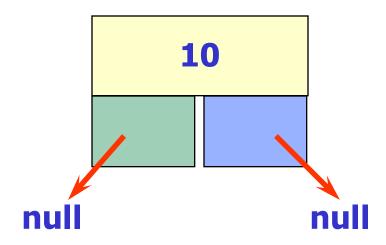
//other methods not shown //refer to the Treeable interface This TreeNode class is similar to the AP TreeNode.

You can obtain the official AP TreeNode class from the college board website. You will be provided with a copy of the AP TreeNode class when you take the AP Computer Science AB exam.

Creating A
Single Tree Node

Treeable node = new TreeNode("10", null,null);
out.println(node.getValue());

out.println(node.getLeft()); out.println(node.getRight());



OUTPUT
10
null
null

Open onetreenode.java

Linking Tree Nodes

Linking Tree Nodes

```
TreeNode node = new TreeNode("10",

new TreeNode("5", null,null),

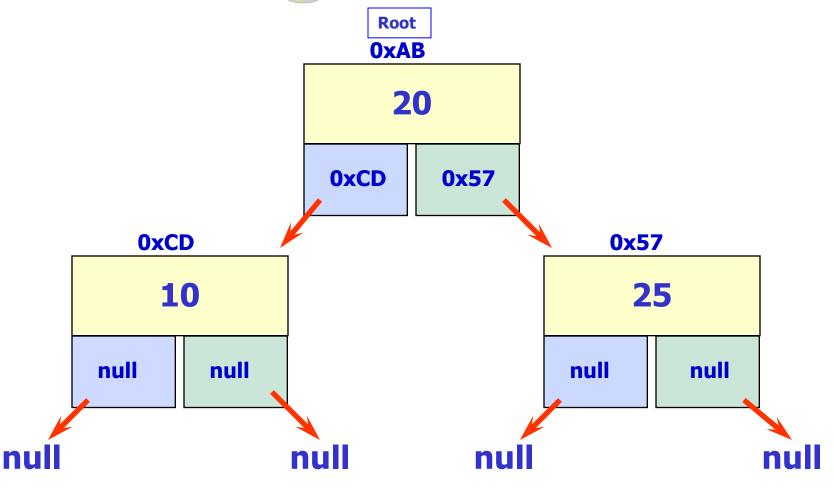
new TreeNode("20", null,null));
```

out.println(node.getValue());
out.println(node.getLeft().getValue());
out.println(node.getRight().getValue());

OUTPUT 10 5 20

Open treene.java

Linking Tree Nodes



Linking Tree Nodes

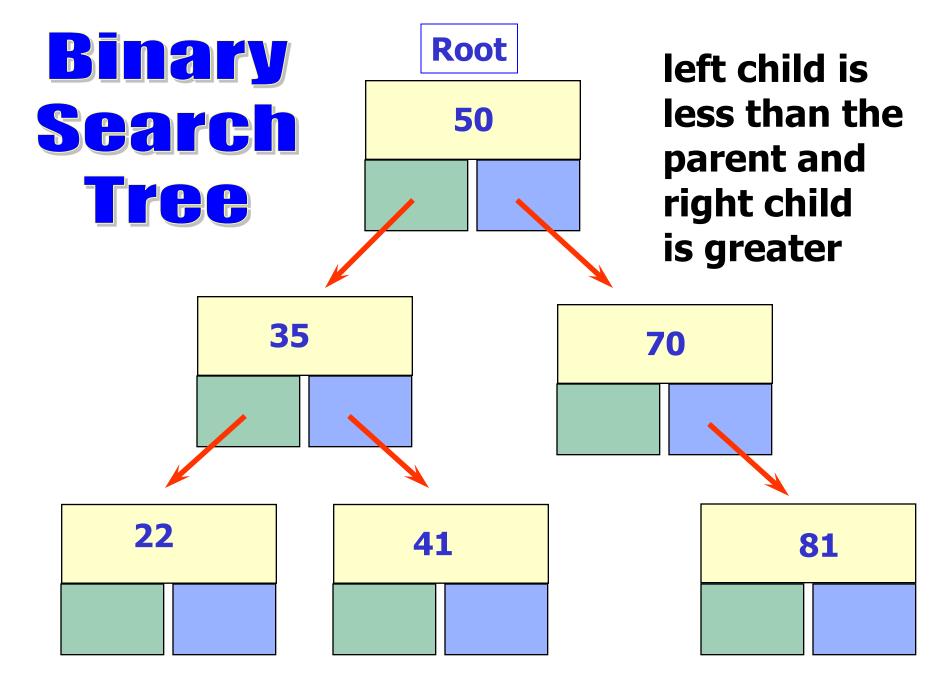
```
TreeNode x = new TreeNode("10",null,null);
TreeNode y = new TreeNode("25", null,null);
TreeNode z = new TreeNode("20", x, y);
```

```
out.println(z.getValue());
out.println(z.getLeft().getValue());
out.println(z.getRight().getValue());
```

