

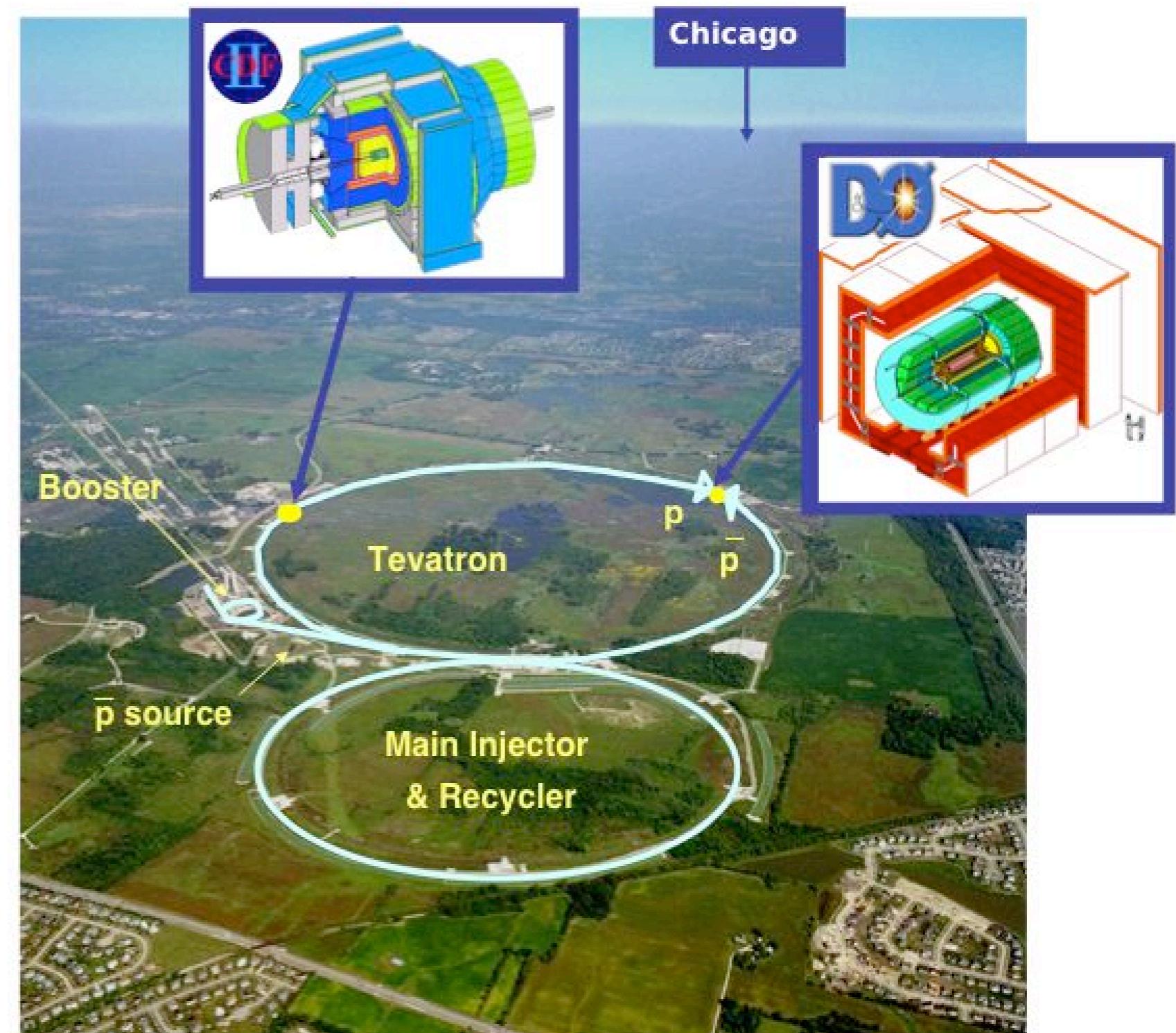
Measuring Single Top Quark Production at DØ With The Matrix Element Method

- The Tevatron and The DØ Experiment
- The Top Quark and Single Top Production
- Single Top Event Signature At DØ
- Tevatron Run IIa Dataset
- Analysis Strategy and Background Estimation
- Matrix Element Method
- Single Top Results with $\sim 1 \text{ fb}^{-1}$

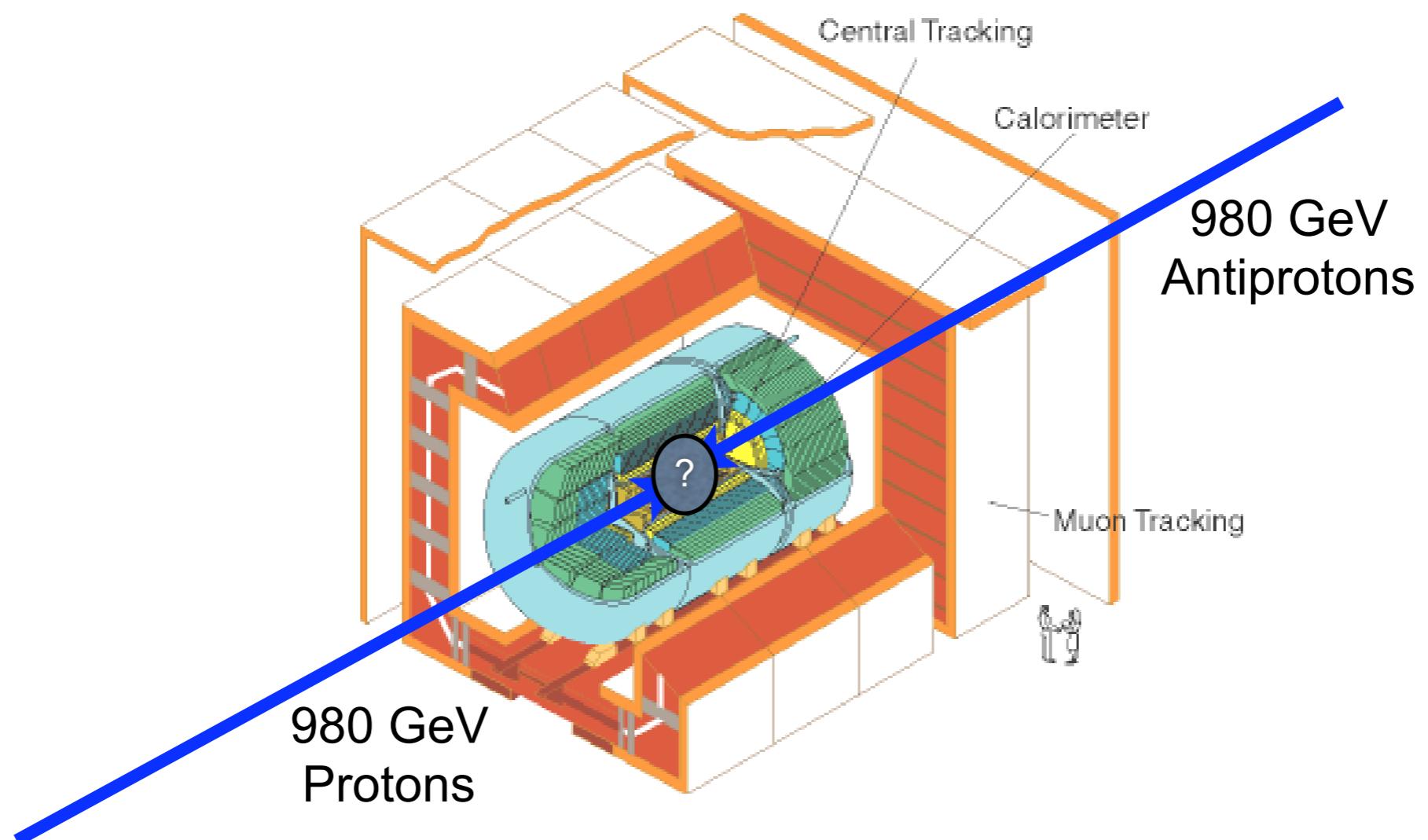
Thomas Gadfort
University of Washington
Ph. D. Thesis Defense
April 20, 2007

The Tevatron at Fermilab

- Tevatron is a proton-antiproton collider
- World's highest energy particle accelerator
 - $\sqrt{s} = 1.96 \text{ TeV}$
- Run I: 1992-1996
 - Top discovery in 1995!
- Run II: 2001 - Present
 - B_s Mixing in 2006
 - Limits on SUSY and Higgs production
- Currently, the only place in the world to study the top quark



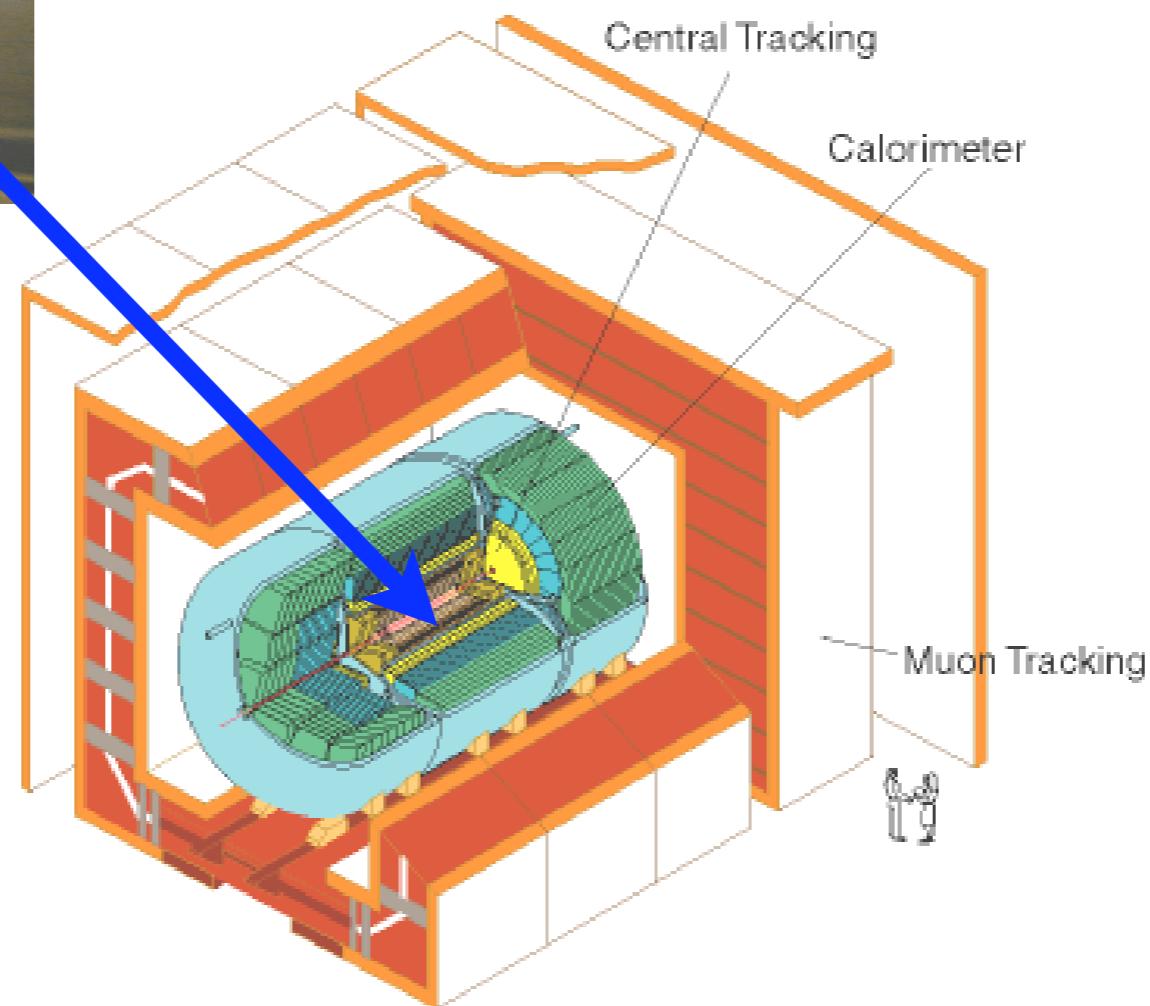
The Run II DØ Experiment



The Run II DØ Experiment



Silicon Detector
Vertex measurement
and tracking close to PV



The Run II DØ Experiment

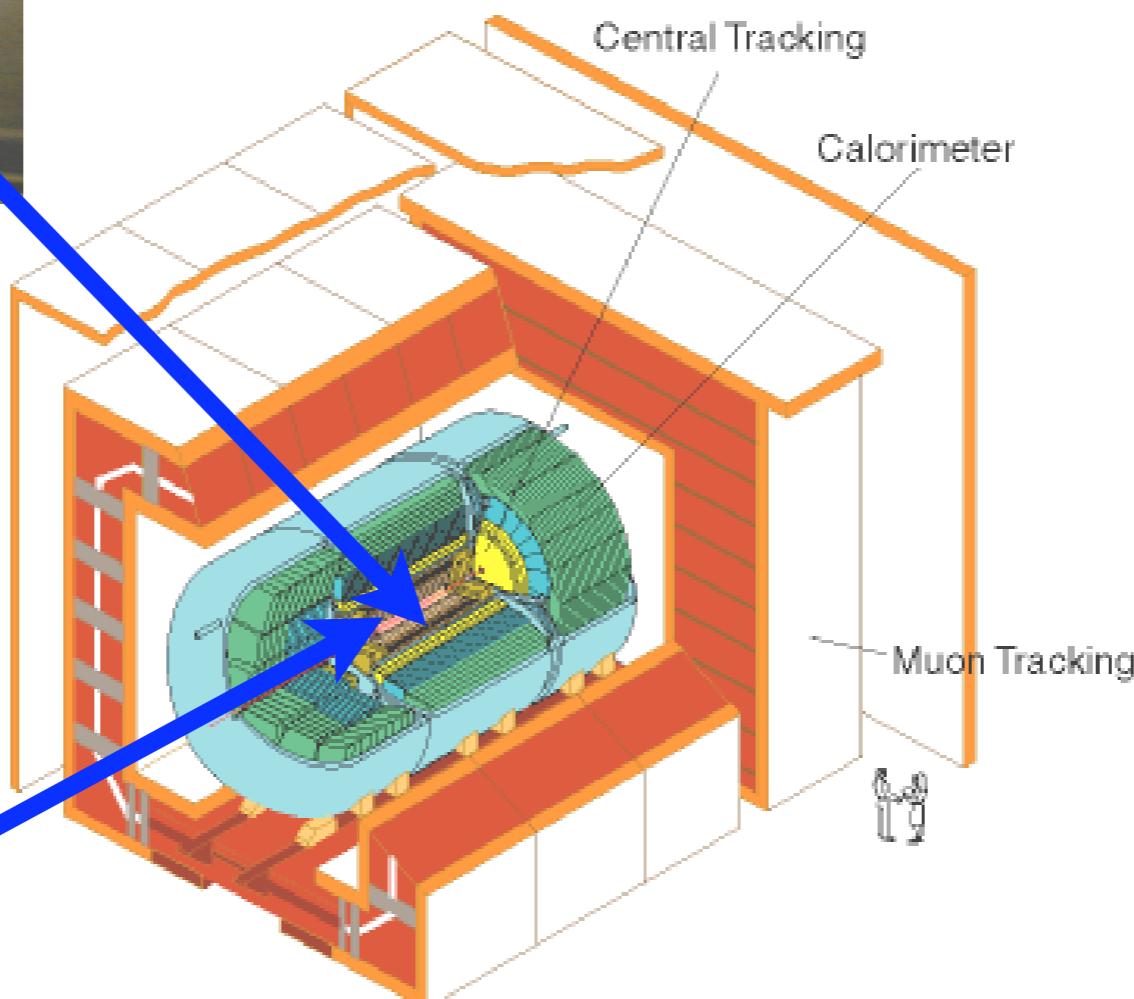
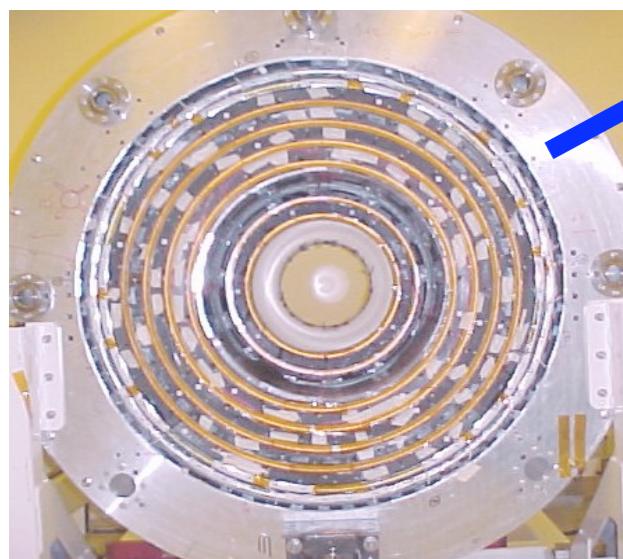


Silicon Detector

Vertex measurement
and tracking close to PV

Fiber Tracker

Charged particle tracking
momentum + charge

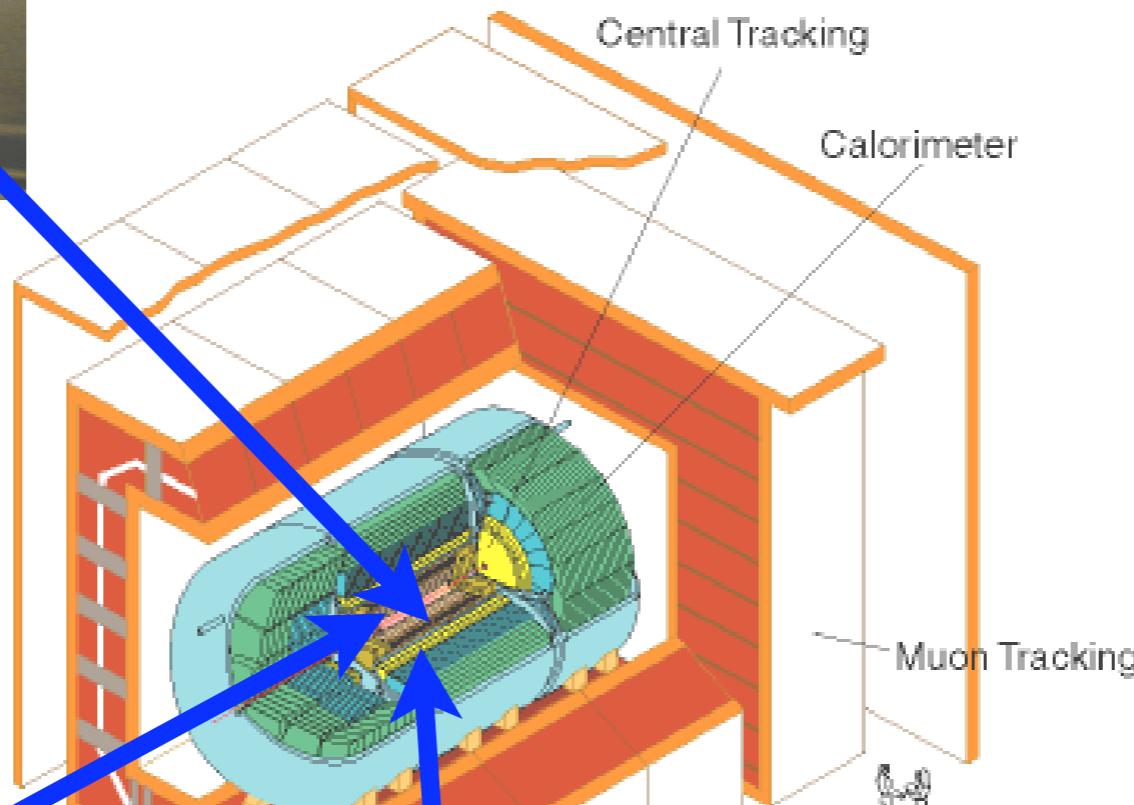


The Run II DØ Experiment



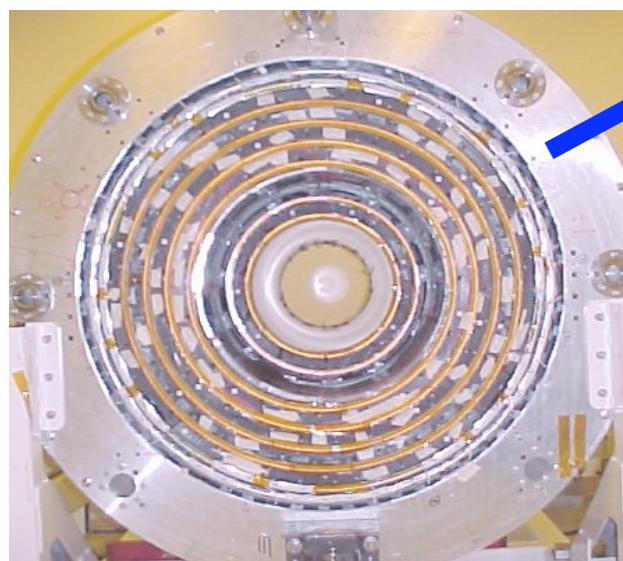
Silicon Detector

Vertex measurement
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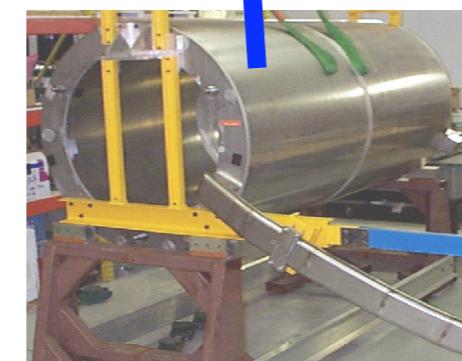


Fiber Tracker

Charged particle tracking
momentum + charge



Solenoid
Trackers in
2 Tesla

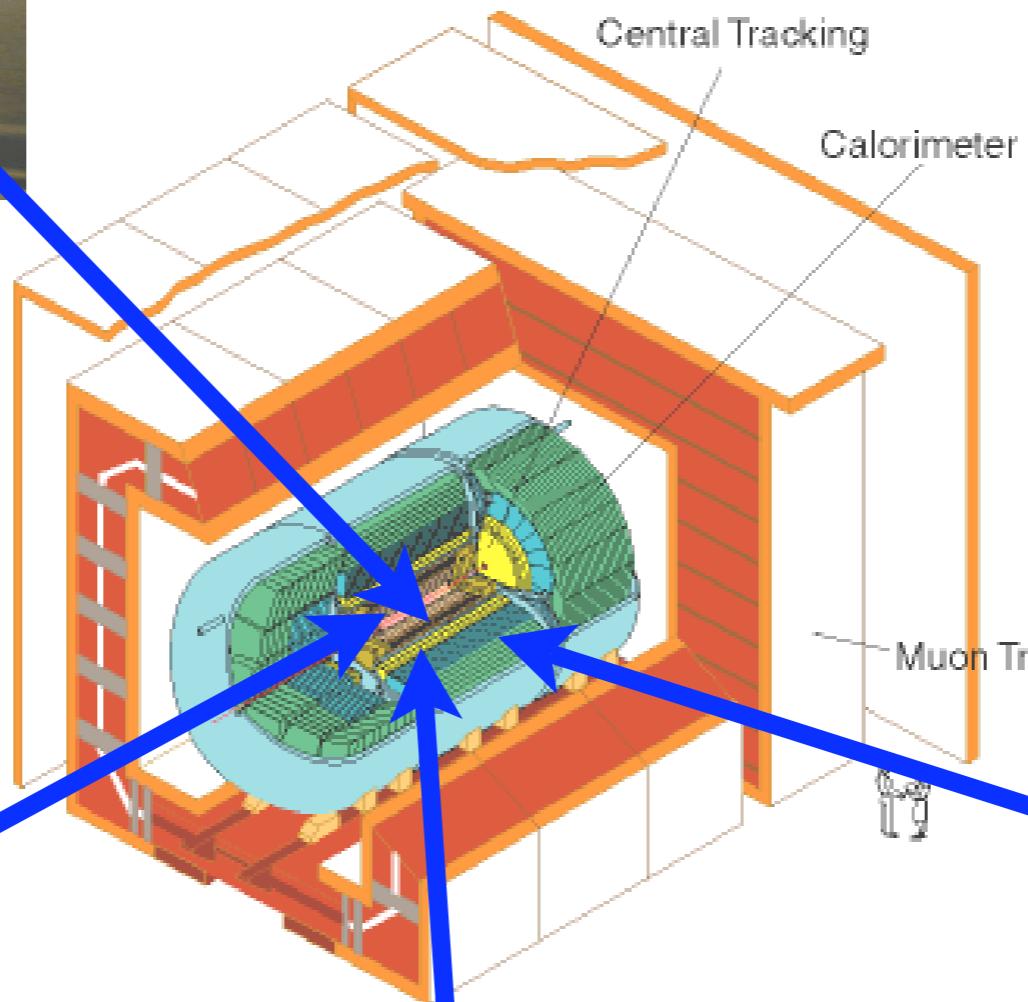


The Run II DØ Experiment



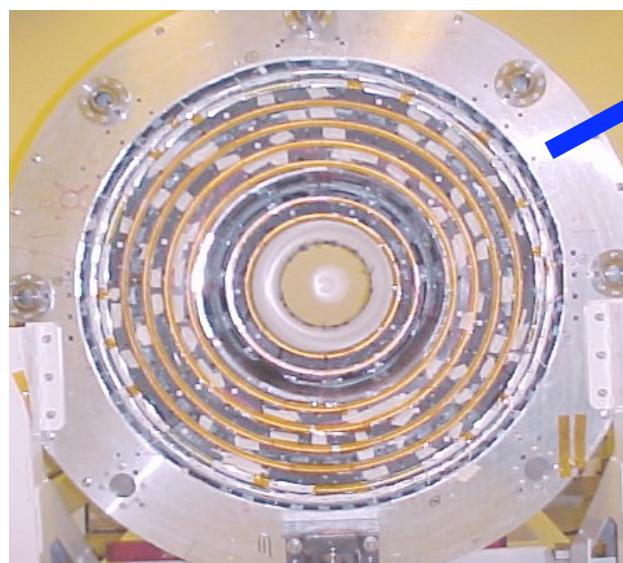
Silicon Detector

Vertex measurement
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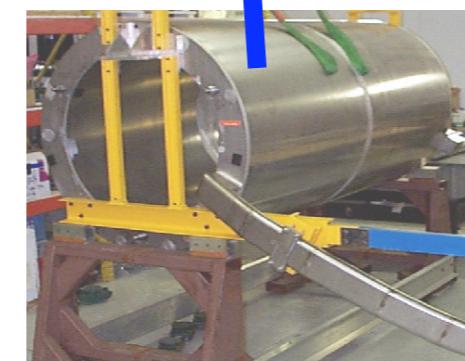


Fiber Tracker

Charged particle tracking
momentum + charge



Solenoid
Trackers in
2 Tesla



EM & Hadronic
Calorimeter
Energy
measurement



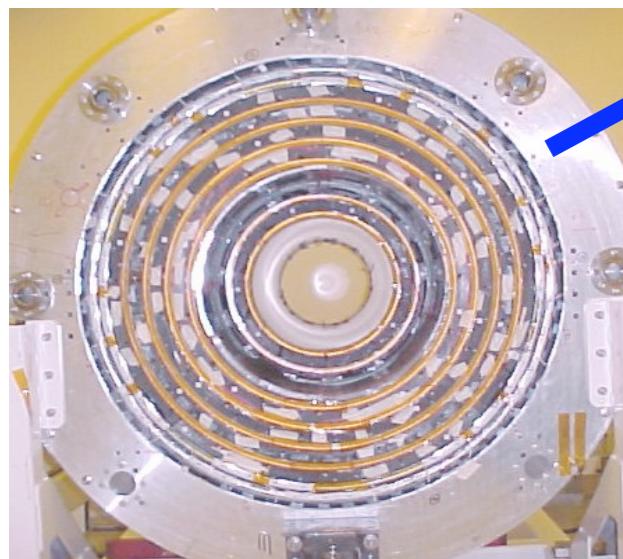
The Run II DØ Experiment



Silicon Detector

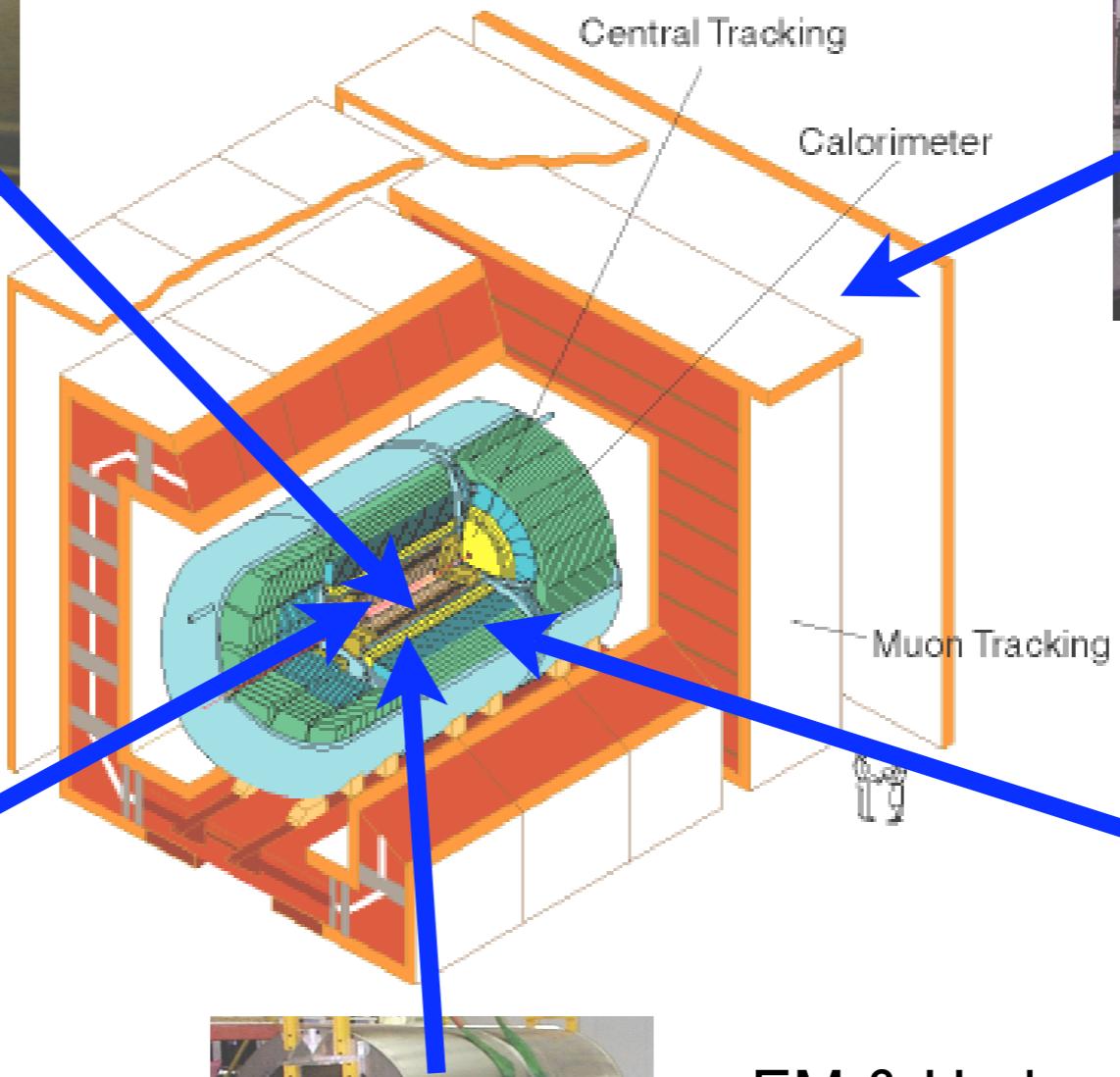
Vertex measurement
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Fiber Tracker
Charged particle tracking
momentum + charge

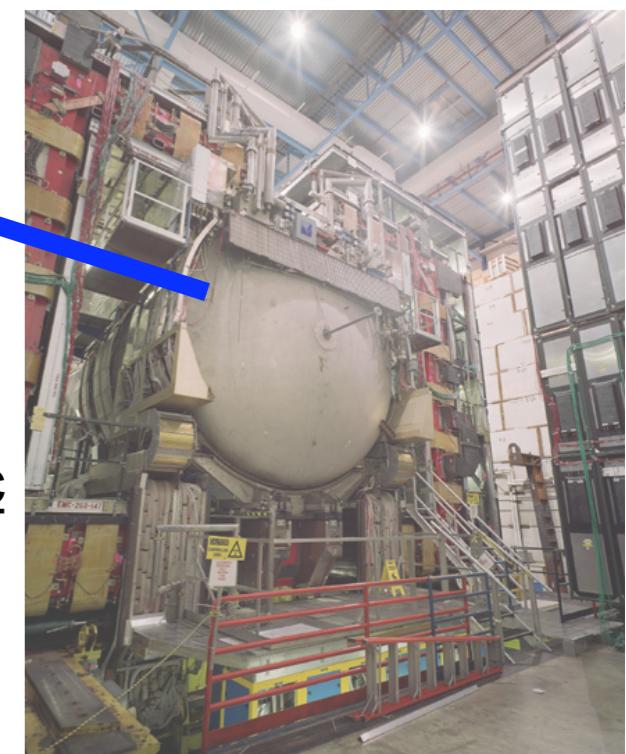
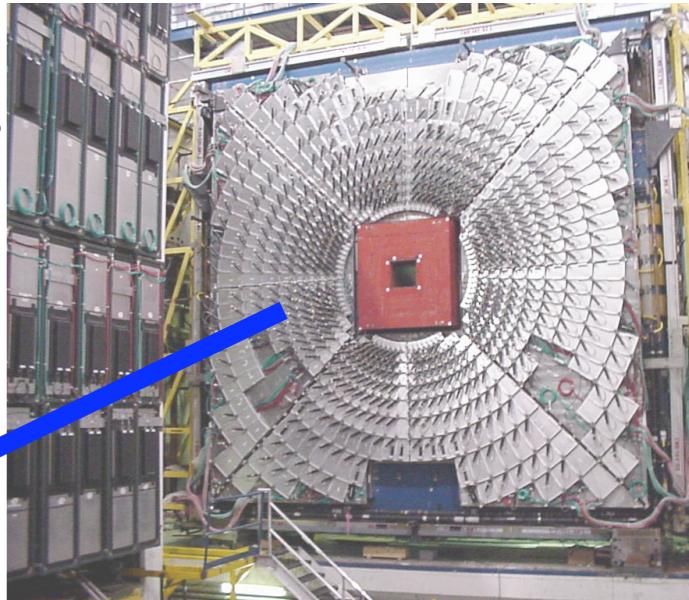


Solenoid
Trackers in
2 Tesla

Muon System
Drift chambers / scintillators
Muon position and tracking



EM & Hadronic
Calorimeter
Energy
measurement

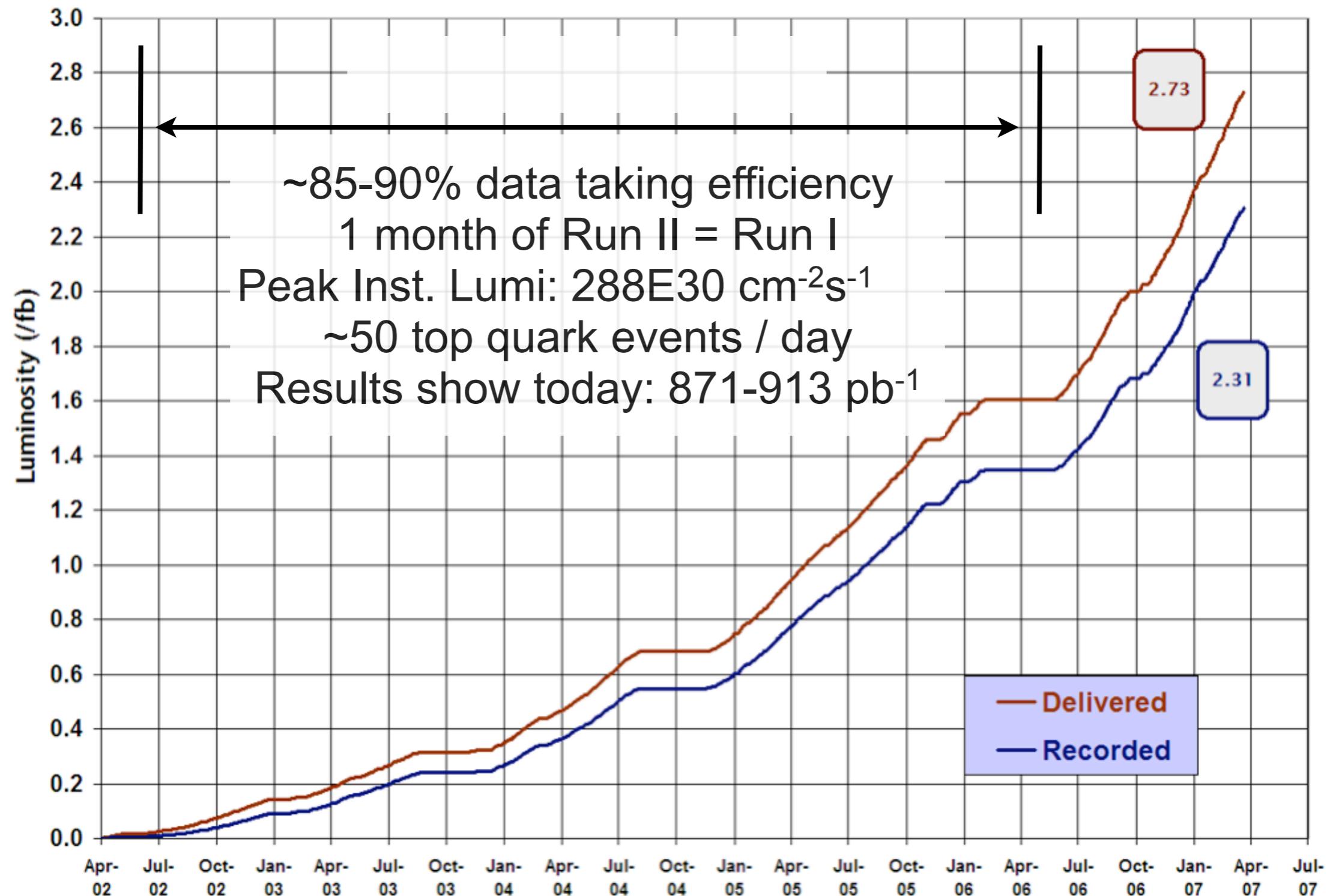


Run II Data Taking



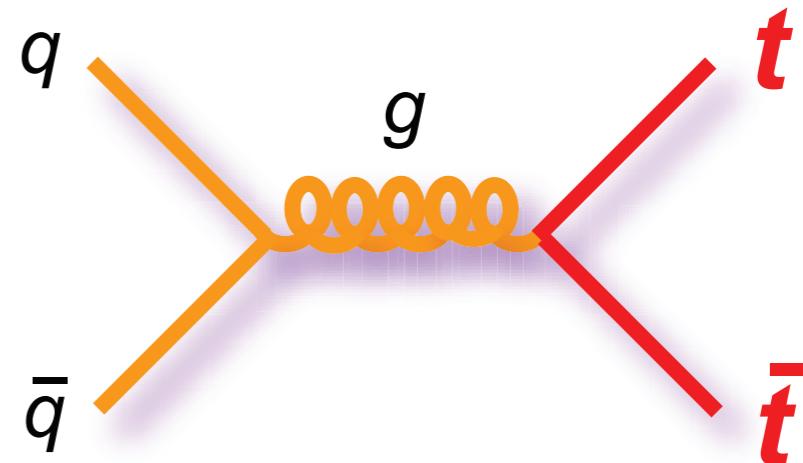
Run II Integrated Luminosity

19 April 2002 - 8 April 2007

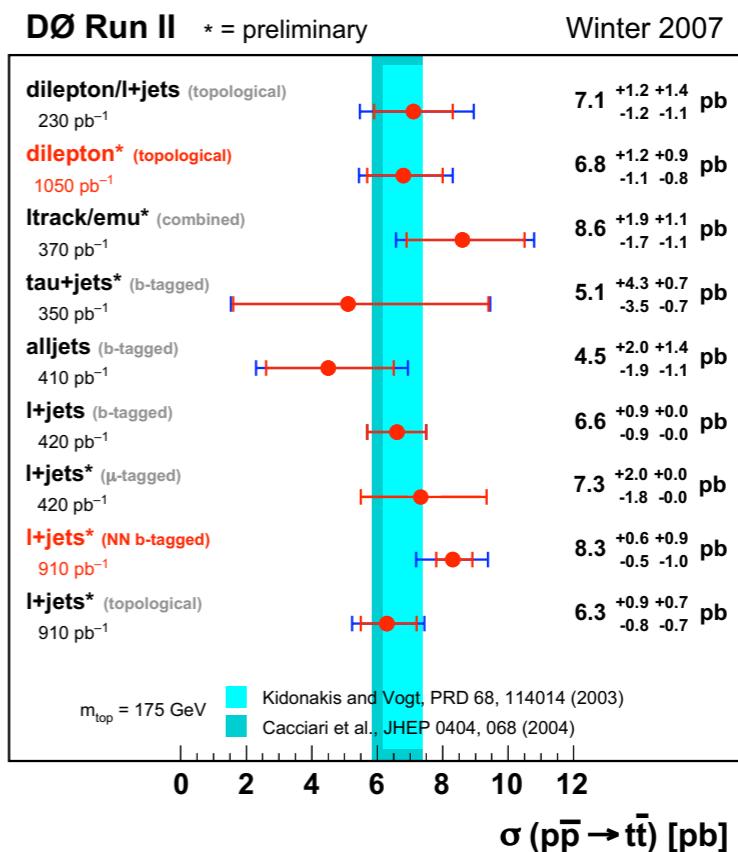


The Top Quark

- Top quark was discovered in 1995 by the CDF and DØ collaborations
- Interesting properties:
 - Very massive
 $m_t = 170.9 \pm 1.8 \text{ GeV}/c^2$
 Tevatron EWWG (hep-ex/0703034)
 - Short lifetime - No QCD bound states
 $\tau_t \approx 3 \times 10^{-25} \text{ s} \ll 1/\Lambda_{\text{QCD}}$
 - Decays as free quark; $\text{BR}(t \rightarrow W b) \approx 1$
 - Studied in QCD pair production
 - For $m_t = 175 \text{ GeV} \rightarrow \sigma(t\bar{t}) = 6.8 \text{ pb}$
 - Occurs in $\sim 1:10$ billion collisions!
 - Rate well measured at Run II

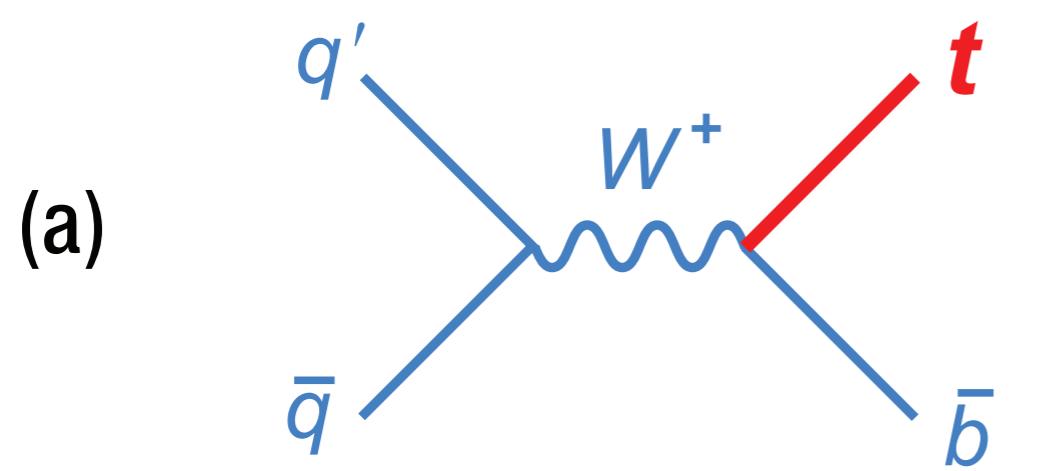


Results From DØ

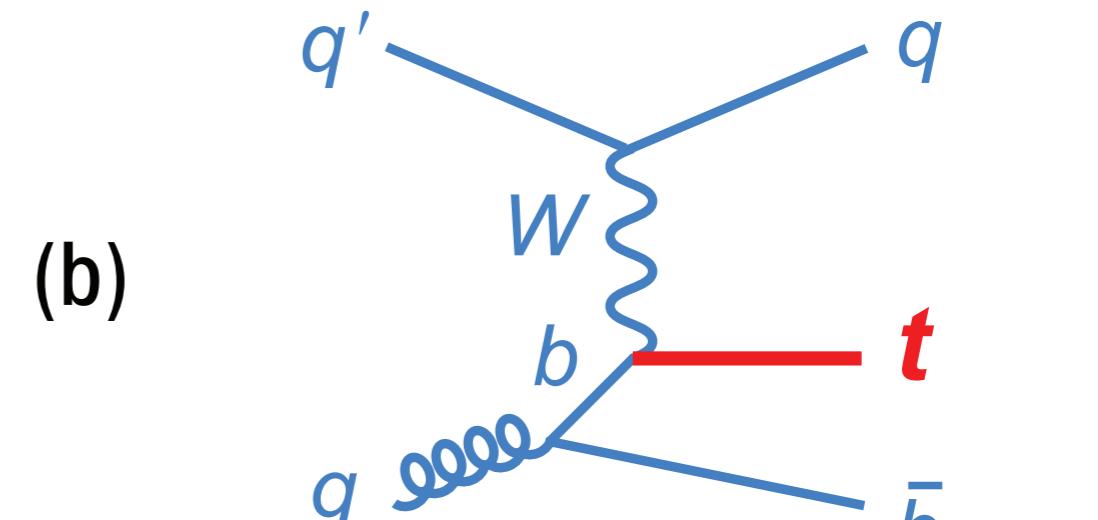


Single Top Quark Production

- Top quarks can also be produced through an electroweak interaction
- Two production modes at the Tevatron



$$\sigma_s^{\text{NLO}} = 0.88 \pm 0.11 \text{ pb}$$



$$\sigma_t^{\text{NLO}} = 1.98 \pm 0.25 \text{ pb}$$

B.W. Harris et. al (hep-ph/0207055)
Z. Sullivan (hep-ph/0408049)

