Reaction-diffusion spatial modeling of COVID-19 in Chicago

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• The COVID Problem

- Project Context and Objectives
- Current Work



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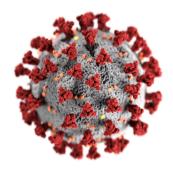
The COVID Problem



Identified in Wuhan, China in December 2019. Caused by the severe acute respiratory syndrome coronavirus 2 (SARS-CoV-2).

In the United States alone, we currently have

- **37,768,911** total cases
- **626,833** total deaths



The COVID Problem



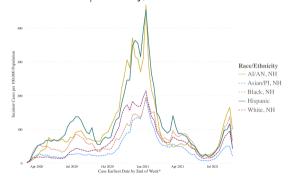
Transmission by exposure to infectious respiratory fluids:

- 1. Inhalation of virus
- 2. Deposition of virus on exposed mucus membranes
- 3. Touching mucous membranes with soiled hands contaminated with virus

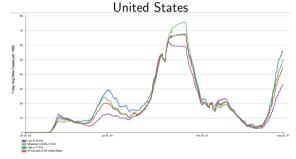
The COVID Problem



COVID-19 weekly cases per 100,000 population by race/ethnicity, United States



COVID-19 weekly case rate per 100,000 population by percentage of county population in poverty,





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Why make a mathematical study of COVID-19?

An epidemic model provides . . .

- a convenient summary of the data
- insight into the underlying processes of the disease spread
- a testing ground for assessing control procedures



Models of infectious diseases are usually variations on the **Kermack-McKendrick model** (1927).



Usual assumptions:

- Population is *homogeneous*
- Transmission is spatially independent



These assumptions don't match reality!

Level of community transmission by county



(a) 7/22/2021

(b) 7/29/2021

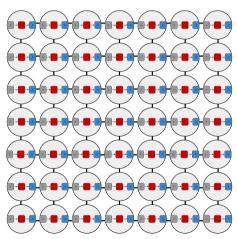






Idea: Use reaction-diffusion to build a spatially explicit model.

- The data clearly shows a diffusive pattern
- Spatial dependence can approximate demographic differences
- Spatially dependent data exists for many scales and regions





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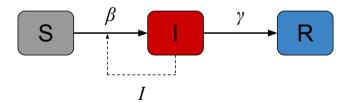
Current Work



Original motivation from Summer 2020 IPRO with Prof. Robert Ellis and Mr. David Eads (NPR). Expanded over Summer 2021 with Prof. Chun Liu and Prof. Yiwei Wang.

Start by defining the zero-dimension model:

- 1. Start with a population of susceptibles (S)
- 2. Some of the population may become infected (I) upon emergence of the virus
- 3. Infected individuals interact with susceptibles at rate eta to draw new members into I
- 4. A fraction of I recover or die at a rate γ moving to the removed (R) population



This represents processes that occur in a "well mixed" situation.

Current Work



The population model at the PDE level is an autonomous diffusion with a source:

$$S_t = \nabla(\mathfrak{D}_s \nabla S) - \beta SI,$$

$$I_t = \nabla(\mathfrak{D}_I \nabla I) + \beta SI - \gamma I,$$

$$R_t = \gamma I.$$

Assumptions:

- The R population has immunity, so we assign $\mathfrak{D}_R = 0$.
- Diffusion performs all relevant spreading.
- Arriving infected individuals form local hotspots.



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