OUTPUT20 10 25

Open treetwo.java

Building a Search Tree





Every item that is added to a search tree is first compared to the root. If the item is larger than the root, a recursive call is made on the right sub tree. If the item is smaller than the root, a recursive call is made on the left sub tree. This process continues until a null reference is found.

d – recursīve 1

```
private TreeNode add(Comparable val, TreeNode tree)
 if (tree == null)
    return new TreeNode(val, null, null);
  int dirTest = val.compareTo(tree.getValue());
  if(dirTest<0)
                 do I go left?
    tree.setLeft(add(val, tree.getLeft()));
  else if(dirTest>0) do I go right?
    tree.setRight(add(val, tree.getRight()));
  return tree;
```

Check to see which direction to go. Go left or right?

AP NOTE

After grading the tree question at the AP reading for several years, I can tell you that you absolutely must know this code!!!!!

add - recursive 2

```
private TreeNode add(Comparable val, TreeNode tree)
 if (tree == null)
   tree = new TreeNode(val, null, null);
 else if (val.compareTo(tree.getValue()) < 0 )
   tree.setLeft(add(val, tree.getLeft()));
 else if (val.compareTo(tree.getValue()) > 0 )
   tree.setRight(add(val, tree.getRight()));
  return tree;
```

Code works the same as 1, but is more compressed.



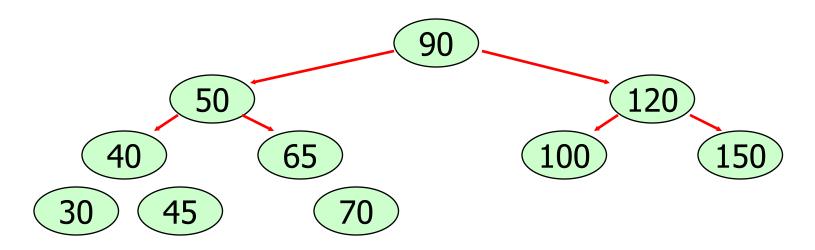
AP NOTE

After grading the tree question at the AP reading for several years, I can tell you that you absolutely must know this code!!!!!

Open addprintone.java

Printing a Search Tree

Tree Traversals



IN-ORDER = 30 40 45 50 65 70 90 100 120 150

PRE-ORDER = 90 50 40 30 45 65 70 120 100 150

POST-ORDER = 30 45 40 70 65 50 100 150 120 90

REV-ORDER = 150 120 100 90 70 65 50 45 40 30

In Order 1

```
private void inOrder(TreeNode tree)
{
   if (tree != null){
      inOrder(tree.getLeft());
      out.print(tree.getValue() + " ");
      inOrder(tree.getRight());
   }
}
```

Data is in the MIDDLE!!!