- Current 95% CL limits

DØ with 370 pb^{-1} $\sigma_s^{D\emptyset} < 5.0 \text{ pb}$

CDF with 700 pb^{-1} $\sigma_s^{CDF} < 3.1 \text{ pb}$

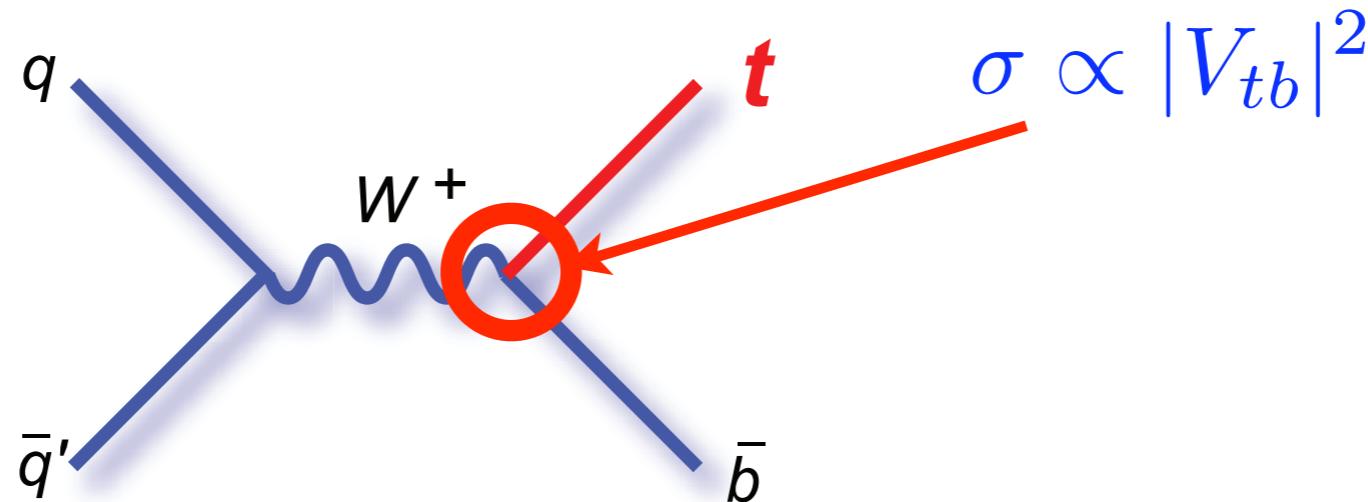
$\sigma_t^{D\emptyset} < 4.4 \text{ pb}$

$\sigma_t^{CDF} < 3.2 \text{ pb}$

Motivation For Measuring Single Top

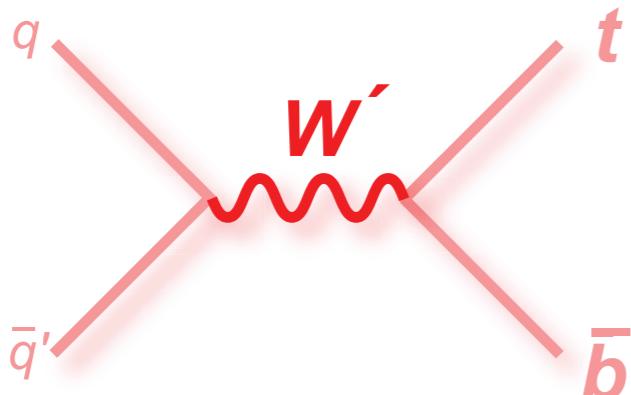
- Test of Standard Model

- Sole method to determine V_{tb} without assuming $VV^\dagger=1 \rightarrow$ Test unitarity

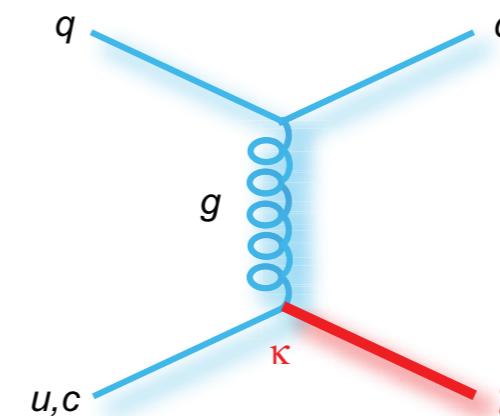


- Source of $\sim 100\%$ polarized top quarks

- Sensitive to beyond the Standard Model processes



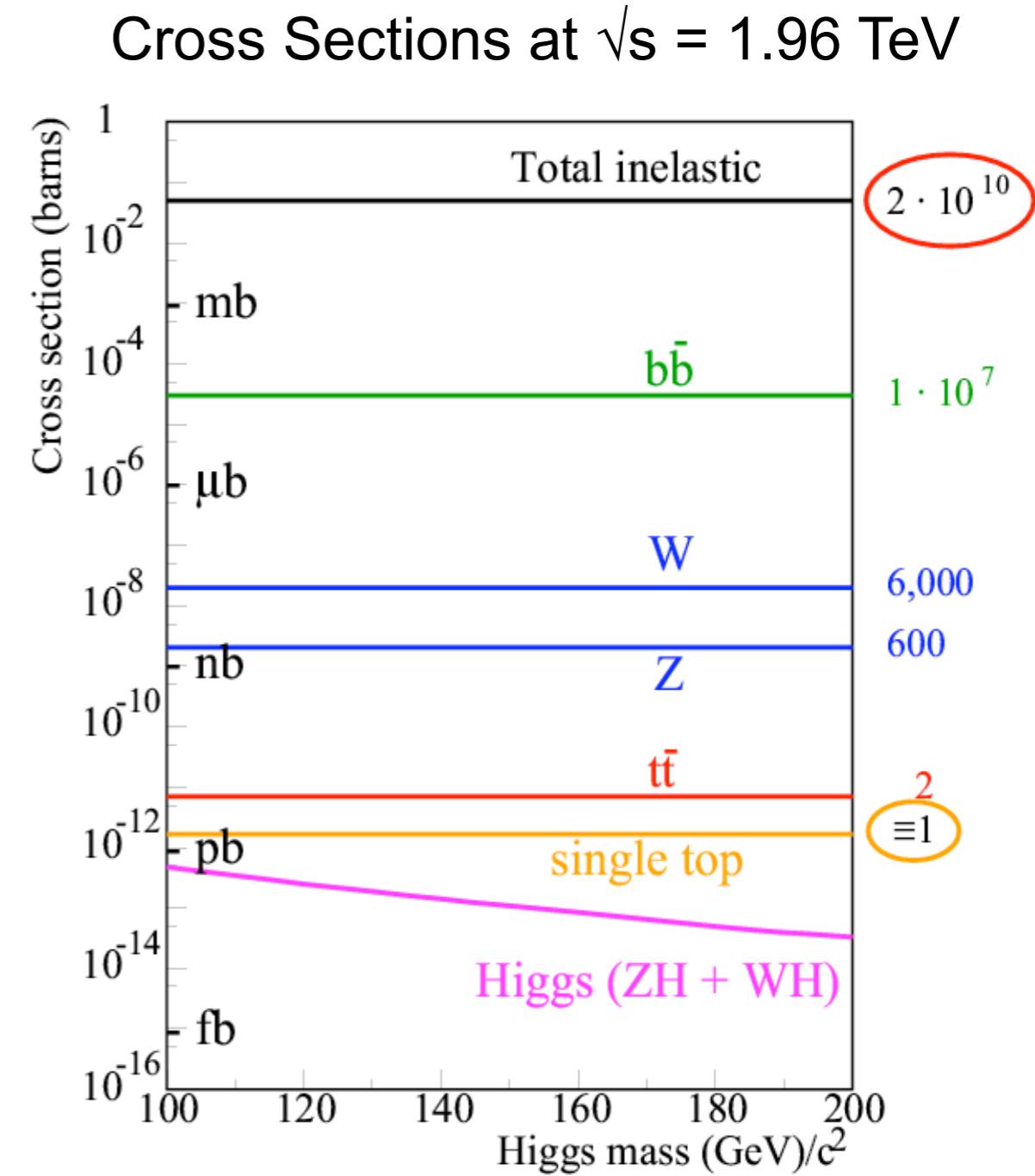
s-channel sensitive
to new resonances



t-channel sensitive to flavor
changing neutral currents

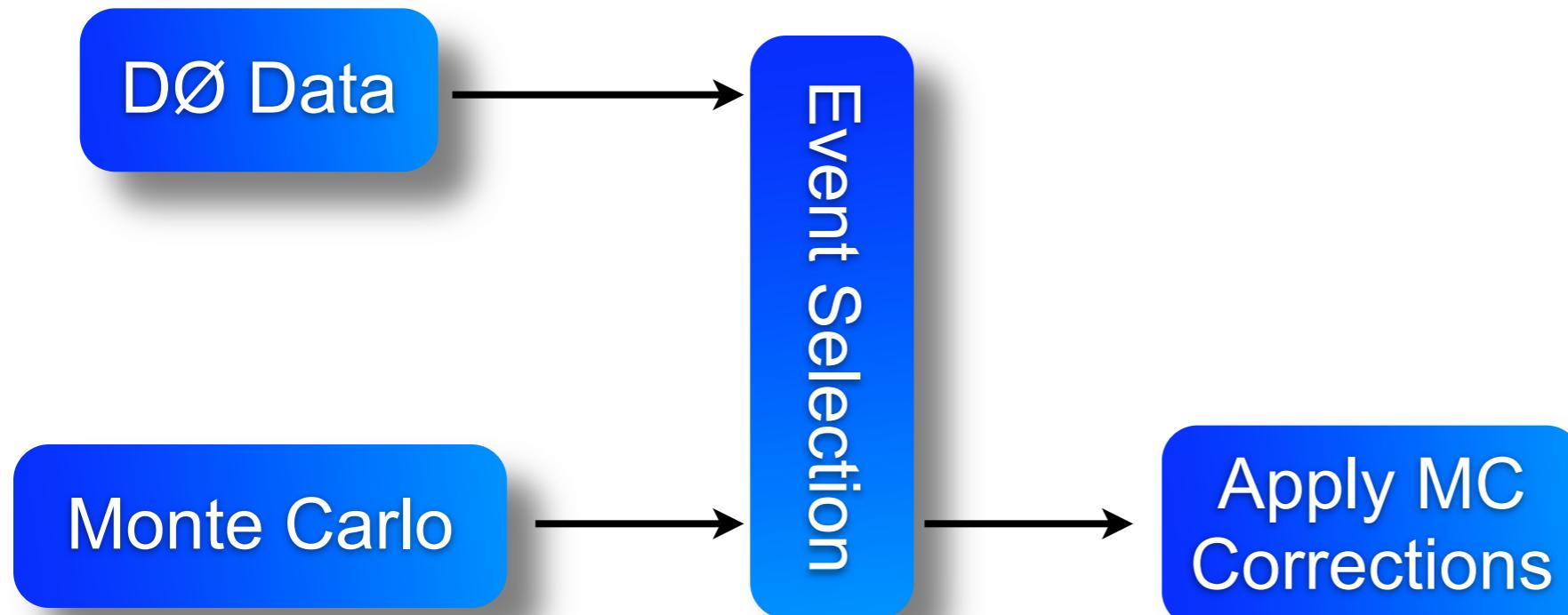
Not An Easy Search

- Low rate: $\sigma(t\bar{b} + tqb) \sim 1/2 \sigma(t\bar{t})$
- Single top quarks produced in 1:20 billion collisions
- Produced ~ once per hour at Tevatron
- Large backgrounds
 - Pair production:
 $t\bar{t} \rightarrow \ell\nu + 2b + 2l$
 $t\bar{t} \rightarrow \ell\nu\ell\nu + 2b$
 - fairly unique = low background rate
 - Single top:
 $tb \rightarrow \ell\nu + 2b$
 $tqb \rightarrow \ell\nu + 2b + 1l$
 - very common = high background rate

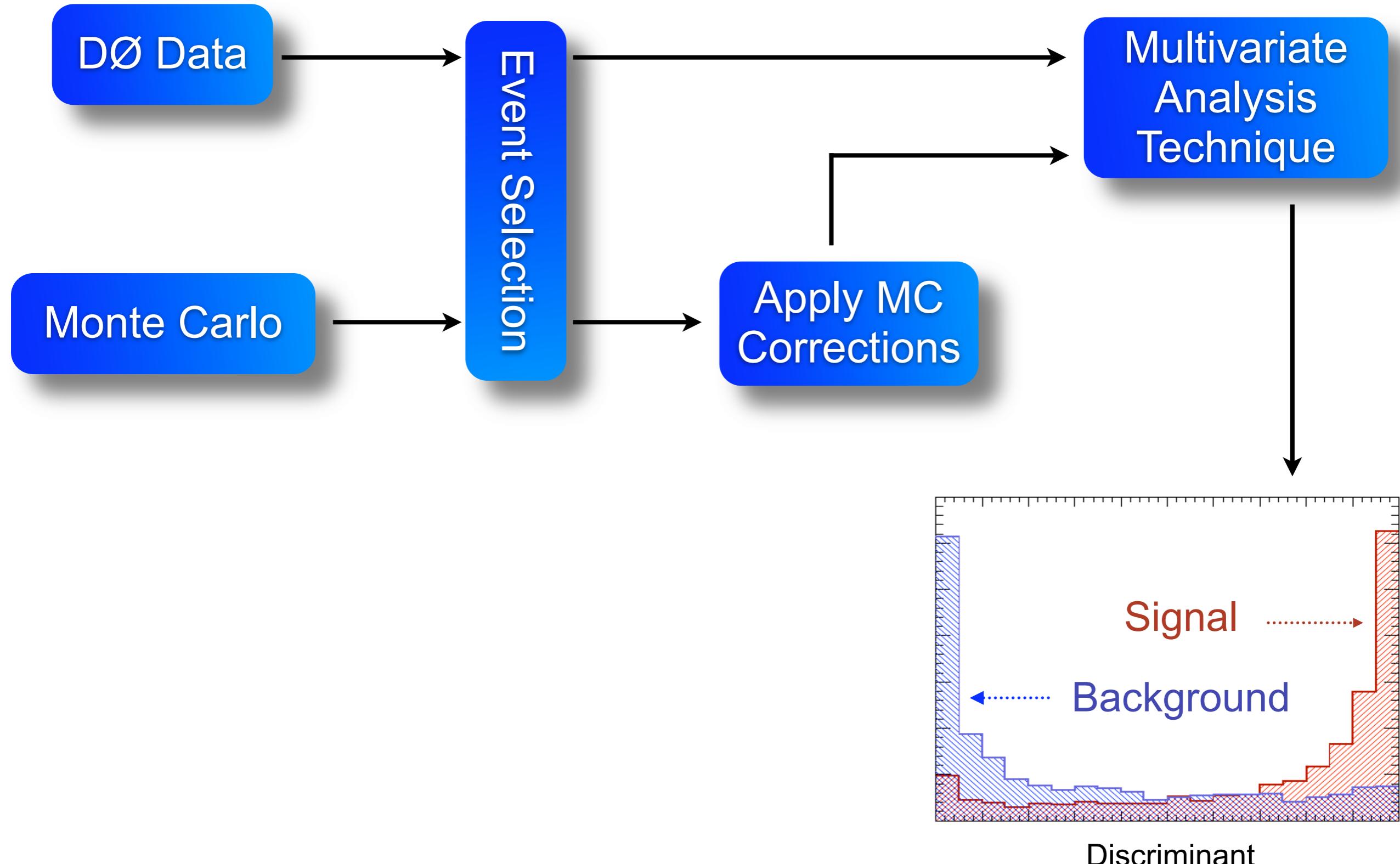


Single Top Analysis Flow

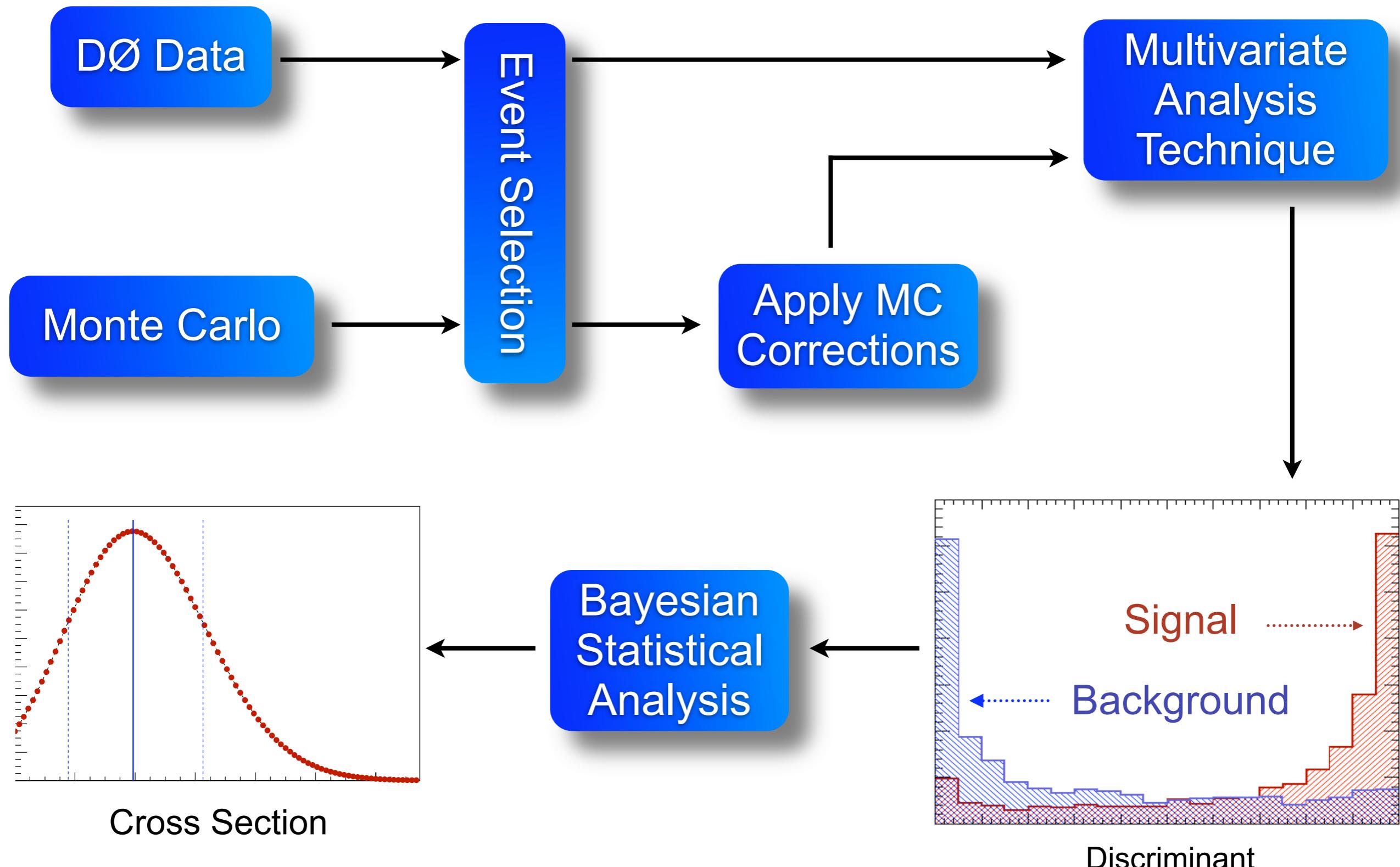
Single Top Analysis Flow



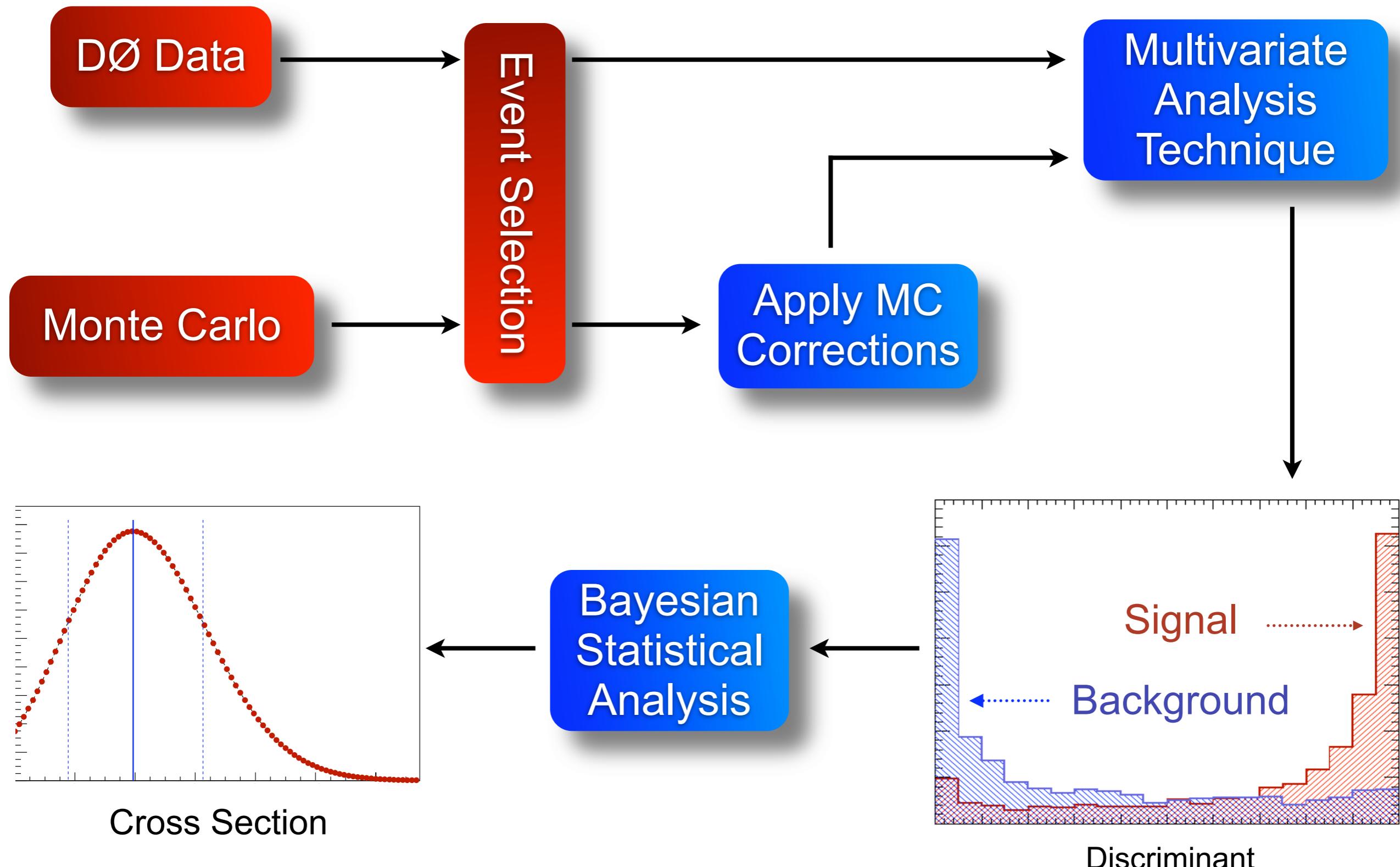
Single Top Analysis Flow



Single Top Analysis Flow

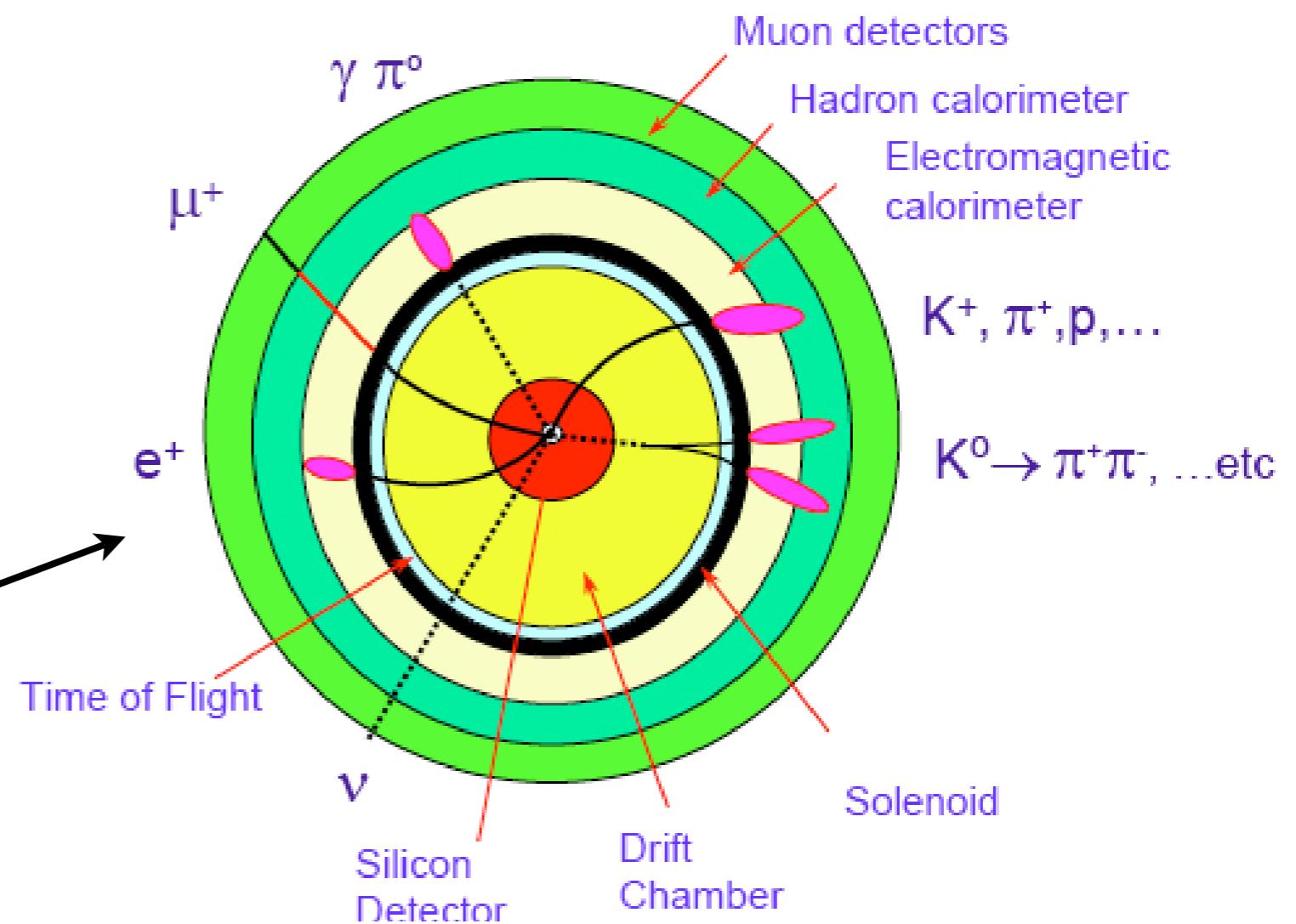
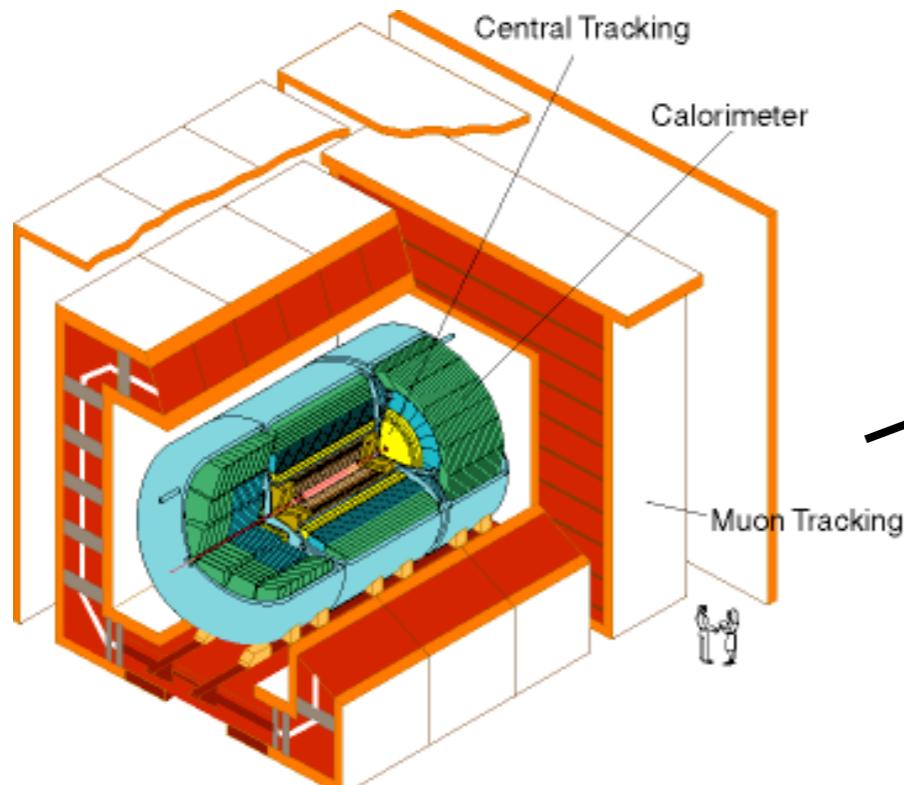
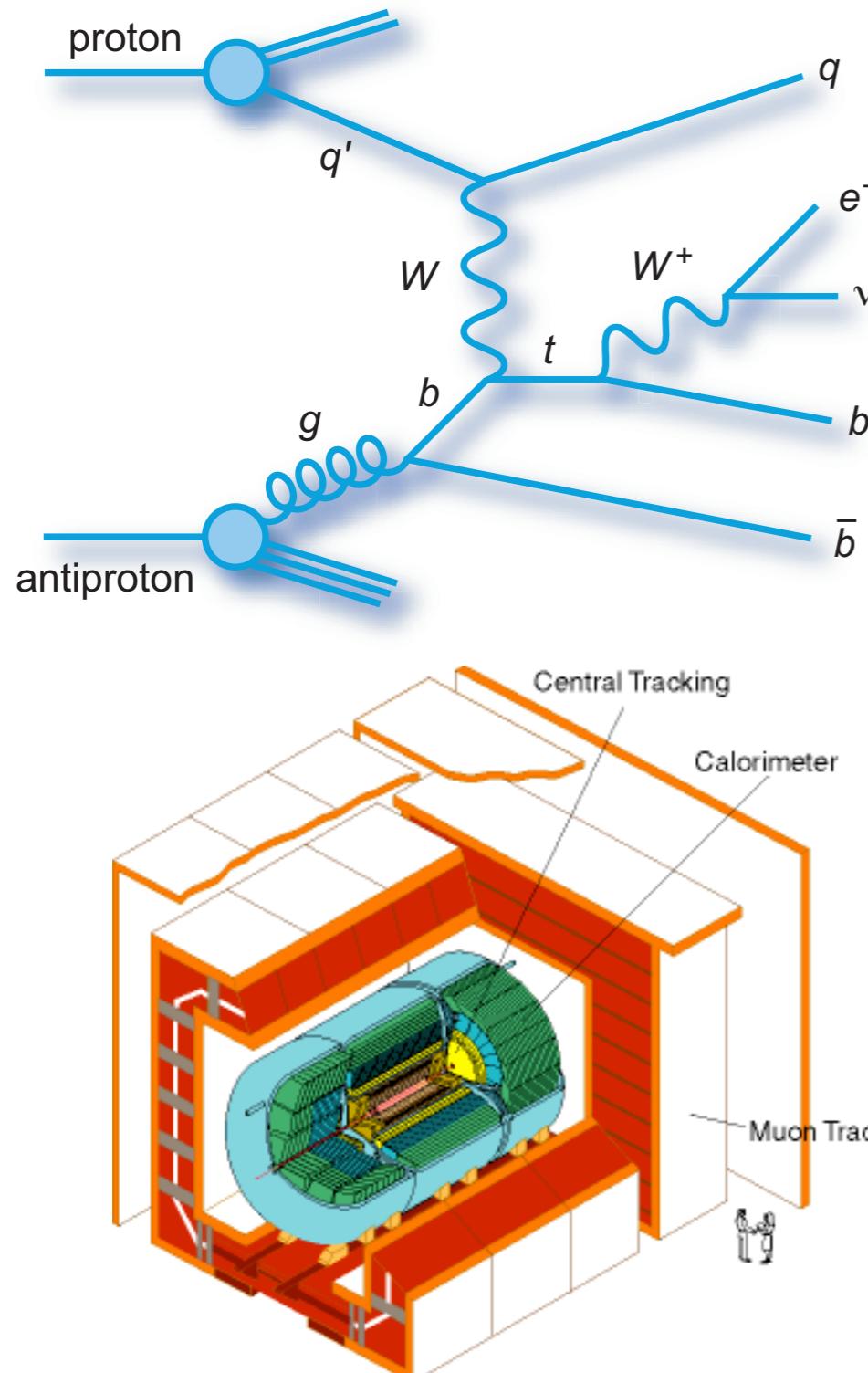


Single Top Analysis Flow



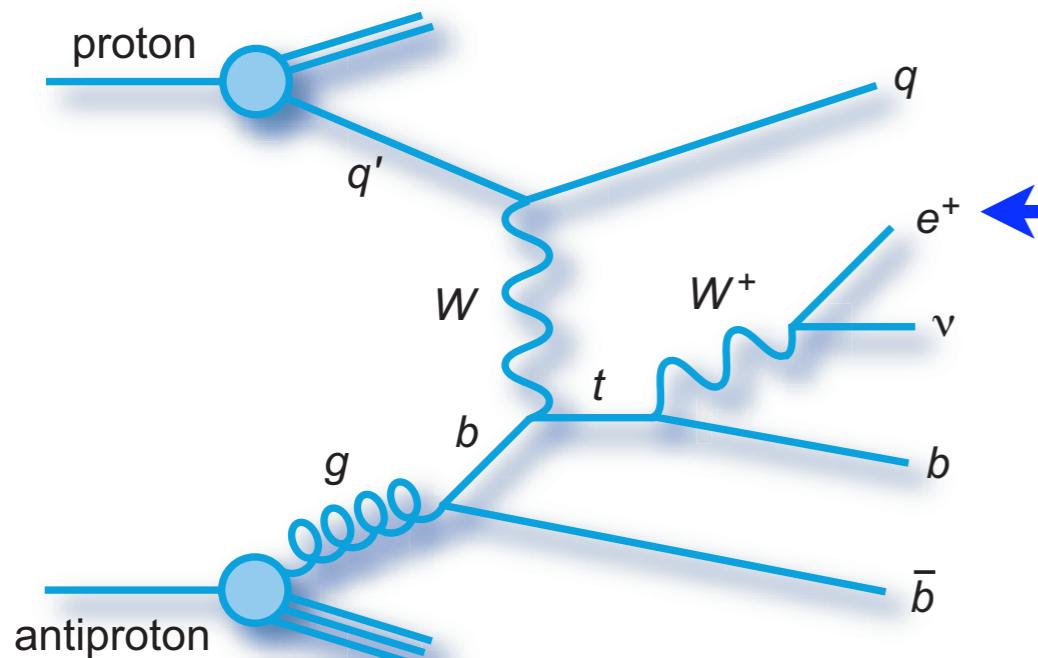
Event Reconstruction and Selection

We look for single top in the lepton+jets decay channel

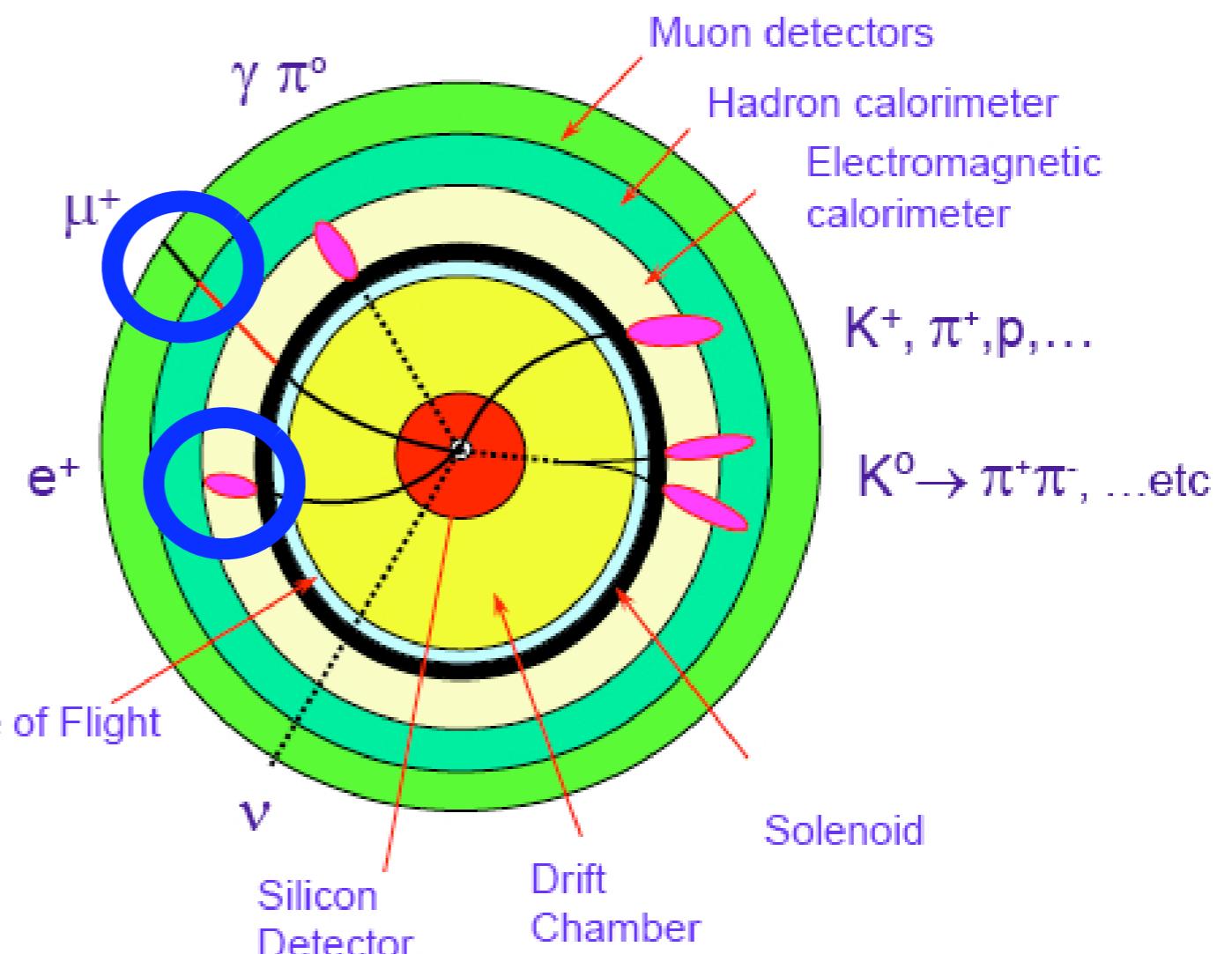


Event Reconstruction and Selection

We look for single top in the lepton+jets decay channel



Electron: Narrow tower in EM Cal
Muon: Hits in the muon system
Select: 1 lepton w/ $P_T > 15$ GeV

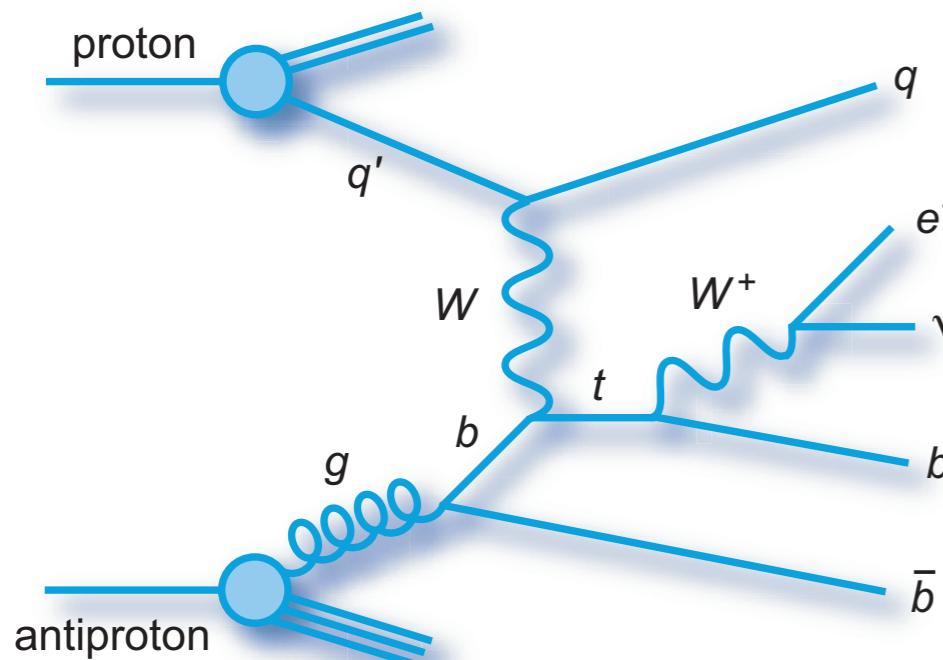


Event Selection

- 1 Lepton w/ $P_T > 15$ GeV

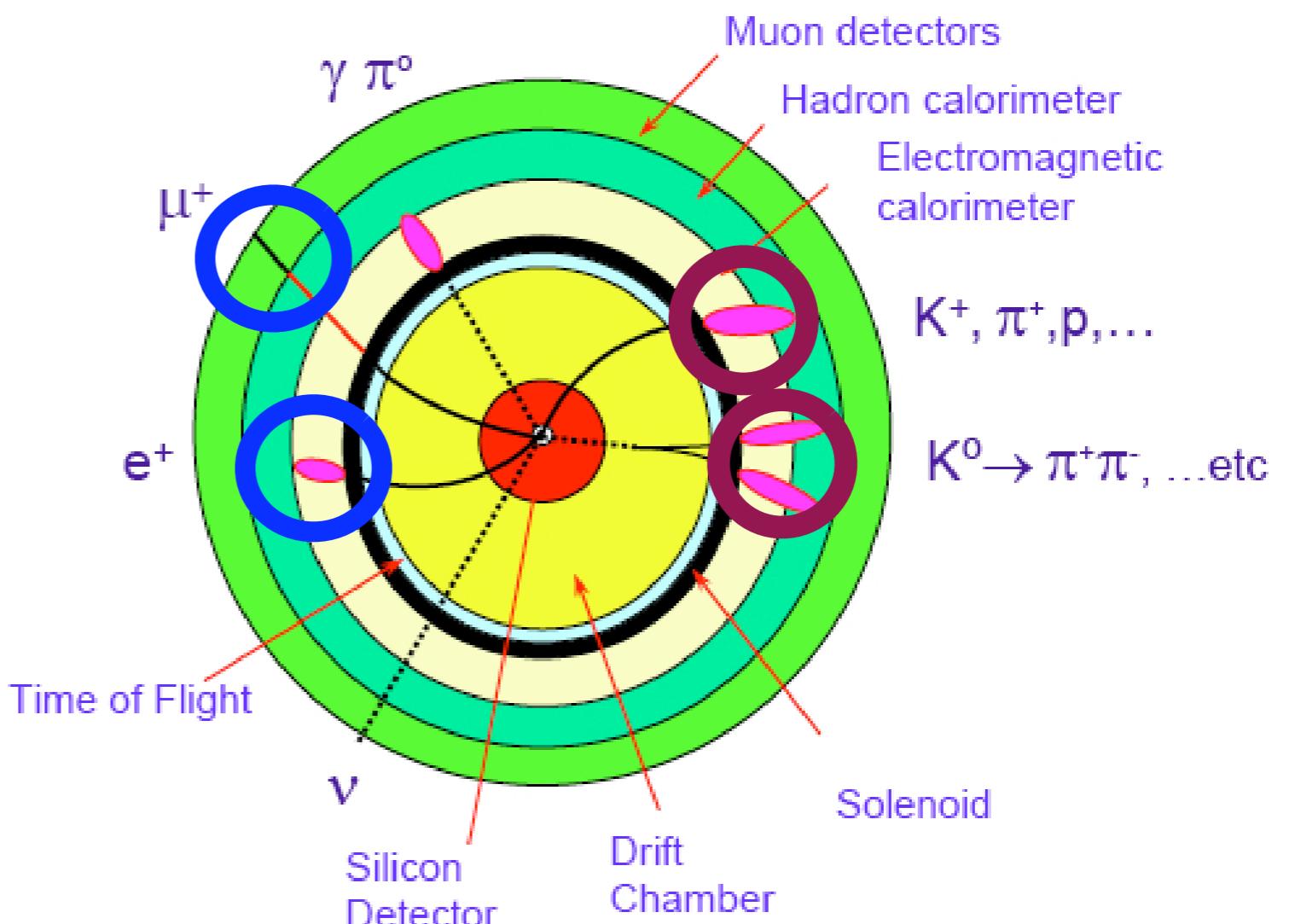
Event Reconstruction and Selection

We look for single top in the lepton+jets decay channel



Narrow cone of particles detected
in the calorimeter - "jet"
Select: 2-4 jets w/ $P_T > 15$ GeV

