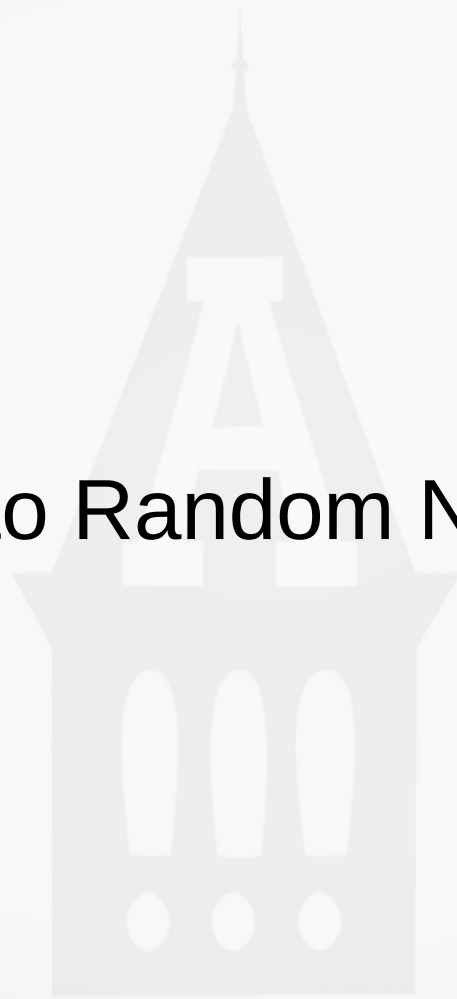


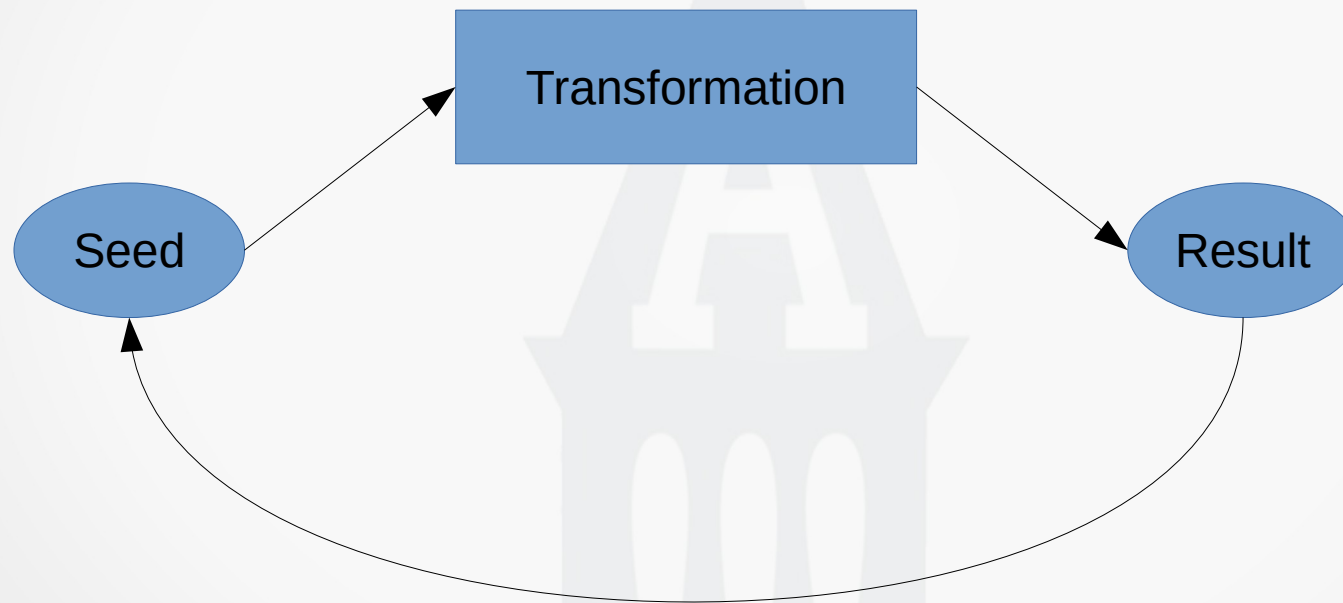
Intro to Random Numbers



Generating Random Numbers

- True Random Number: www.random.org
- Pseudo Random Number Generator (PRNG)
 - Linear Congruential Generator (LCG)
 - https://en.wikipedia.org/wiki/Linear_congruential_generator
 - Mersenne Twister (MT)
 - https://en.wikipedia.org/wiki/Mersenne_Twister
 - XorShift
 - <https://en.wikipedia.org/wiki/Xorshift>
 - PCG Family
 - <http://www.pcg-random.org/>
- Tests of Randomness
 - https://en.wikipedia.org/wiki/Randomness_tests
- Very good analysis of random number techniques & performance
 - <https://www.pcg-random.org/posts/bounded-rands.html>
 - <https://www.pcg-random.org/>

Generating Random Numbers



Simple Example - LCG

$$X_{n+1} = (aX_n + c) \bmod m$$

- X_0 is the initial “seed”
- X_n is the previous result
- X_{n+1} is the next result
- If $c = 0$
 - (or) m may be prime
 - (or) m may be power of 2
- $a - 1$ should be divisible by m 's prime factors; if m is not prime
- c and m should be coprime
 - coprime : Have no common factors other than 1
 - e.g., 21 and 22 are coprime
 - factors for 21 are : 1, 3, 7, 21
 - factors for 22 are : 1, 2, 11, 22