In Order 2

```
private void inOrder(TreeNode tree)
{
  if (tree == null)
    return;
  inOrder(tree.getLeft());
  out.print(tree.getValue() + " ");
  inOrder(tree.getRight());
}
```

This is an alternative to the previous example.

Data is in the MIDDLE!!!

In Order 3

```
private String inOrder(TreeNode tree)
{
  if (tree != null)
    return inOrder(tree.getLeft())
        + tree.getValue() + " " +
        inOrder(tree.getRight());
  return "";
}
```

This is another alternative approach.

Data is in the MIDDLE!!!

Binary Tree Traversals

In-Order

Pre-Order

Post-Order Beeff



Reverse-Order



Open addprinttwo.java

Searching a Tree

Searching Trees

To search a tree, you will use the same basic logic that you used to add a new node.

First, compare the current node to the search value and see if it is a match. If it is not a match, check to see if you need to search the left sub tree or the right sub tree. Repeat.

Sounds like a binary search.

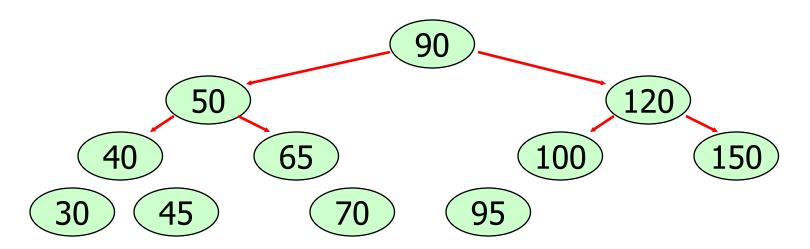
Searching Trees

```
private boolean search(Comparable val, TreeNode tree)
  if(tree != null)
    int dirTest = val.compareTo(tree.getValue());
    if(dirTest == 0)
      return true;
    else if (dirTest < 0)
      return search(val, tree.getLeft());
    else if (dirTest > 0)
      return search(val, tree.getRight());
  return false;
```

Open contains.java

Tree Operations

Tree Operations



WIDTH - 7

HEIGHT - 3

NUMLEAVES - 5

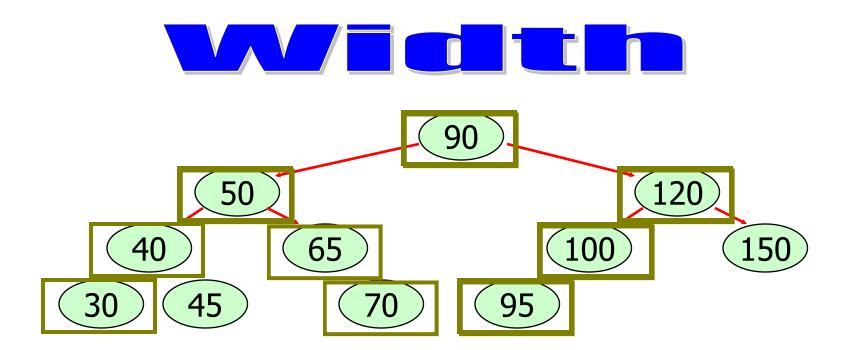
NUMLEVELS - 4

NUMNODES - 11

ISFULL - NO

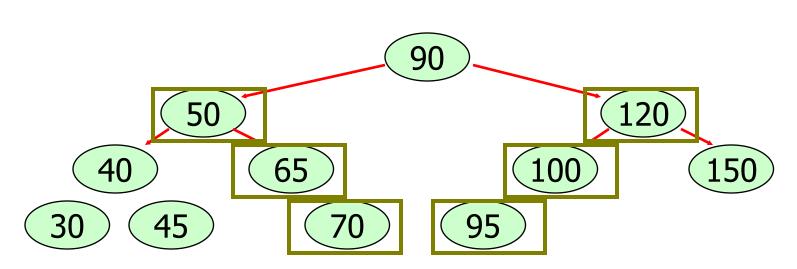
Binary Trees

- Width dist between two furthest leaves in the tree does not have to go through the root
- Height longest path from root to a leaf # of links from root to farthest leaf
- Level a group of equal nodes the root is level - 0 the children of the root - level - 1