Electron: Narrow tower in EM Cal
Muon: Hits in the muon system
Select: 1 lepton w/ $P_T > 15$ GeV

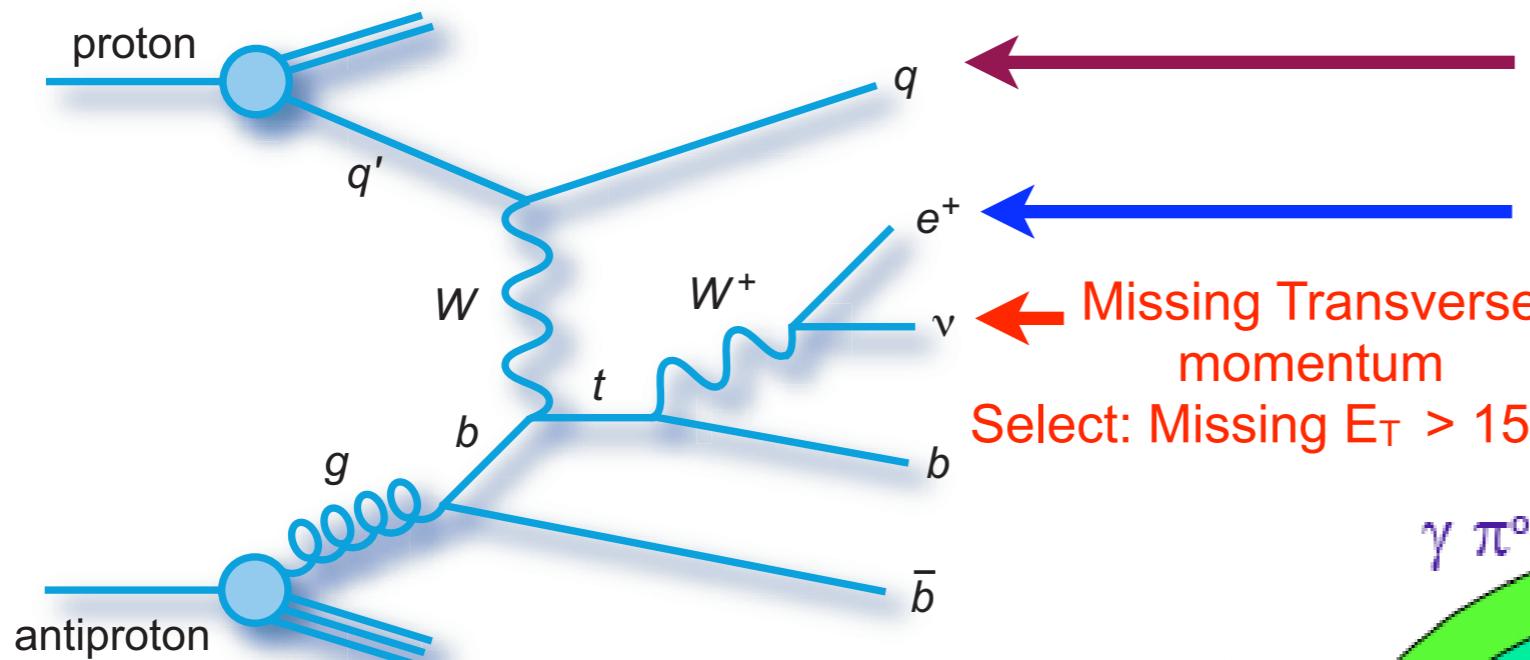


Event Selection

- 1 Lepton w/ $P_T > 15$ GeV
- 2-4 Jets w/ $P_T > 15$ GeV

Event Reconstruction and Selection

We look for single top in the lepton+jets decay channel



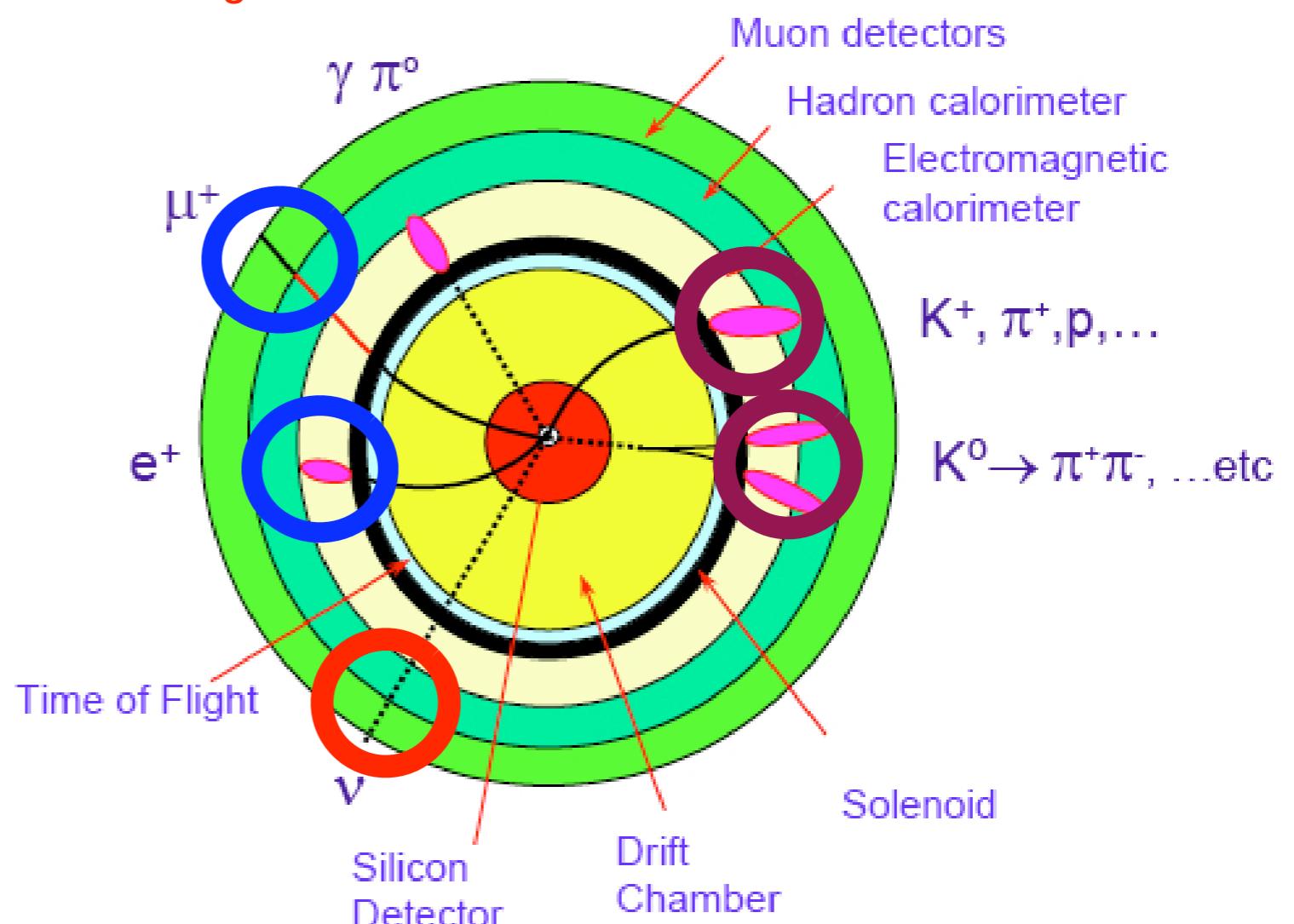
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Select: 2-4 jets w/ $P_T > 15$ GeV

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Select: 1 lepton w/ $P_T > 15$ GeV

Select: Missing $E_T > 15$ GeV

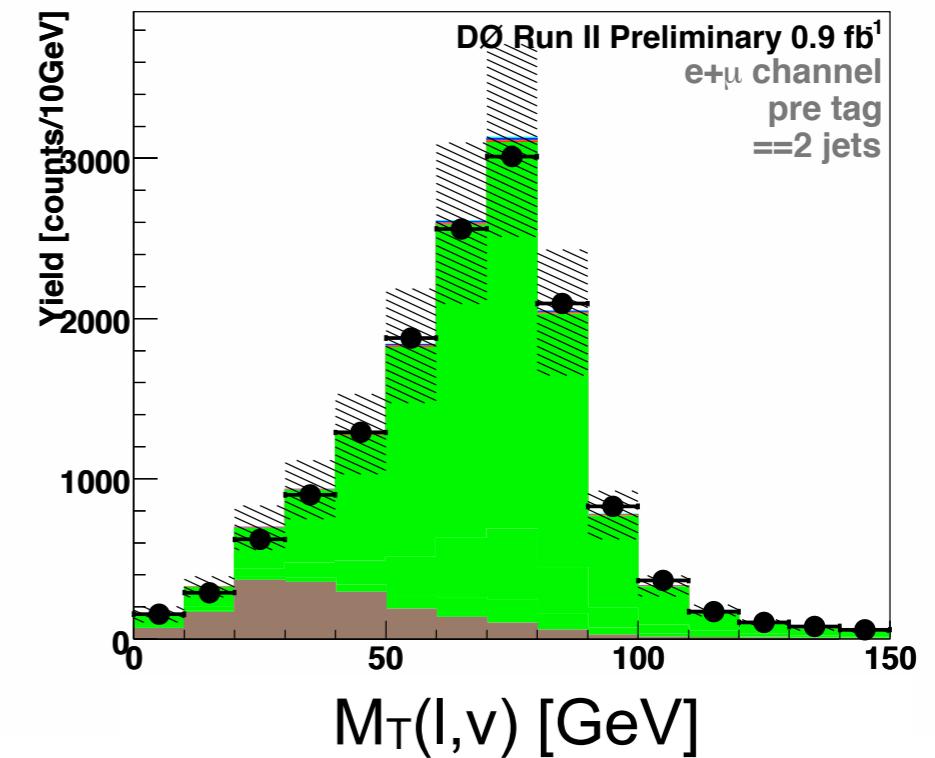
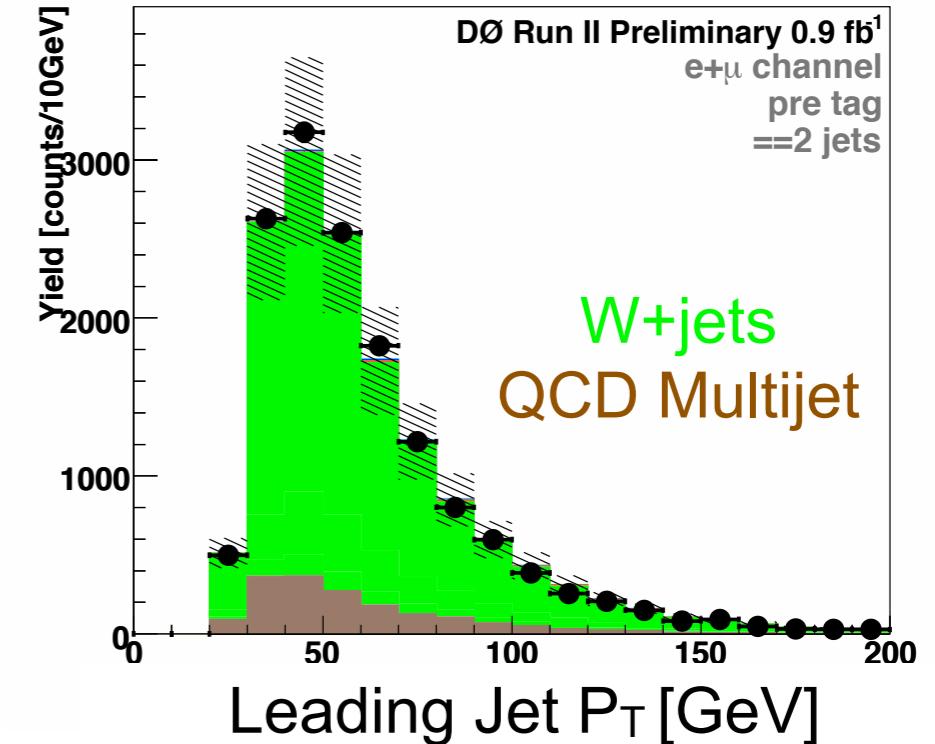
Event Selection

- 1 Lepton w/ $P_T > 15$ GeV
- 2-4 Jets w/ $P_T > 15$ GeV
- Missing $E_T > 15$ GeV



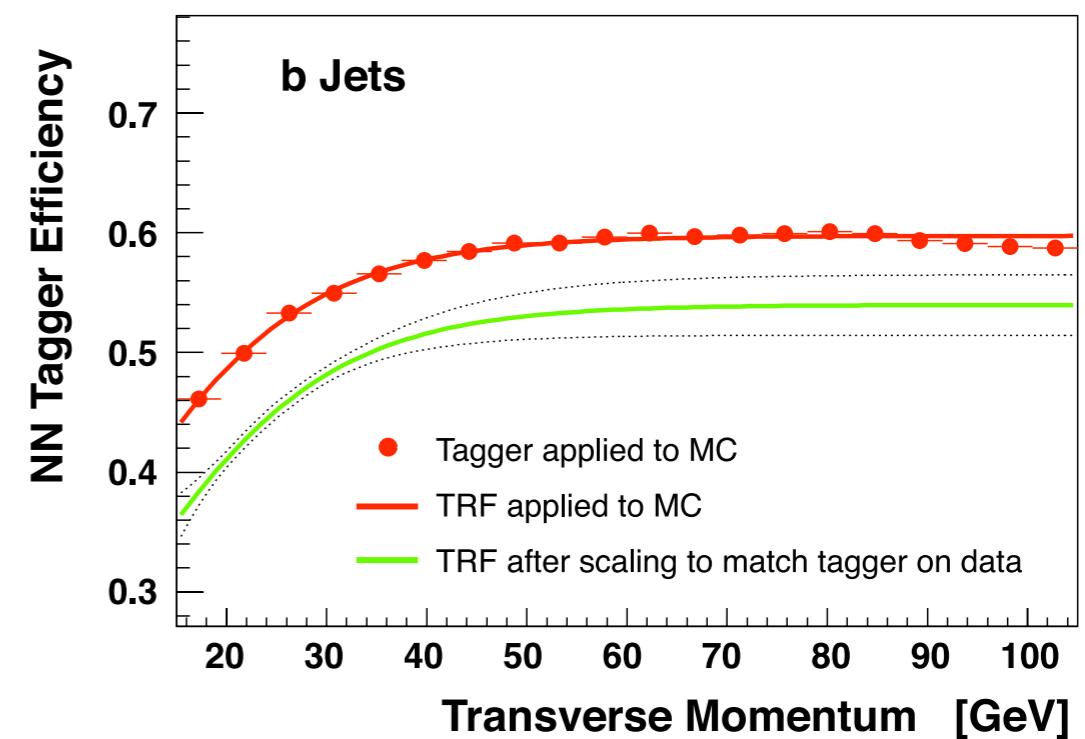
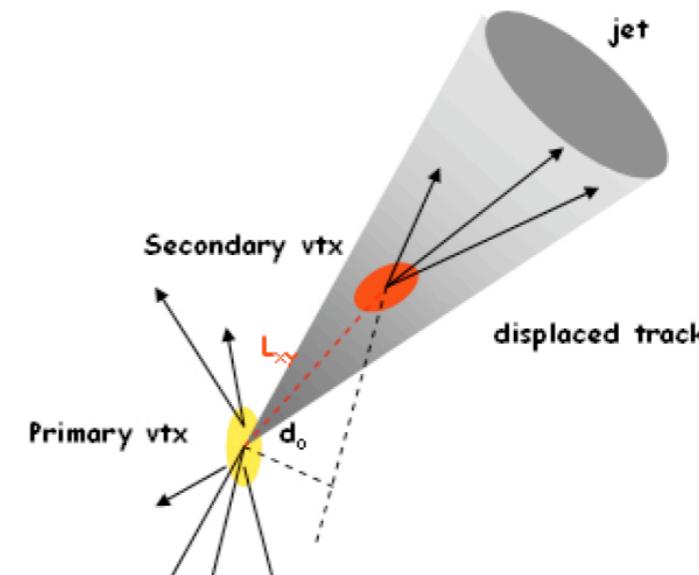
W+jets Background Normalization

- Large W+jets sample after event selection
 - Signal to Background $\sim 1:200$
 - Backgrounds are W+jets and QCD Multijet
- Normalize W+jets to data in low signal region
 - Shape taken from Monte Carlo
 - W+jets - ALPGEN w/ MLM matching
 - Multijet - data events
 - $\sigma'(W+jets) \sim 1.5 \times \sigma_{LO}$
 - W+cc(bb) scaled by an additional 1.5 (effective k factor) - Measured in data



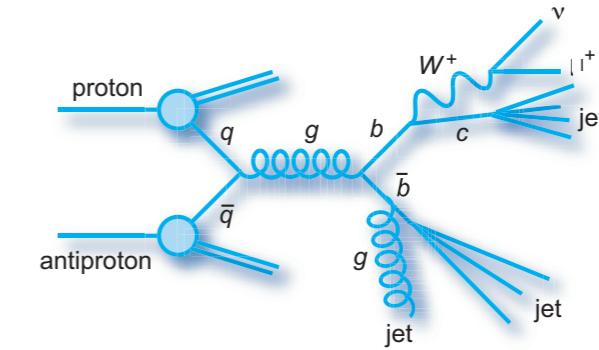
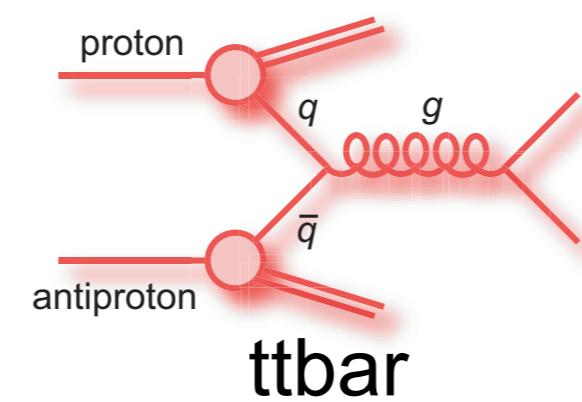
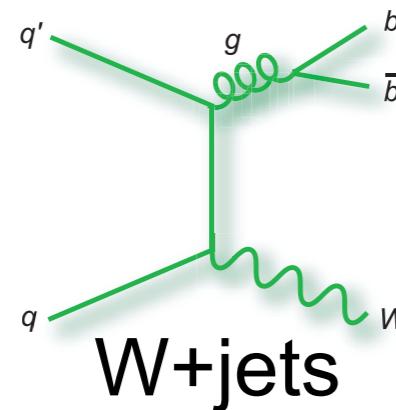
b-Tagging Algorithm

- Single top events have at least one *b* quark while largest background does not
- Would like to select events with ≥ 1 *b* quark. Need to know jet flavor.
- Use neural network trained on B Hadron Characteristics
 - Relatively long lived (weak decay)
→ Displaced decay vertex (\sim mm)
 - Higher track multiplicity
 - Relatively large $M(\text{tracks})$
- Apply tagging probability to MC (TRF) parameterized in P_T and η
 - TRF(*b* quark) $\sim 50\%$
 - TRF(*c* quark) $\sim 10\%$
 - TRF(*l* quark) $\sim 0.5\%$



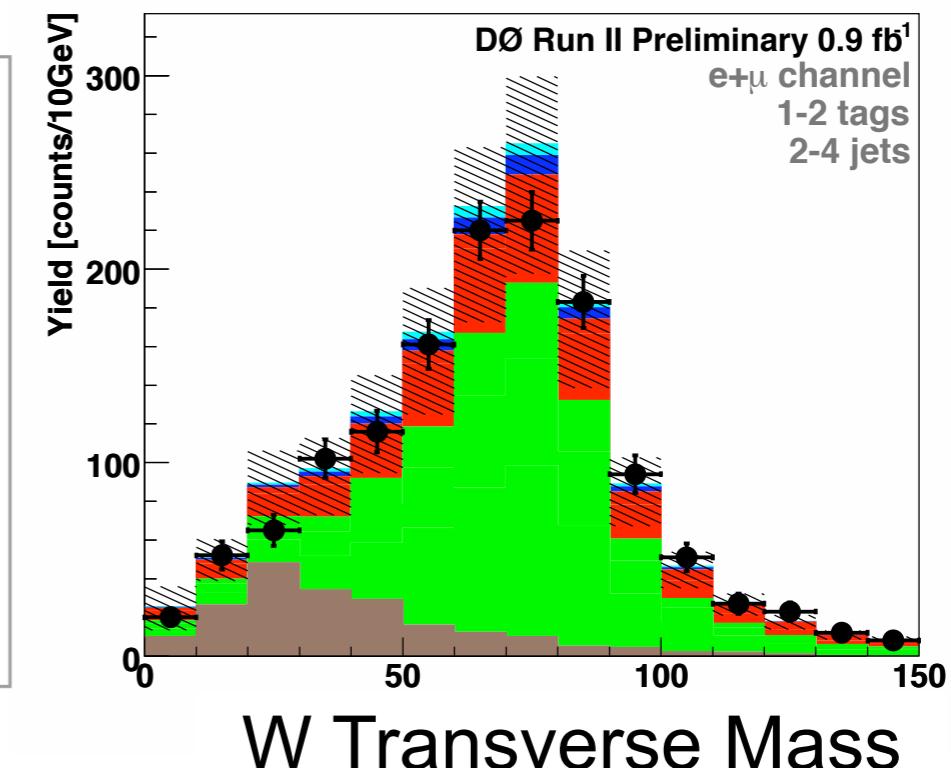
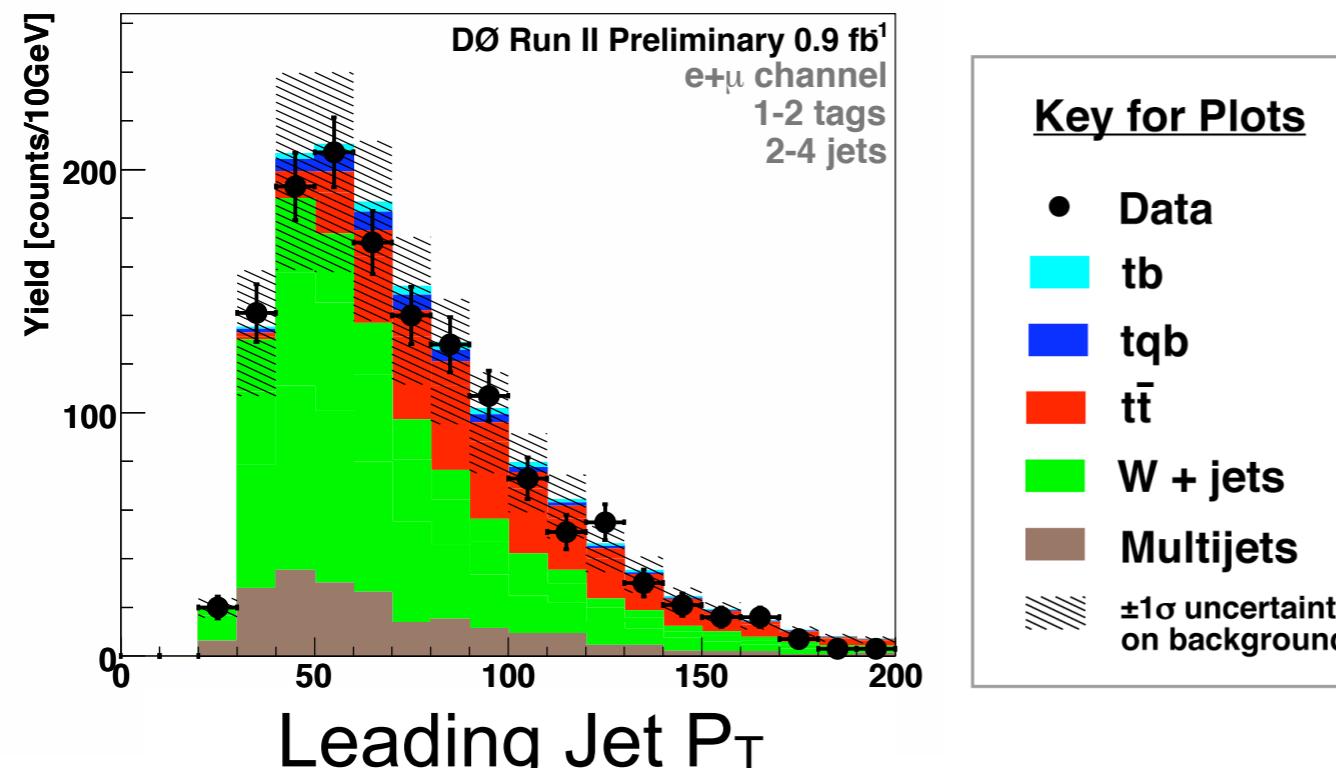
Backgrounds After b -Tagging

- Three main backgrounds after selecting events with ≥ 1 b -jet

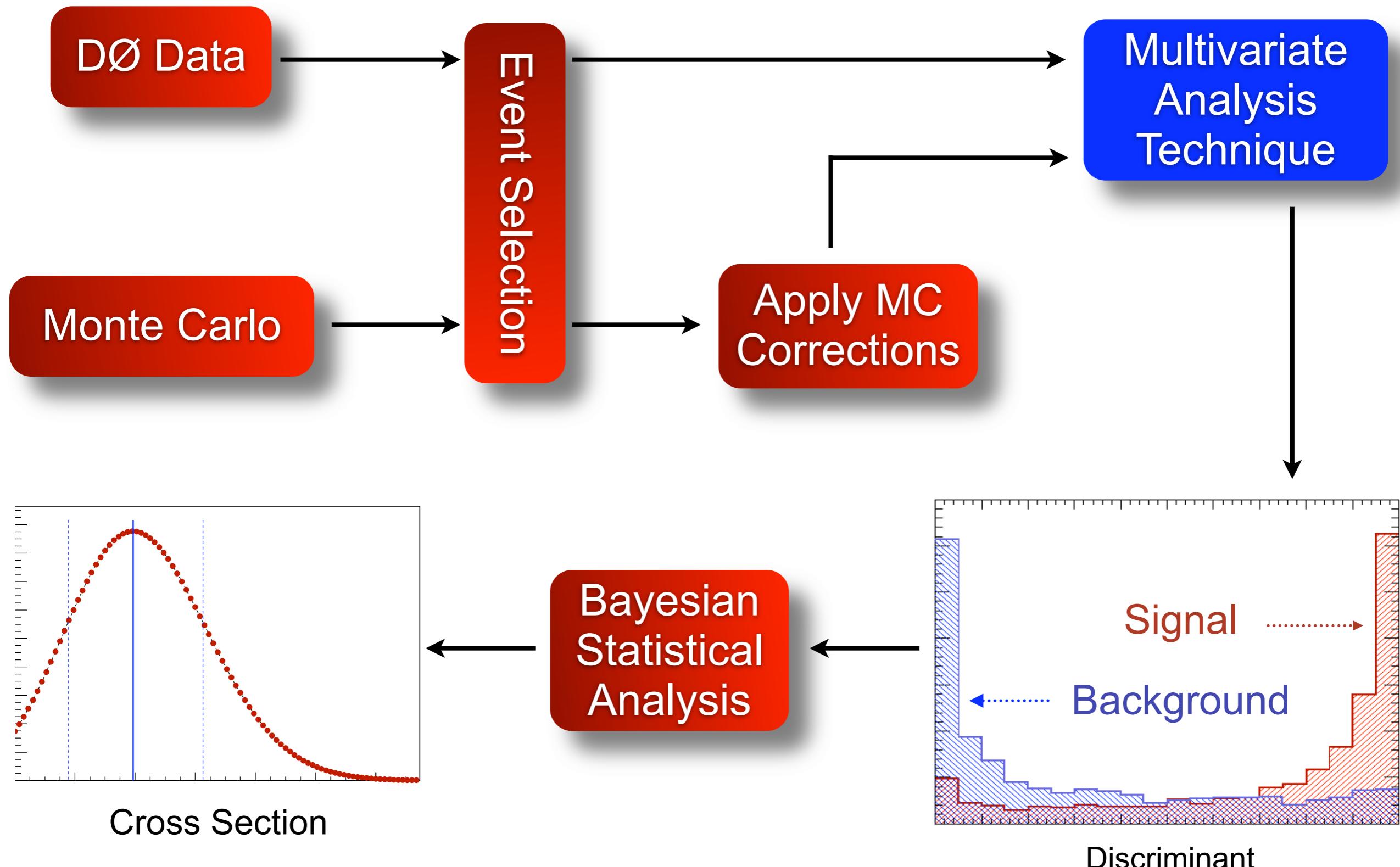


QCD Multijet

- $t\bar{t}$ is modeled using ALPGEN and normalized to NLLO cross section (6.8 pb)
- Good agreement between data and expectation after b -tagging

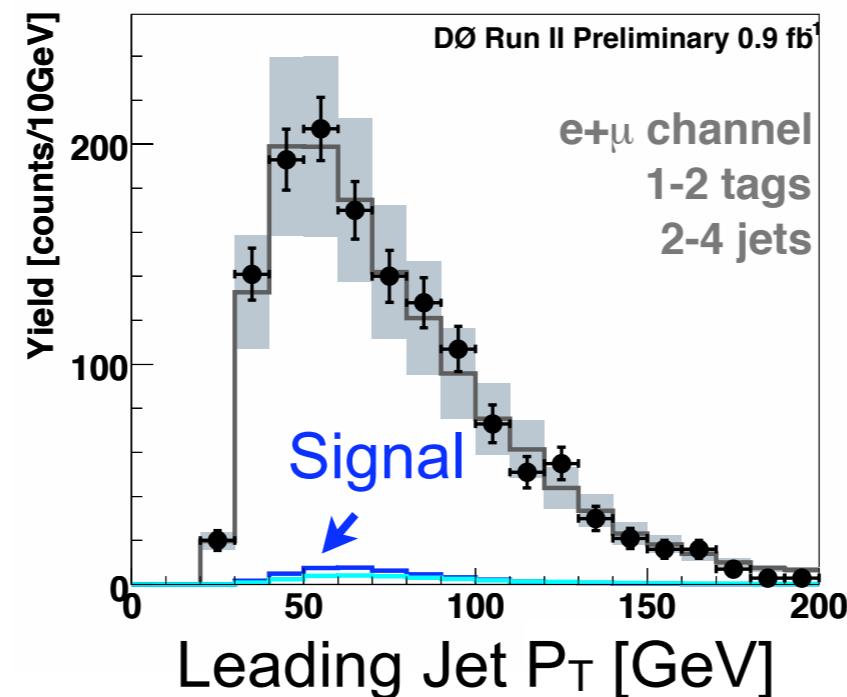


Single Top Analysis Flow

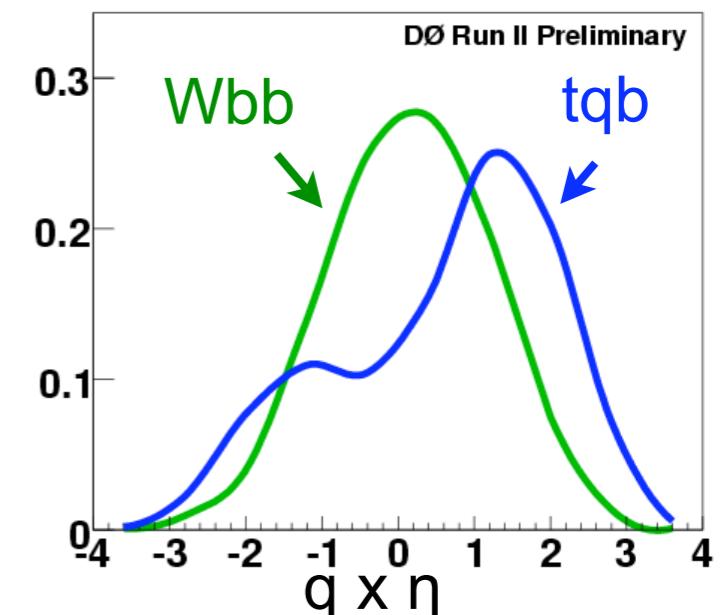


Motivation For Matrix Element Analysis

- Single top search suffers from large backgrounds after event selection
- After tagging, S:B $\sim 1:20$ and systematic errors $>$ signal \Rightarrow no counting experiment



- Common idea: Look at variables that separate signal and background
- Ex. charge of lepton $\times \eta$ of un-tagged jet
- Can combine variables into event probability using neural network, decision tree, etc...

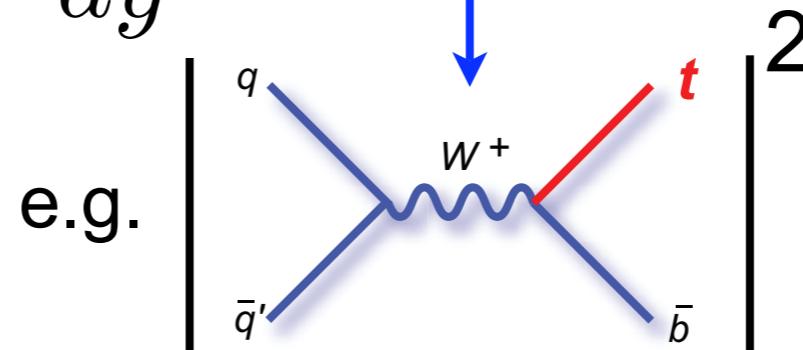


Matrix Element Analysis

- For each event, define a probability it originated from signal or background
- Define as the normalized N-dimensional differential cross section for process i

$$P_i(\vec{y}) \equiv \frac{1}{\sigma_i} \frac{d\sigma_i}{dy} ; \frac{d\sigma_i}{dy} \propto |\mathcal{M}_i|^2 ; i = S, B$$

- $\mathbf{y} \equiv$ parton-level four-vectors



- Account for detector by convoluting with detector resolution function
- Map parton state (\mathbf{y}) to detector state (\mathbf{x})

$$P_i(\vec{x}) \equiv \frac{1}{\sigma_i} \int \frac{d\sigma_i}{dy} \times W(\vec{x}|\vec{y}) dy$$

- $W(\mathbf{x}|\mathbf{y})$ is called the transfer function

Matrix Element Analysis

- For each event compute the following detector level differential cross section

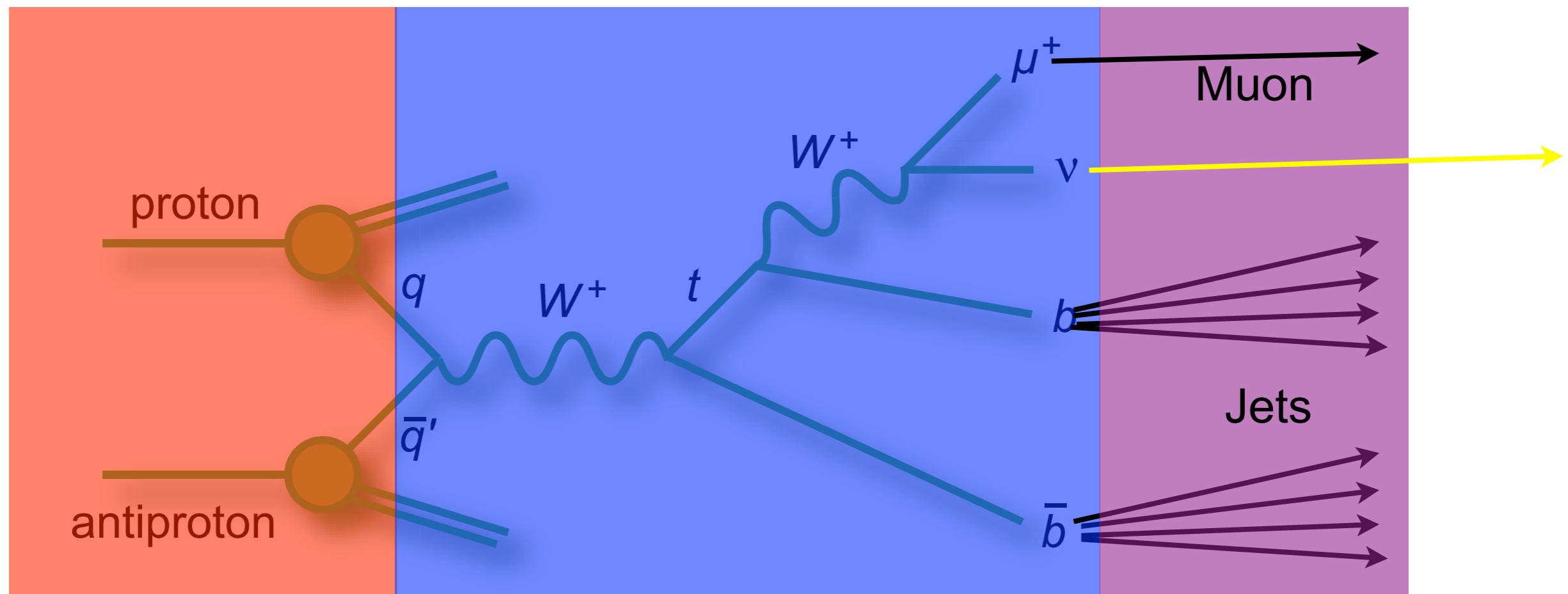
$$\underbrace{\frac{d\sigma}{d\vec{x}}}_{\text{Detector level differential cross section}} \propto \int \underbrace{\frac{f(q_1)}{q_1} \frac{f(q_2)}{q_2} dq_1 dq_2}_{\text{CTEQ6 Parton distribution functions}} \times \underbrace{|\mathcal{M}(\vec{y})|^2 d\Phi(\vec{y})}_{\text{LO matrix elements from Madgraph times PS factor}} \times \underbrace{W(\vec{y}|\vec{x})}_{\text{Map parton state } \mathbf{y} \text{ onto detector state } \mathbf{x}}$$

Detector level differential cross section

CTEQ6 Parton distribution functions

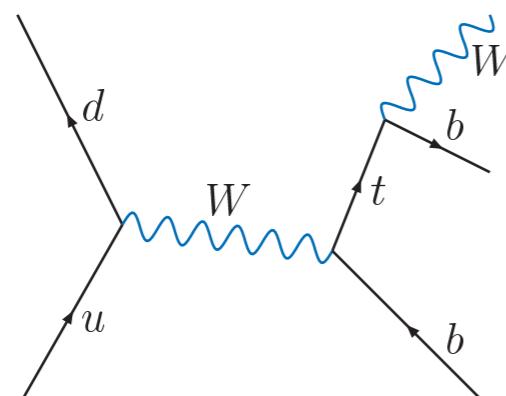
LO matrix elements from Madgraph times PS factor

Map parton state \mathbf{y} onto detector state \mathbf{x}

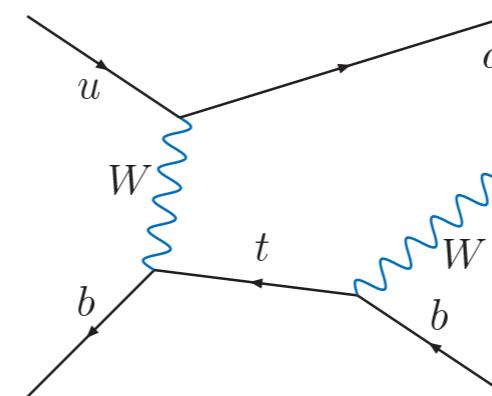


Signal & Background Processes

- Must match number of jets to number of generated partons
- Signal Processes

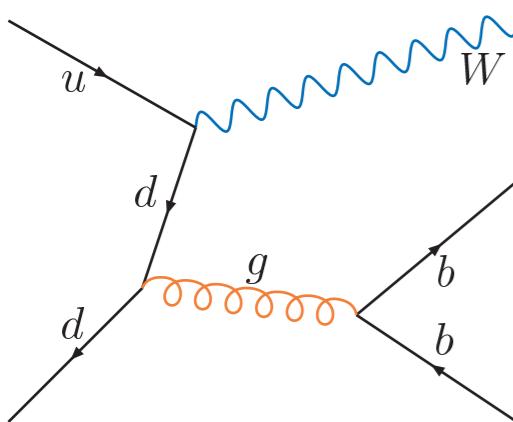


s-channel w/ 2 jets

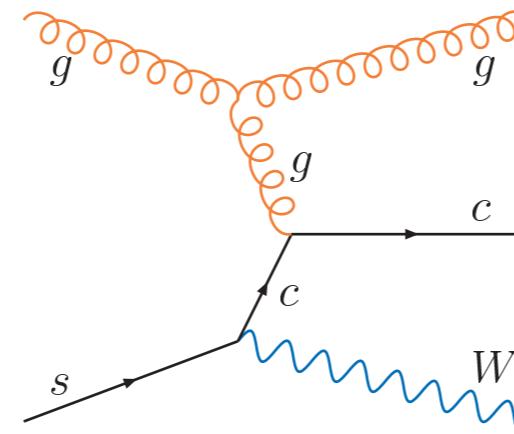


t-channel w/ 2 jets

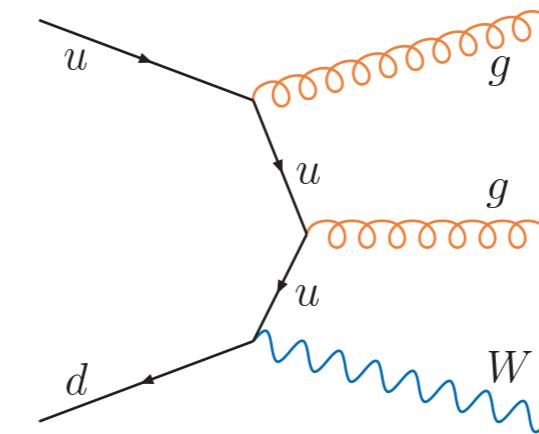
- Background Processes



Wbb w/ 2 jets



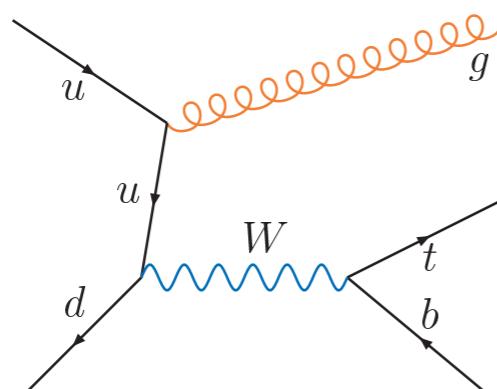
Wcg w/ 2 jets



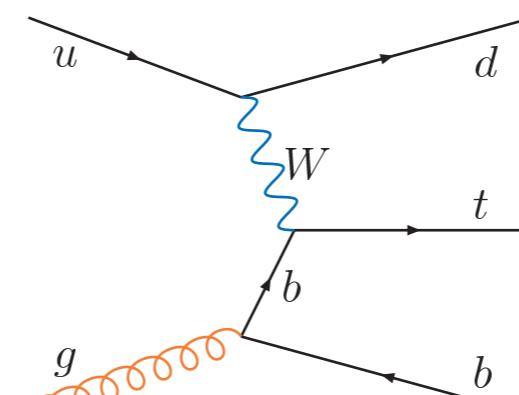
Wgg w/ 2 jets

Signal & Background Processes

- Must match number of jets to number of generated partons
- Signal Processes

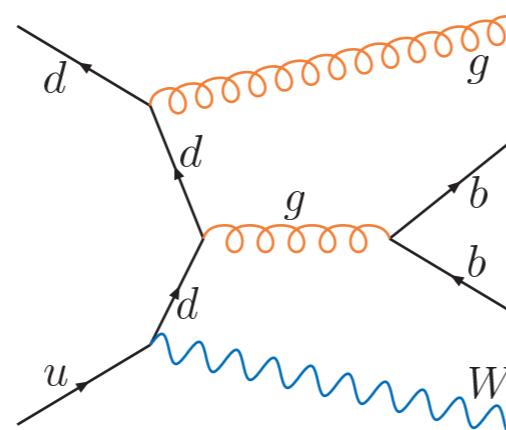


s-channel w/ 3 jets



t-channel w/ 3 jets

- Background Processes



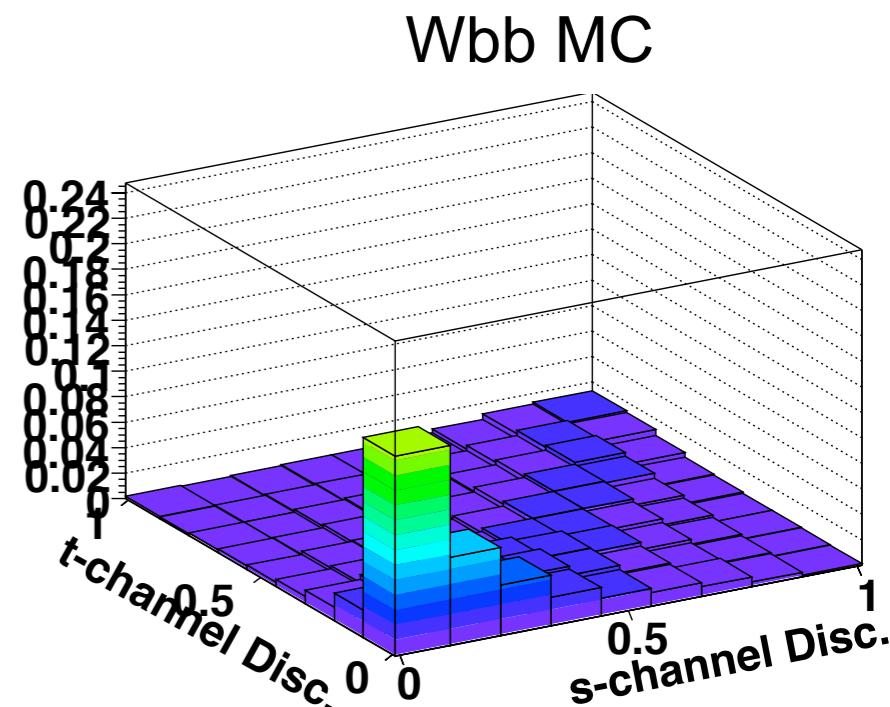
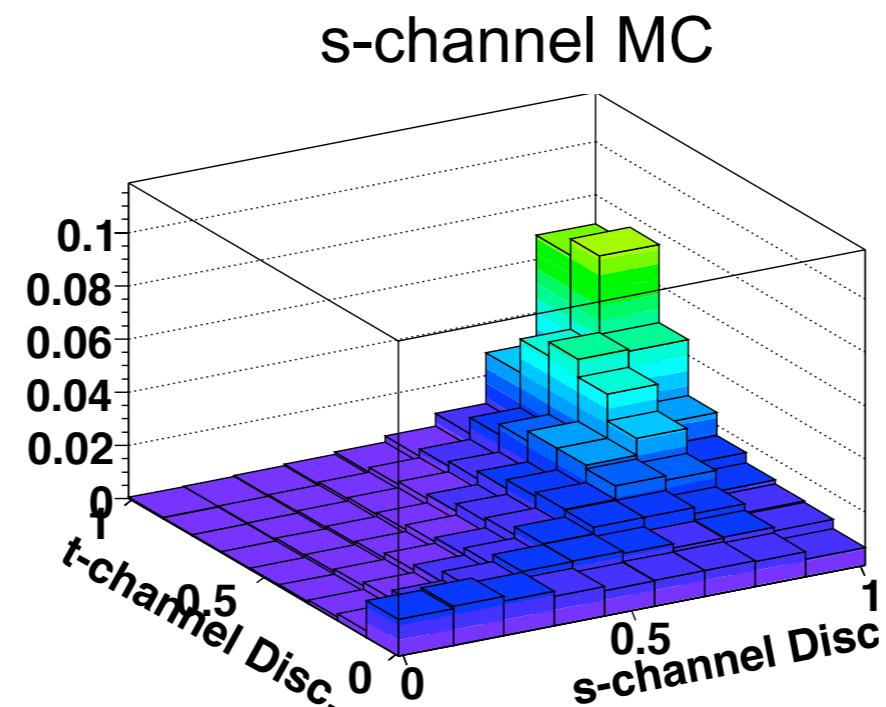
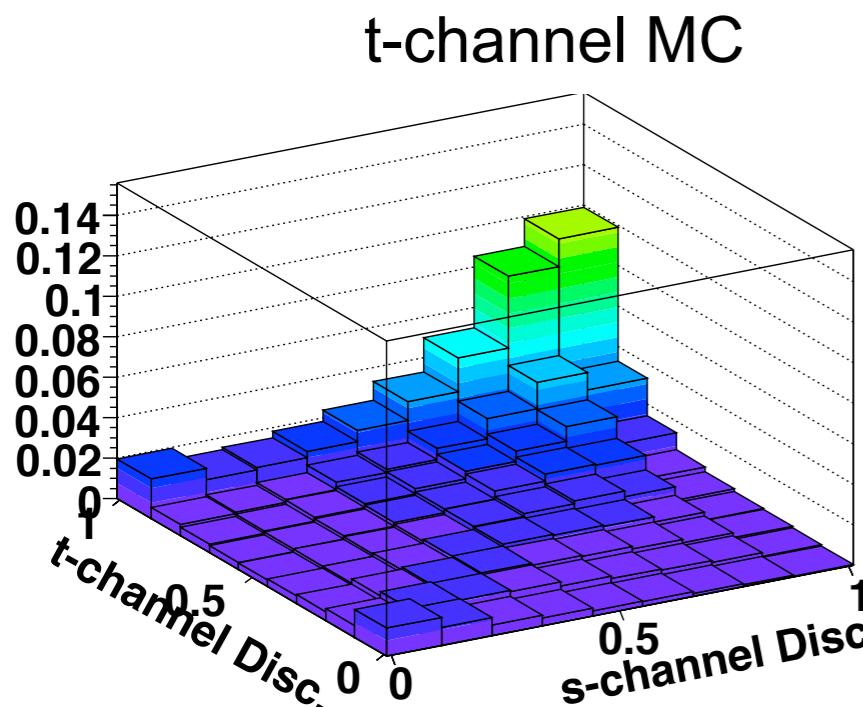
$Wbbg$ w/ 3 jets