Example RNG Results



Random Numbers - Misc

- Multi-Threading (The Biggest Bug!)



Random Numbers - Misc

- Multi-Threading (The Biggest Bug!)
- Distributed



Random Numbers - Misc

- Multi-Threading (The Biggest Bug!)
- Distributed
- Replay Reproducibility



Random Numbers - Misc

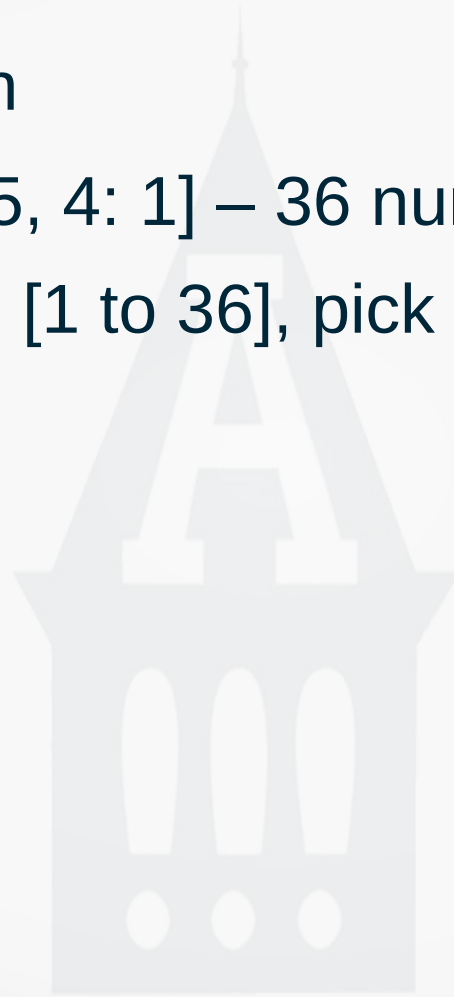
- Multi-Threading (The Biggest Bug!)
- Distributed
- Replay Reproducibility
- Other Distributions
 - Over integer range
 - Gaussian distribution
 - Circle perimeter
 - Area distribution (rectangle, triangle, circle, ...)
 - others...

Random Numbers - Misc

- Multi-Threading (The Biggest Bug!)
- Distributed
- Replay Reproducibility
- Other Distributions
 - Over integer range
 - Gaussian distribution
 - Circle perimeter
 - Area distribution (rectangle, triangle, circle, ...)
 - others...
- Pre-compute, store in memory

More Misc

- Custom Distribution
 - [1: 20, 2: 10, 3: 5, 4: 1] – 36 numbers
 - Generate rnd [1 to 36], pick accordingly



More Misc

- Custom Distribution
 - [1: 20, 2: 10, 3: 5, 4: 1] – 36 numbers
 - Generate rnd [1 to 36], pick accordingly
- Replacement
 - With – Put number back in
 - Without – Don't put number back in