WIDTH - 7

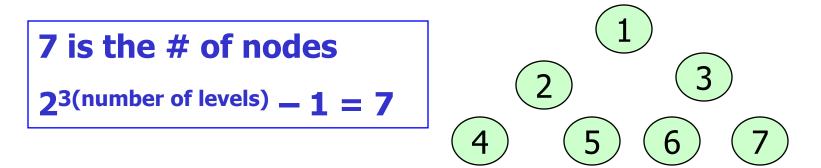




HEIGHT - 3

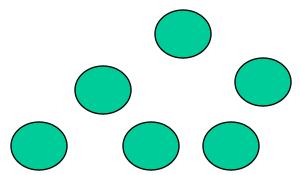


In a full binary tree, every parent has exactly two children or no children at all. The number of nodes in the tree will equal 2 raised to the number of levels -1 if the tree if full.



A Complete Tree

In a complete tree, every level that can be filled is filled. Any levels that are not full have all nodes shifted as far left as possible.



getNumLevels Algo

```
int getNumLevels(TreeNode tree)
  if (tree==null)
   return something;
  else
   numLeft = getNumLevels of the left
   numRight = getNumLevels of the right
   if (numLeft > numRight)
      return 1 + numLeft;
   else
      return 1 + numRight;
```

getNumLevels Algo

```
public int getNumLevels()
  return getNumLevels(root);
private int getNumLevels(TreeNode tree)
 if(tree==null) return 0;
 else
   int numLeft = getNumLevels(tree.getLeft());
   int numRight = getNumLevels(tree.getRight());
   if(numLeft > numRight)
     return 1 + numLeft;
   return 1 + numRight;
```

getNumLevels Algo

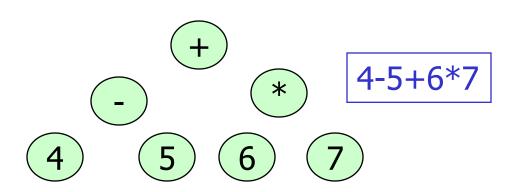
```
public int getNumLevels()
  return getNumLevels(root);
private int getNumLevels(TreeNode tree)
 if(tree==null) return 0;
 else
   return
       1 + Math.max(getNumLevels(tree.getLeft(),
                  getNumLevels(tree.getRight());
```

Open numlevels.java

Fancy Trees

Expression Tree

A binary expression tree is a binary tree in which each parent node contains an operator and each leaf contains a number.



Threaded Tree

A threaded binary tree is a binary tree with an additional reference in each node that is used to point from a child back to its parent.

Threaded Tree

public class ThreadedTreeNode {

private Comparable treeNodeValue; private ThreadedTreeNode leftTreeNode; private ThreadedTreeNode rightTreeNode; private ThreadedTreeNode parentTreeNode;

//constructors and methods not shown

}

Threaded Tree null 50 35 70 null null null null

Big-O Notation

Big-O notation is an assessment of an algorithm's efficiency. Big-O notation helps gauge the amount of work that is taking place.

Common Big O Notations:

O(1) $O(Log_2N)$

 $O(2^N) \qquad O(N^2)$

 $O(N Log_2N)$ O(N)

 $O(Log_2N)$ $O(N^3)$

Binary Search Tree

traverse all nodes O(N)

search for an item O(log₂N)

remove any item O(log₂N)

location unknown

get any item O(log₂N)

location unknown

add item at the end $O(log_2N)$

add item at the front O(1)

A binary tree node has a reference to its left and right nodes. Nodes are ordered.

These notations assume the tree is balanced or near balanced.

Start Work on the labs