Matrix Element Discriminant

- Combine signal and background probability densities using the *a-posteriori* Bayesian probability density for signal given the event
- Two discriminants: s-channel as signal and t-channel as signal

$$D_{tb|tqb}(\vec{x}) = \frac{P_{tb|tqb}(\vec{x})}{P_{tb|tqb}(\vec{x}) + P_{\text{Background}}(\vec{x})}$$

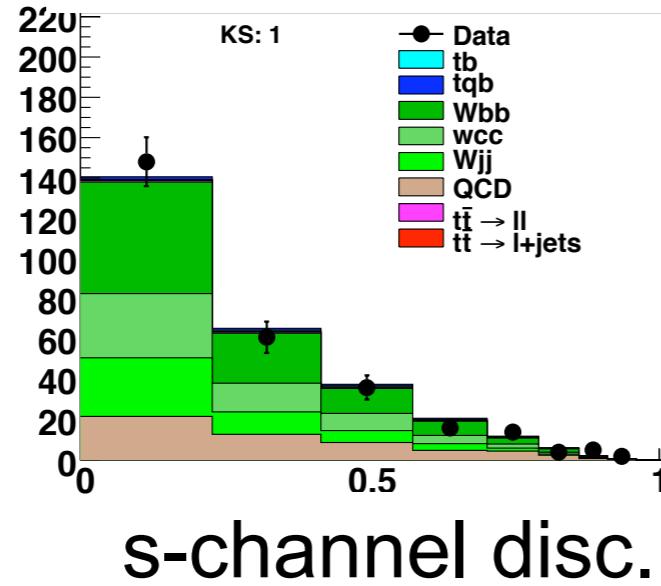
- Result: Nice separation of signal and background



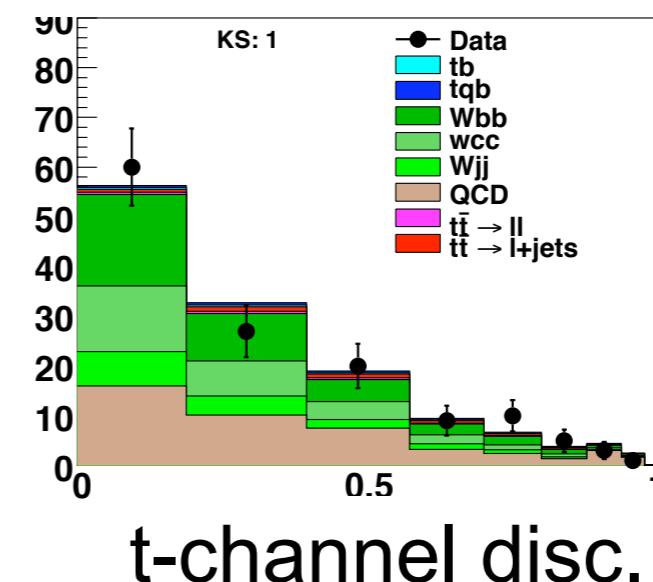
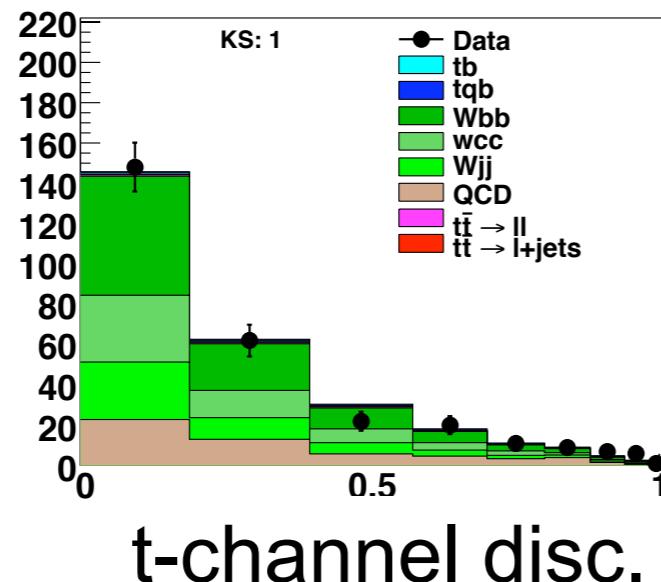
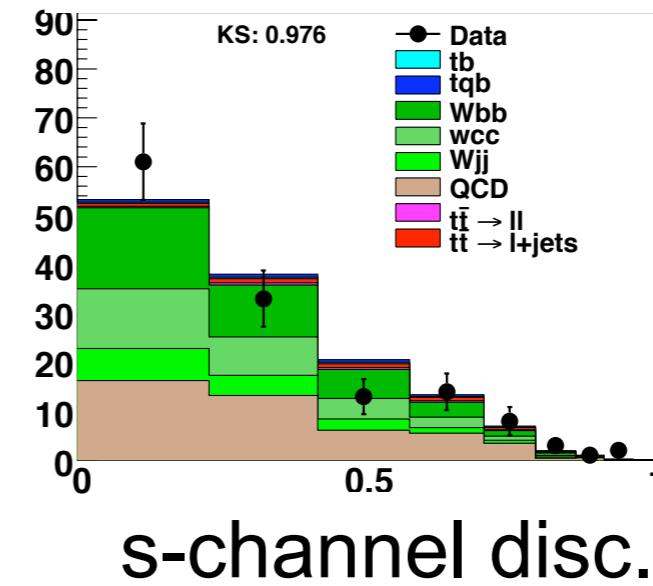
Cross Check W+jets Estimation

- Calculate discriminant in regions with little signal to cross check background
- Define: W+jets sample ($H_T < 175$ GeV) $H_T = \sum_{\text{jets}} P_T(\text{jet}) + P_T(e, \mu) + E_T$

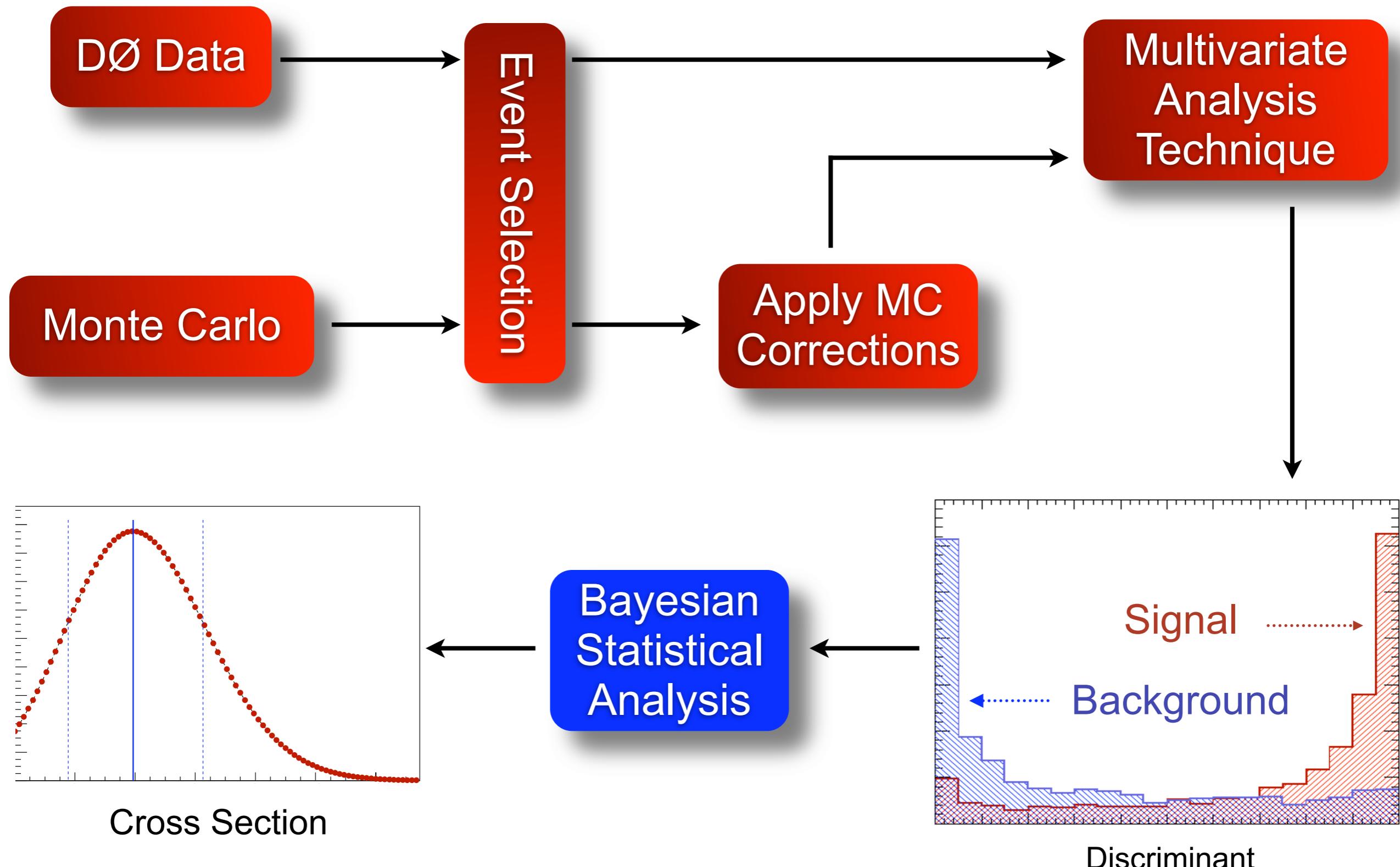
Events with 2 jets



Events with 3 jets



Single Top Analysis Flow

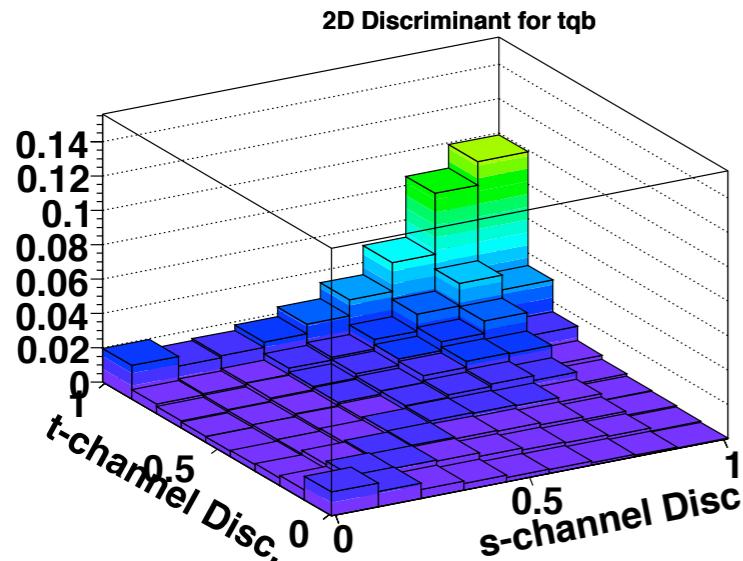


Cross Section Measurement Method

- ➊ Determine cross section by calculating the Bayesian posterior density function
 - ➋ Question: What is the probability density for the cross section given the data?

$$P(\sigma|N_{obs}) = \underbrace{\beta}_{\text{Normalization}} \times \underbrace{\int \mathcal{L}(N_{obs}|\alpha, n_B, \sigma) \times \pi(\alpha, n_B) \pi(\sigma) d\alpha dn_B}_{\text{Integrate over "nuissance" parameters}}$$

$$\mathcal{L}(N_{obs}|n_{exp}) = \frac{n_{exp}^{N_{obs}} e^{-n_{exp}}}{N_{obs}!}$$



Acceptance and Background Prior

- Sample multivariate Gaussian with
 $\mu=[\alpha, n]$ and $\sigma=[\delta\alpha, \delta n]$
(next slide)

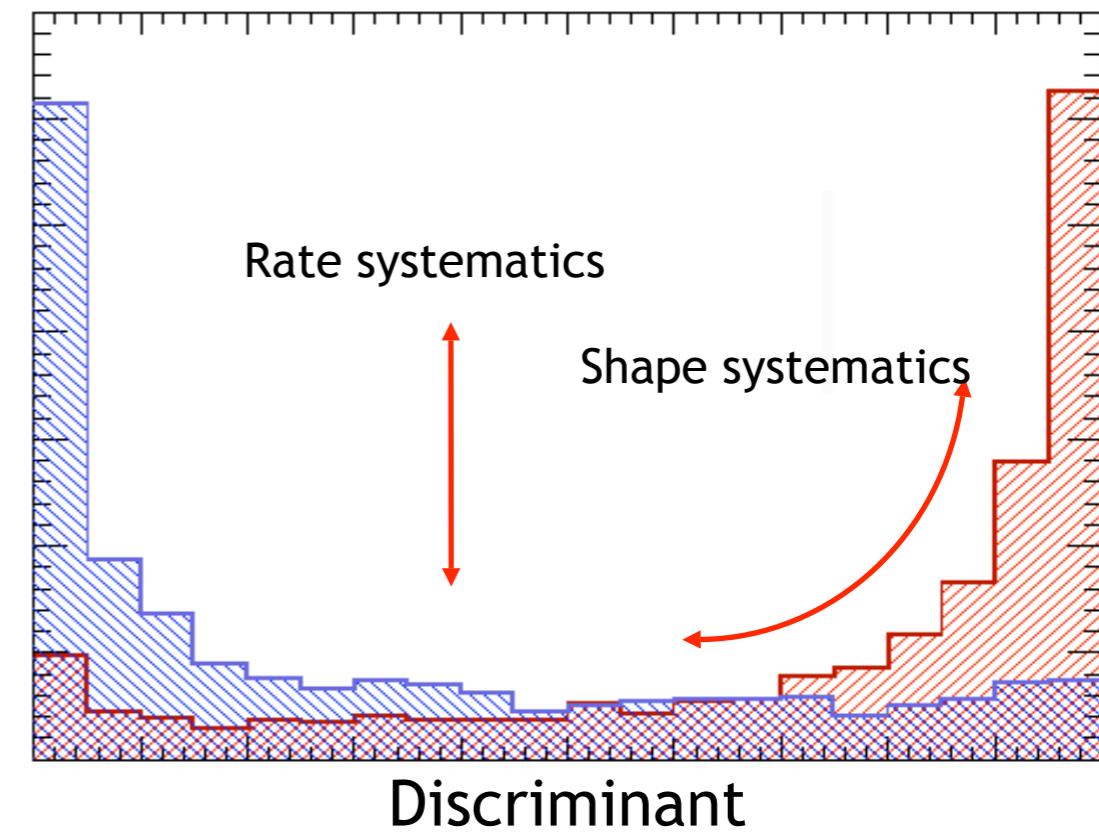
Cross Section Prior

$$\pi(\sigma) = \frac{1}{\sigma_{\max}}, 0 < \sigma < \sigma_{\max}$$

Systematic Errors

- Uncertainty in model, energy scale, or normalization affect signal and background yields → uncertainty on cross section
- Size of systematic determined by rerunning analysis with ± 1 sigma errors
- Systematics in **BLUE** and **GREEN** affect rate and **RED** affects rate and shape

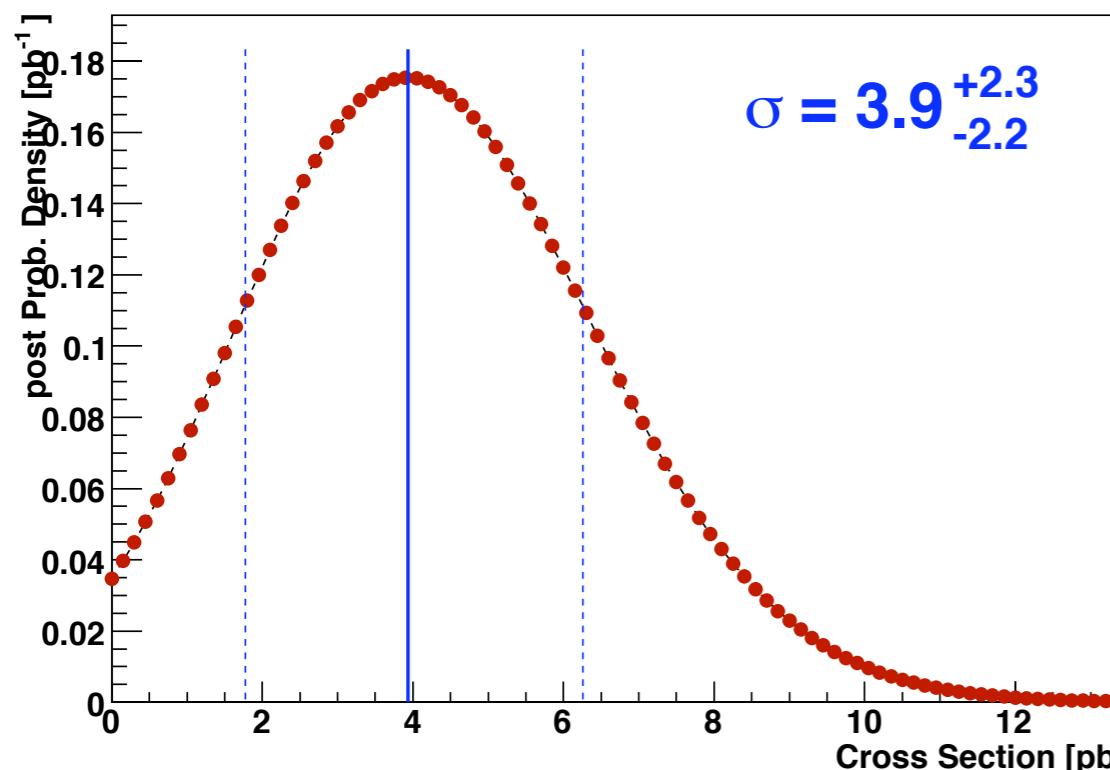
Source of Uncertainty	Size
Top pairs normalization	18%
W+jets & multijets normalization	18–28%
Integrated luminosity	6%
Trigger modeling	3–6%
Lepton ID corrections	2–7%
Jet modeling	2–7%
Other small components	Few %
Jet energy scale	1–20%
Tag rate functions	2–16%



Cross Section Measurement Method

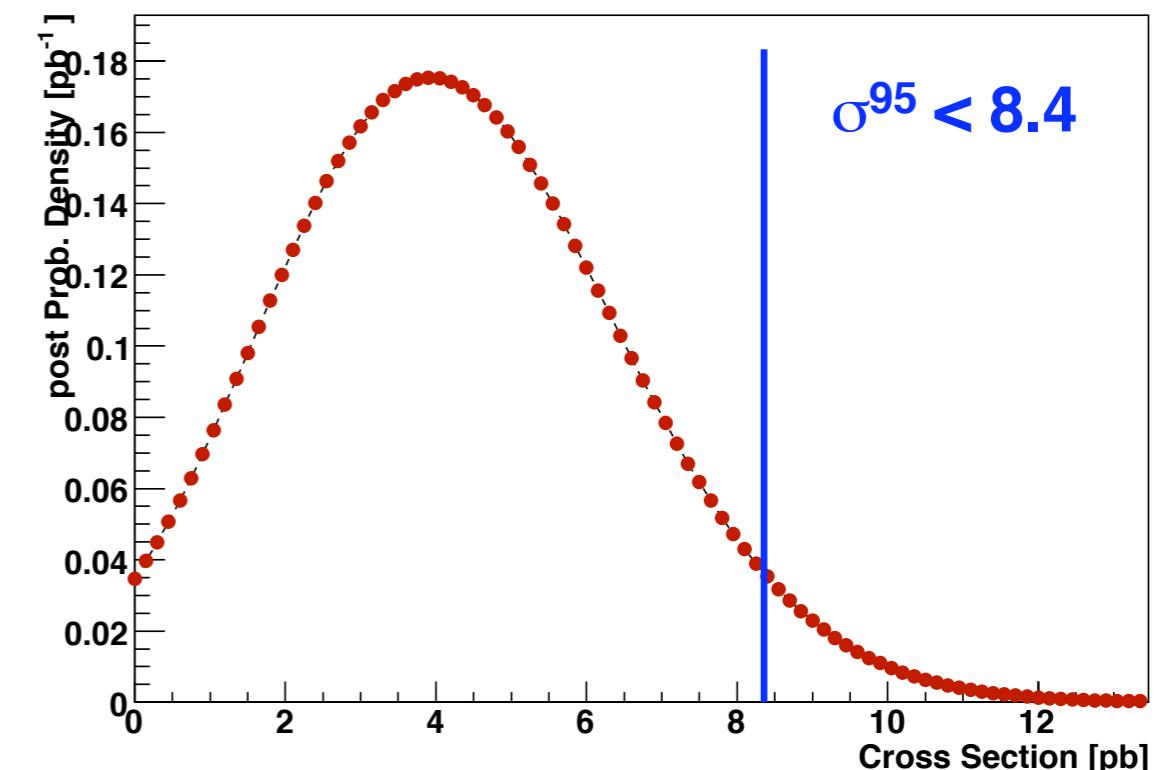
- Two possibilities: (1) excess of data over background and (2) no excess

Bayesian Posterior Density Function



excess → cross section

Bayesian Posterior Density Function

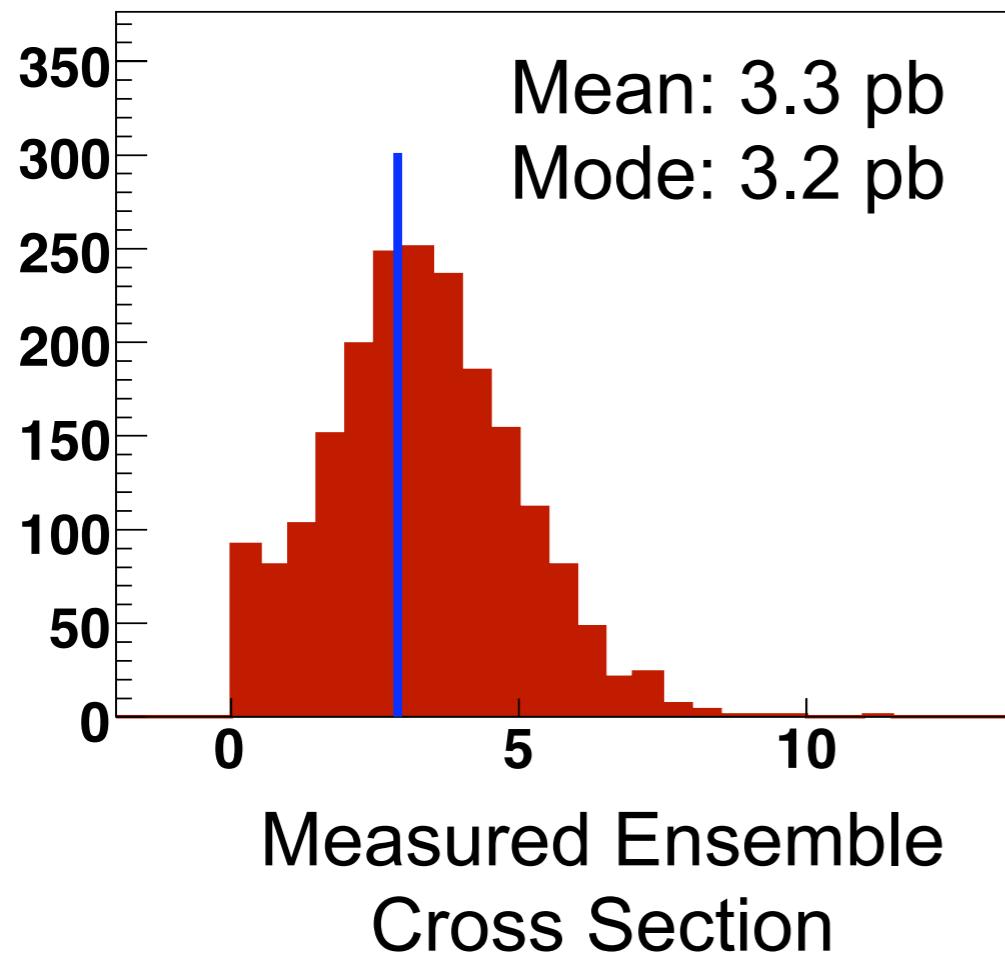


no excess → upper limit

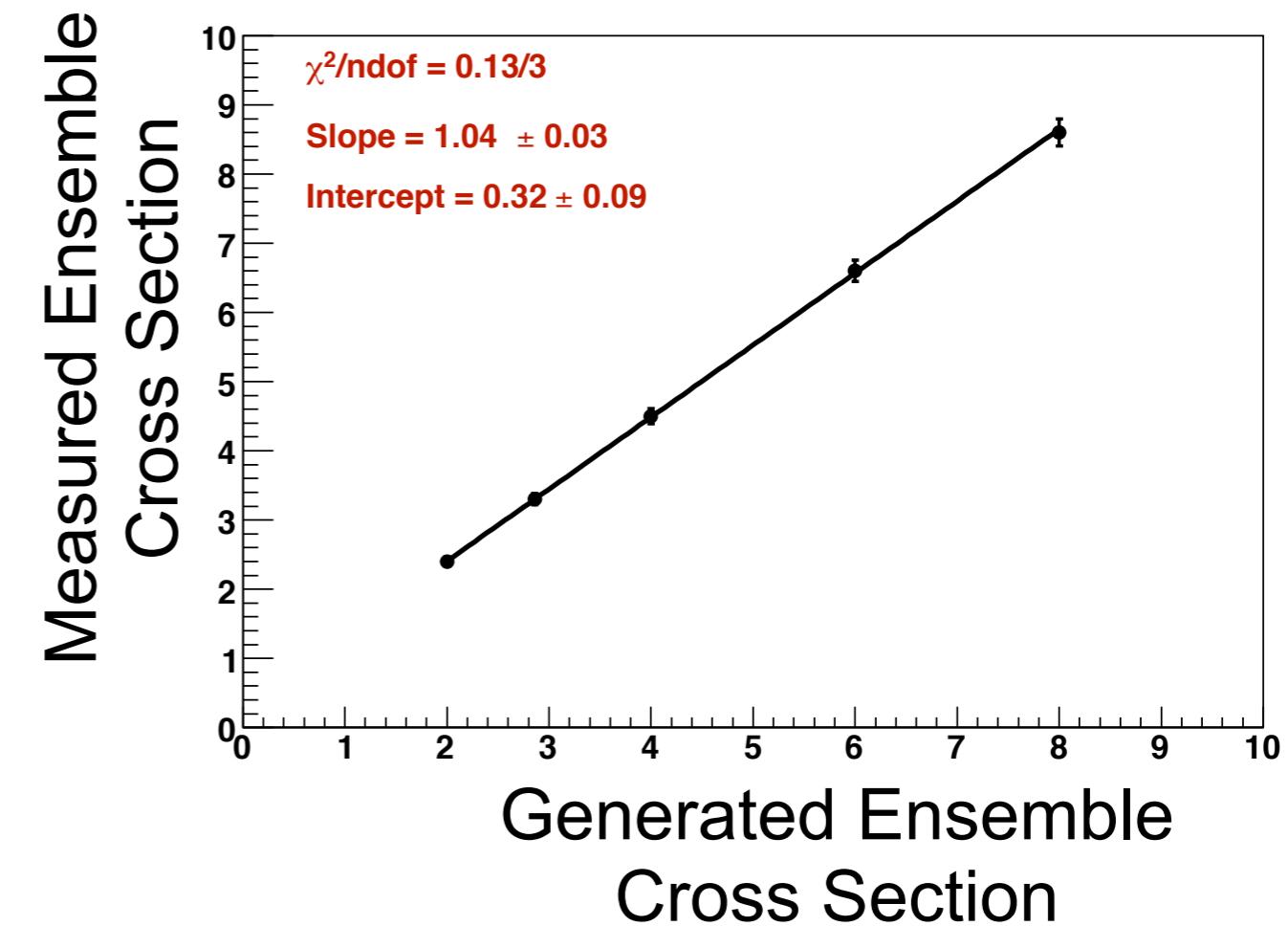
Linearity of Cross Section Measurement

- Test procedure before running on data
- Create ensembles with known signal fraction and measure cross section
- Plot: input vs measured cross section

Standard Model
Ensemble: $\sigma = 2.9 \text{ pb}$

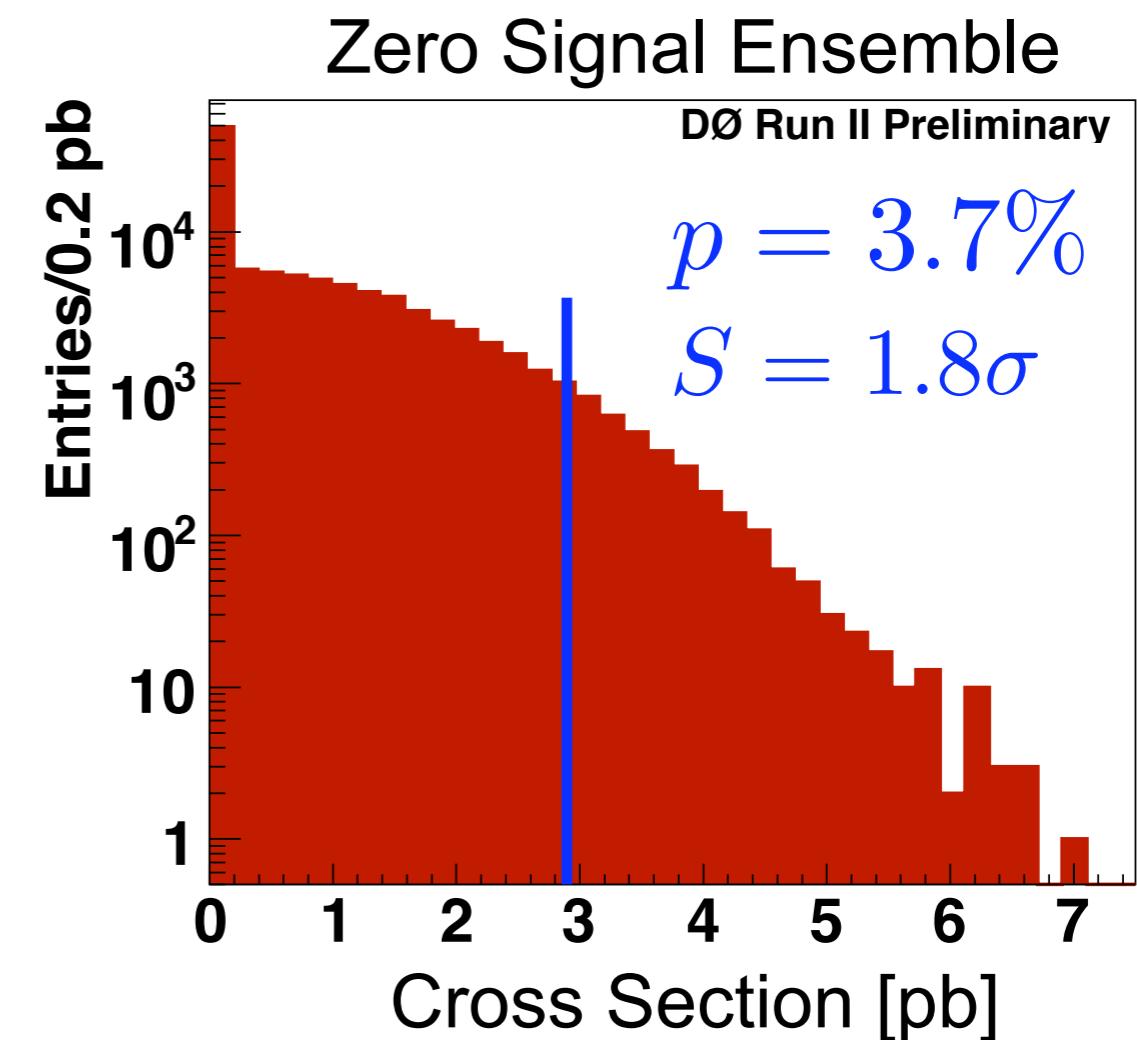
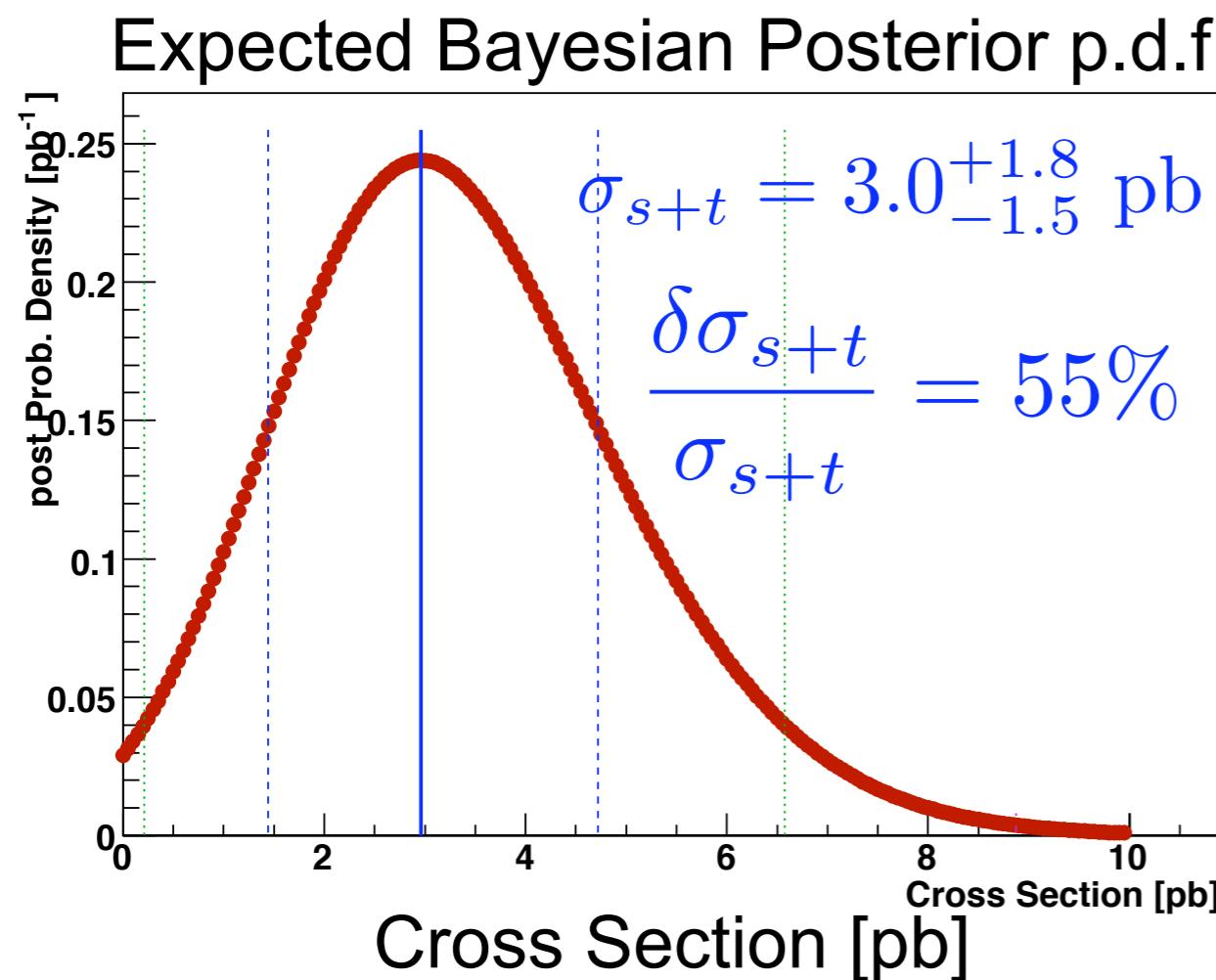


Linearity of Measurement



Expected Cross Section Resolution

- Check expected cross section resolution
 - Perform analysis with $N_{\text{obs}} = N_{\text{signal}} + N_{\text{back}}$
- Check sensitivity to background fluctuation
 - Create ensemble with zero signal fraction. Calculate p -value for SM single top



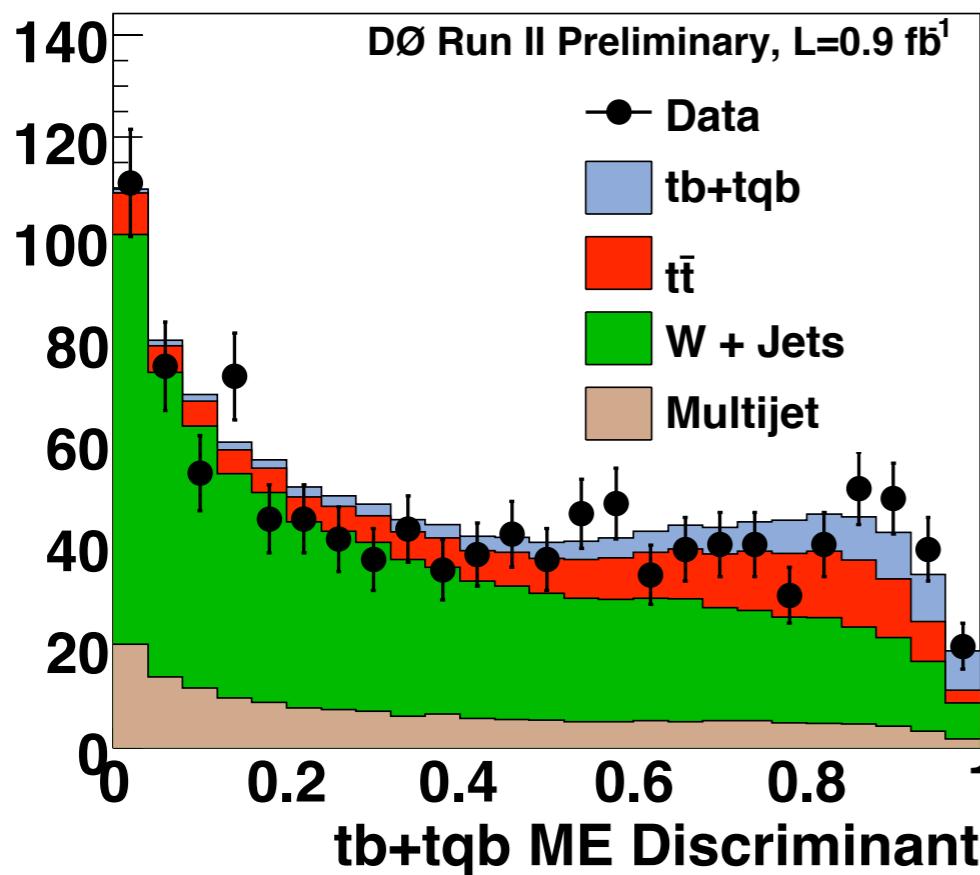
Results with $\sim 1 \text{ fb}^{-1}$

Excess of Data Above Background

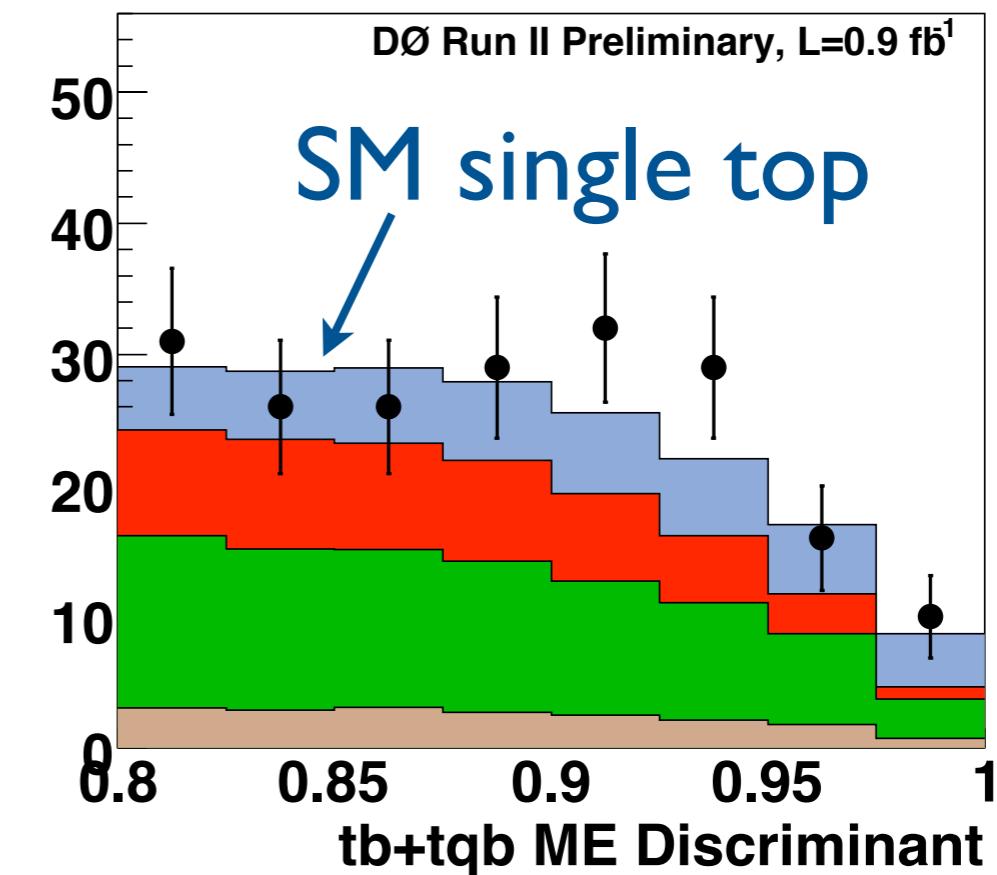
- Evaluating discriminant on data, single MC, and background MC, an excess of data over the background was observed!

$$\sigma_{tb+tqb} = 4.6^{+1.8}_{-1.5} \text{ pb}$$

- Visually demonstrated using 1D discriminant



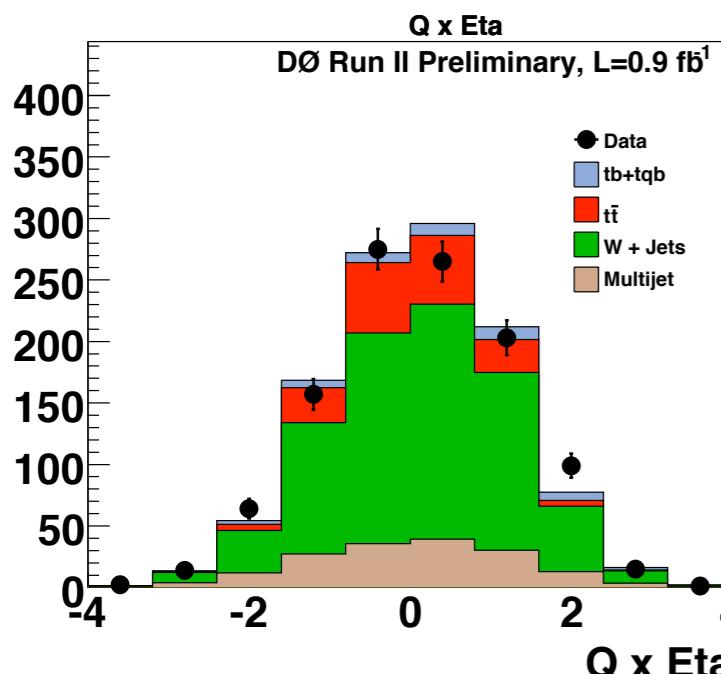
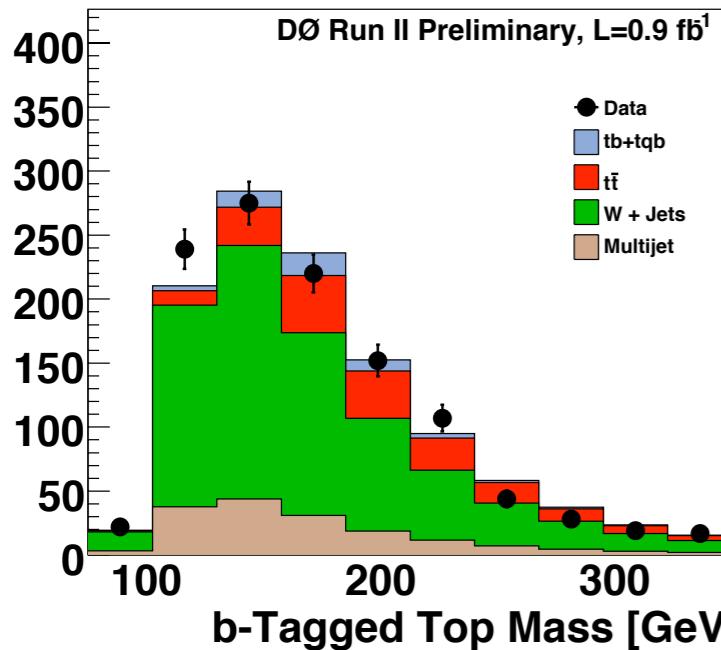
Zoom →



Consistent with Single Top?

- Look at $M(l, v, b\text{-tagged jet})$ and $q \times \eta$. Expect $M(l, v, b\text{-tagged jet}) \sim 175$ (top mass) and $q \times \eta$ to be asymmetric w/ peak in forward direction ($+\eta$)

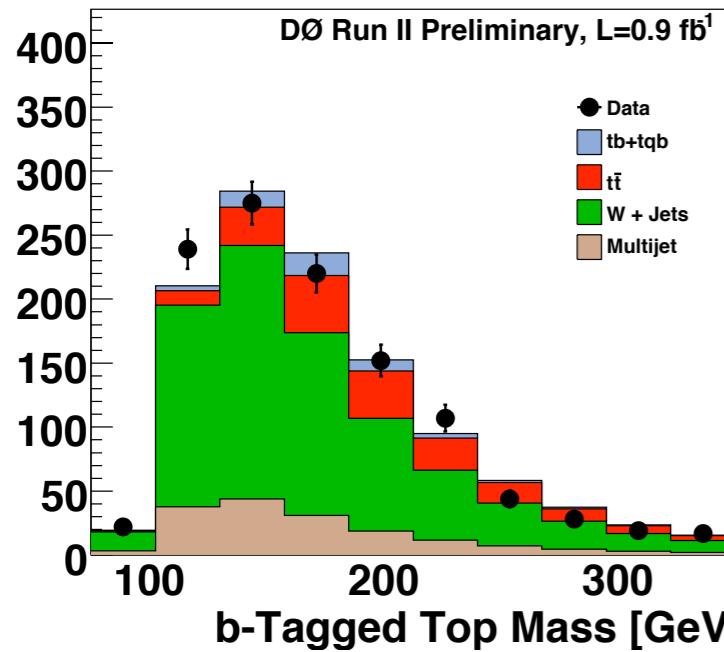
All Events



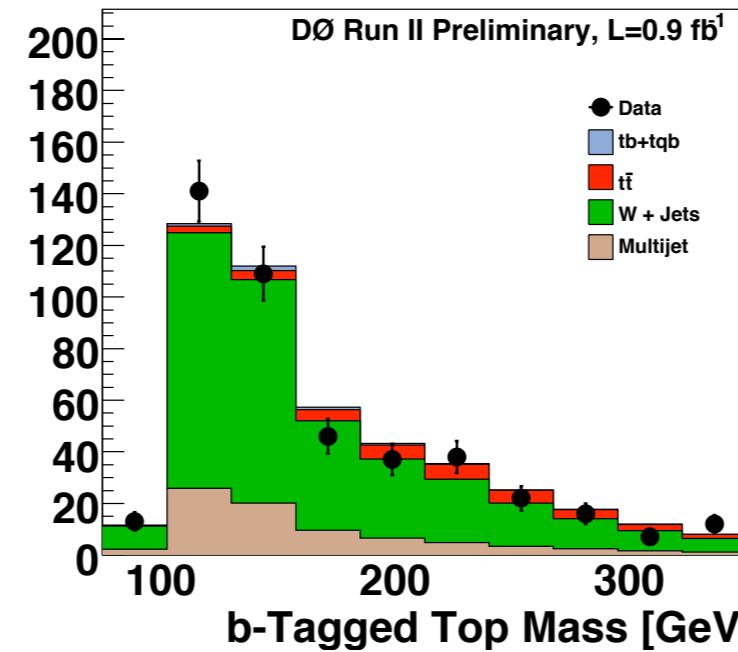
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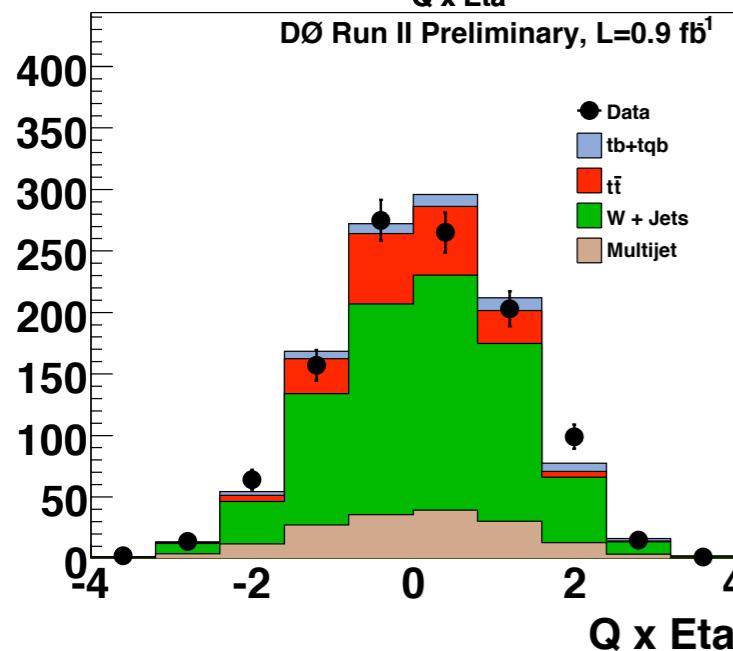
All Events



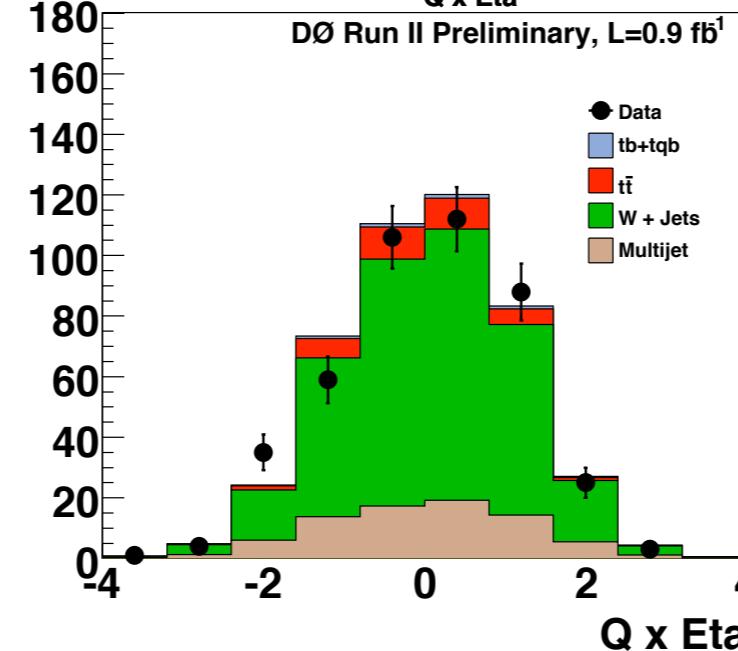
Background-like w/ $D < 0.4$



$Q \times \eta$



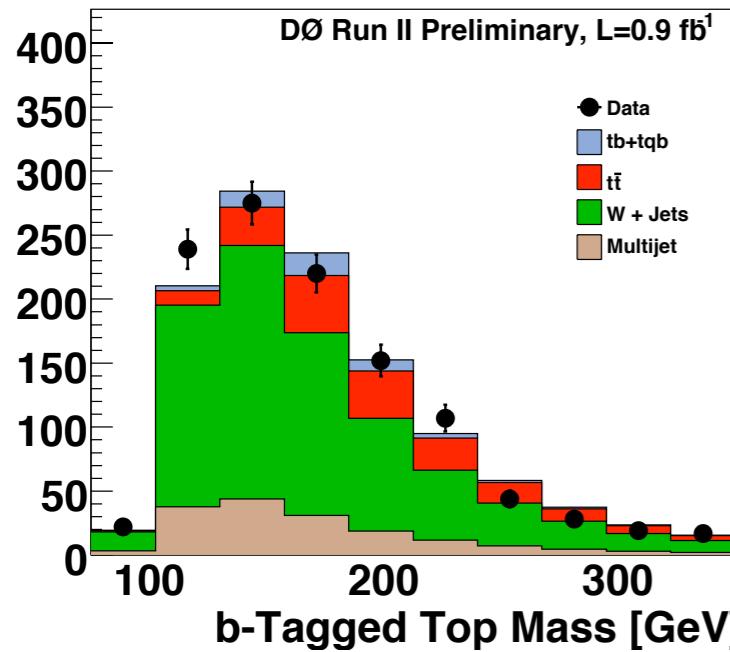
$Q \times \eta$



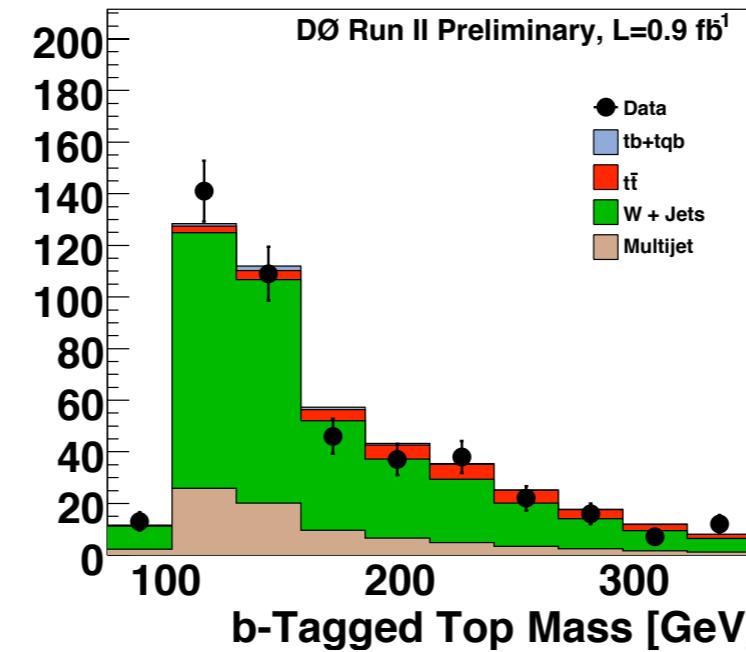
Consistent with Single Top?

- Look at $M(l, v, b\text{-tagged jet})$ and $q \times \eta$. Expect $M(l, v, b\text{-tagged jet}) \sim 175$ (top mass) and $q \times \eta$ to be asymmetric w/ peak in forward direction ($+\eta$)

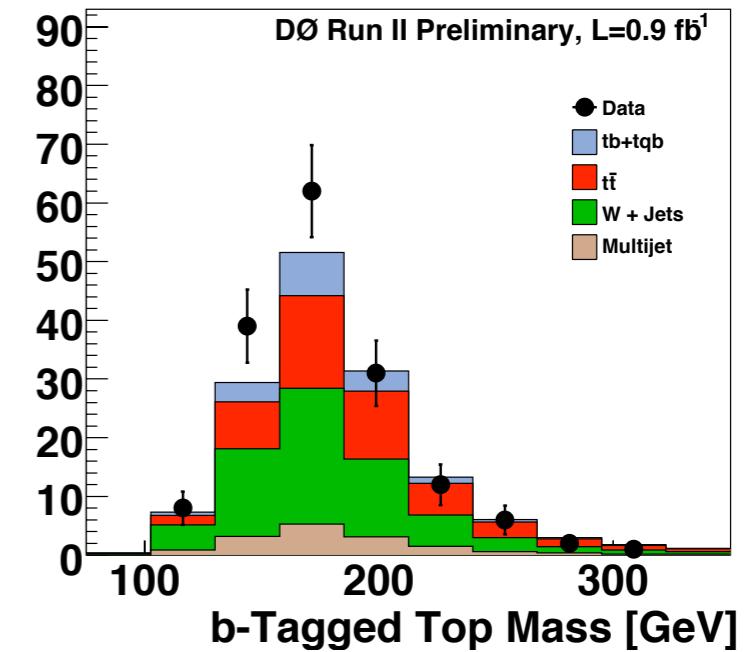
All Events



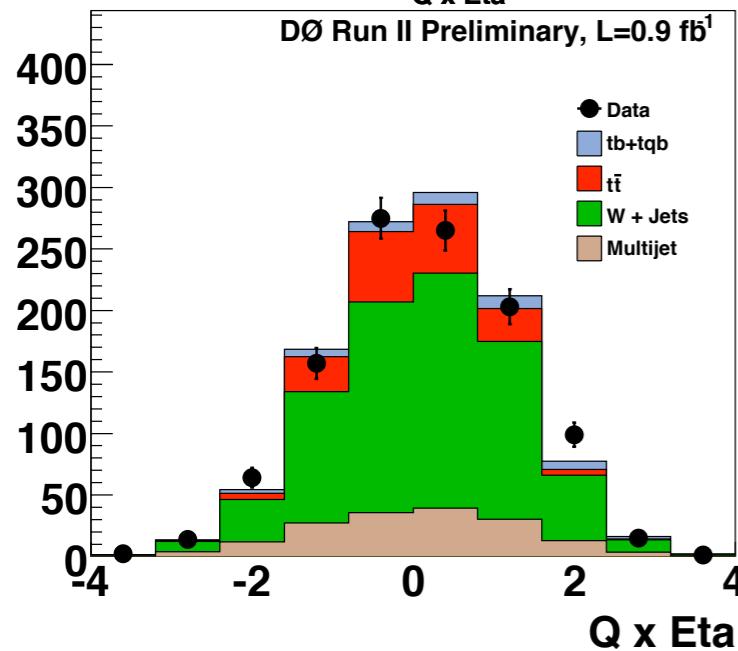
Background-like w/ $D < 0.4$



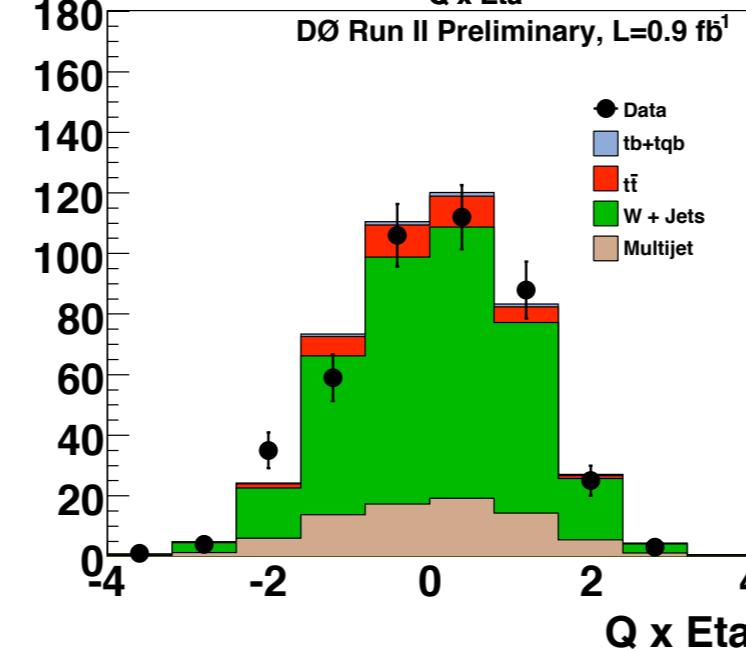
Signal-like w/ $D > 0.7$



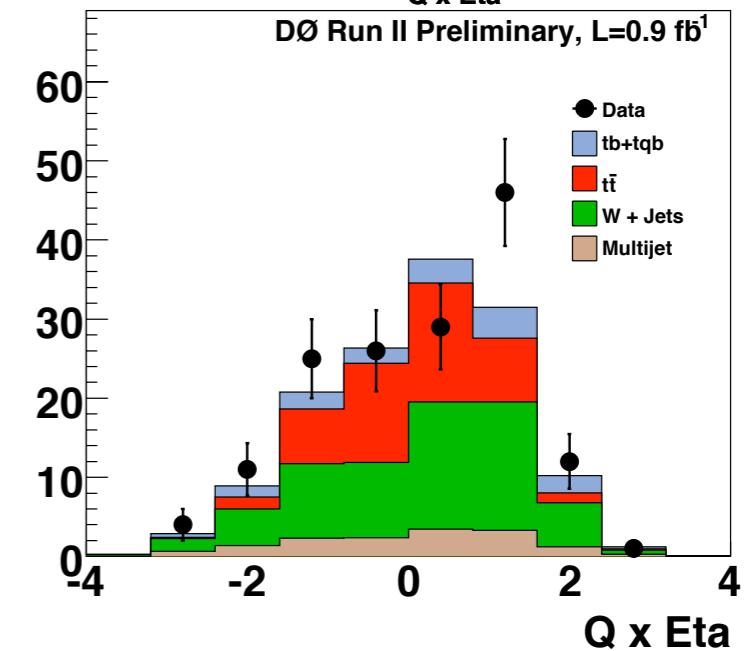
$Q \times \eta$



$Q \times \eta$

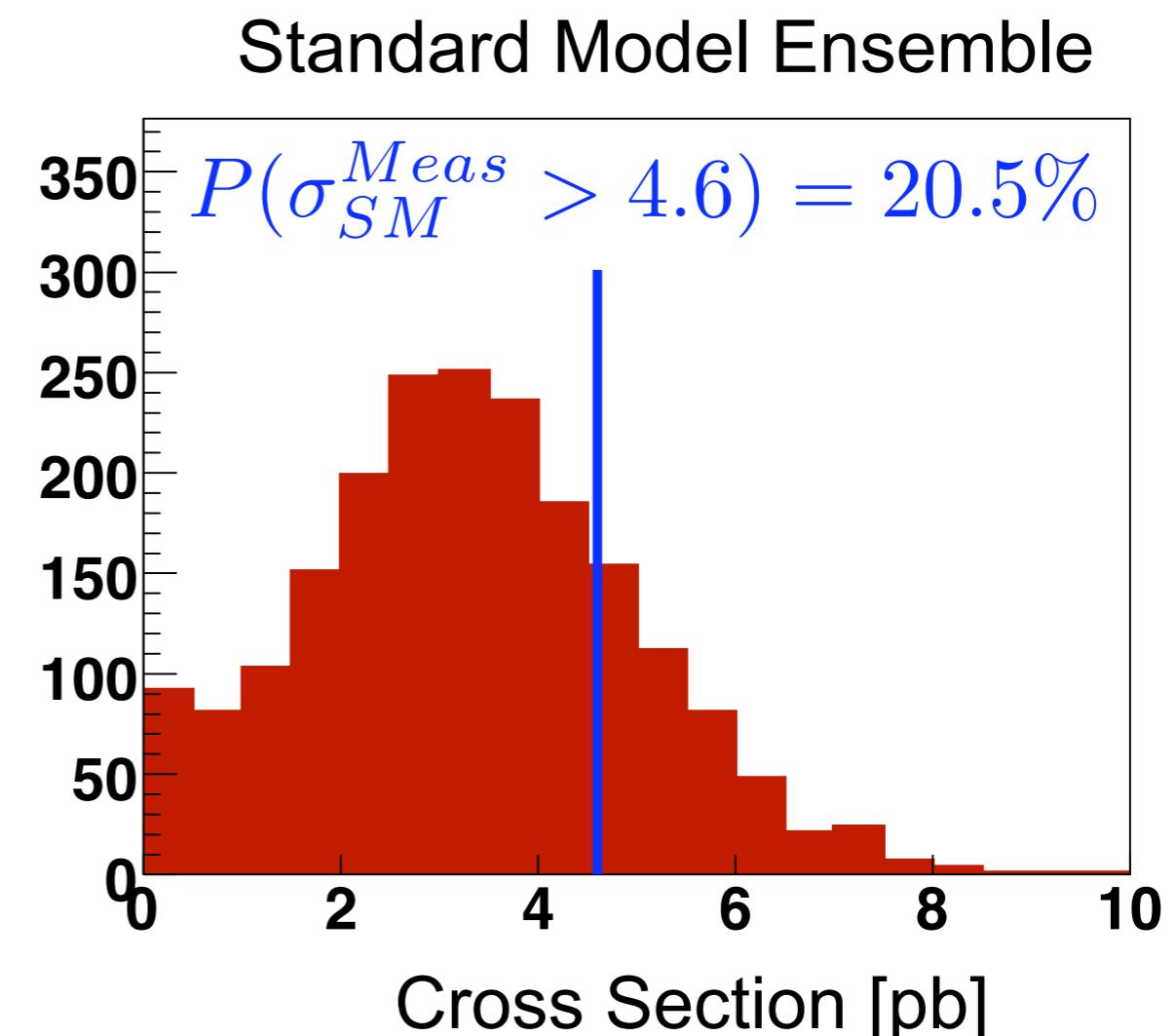
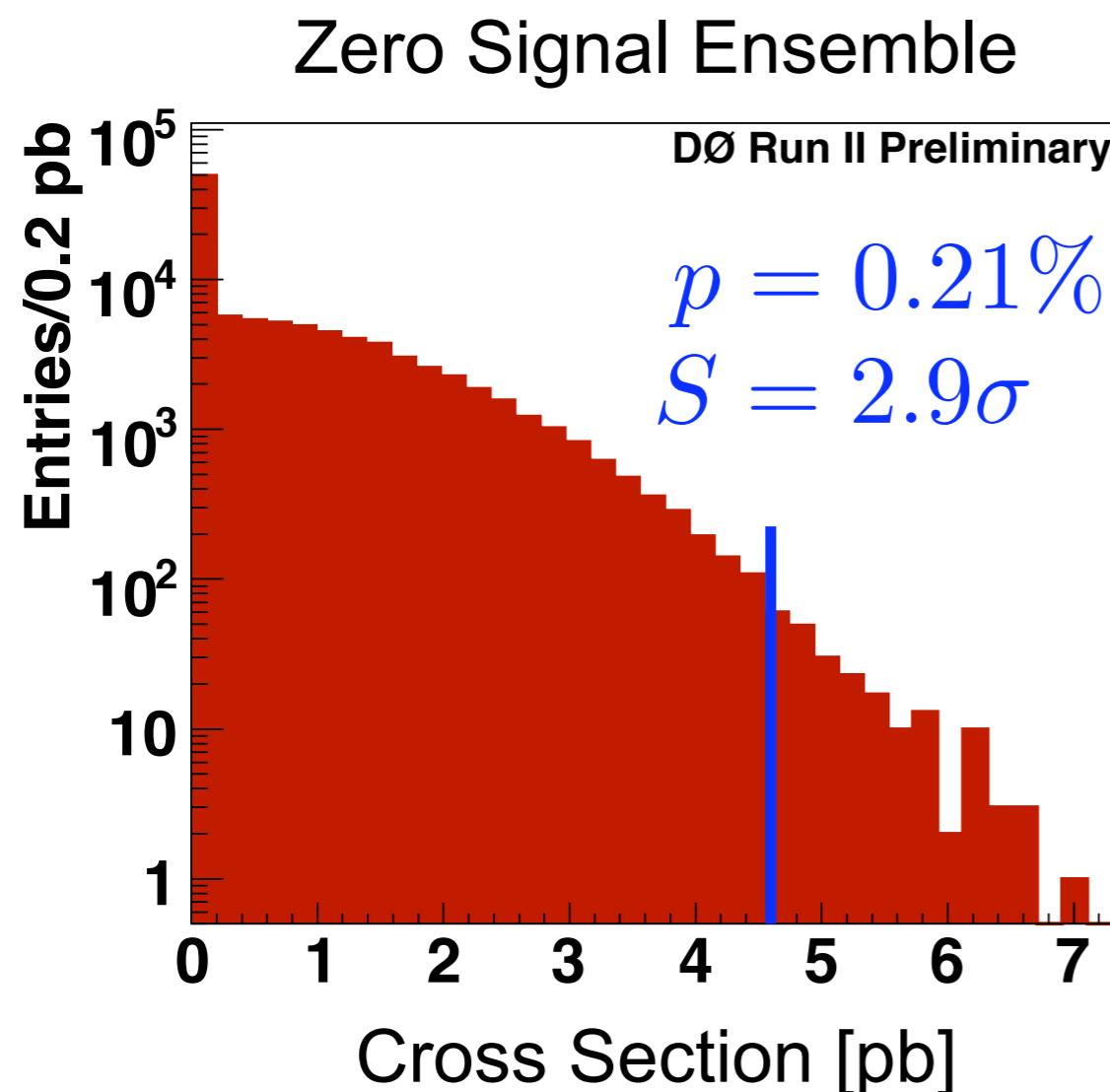


$Q \times \eta$



Significance and SM Compatibility

- ➊ Determine probability of upward fluctuation from background (p -value)
- ➋ Determine compatibility with SM prediction



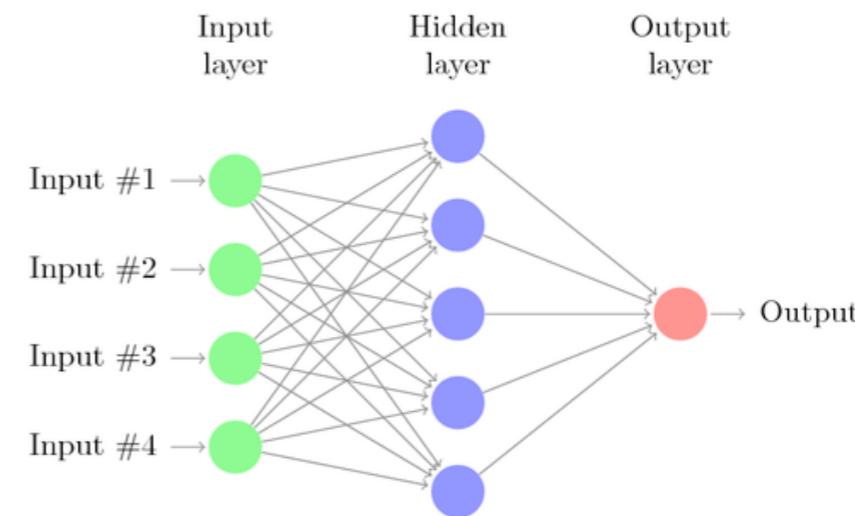
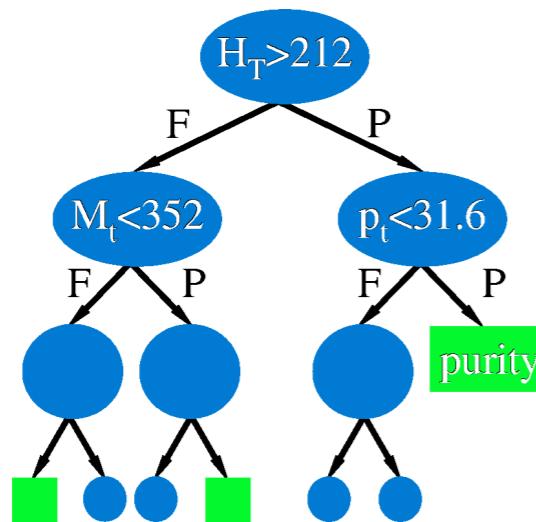
One of Three Single Top Analyses

- DØ performed three searches for single top production

- Matrix Element (you just heard about this)

- Boosted Decision Trees

- Bayesian Neural Network



	Bayesian NN		Matrix Element		Decision Trees	
	Exp.	Obs.	Exp.	Obs.	Exp.	Obs.
$\sigma(t\bar{b}+t\bar{q}b)[pb]$	$3.2^{+2.0}_{-1.8}$	5.0 ± 1.9	$3.0^{+1.8}_{-1.5}$	$4.6^{+1.8}_{-1.5}$	$2.7^{+1.6}_{-1.4}$	4.9 ± 1.4
Significance	1.3σ	2.4σ	1.8σ	2.9σ	2.1σ	3.4σ

**First evidence for single top quark production!
SM compatibility is 11%.**

Single Top Announcement

- Announced at Fermilab Wine & Cheese seminar on December 8, 2006



SCIENTIFIC
AMERICAN

Alone at the Top

CLOSER TO GOD: FERMILAB MAKES SOLO TOP QUARKS BY ALEXANDER HELLEMANS

CERN
COURIER

Scientists at the D0 experiment discover new path to the top

DZero finds evidence of rare single top quark; Observation marks a step closer to finding Higgs boson

Batavia, Ill.—Scientists of Fermi National Accelerator Laboratory announced December 8, 2006 the first clear evidence of a subatomic process involving the production of a single top quark, a prediction made by particle physicists in the 1970s. In the longer term, the team hopes to search for an even more elusive particle—the Higgs boson.

HIGH-ENERGY PHYSICS

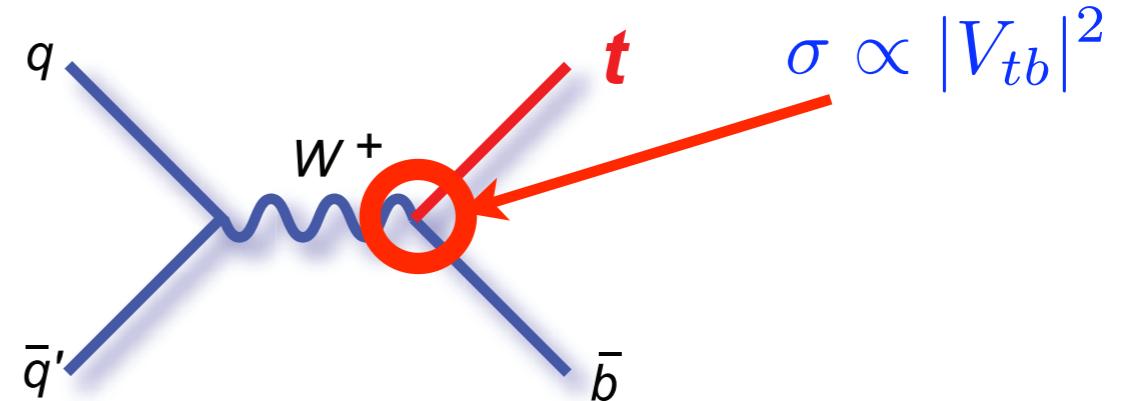
Top quarks go it alone

The first, long-sought evidence for the production of single top quarks, by the weak interaction, has been reported from a sophisticated analysis of a large number of proton-antiproton collisions at the Tevatron.

nature
physics

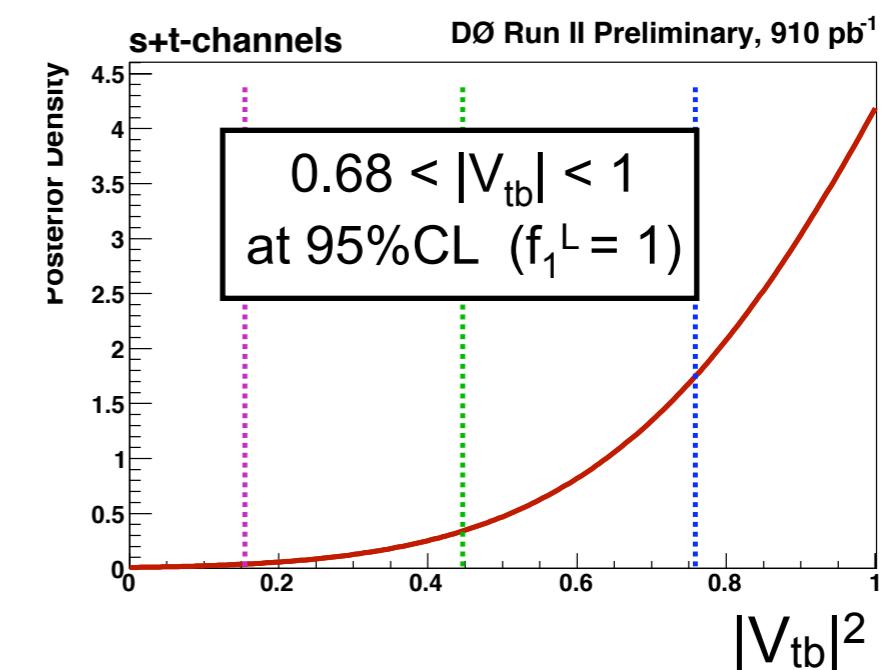
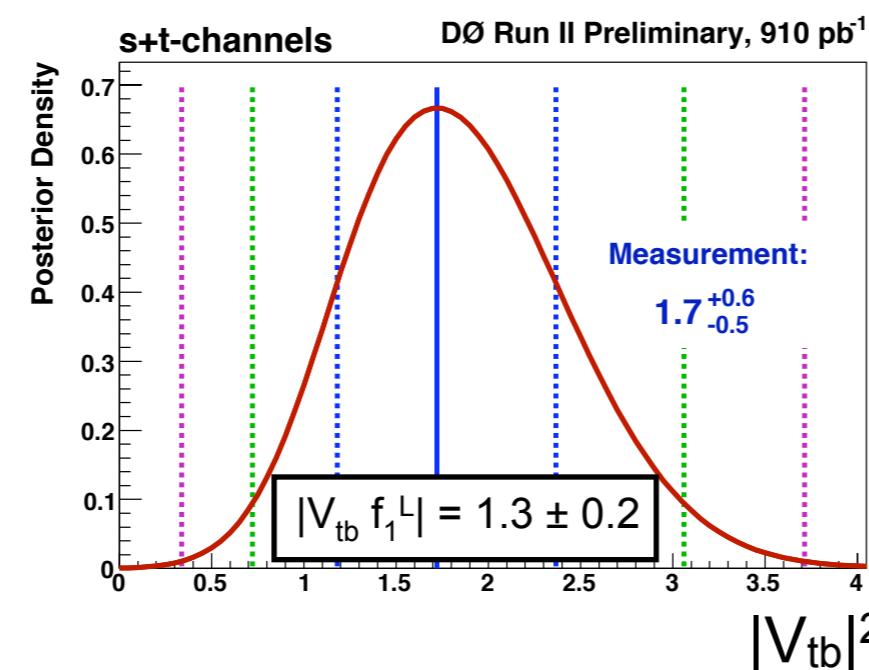
Single Top Measurement $\rightarrow V_{tb}$

- After measuring single top cross section, we turn around and determine V_{tb}
- Use decision tree measurement for V_{tb}
- Assume:
 - $|V_{td}|^2 + |V_{ts}|^2 \ll |V_{tb}|^2$
 - Pure V-A and CP conserving vertex
- Does not assume three quark generations
- Build posterior for $P(V_{tb} | N_{obs})$ integrating over additional theoretical errors



Additional theoretical uncertainties		
	tb	tqb
Top mass	13 %	8.5 %
Scale	5.4 %	4.0 %
PDF	4.3 %	10 %
α_s	1.4 %	0.01 %

hep-ph/0408049



Combined DØ Single Top Result

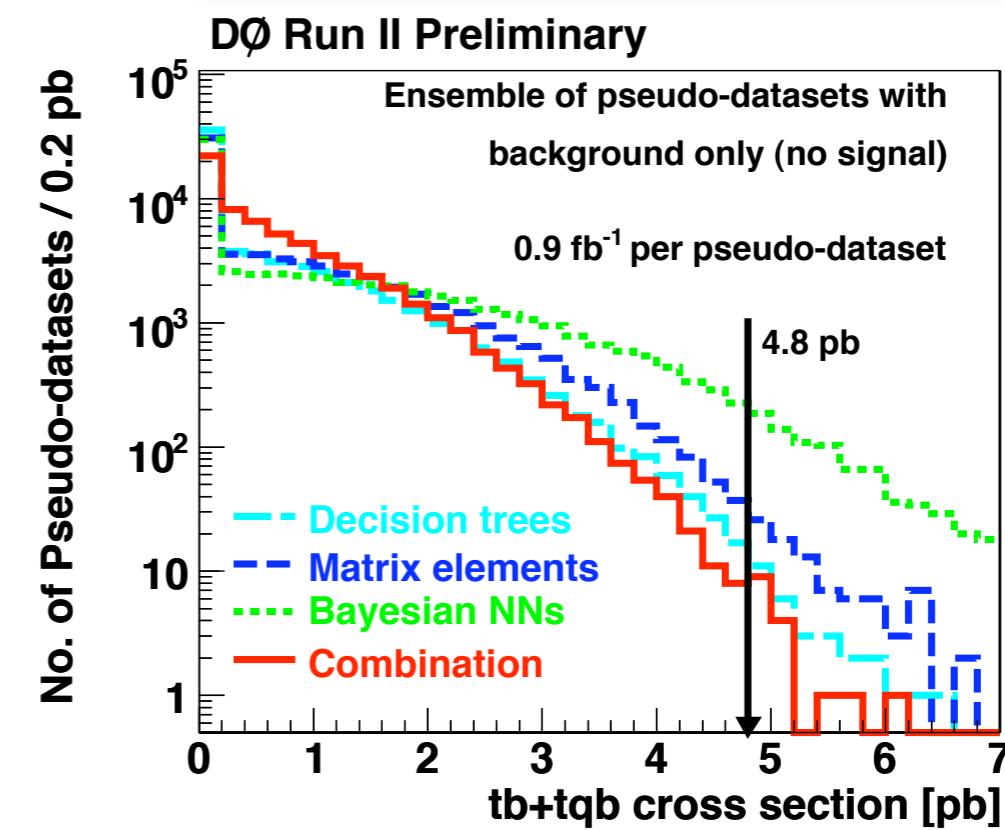
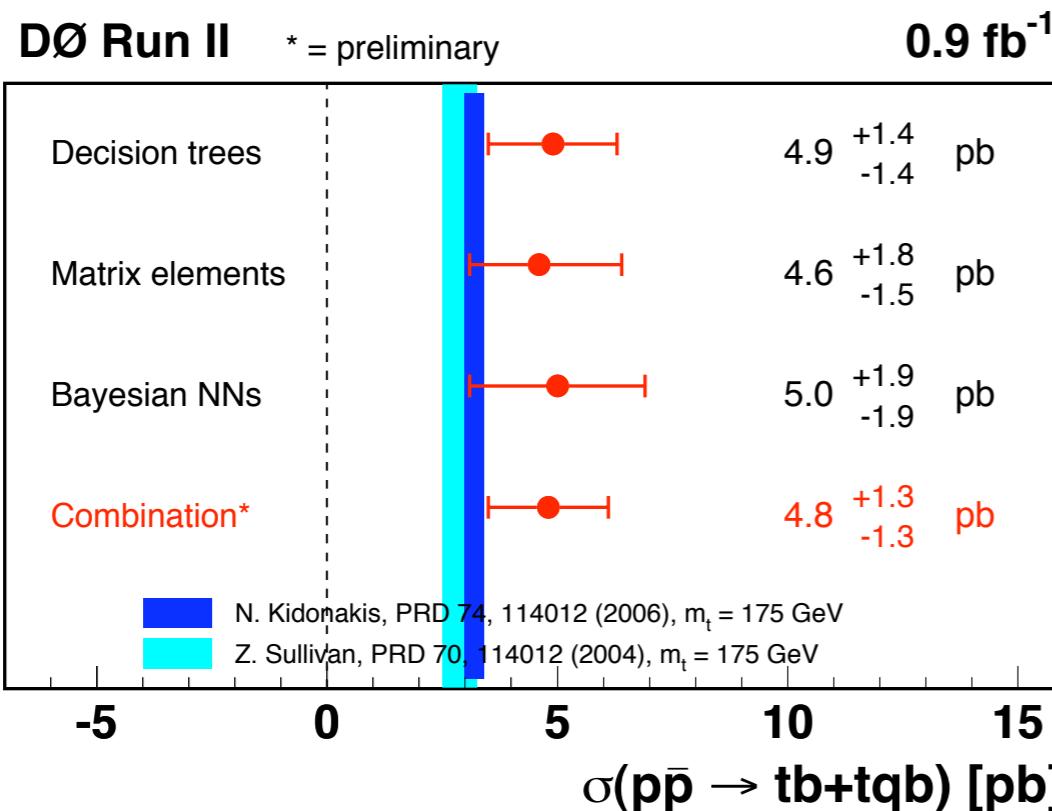
- The matrix element, Bayesian neural network, and decision tree analyses were combined using the BLUE (Best Linear Unbiased Estimator) method

$$\sigma_{\text{comb}} = w_{BNN}\sigma_{BNN} + w_{DT}\sigma_{DT} + w_{ME}\sigma_{ME}$$

- Need to know correlation between analyses to determine weights

$$\sigma_{\text{comb}} = 4.8 \pm 1.3 \text{ pb}$$

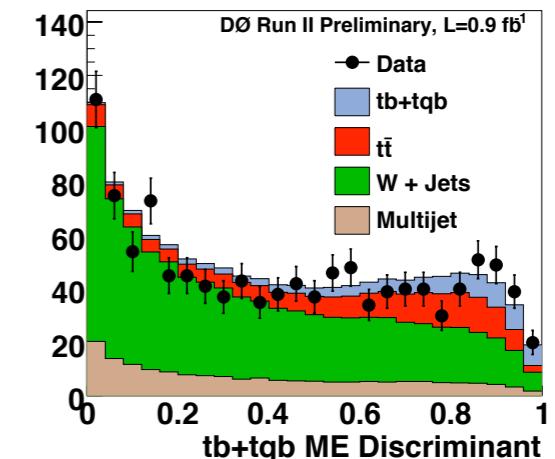
$$\text{Sig} = 3.5\sigma$$



Conclusion

- Using $\sim 1 \text{ fb}^{-1}$ of DØ Run IIa data, we measure the combined tb+tqb single top cross section with the matrix element method as

$$\sigma_{tb+tqb} = 4.6^{+1.8}_{-1.5} \text{ pb}$$



- Three DØ single top analyses are combined and measure a cross section of

$$\sigma_{\text{comb}} = 4.8 \pm 1.3 \text{ pb}$$

$$\text{Sig} = 3.5\sigma$$

- The three single top measurements were recently accepted for publication by PRL [hep-ex/0612052]
- PRD including combination is coming soon
- DØ has more than 2 fb^{-1} of data on tape: Push towards 5σ , measure σ_{tb} and σ_{tqb} , and of course, keep an eye out for new physics

Thanks

- Gordon Thanks for taking me as a student and getting me into the game
- Aran Thanks for answering the 10 million questions I have and keeping me company at Fermilab
- My committee Thanks for listening and reading
- DØ Single top group + Matrix Element working group
Special thanks to Aurelio Juste for getting me started with matrix elements
- Good friends Thanks for the Key West trip in January
(20 degrees in Chicago and 80 degrees in Key West)
- Ruth I couldn't have done it without you

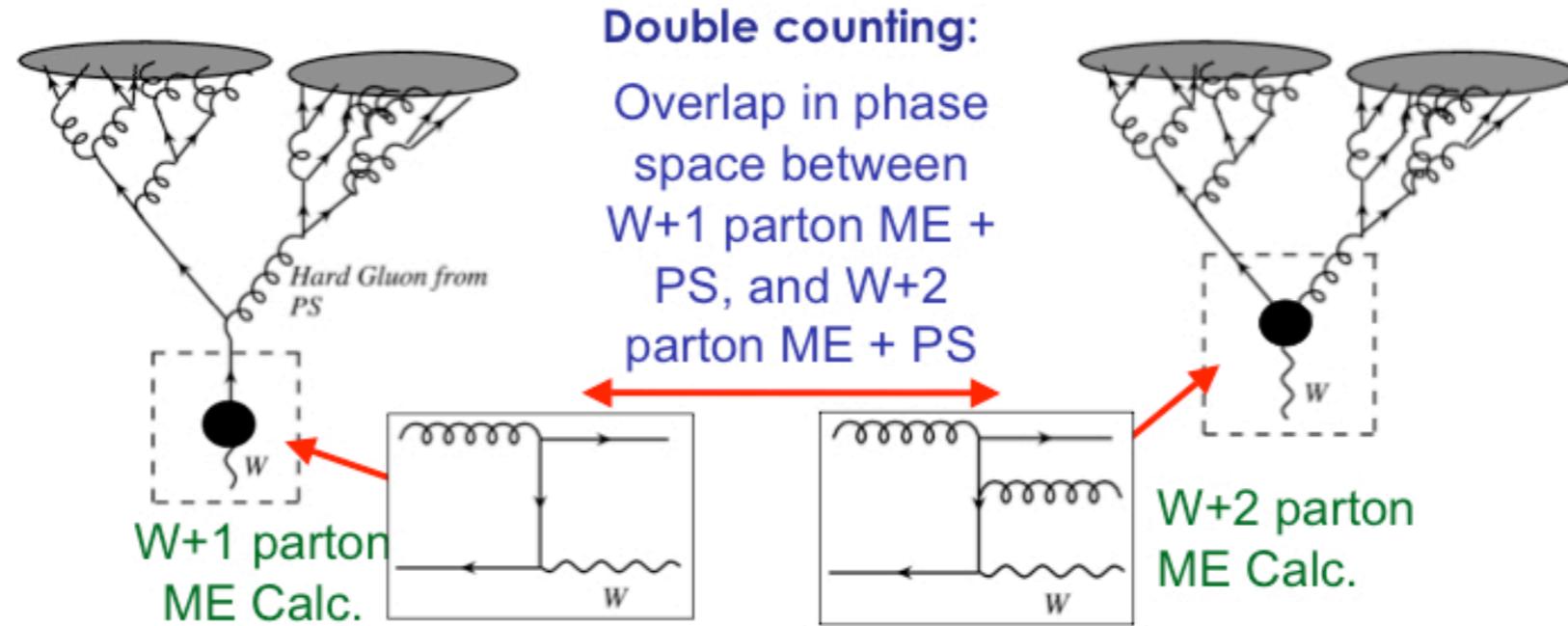


Backup Slides

MLM Matching

- Monte Carlo generators use $2 \rightarrow N$ matrix element calculation with parton shower to simulate “soft” QCD processes
- Problem: Double counting phase space when combining samples after parton shower has added jets

- Example:



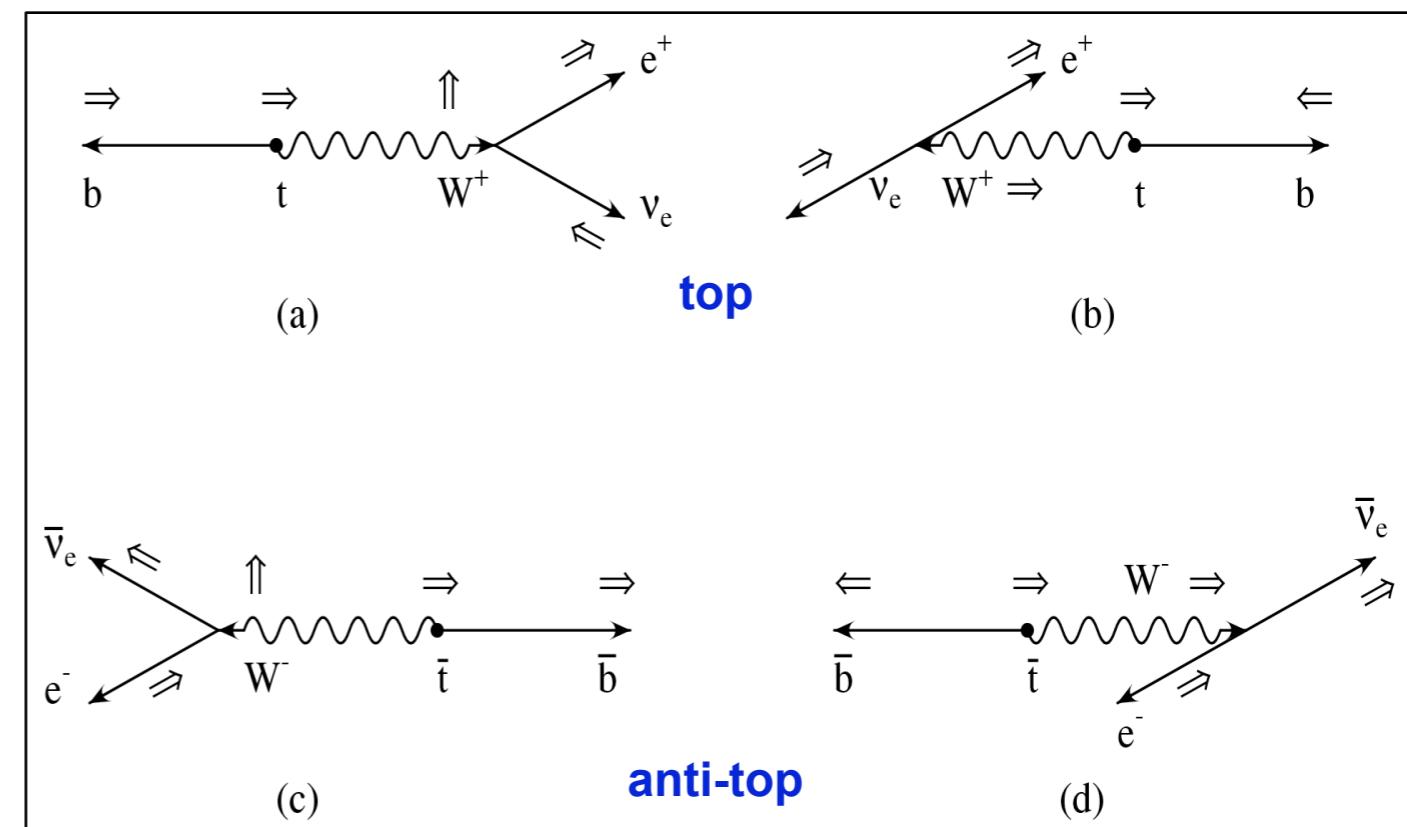
- Solution: ME+PS matching - DØ uses MLM matching scheme
- MLM scheme: (1) generate independent parton samples (e.g. $W+0lp$, $W+1lp$, etc..), (2) Run parton shower, (3) Run jet clustering algorithm, (4) Keep event if $N_{\text{partons}} = N_{\text{jets}}$

Top Polarization

- Top quark is 100% polarized along the direction of the d-type quark

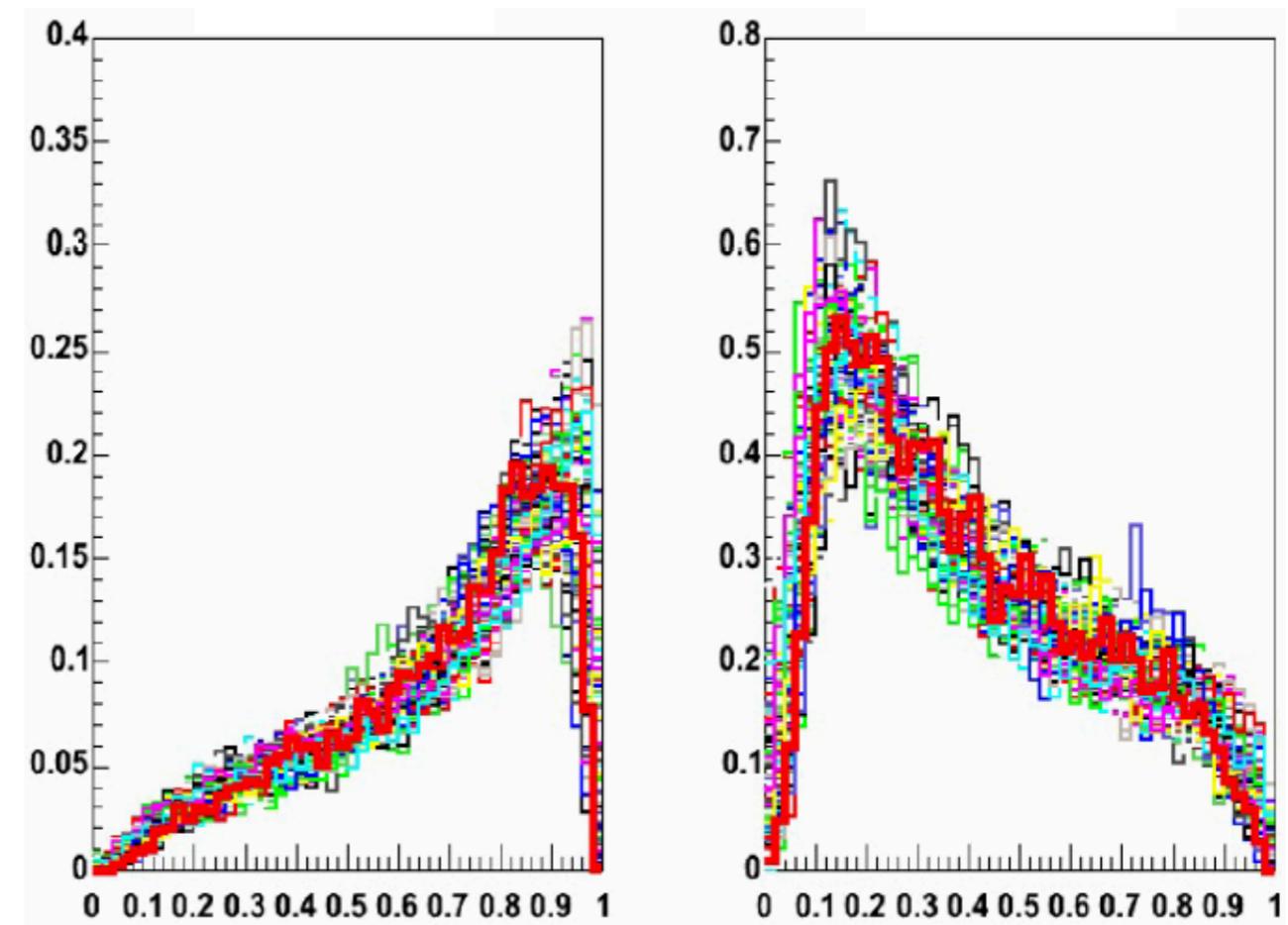
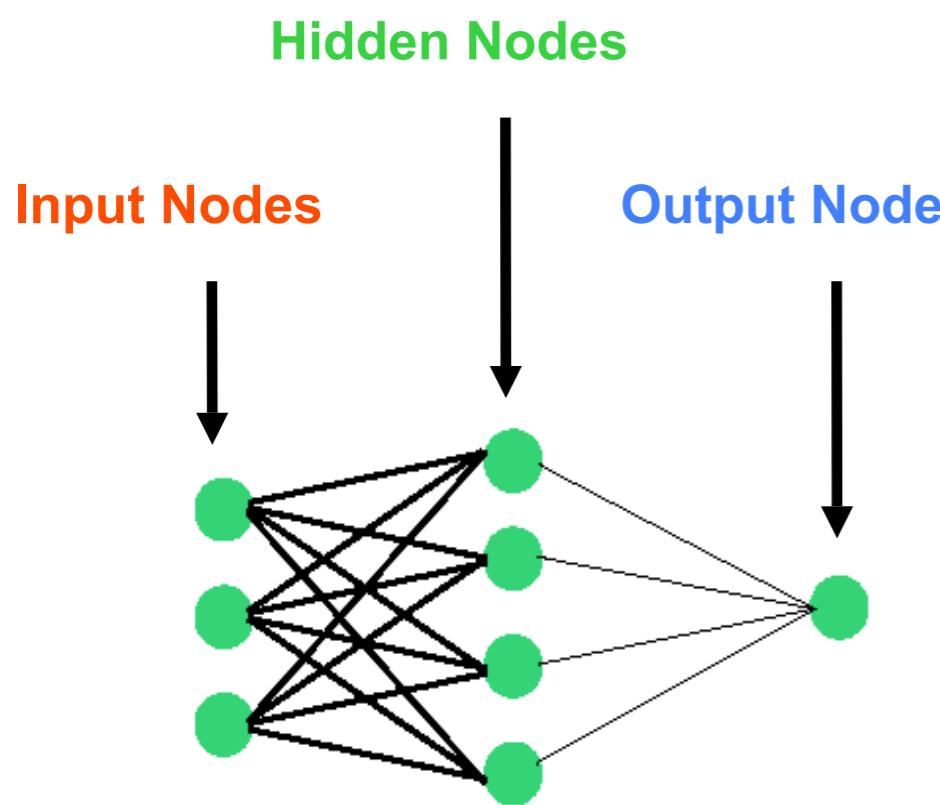
Mahlon and Parke [hep-ph/9611367]

- Top quark polarization is also correlated to the momentum of the lepton from the W decay since both top and W decay electroweakly.
 - Boost into top quark rest frame
 - Choose top quark spin to be in the direction of d-type quark
 - $|M|^2 \propto 1 + \cos(\theta_{\text{lep-d}})$
- tb: 98% polarization if we choose the antiproton direction
- tqb: 96% polarization if we choose the spectator (d-type) quark direction



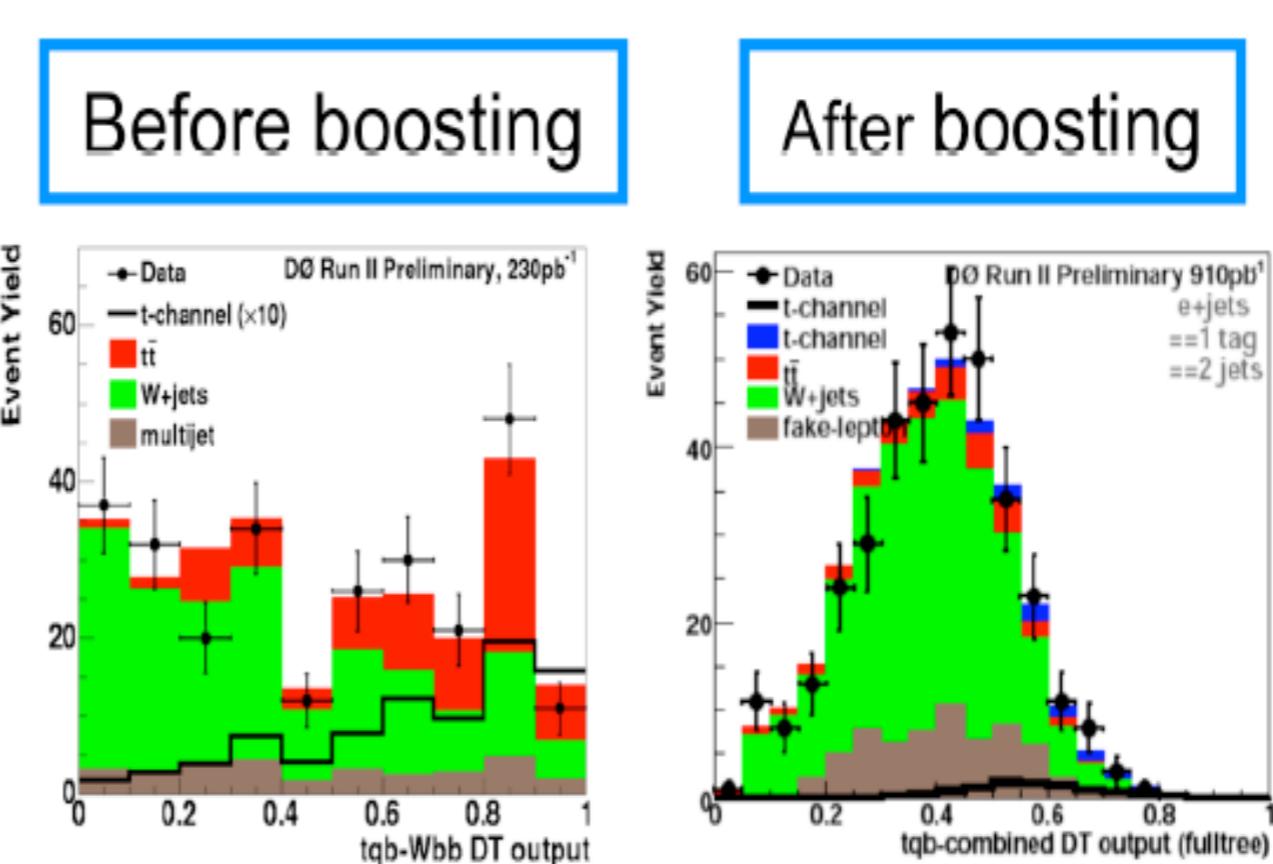
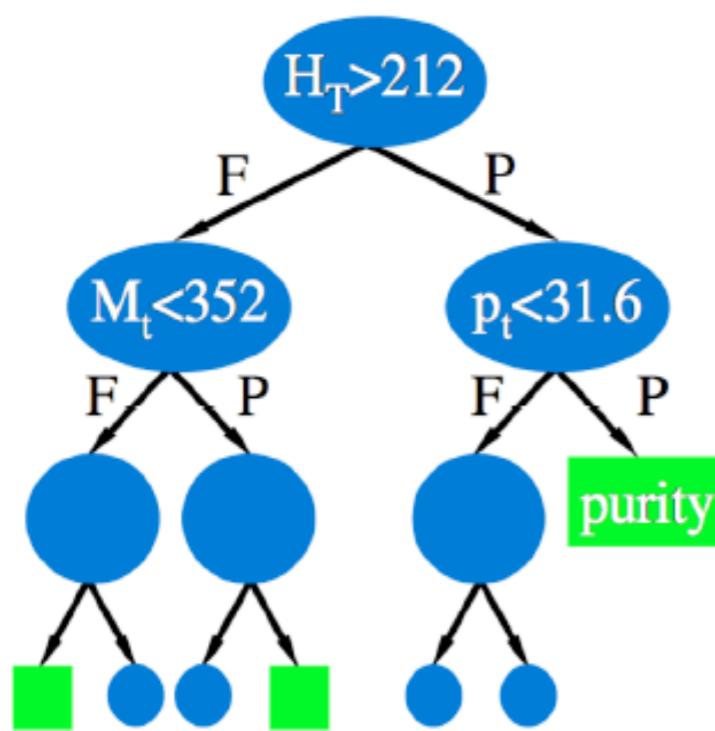
Bayesian Neural Networks

- Use 24 variables for training networks (**input nodes**).
- Train network on signal and background simulated events:
 - Signal tends to one and background tends towards zero (**output node**).
- Average many different networks for stability (**hidden nodes**).
- Less prone to over-training.



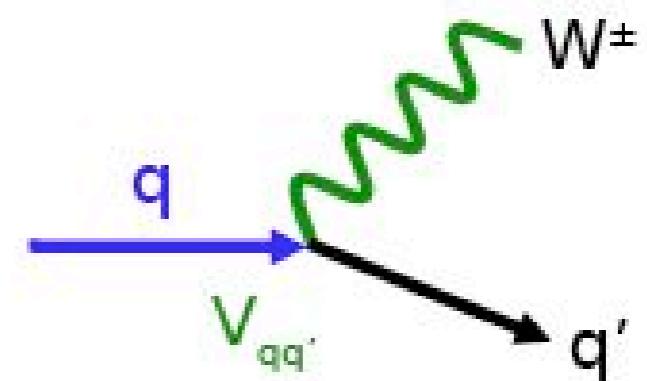
Decision Trees

- Goal: recover events that fail a simple cut-based analysis
- Use 49 variables for training: most discriminating variables $M(\text{all jets})$, $M(W, \text{b-tag1})$, $\cos(\text{b-tag1}, \text{lepton})$, $Q(\text{lepton}) * \eta(\text{untagged1})$
- Decision tree output for each event = leaf purity: $N_S/(N_S+N_B)$
- Train network on signal and background simulated events:
 - Signal tends to one and background tends towards zero
- Boosting: retrain 20 times to improve “weak classifier”



$|V_{tb}|$

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & \textcircled{V_{tb}} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$



► Most general Wtb vertex:

$$\Gamma_{tbW}^\mu = -\frac{g}{\sqrt{2}} V_{tb} \left\{ \gamma^\mu [f_1^L P_L + f_1^R P_R] - \frac{i \sigma^{\mu\nu}}{M_W} (p_t - p_b)_\nu [f_2^L P_L + f_2^R P_R] \right\}$$

► Assume:

- **SM top decay:** $V_{td}^{-2} + V_{ts}^{-2} \ll V_{tb}^{-2}$
- Pure V-A interaction: $f_1^R = 0$
- CP conservation: $f_2^L = f_2^R = 0$

We are effectively measuring the strength of the V-A coupling:

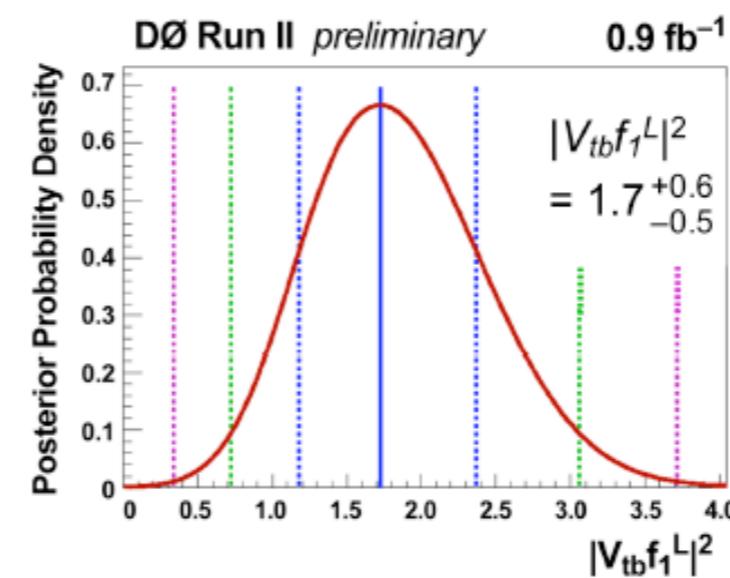
$|V_{tb} f_1^L|$, which can be > 1

Vtb

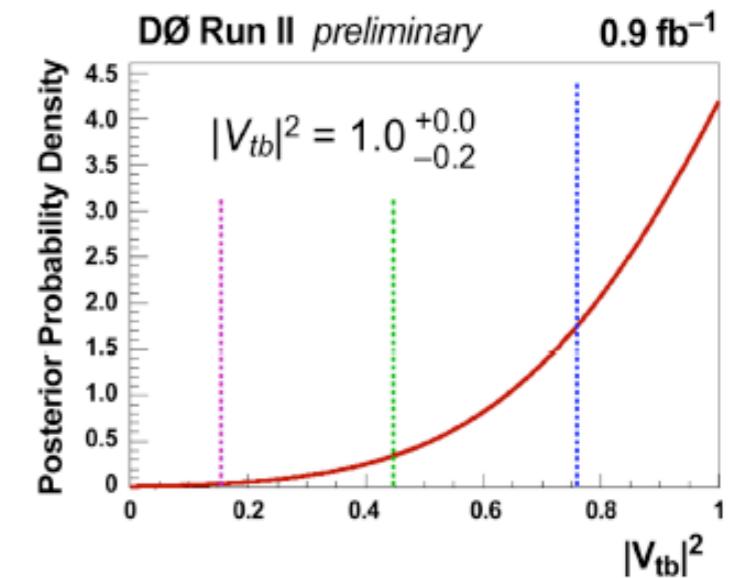
$$\Gamma_{Wtb}^\mu = -\frac{g}{\sqrt{2}} \textcolor{red}{V_{tb}} \left\{ \gamma^\mu [f_1^L P_L + f_1^R P_R] - \frac{i\sigma^{\mu\nu}}{M_W} (p_t - p_b)_\nu [f_2^L P_L + f_2^R P_R] \right\}$$

- Assuming standard model production:
 - Pure V-A and CP conserving interaction: $f_1^R = f_1^L = f_2^R = 0$.
 - $|V_{td}|^2 + |V_{ts}|^2 \ll |V_{tb}|^2$ or $B(t \rightarrow W b) \sim 100\%$.

Additional theoretical uncertainties		
	$t b$	$t q b$
Top mass	13 %	8.5 %
Scale	5.4 %	4.0 %
PDF	4.3 %	10 %
α_s	1.4 %	0.01 %



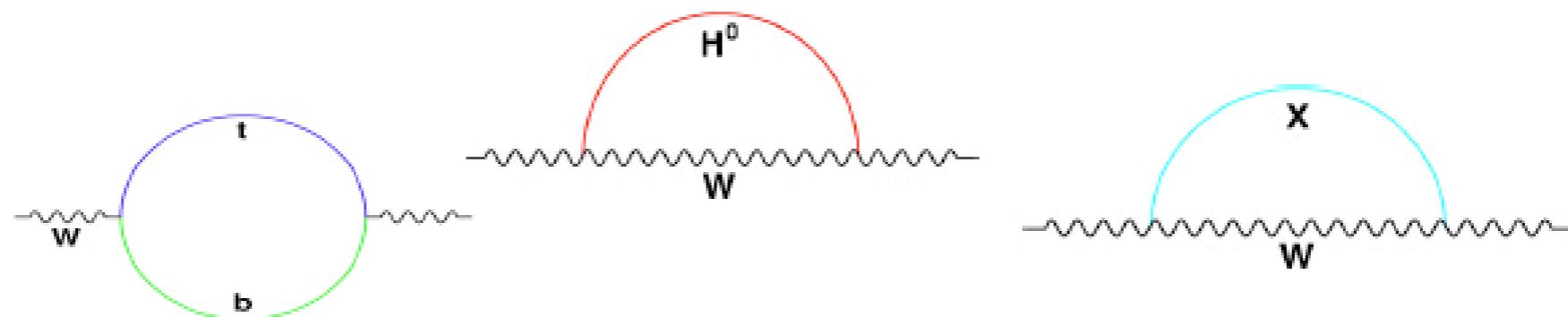
$$|V_{tb} f_1^L| = 1.3 \pm 0.2$$



$0.68 < |V_{tb}| < 1$
at 95%CL ($f_1^L = 1$)

Radiative Corrections To W Mass

- Radiative corrections due to heavy quark and Higgs loops and exotica



Motivate the introduction of the ρ parameter: $M_W^2 = \rho M_Z^2 \cos^2\theta_W$

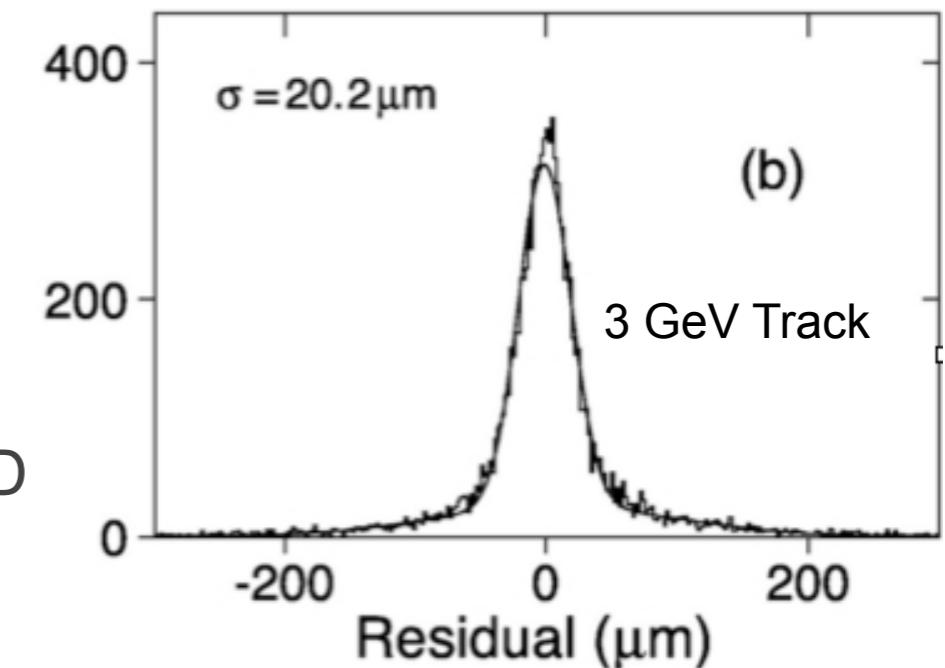
with the predictions $(\rho - 1) \sim M_{top}^{-2}$ and $(\rho - 1) \sim \ln M_H$

- In conjunction with M_{top} , the W boson mass constrains the mass of the Higgs boson, and possibly new particles beyond the standard model

Detector Alignment and Calibration

Tracker

- Optical survey determines position of the SMT and CFT elements.
- Cosmic rays and tracks to inter-align tracker elements. CFT calibrated with 450 nm from LED



Solenoidal Magnetic Field

- Measured by Hall probes located the detector

Calorimeter

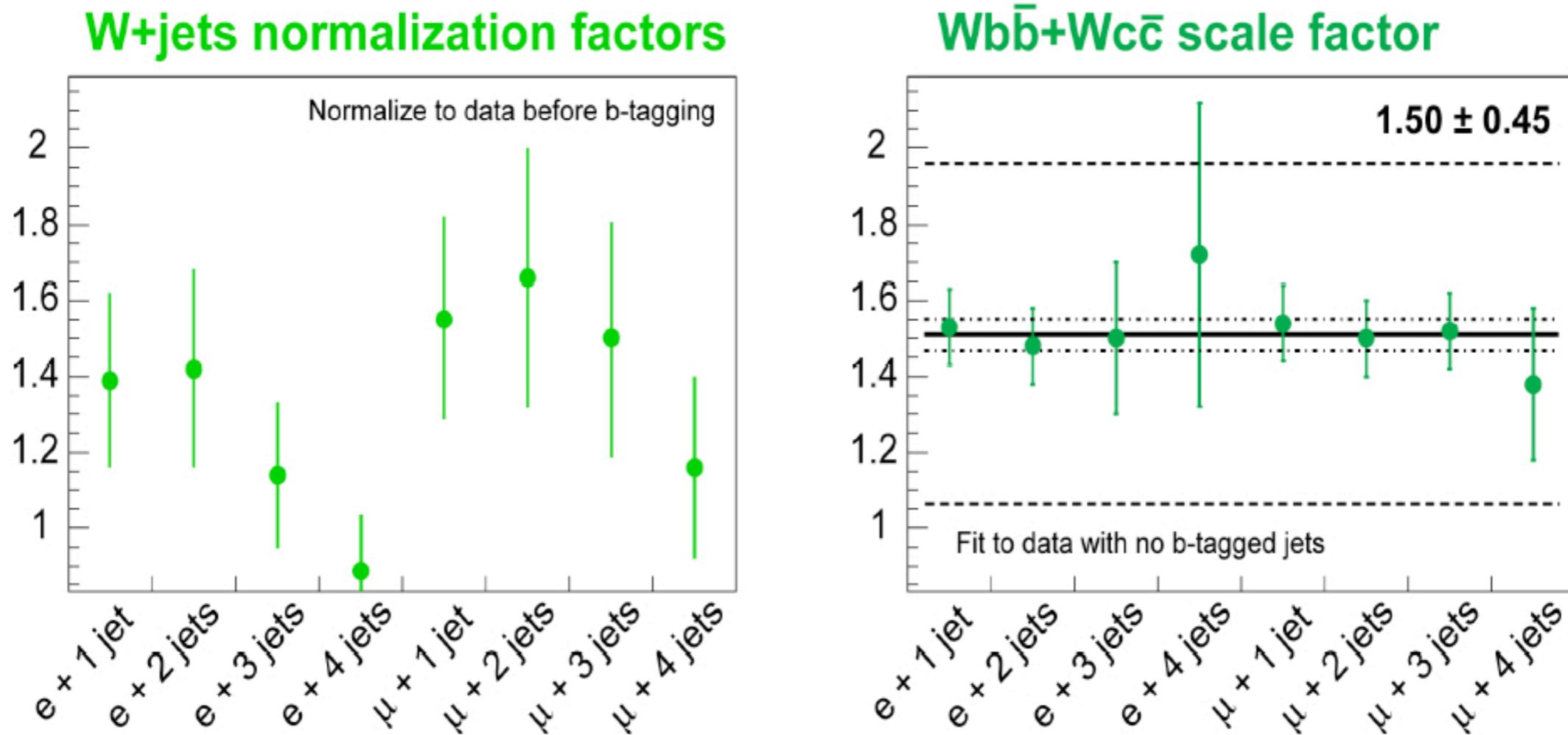
- Calibrated by pulser boards. Liquid Argon purity measured w/ ^{241}Am
- Energy scale measured “offline” using dijet and photon+jet events

Muon

- Scintillators are monitored and calibrated using a LED source.
- Muon momentum scale measured “offline” using $Z \rightarrow \mu\mu$ events

k-Factor

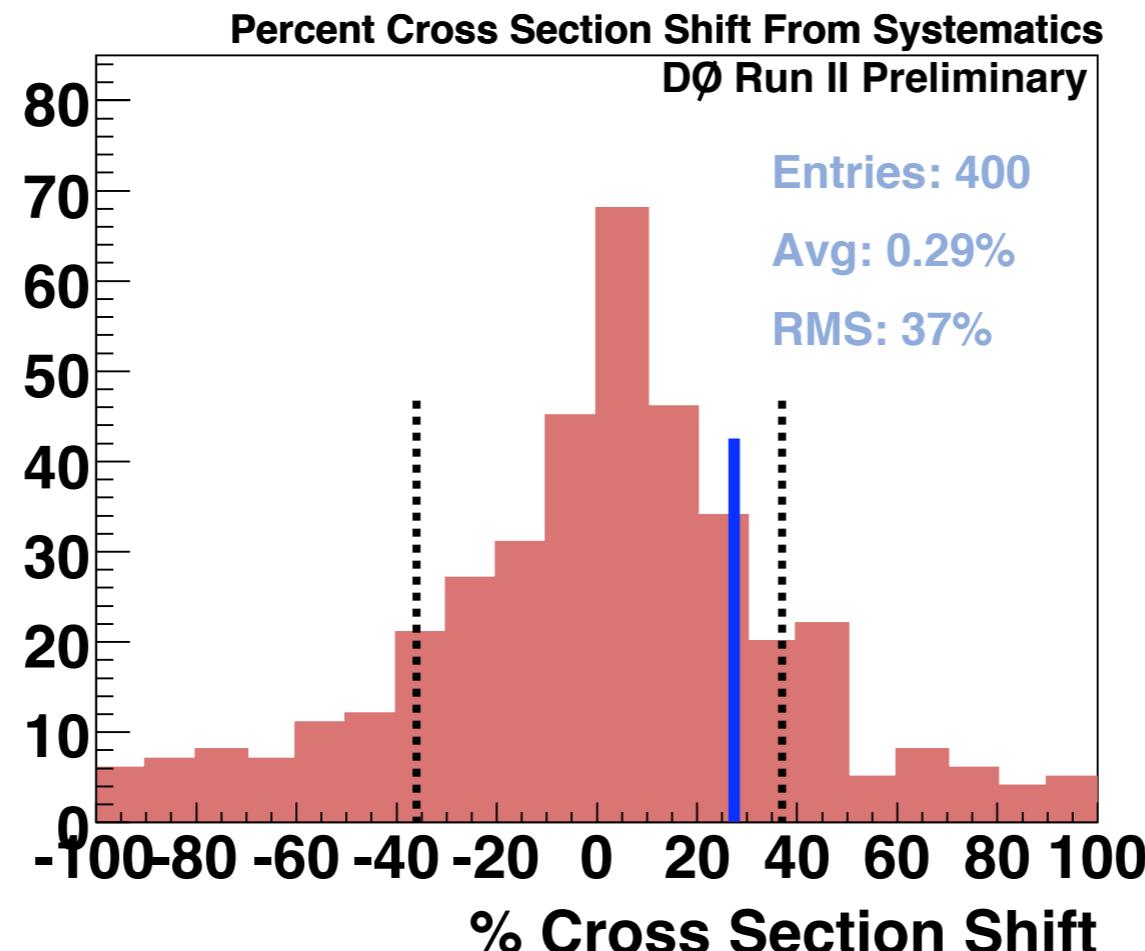
- Problem: Can not use MCFM (NLO calculation) for W+jets because of matching and MCFM does not include certain relative processes
- Solution: Measure effective k-factor in data
- Data = $\alpha(W_{bb}+W_{cc}) + W_{jj} + tt\bar{t} + QCD\text{ Multijet}$
- Measure in $=0 b$ -tag sample to remove bias from signal dataset



Cross Section Shift When Adding Syst.

- When including systematics, we see a 27% increase in the cross section.
- Can test this with SM ensembles with and without systematics.

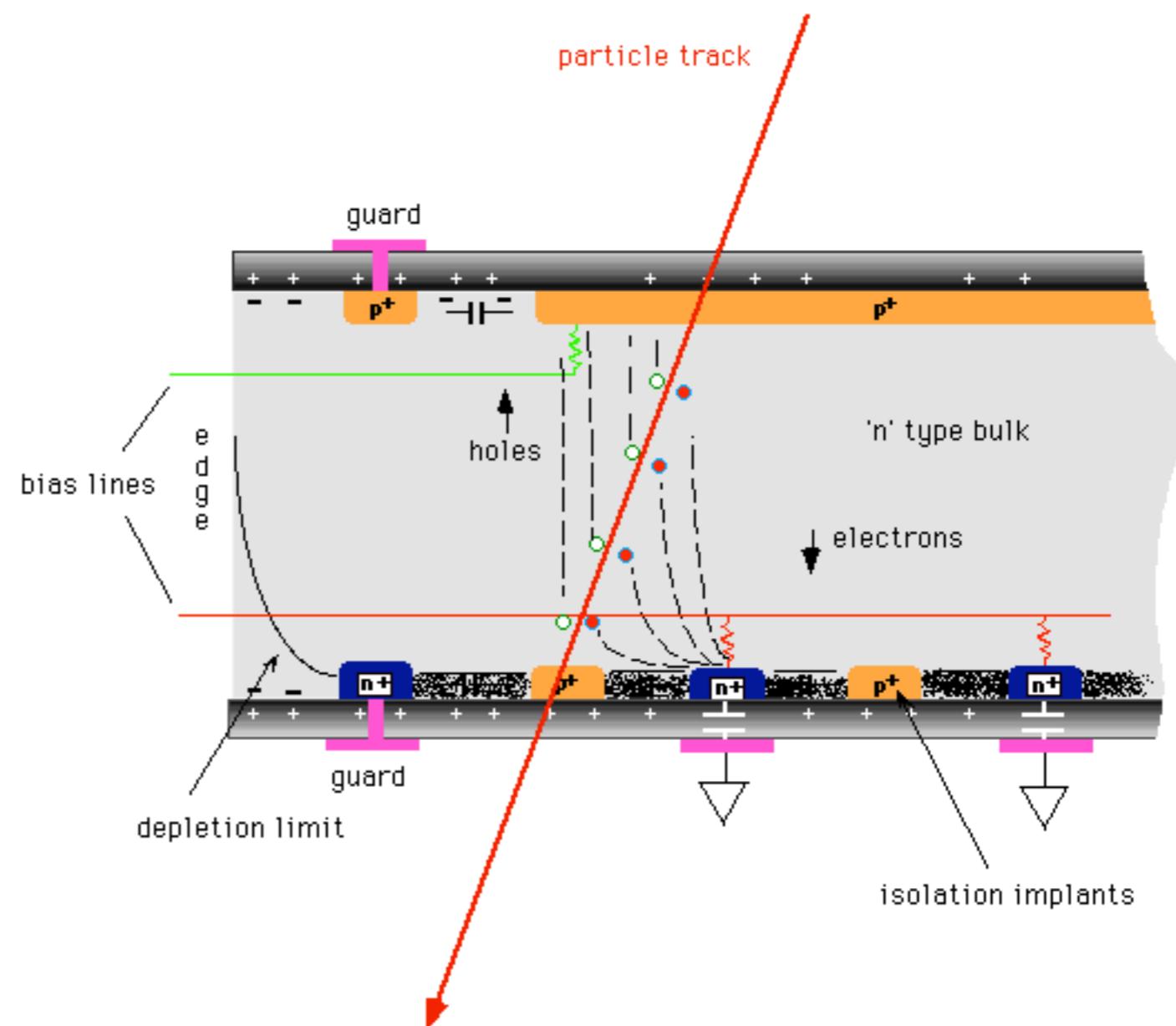
$$\% \text{Shift} = \frac{\sigma_{\text{sys}} - \sigma_{\text{nosys}}}{\sigma_{\text{nosys}}}$$



- Our measured % shift falls within the 1σ bands \Rightarrow Our shift is reasonable

Silicon Detectors

- Charged particle interacts with the silicon to produce electron-hole pairs (electrons are moved from the valence to the conduction band)
- The application of a bias voltage produces an electric field, which causes the electrons and holes to move toward active sensors
- E \propto pulse height
- Silicon detectors are characterized by their dark current
- current flowing from the detector when reversed biased



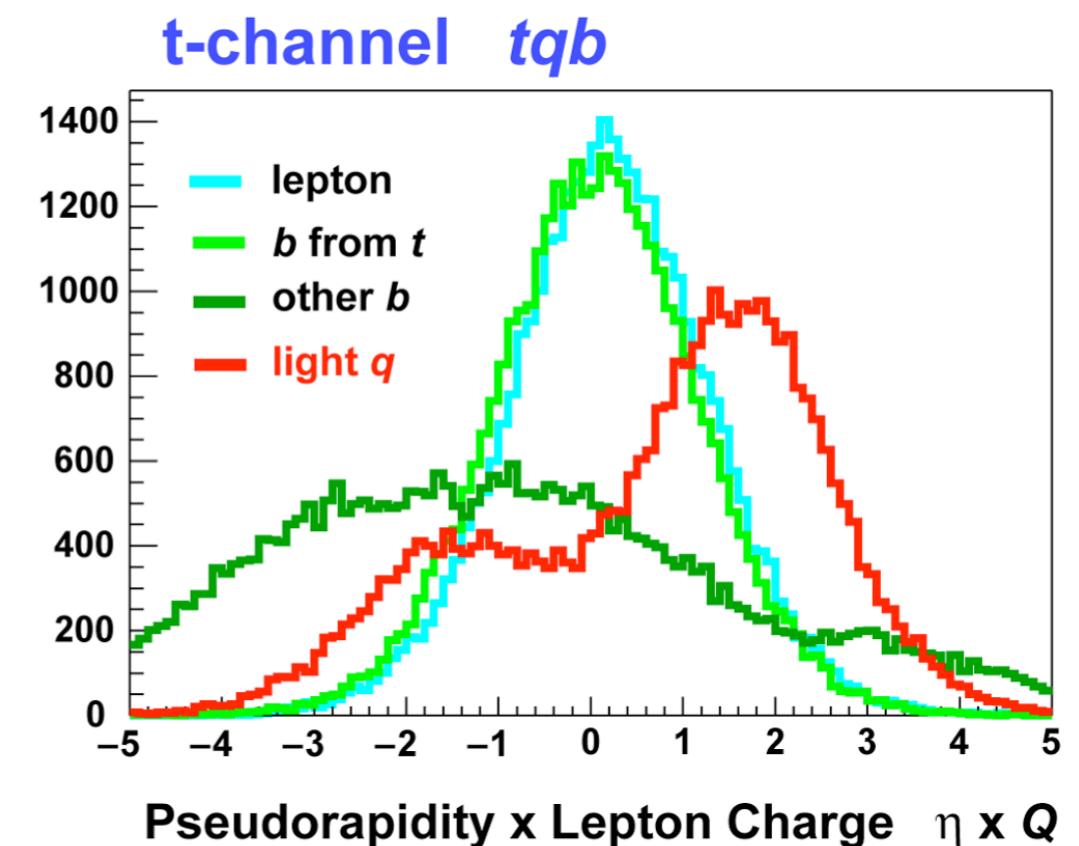
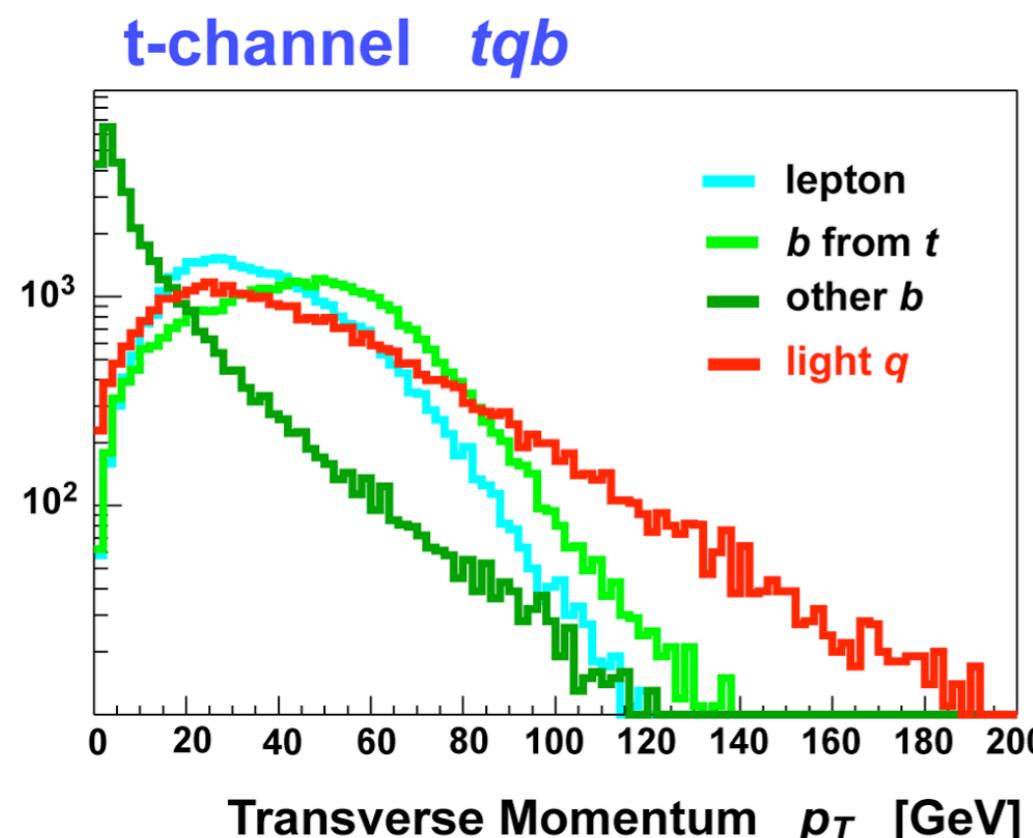
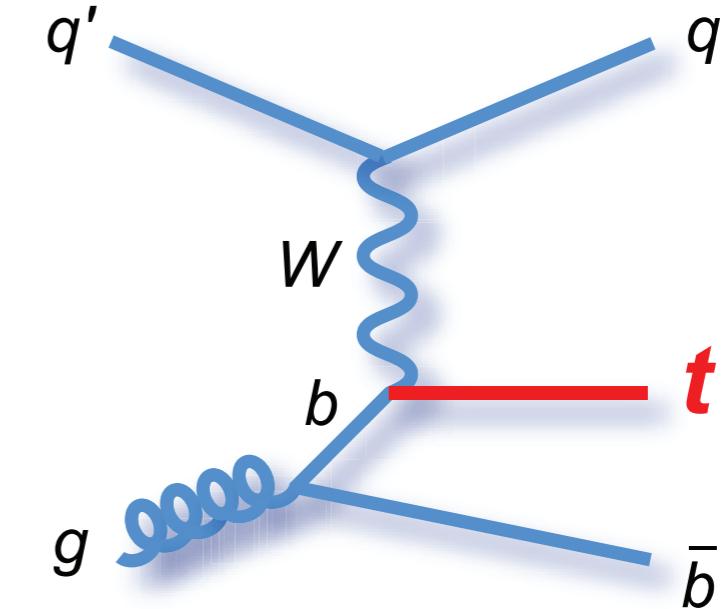
Single Top At The Parton Level

- We generate single top signal using CompHEP+Pythia

- Features:

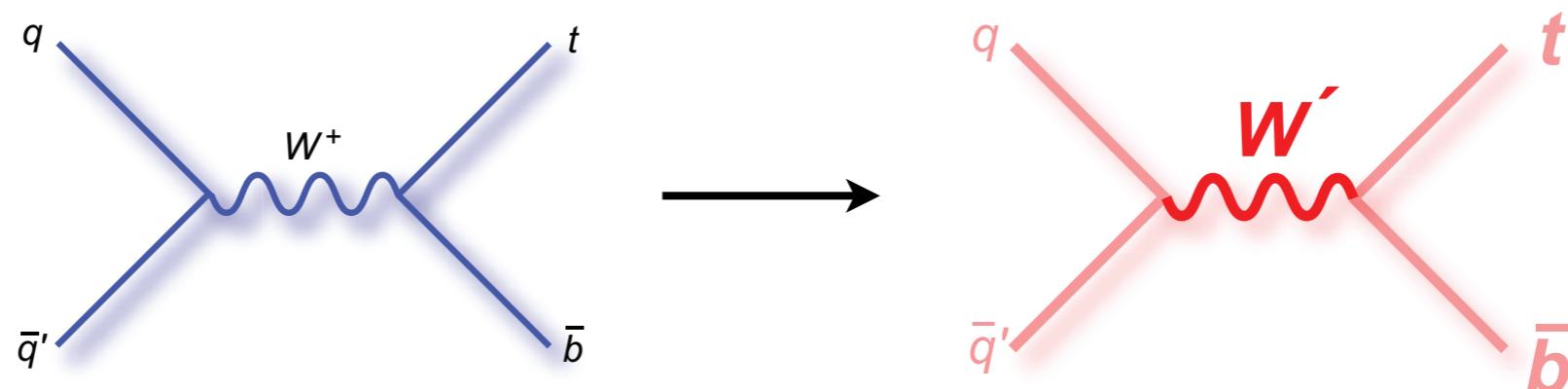
- Spin information is retained through decay chain (important for top)
- Effective NLO generator. It reproduces NLO distributions from ZTOP and MCFM

- Parton-level t-channel P_T and η distributions

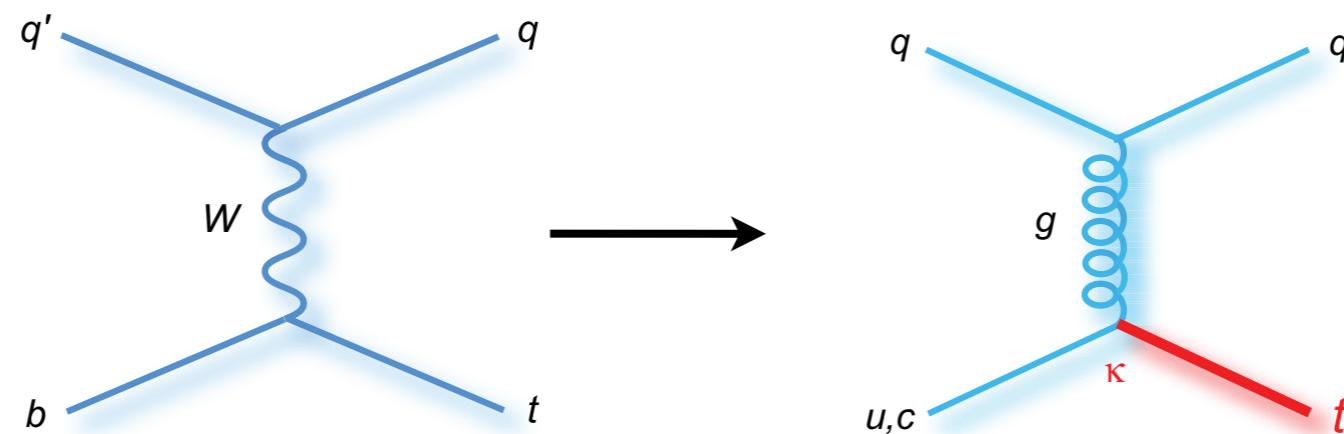


More Motivation For Measuring Single Top

- Single top is sensitive to physics BTSM
- s-channel is sensitive to charged bosons



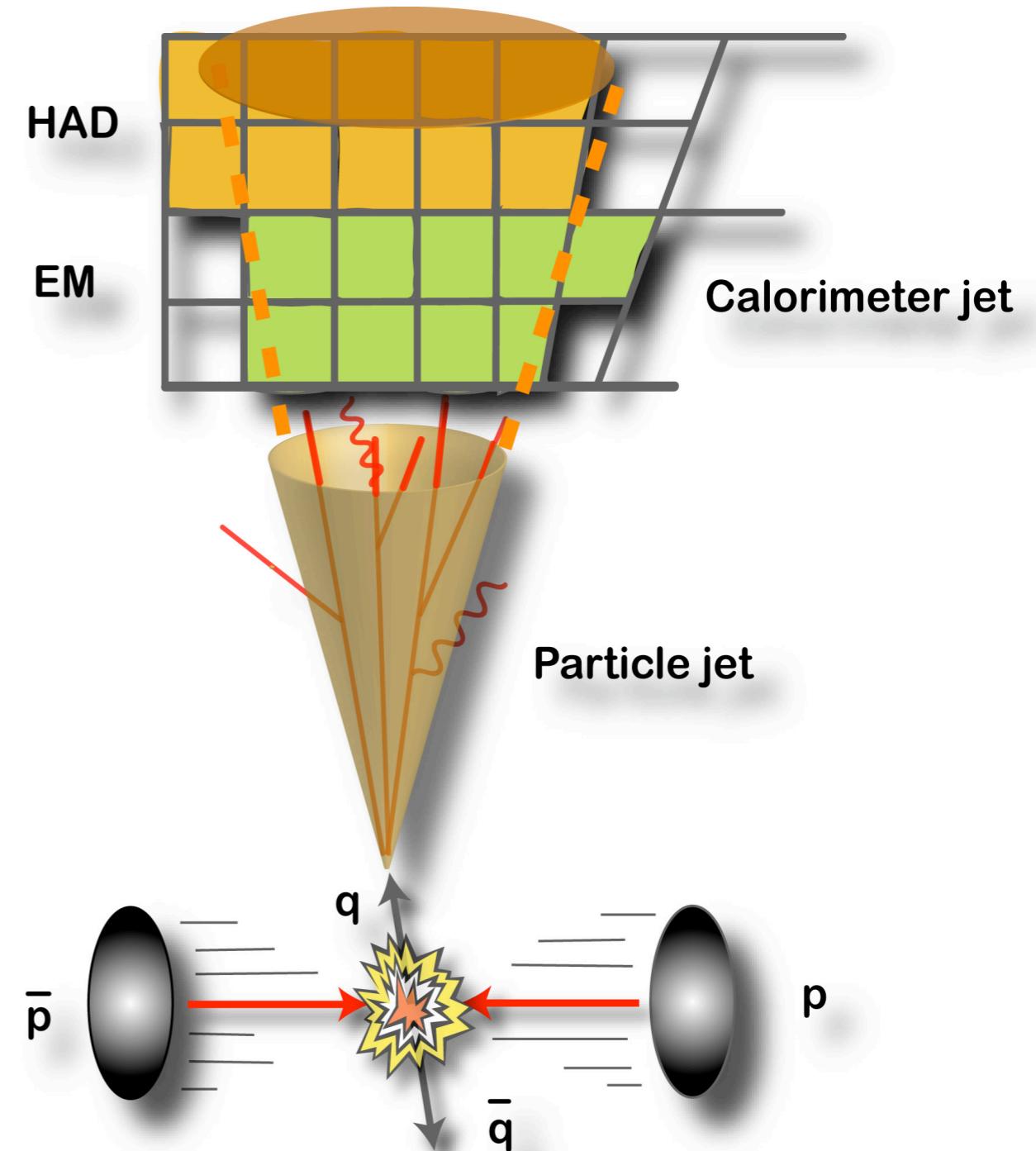
- DØ w/ 230 pb^{-1} ; $M(W'_R \rightarrow qq', l\nu) > 630 \text{ GeV}$ and $M(W'_R \rightarrow qq') > 670 \text{ GeV}$ [hep-ex/0607102]
- CDF w/ 955 pb^{-1} ; $M(W'_R \rightarrow qq') > 760 \text{ GeV}$ ($M(W'_R) > M(\nu_R)$) and $M(W'_R \rightarrow qq') > 790 \text{ GeV}$ ($M(W'_R) < M(\nu_R)$)
- t-channel is sensitive to flavor changing neutral currents in the top section



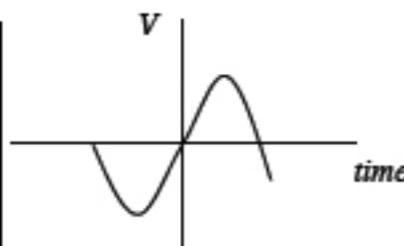
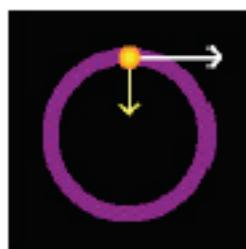
- DØ w/ 230 pb^{-1} ; $K_{cq}/\Lambda < 0.15 \text{ TeV}^{-1}$ and $K_{uq}/\Lambda < 0.037 \text{ TeV}^{-1}$ [hep-ex/0702005]

Transfer Functions: $W(x|y)$

- Map parton to detector object
- Account for detector resolution
- Electrons ($Z \rightarrow ee$ Monte Carlo)
 - Central only; $f(E_e, \theta)$
- Muons ($Z \rightarrow \mu\mu$ Monte Carlo)
 - w/ and w/o SMT hits; $f(q/p_T)$
 - Central ($|\eta| < 1.6$) and forward ($1.6 < |\eta| < 2$)
- Jets (ttbar Monte Carlo)
 - 3 jet types (light, b, $b \rightarrow \mu$); $f((E_j, E_p))$



Acceleration



$$mv^2/R = evB \\ \Rightarrow R = mv/eB \\ = p/eB$$

And as the particle speeds up, the frequency of the cavity must change in step ("in sync")

thus, we use RF cavities and power sources...

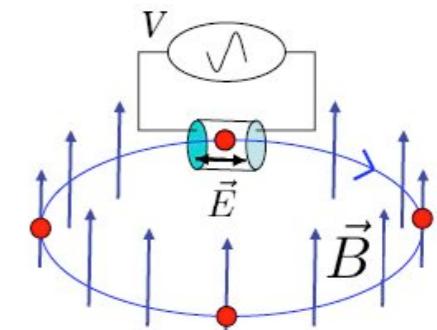
FM Radio Stations: 88 - 108 MHz!

What frequencies do we need?

Let's say $v \sim c$, and say $R = 1 \text{ m}$

then,

$$f = v / 2\pi R \\ = (3 \times 10^8 \text{ m/s}) / (2\pi \text{ 1m}) \\ = 5 \times 10^7 / \text{s} = 50 \text{ MHz}$$

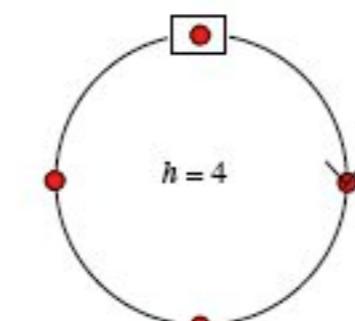
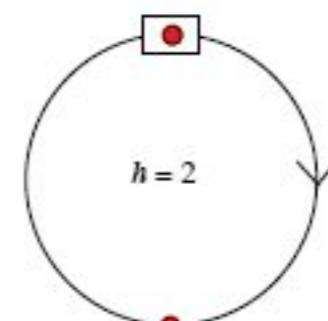
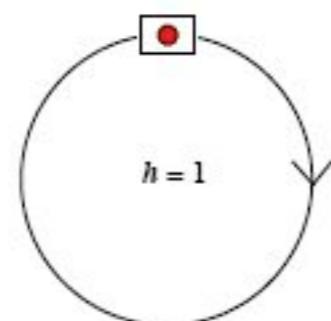


$$\text{Voltage} = V \sin(2\pi f t + \delta)$$

$$f = 1/T = v / 2\pi R$$

Each revolution, energy changes by amount
 $\Delta E = e V \sin(\delta)$

- If the RF cavity frequency is twice the revolution frequency, then there can be two bunches sustained in the synchrotron. If $f_{rf} = h \times f_0$, then there can be h bunches.



Tevatron

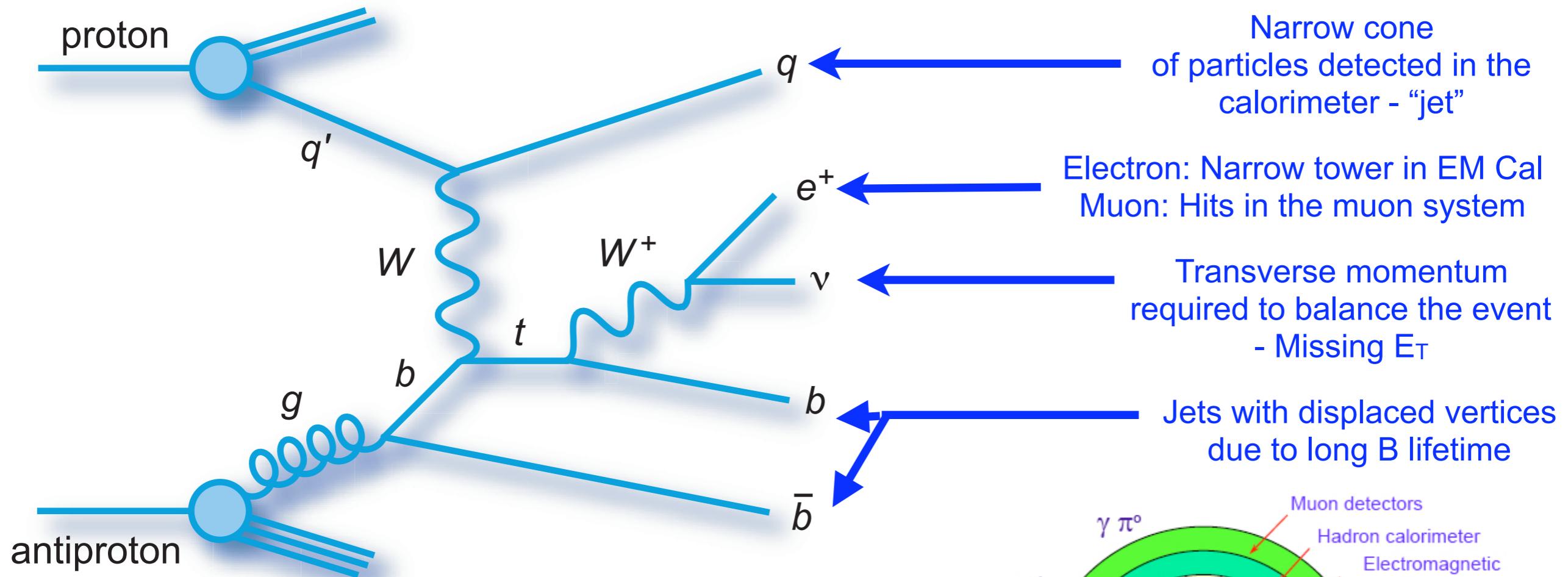
$$R = 1000 \text{ m} \\ h = 1113$$



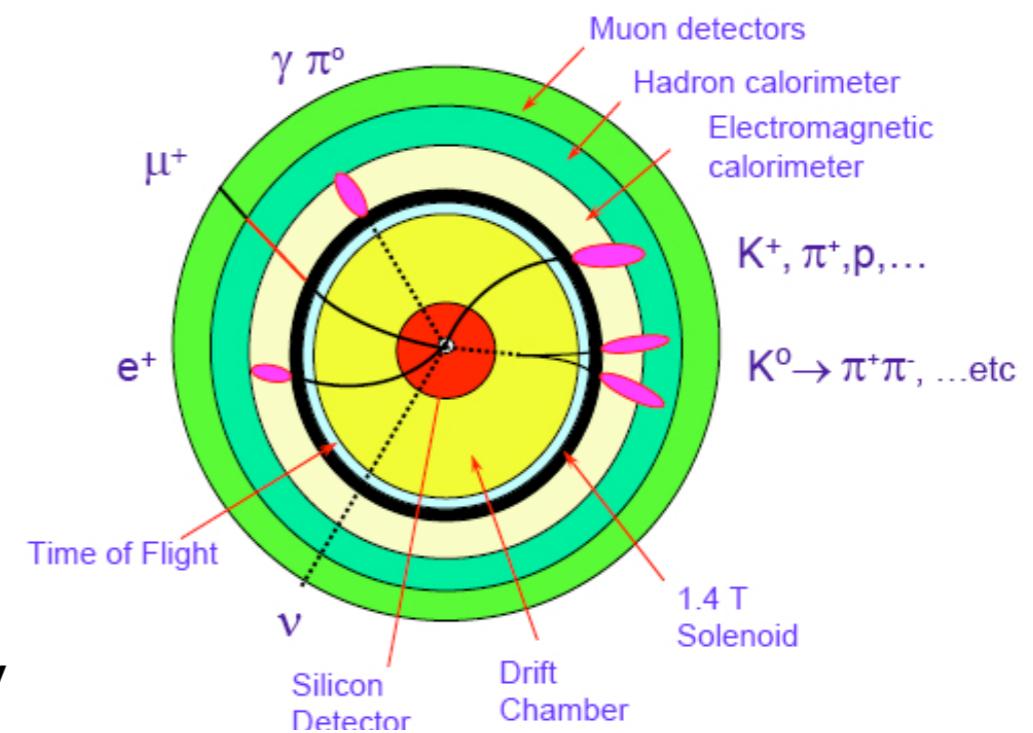
$$R = 500 \text{ m} \\ h = 588$$

Single Top Search Strategy

- We look for single top in the “lepton+jets” decay channel



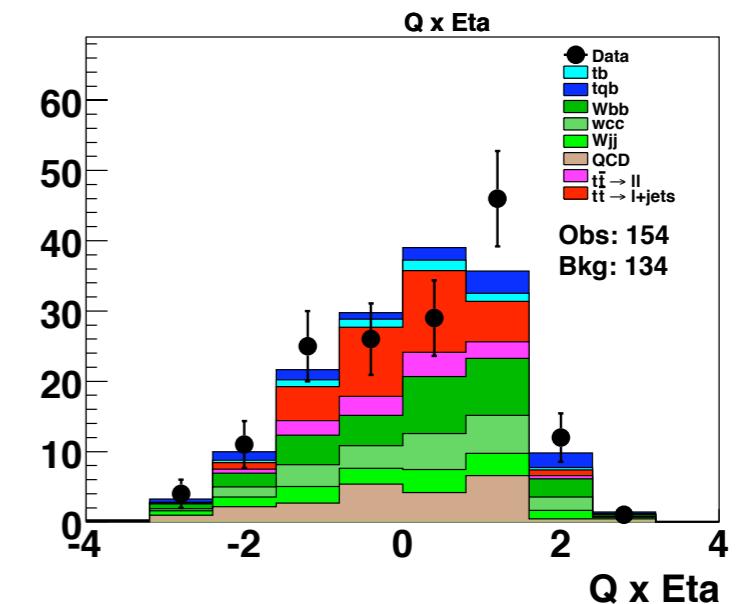
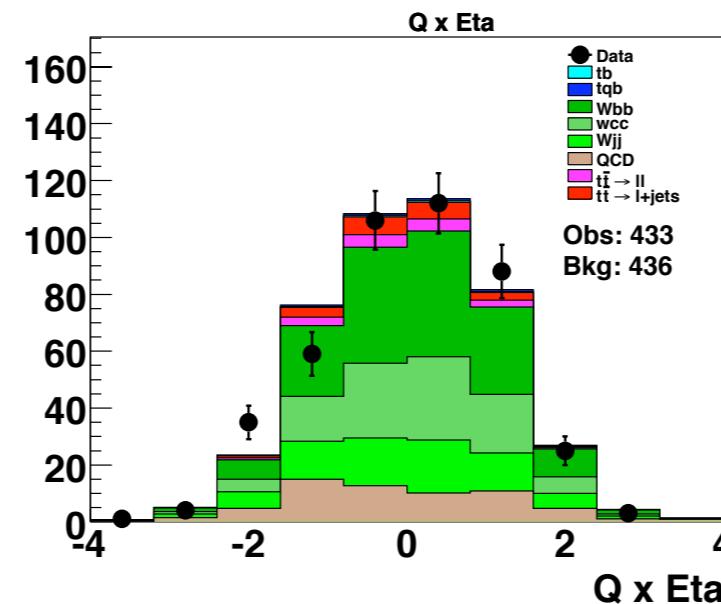
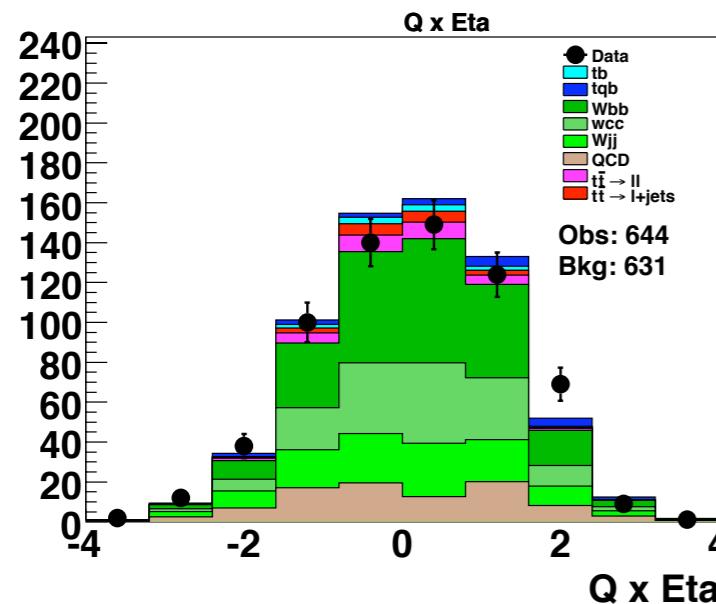
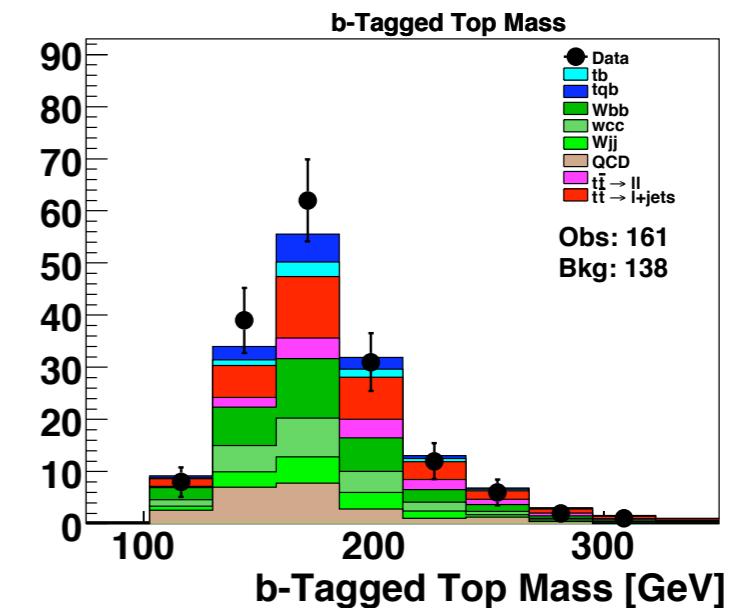
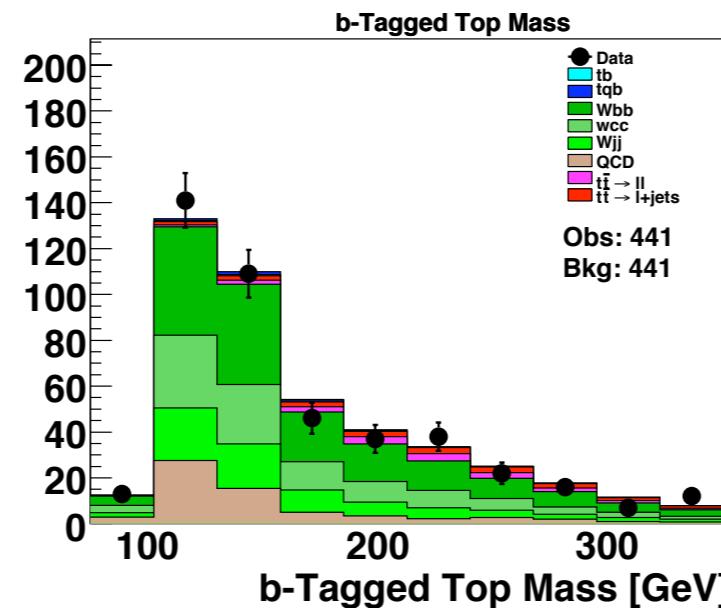
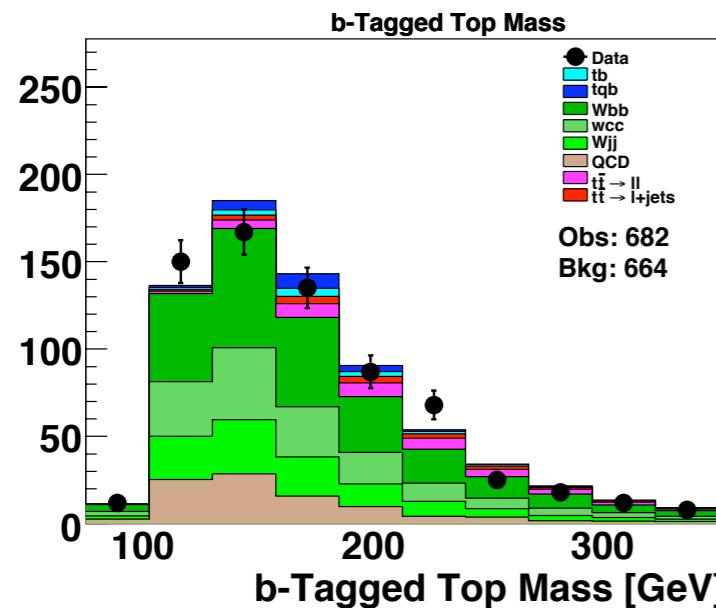
- Maximize signal acceptance
 - Electron or muon with $P_T > 15 \text{ GeV}$
 - Missing $E_T > 15 \text{ GeV}$
 - Between two and four jets with $P_T > 15 \text{ GeV}$



Event Characteristics



Look at variables sensitive to single top before and after a cut on the discriminant.



All Events

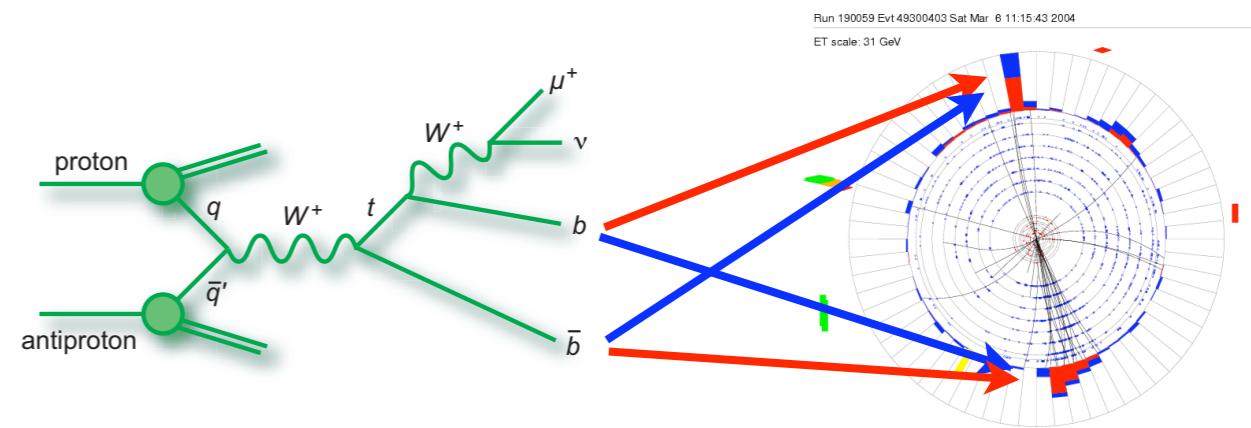
$D(x) < 0.4$

$D(x) > 0.7$

Jet-Parton Assignment

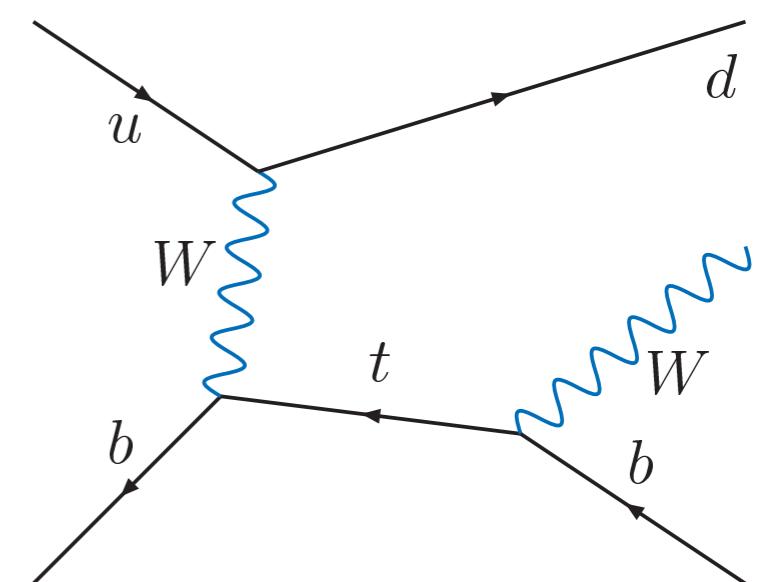
- We must sum over all jet parton combinations to ensure we choose the correct assignment.

$$d\sigma(\vec{x}) = \sum_{\text{comb}} \varepsilon_{\text{comb}} \times d\sigma_{\text{comb}}(\vec{x})$$



- If we no knowledge of the correct assignment, then $\varepsilon_{\text{comb}} = \text{constant}$
- We can use b-tagging TRFs to help assign b jets to b quarks and untagged jet to light quarks.
 - If jet is b-tagged and parton is b quark, then weight by b TRF.
Same for charm and light quarks.
- Example: Single tagged t-channel event.
Final state is b quark and light quark

$$d\sigma(\vec{x}) = \varepsilon_b(1 - \varepsilon_l)d\sigma_{bl} + (1 - \varepsilon_b)\varepsilon_l d\sigma_{lb}$$

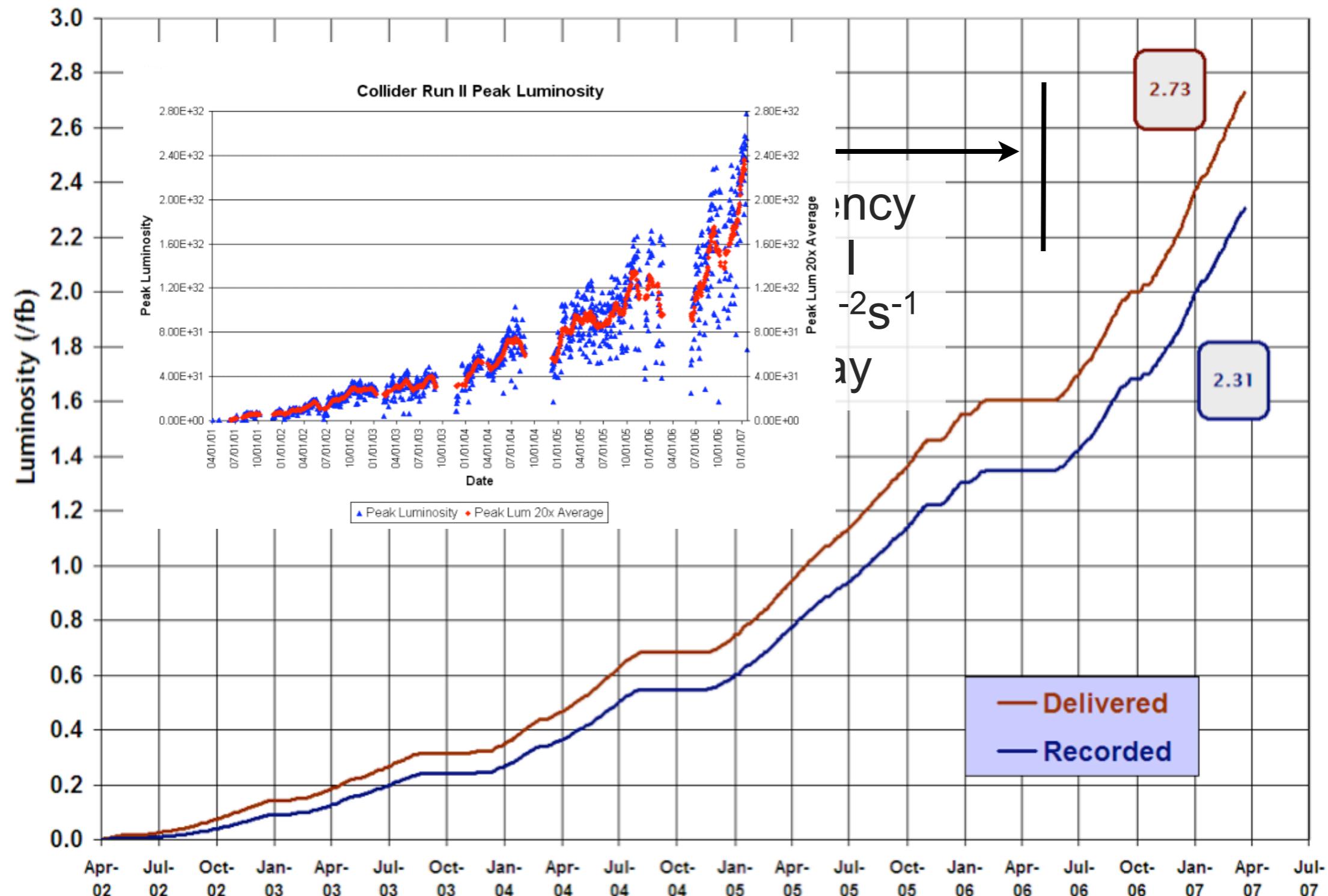


Run II Data Taking



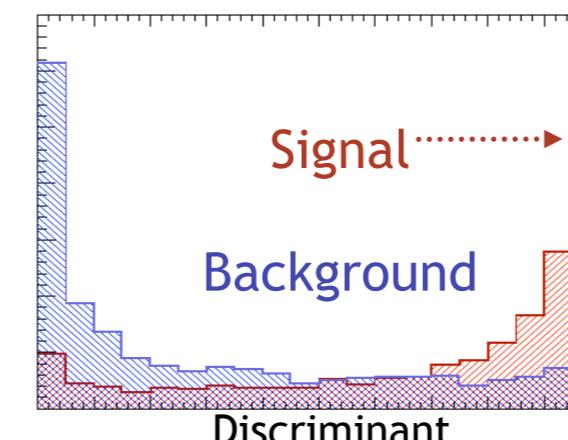
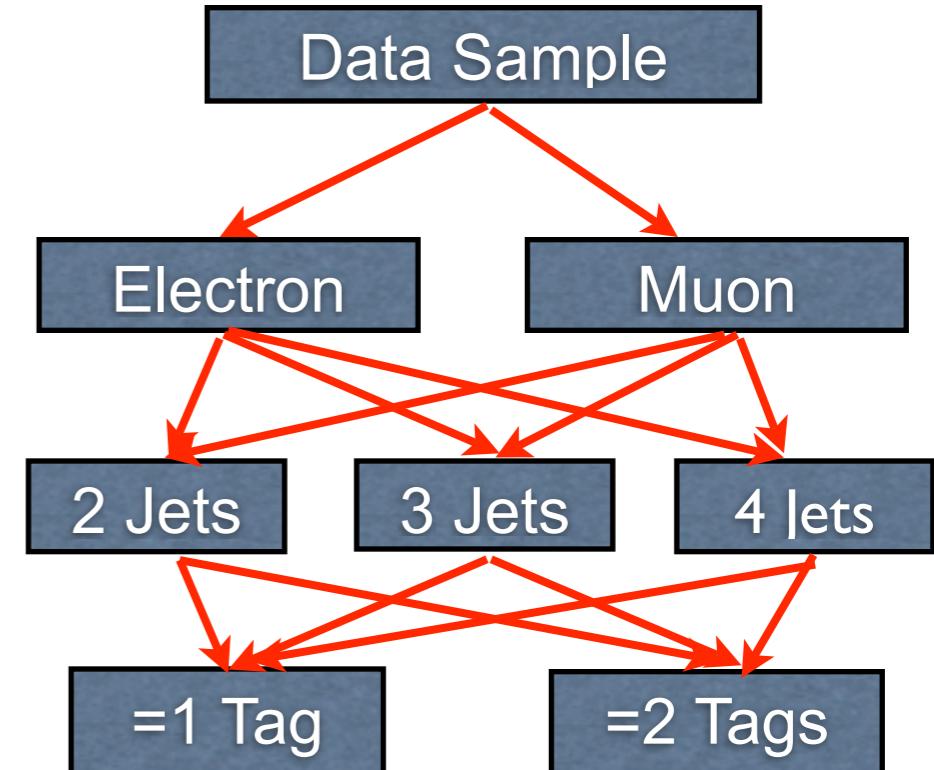
Run II Integrated Luminosity

19 April 2002 - 8 April 2007



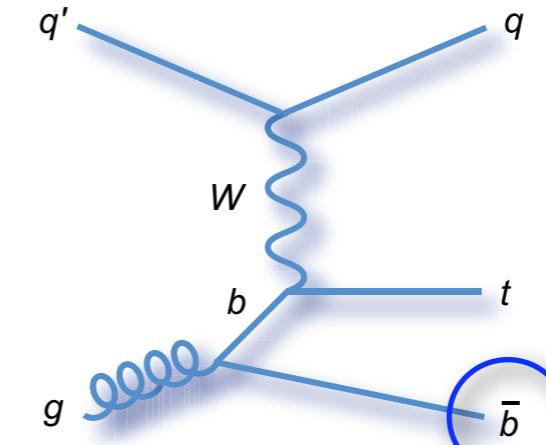
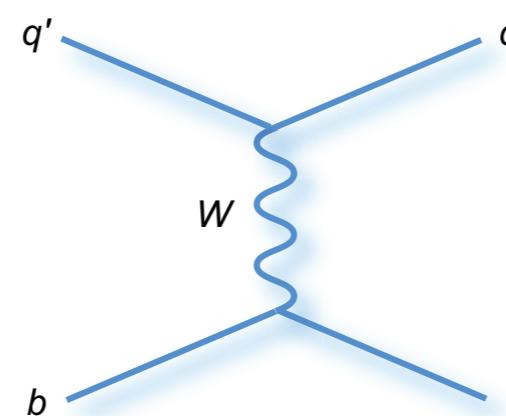
Single Top Measurement Strategy

- Select W+jet-like events
 - Maximize single acceptance while ensuring backgrounds are well-modeled
- Divide data sample by number of jets, W decay lepton, and number b-tags
 - Lepton: trigger separately on electron and muon. Backgrounds also different
 - Jets: s-channel and t-channel in two jet bin, while t-channel also in third
 - b-tags: s-channel and t-channel with one tag, while s-channel should have two
- Separate signal and background
 - **Matrix element method**, boosted decision trees, bayesian neural networks
- Combine samples when determining cross section



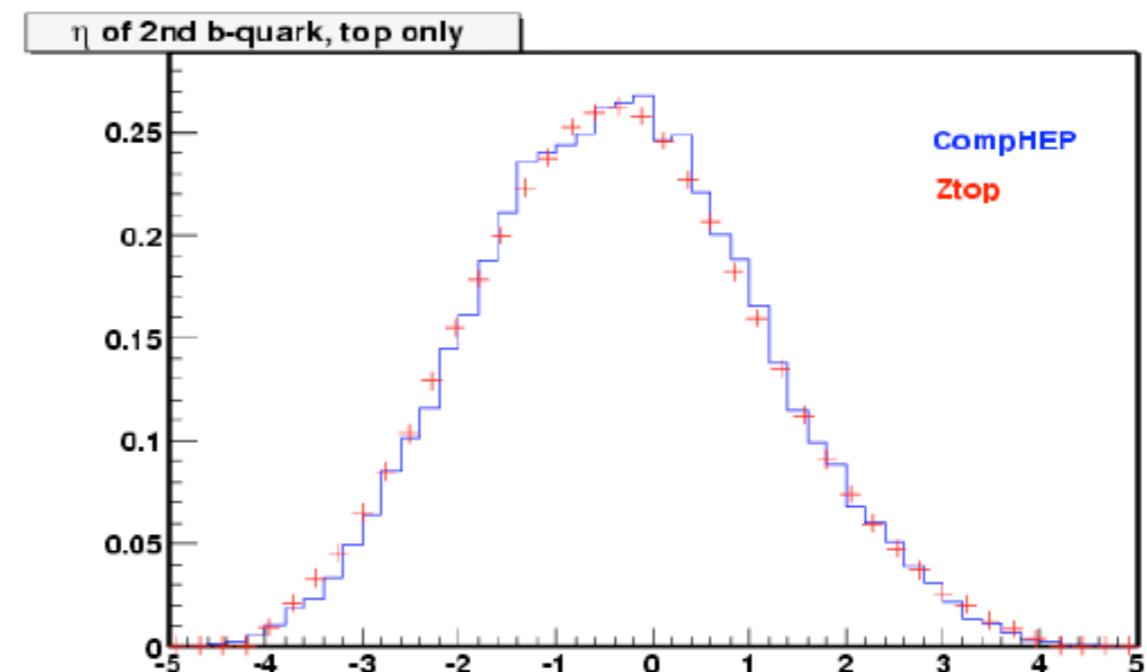
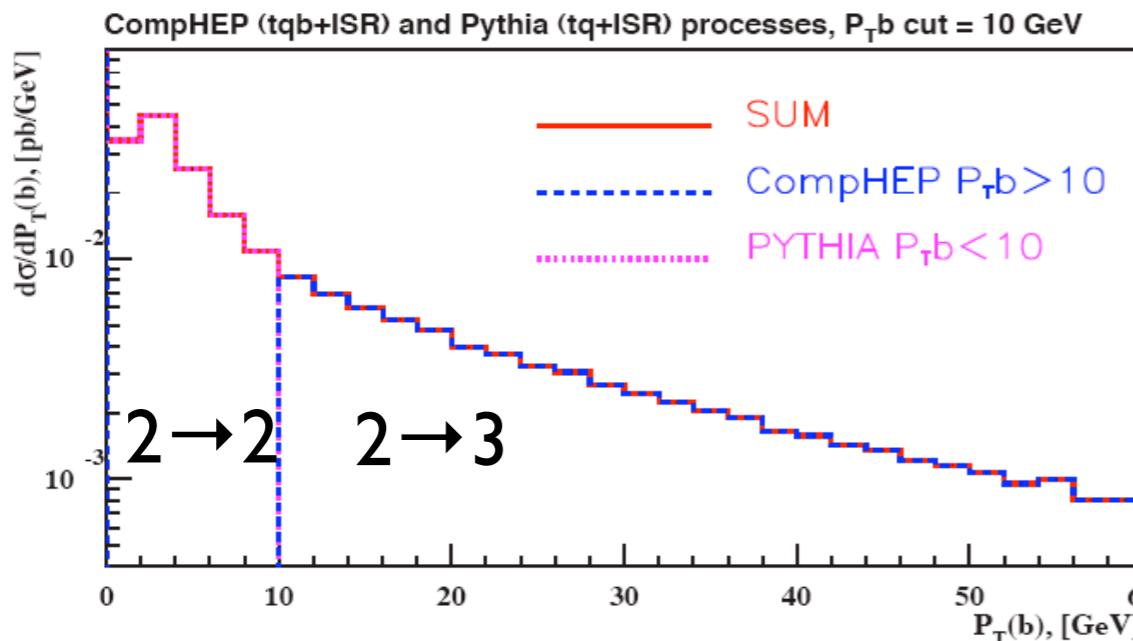
Single Top Event Generation

- Use CompHEP+Pythia parton shower to model signal
- Avoid double counting when



- Procedure:

- Define two regions of phase space: (1) $p_T(b) < 10 \text{ GeV}$ and (2) $p_T(b) > 10 \text{ GeV}$
- (1) use 2 \rightarrow 2 diagram with Pythia $g \rightarrow bb$; (2) use 2 \rightarrow 3 diagram from CompHEP



Combined Result

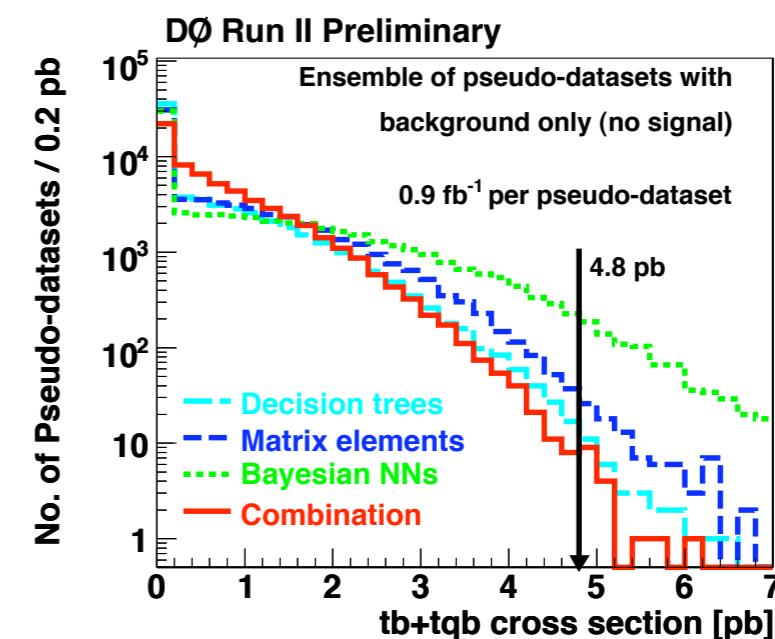
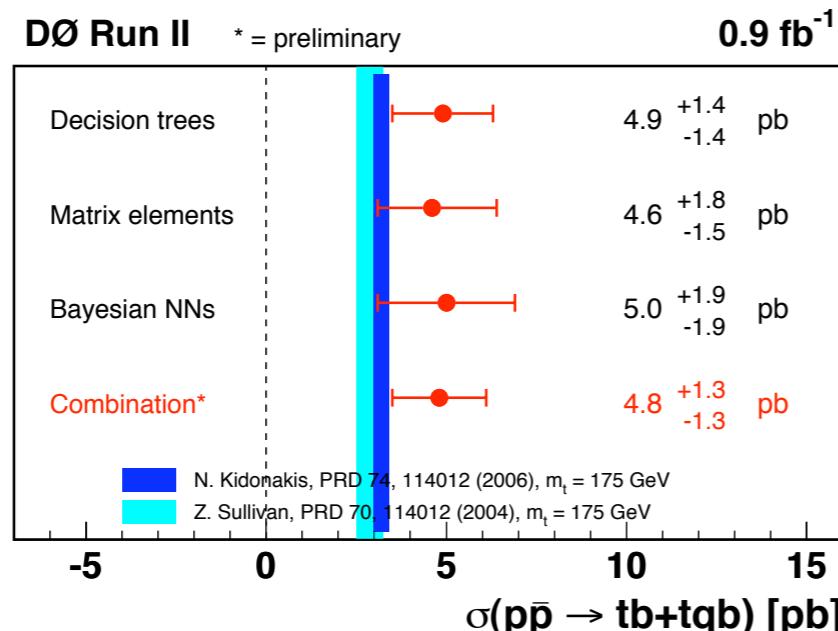
- The matrix element, Bayesian neural network, and decision tree analyses were combined using the BLUE (Best Linear Unbiased Estimator) method

$$\sigma_{\text{comb}} = w_{BNN}\sigma_{BNN} + w_{DT}\sigma_{DT} + w_{ME}\sigma_{ME}$$

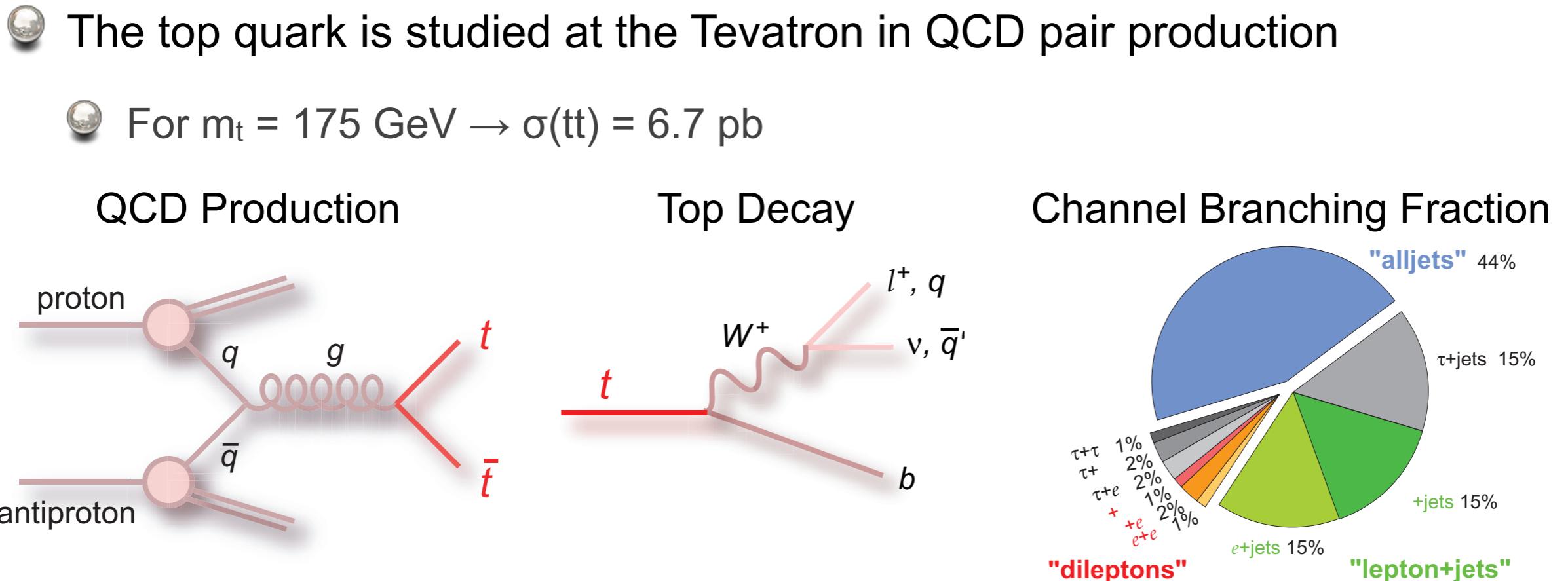
- Need to know correlation between analyses to determine weights
- Use Standard Model ensemble set

$$w_i = \frac{\sum_j \text{Cov}^{-1}(\sigma_i, \sigma_j)}{\sum_{i,j} \text{Cov}^{-1}(\sigma_i, \sigma_j)}$$

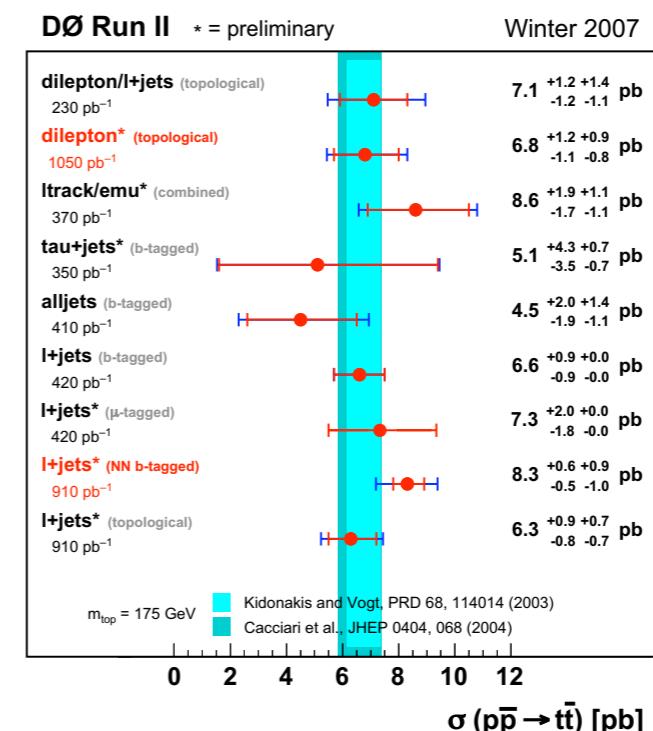
$$\rho = \begin{pmatrix} DT & ME & BNN \\ 1 & 0.57 & 0.51 \\ 0.57 & 1 & 0.45 \\ 0.51 & 0.45 & 1 \end{pmatrix}$$



QCD Top Pair Production

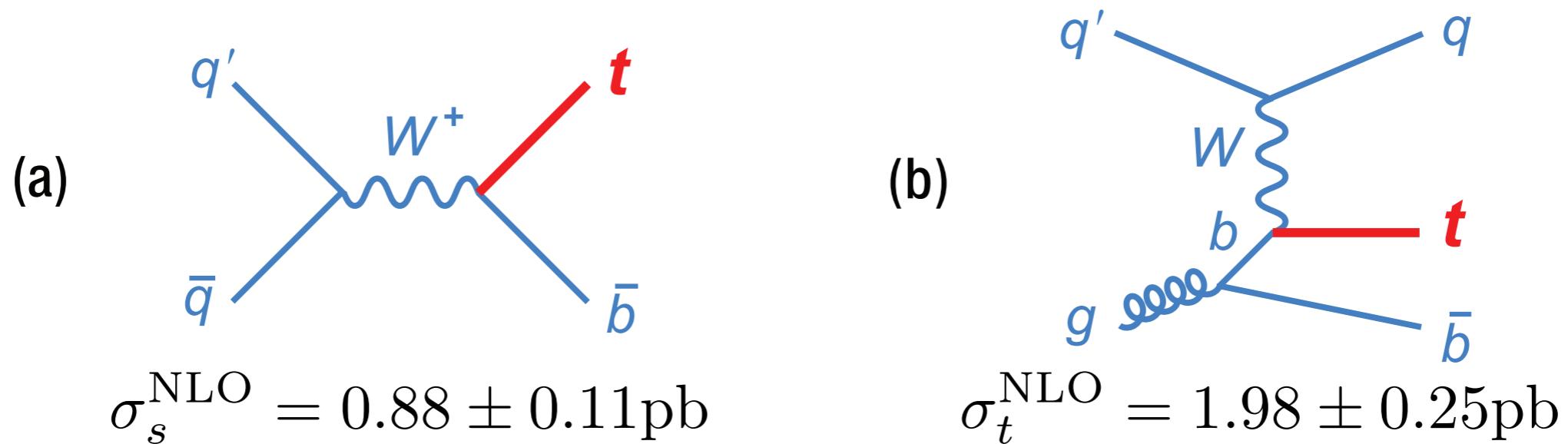


- Well measured at Run II by DØ and CDF



Single Top Quark Production

- Top quarks can also be produced through an electroweak interaction
- Two production modes at the Tevatron



- Motivation (1) : W - t - b electroweak vertex in production $\Rightarrow \sigma_{tb+tqb} \propto |V_{tb}|^2$
- If three quark generations $\rightarrow |V_{tb}|$ is highly constrained

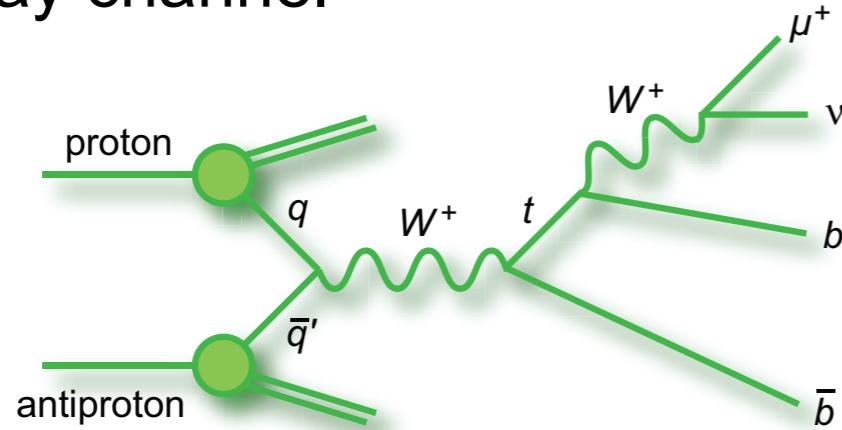
$$|V_{tb}| = 0.999100^{+0.000034}_{-0.000004}$$

- Measured lower limits assuming unitarity $|V_{tb}| > 0.78$

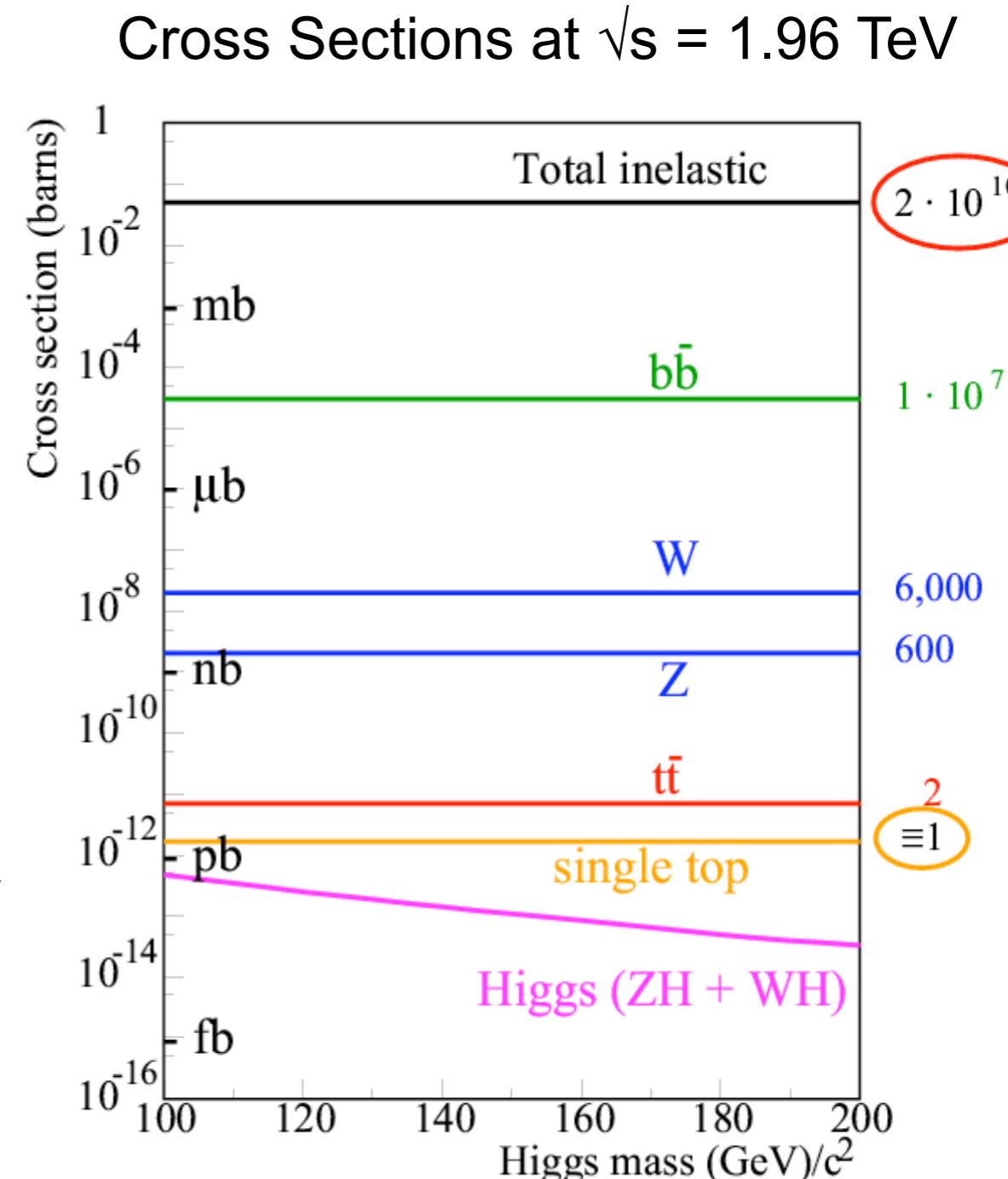
D. Acosta et. al (hep-ex/0505091)
V. M. Abazov et al. (hep-ex/0603002)

Single Top Search Strategy

- ➊ Tevatron produces one single top event for every 20 billion collisions
- ➋ Still $\sim 15\text{-}20$ events per day
- ➌ Look for single top in lepton+jets decay channel

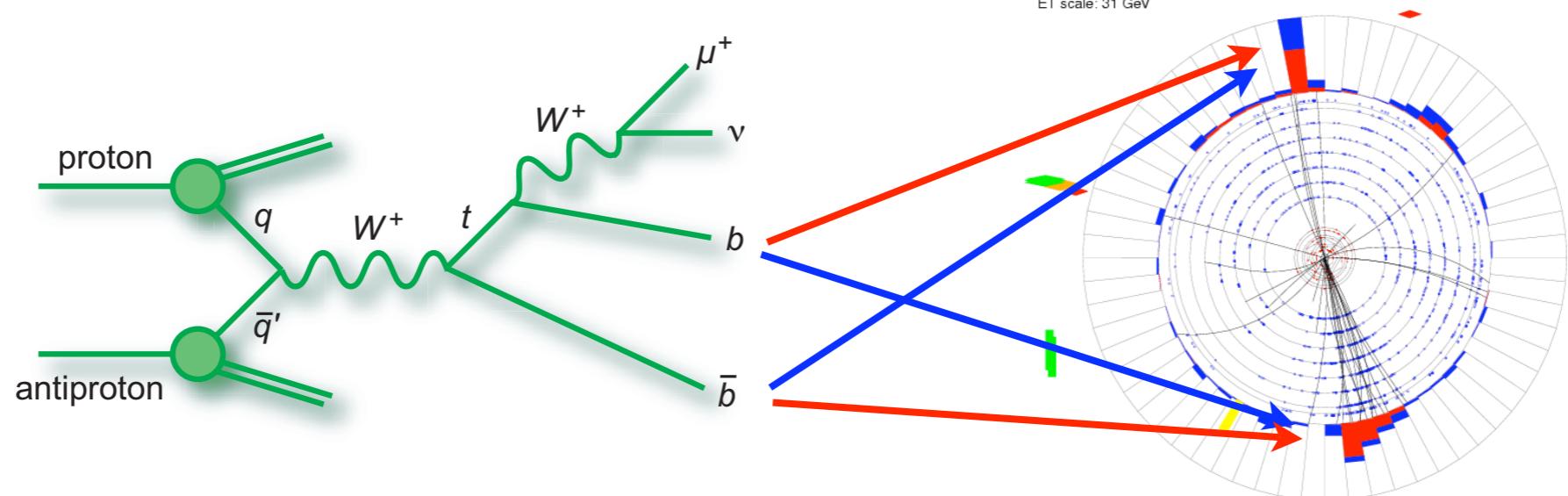


- ➍ Trigger on one lepton + b from top decay
- ➎ Select W+jets-like events:
 - ➏ One high p_T lepton from W decay
 - ➏ large missing E_T (do not detect the neutrino from W decay)
 - ➏ Between two and four jets



Jet to Parton Assignment

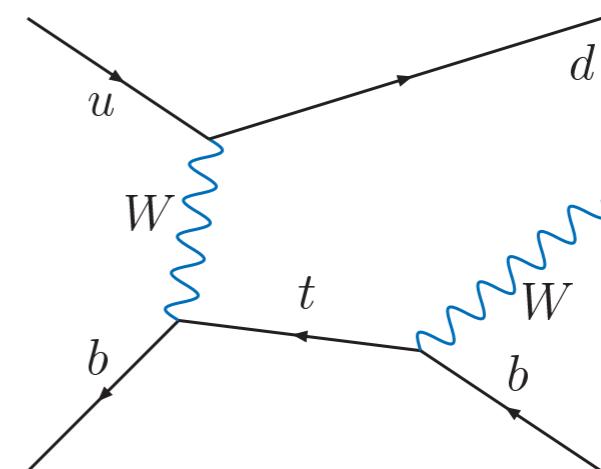
- Events with two jets have two possible jet-parton permutations



- Define event probability as weighted sum over all jet-parton permutations

$$P(\vec{x}) = \sum_i \varepsilon_i \times P_i$$

- Weight permutations by b -tagging probability depending on parton flavor
 - b -tagged jet matched to b quark
 - ! b -tagged jet matched to light quark

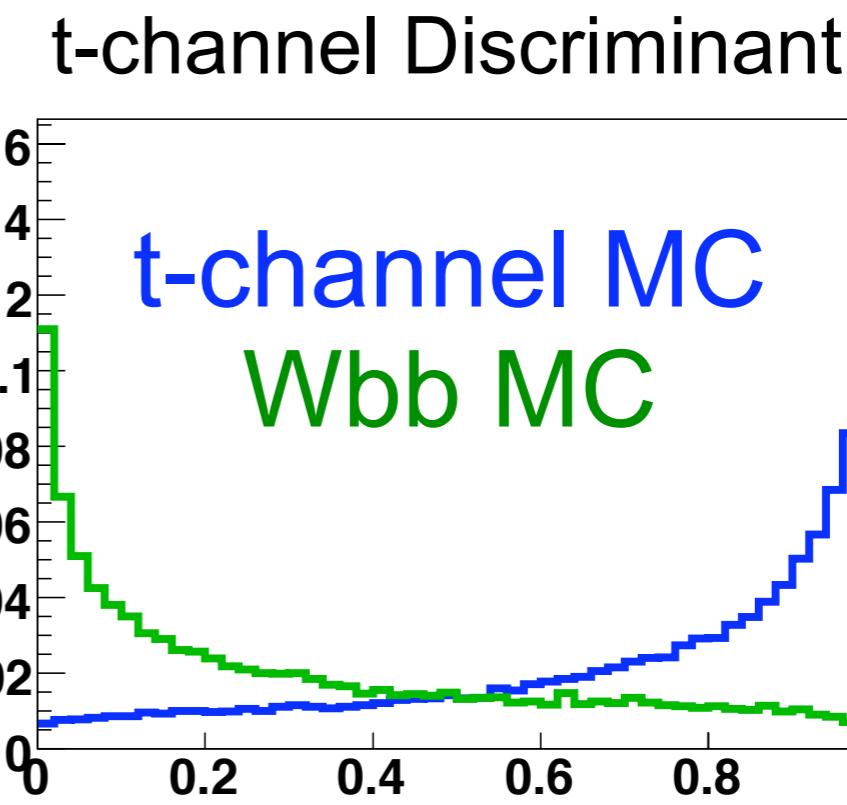
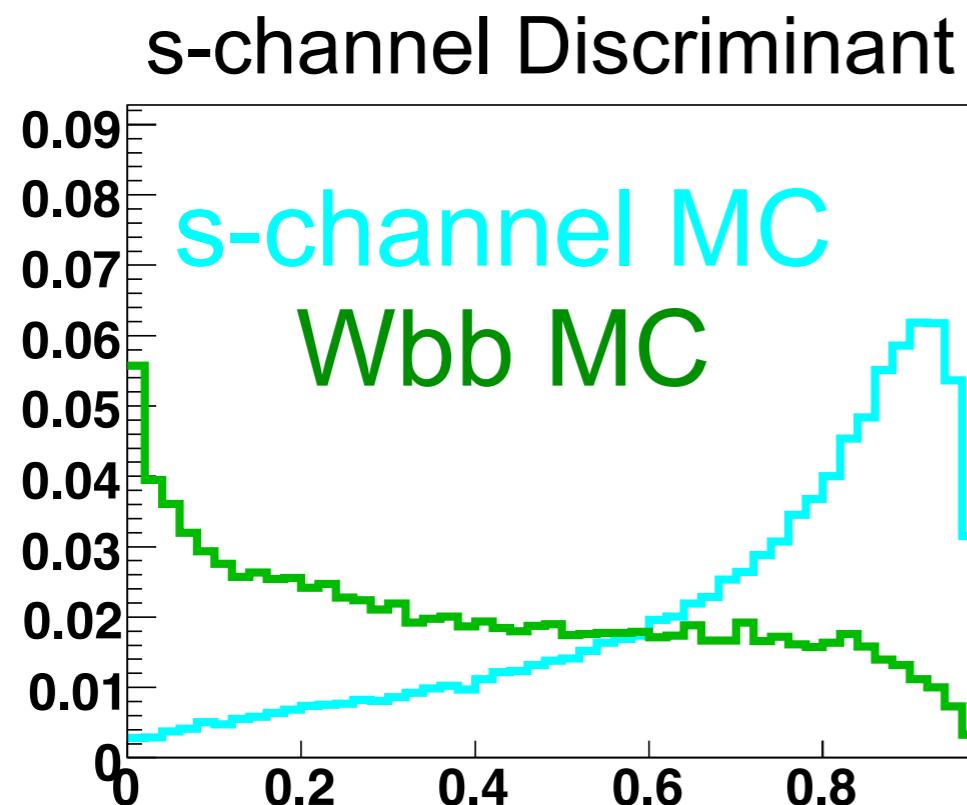


Matrix Element Discriminant

- Combine signal and background probability densities using the *a-posteriori* Bayesian probability density for signal given the event
- Two discriminants: s-channel as signal and t-channel as signal

$$D_{tb|tqb}(\vec{x}) = \frac{P_{tb|tqb}(\vec{x})}{P_{tb|tqb}(\vec{x}) + P_{\text{Background}}(\vec{x})}$$

- Performance on signal and background Monte Carlo events

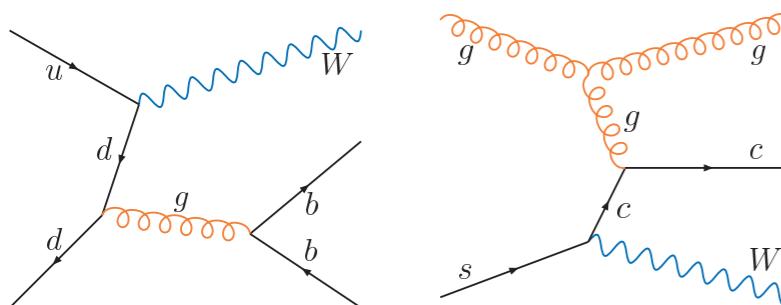


Matrix Element Discriminant

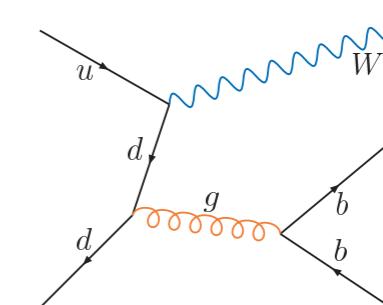
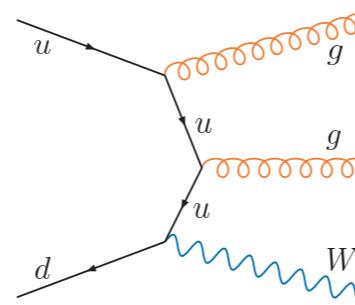
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$$D_{tb|tqb}(\vec{x}) = \frac{P_{tb|tqb}(\vec{x})}{P_{tb|tqb}(\vec{x}) + P_{\text{Background}}(\vec{x})}$$

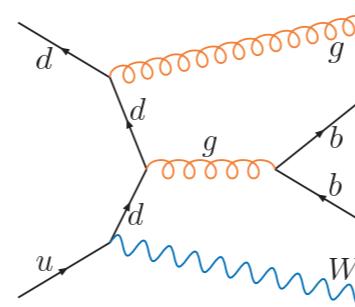
- $P_{\text{Background}}$ depends on number of *b*-tags and number of jets



Events w/ 2 jets and one *b*-tag



Events w/ 2 jets and two *b*-tags

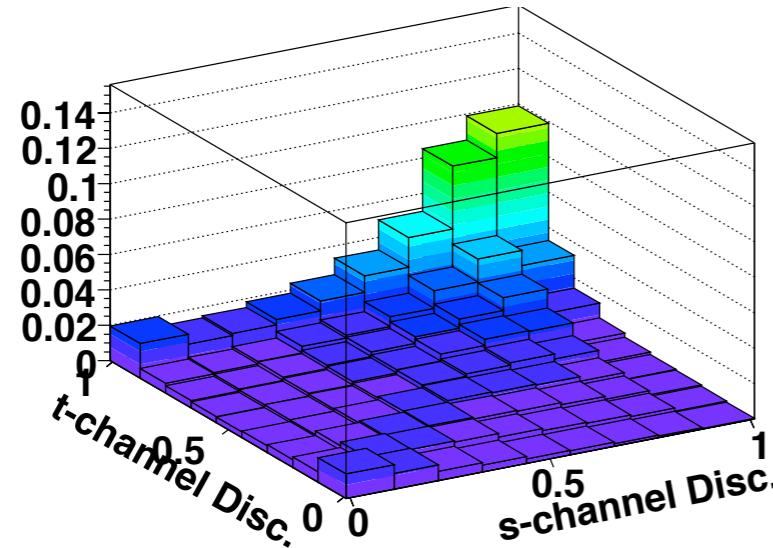


Events w/ 3 jets and one or two *b*-tags

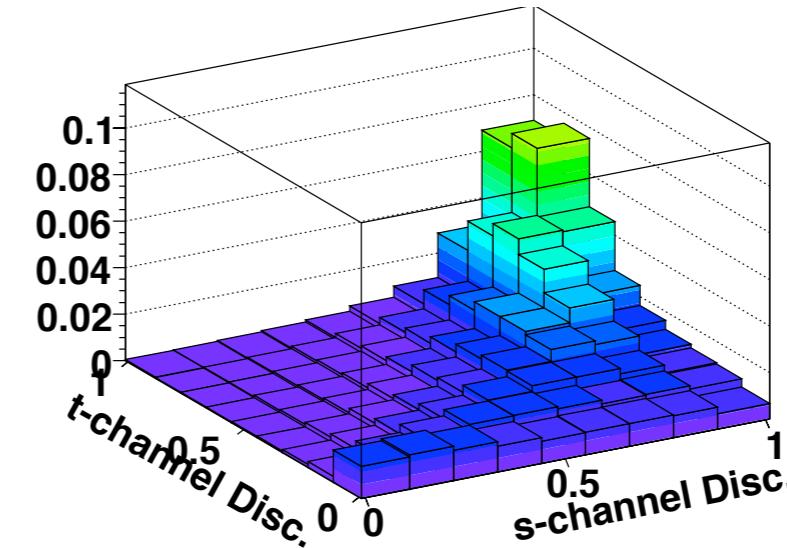
Discriminant Performance

- Calculate discriminant for signal and background Monte Carlo events

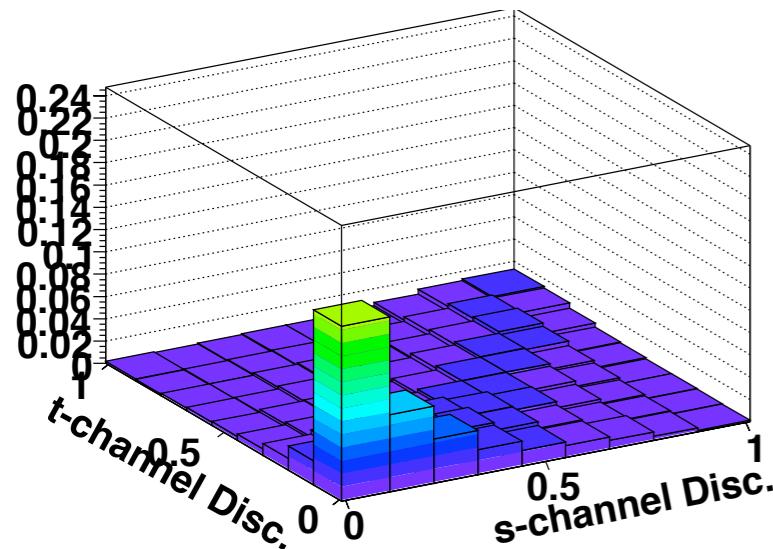
t-channel MC



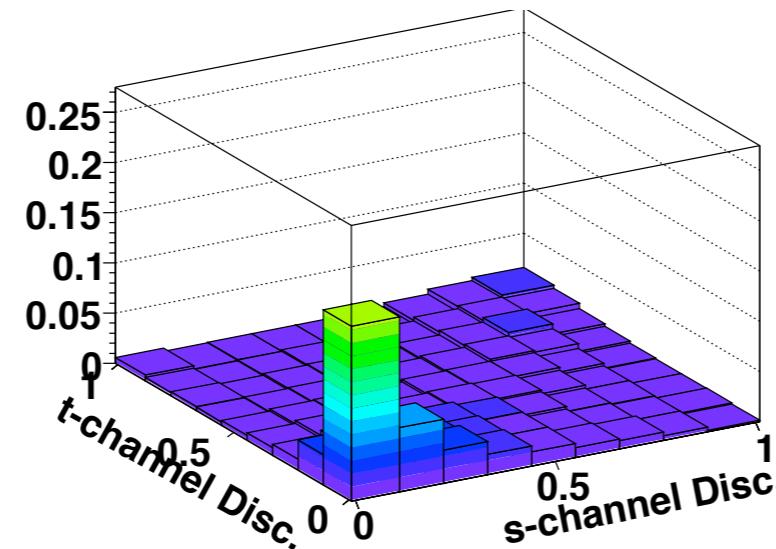
s-channel MC



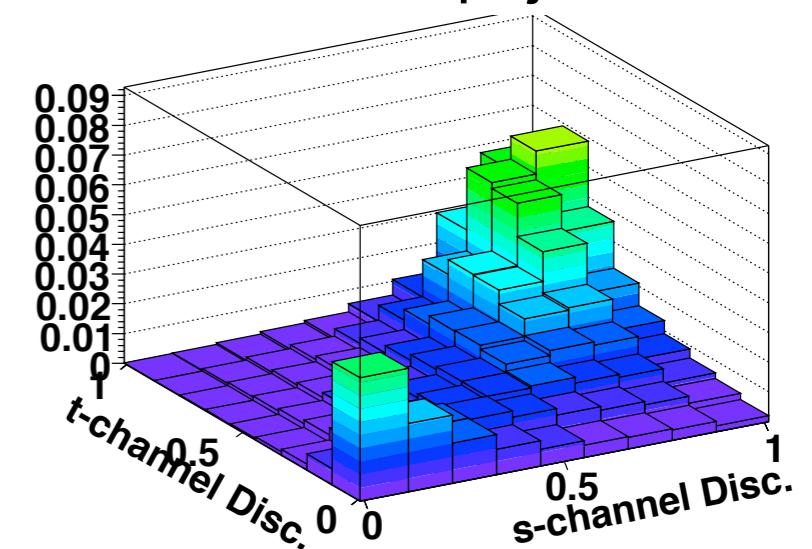
Wbb MC



Wjj MC



ttbar → lep+jets MC



Cross Section Measurement Method I

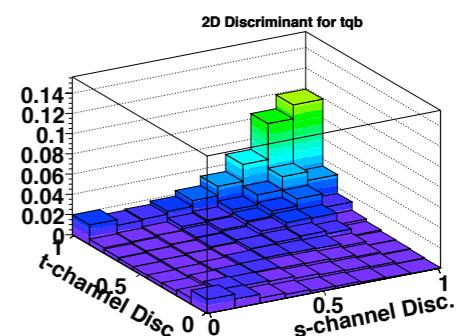
- Determine cross section by calculating the Bayesian posterior density function
- Bayes Theorem (general): $P(A|B) = \frac{P(B|A)P(A)}{P(B)}$
- Bayes Theorem (high energy physics)

$$P(n_{exp}|N_{obs}) = \frac{P(N_{obs}|n_{exp})P(n_{exp})}{P(N_{obs})}$$

$$n_{exp} \rightarrow n_{sig} + n_{back} = a \times \sigma_{sig} + \sum_i n_{back,i}$$

- $P(N_{obs}|n_{exp})$: Likelihood of observing N events given n expected

$$P(N_{obs}|n_{exp}) \rightarrow \mathcal{L}(N_{obs}|n_{exp}) = \frac{n_{exp}^{N_{obs}} e^{-n_{exp}}}{N_{obs}!}$$



- $P(n_{exp})$: $P(n_{exp}) \rightarrow \pi(n_{exp}) \rightarrow \pi(a, \vec{n}_{back}, \sigma) = \pi(\sigma) \times \pi(a, \vec{n}_{back})$
- $P(N_{obs})$: Normalization

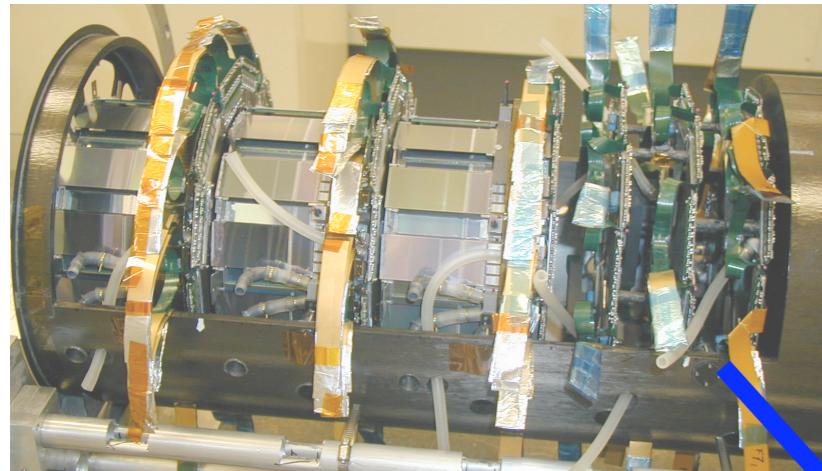
$$\pi(\sigma) = \frac{1}{\sigma_{max}}, 0 < \sigma < \sigma_{max}$$

Cross Section Measurement Method II

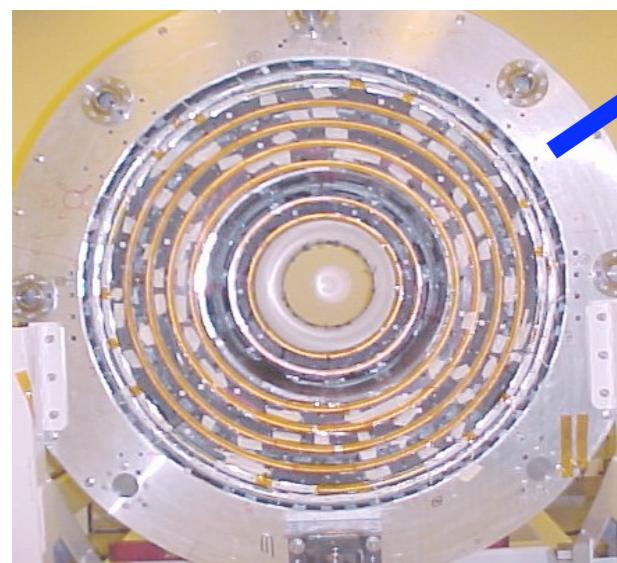
- Acceptance a and background estimate n_{back} have errors due to systematic uncertainties of signal and background yields
 - $\pm\delta a = |\text{Signal}(\pm 1\sigma \text{ factor}) - \text{Signal}(\text{Nominal})| / \text{Signal}(\text{Nominal})$
 - $\pm\delta n_{back} = |\text{Background}(\pm 1\sigma \text{ factor}) - \text{Background}(\text{Nominal})| / \text{Background}(\text{Nominal})$
- Example:
 - Jet Energy Scale: factor applied to jets to correct measured jet energy back to the particle level.
 - Apply nominal JES to signal and background to get nominal yields
 - Apply $\pm 1\sigma$ JES to signal and background to get $\pm 1\sigma$ yields
- $\pi(a, \vec{n}_{back})$ is then sampled from multivariate Gaussian: $G([\pm\delta a, \pm\delta n_{back}])$

Source of Uncertainty	Size
Top pairs normalization	18%
W+jets & multijets normalization	18–28%
Integrated luminosity	6%
Trigger modeling	3–6%
Lepton ID corrections	2–7%
Jet modeling	2–7%
Other small components	Few %
Jet energy scale	1–20%
Tag rate functions	2–16%

The Run II DØ Experiment



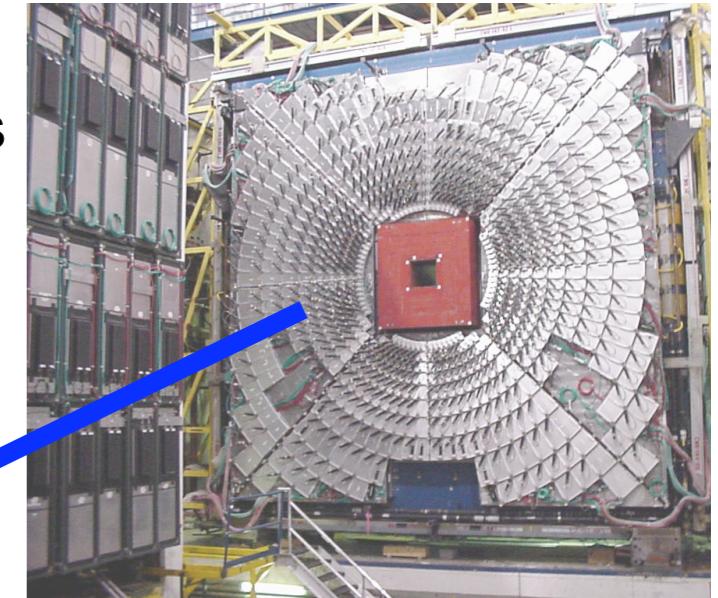
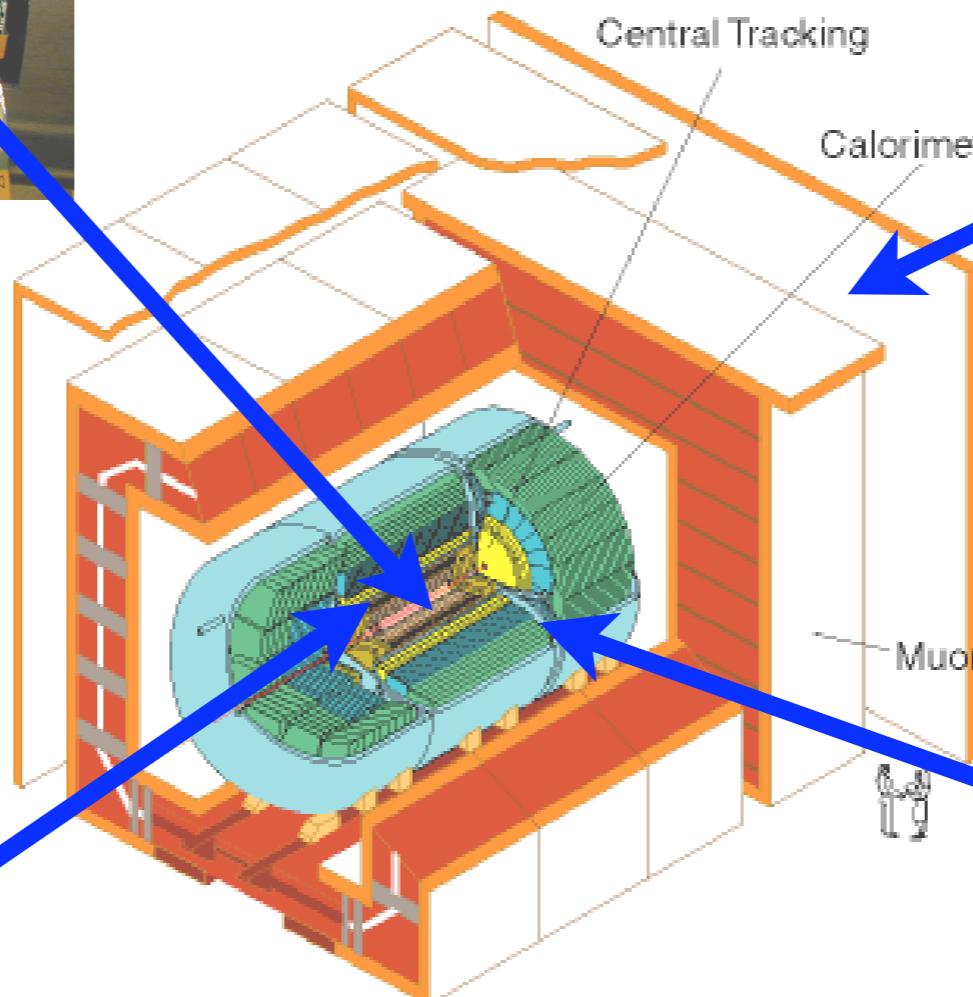
Silicon Detector
Vertex measurement
and tracking close to PV



Fiber Tracker
Charged particle tracking
momentum + charge

Muon System

Drift chambers / scintillators
Muon position and tracking



Liquid Ar/Ur Calorimeter

Energy measurement for
electrons, photons, and hadrons

