# Project 1 BASICS ON CURVE FITTING

#### Part 1 and 2

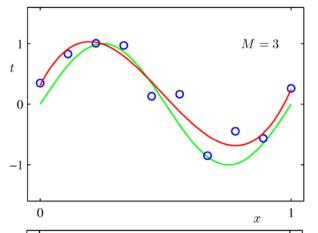
Energy Minimization

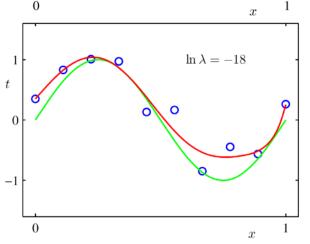
$$E(\mathbf{w}) = \frac{1}{2} \sum_{n=1}^{N} \{y(x_n, \mathbf{w}) - t_n\}^2$$

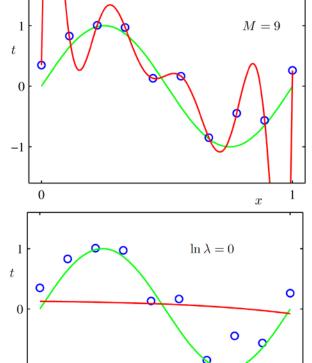
Energy Minimization with Regulation

$$\widetilde{E}(\mathbf{w}) = \frac{1}{2} \sum_{n=1}^{N} \{y(x_n, \mathbf{w}) - t_n\}^2 + \frac{\lambda}{2} ||\mathbf{w}||^2$$

Note: when  $\ln \lambda = 0$ , it is the same as without regularization



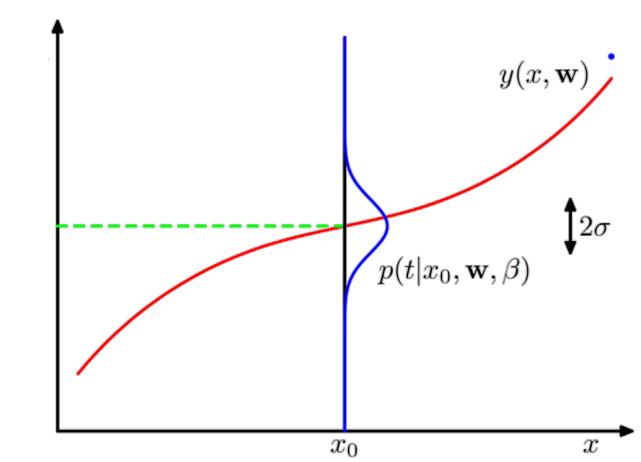




#### Part 3

- Maximum Likelihood
  - Find the beta parameter around the line by minimizing:

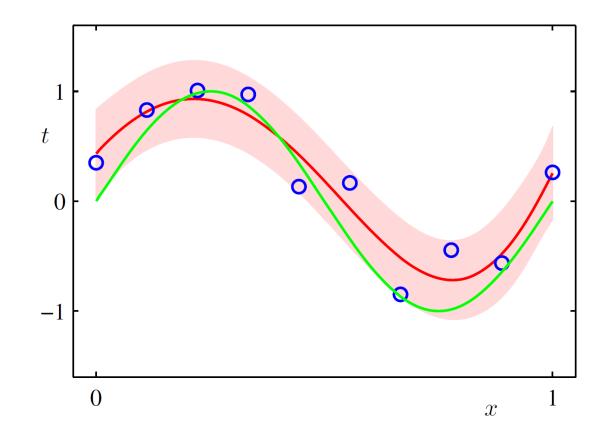
$$\ln p(\mathbf{t}|\mathbf{x}, \mathbf{w}, \beta) = -\frac{\beta}{2} \sum_{n=1}^{N} \left\{ y(x_n, \mathbf{w}) - t_n \right\}^2$$
$$+ \frac{N}{2} \ln \beta - \frac{N}{2} \ln(2\pi).$$



### Part 4

- Maximum a Posteriori
  - Regularizing weights with hyperparameter alpha

$$\frac{\beta}{2} \sum_{n=1}^{N} \{y(x_n, \mathbf{w}) - t_n\}^2 + \frac{\alpha}{2} \mathbf{w}^{\mathrm{T}} \mathbf{w}$$



## Tips

- Do not wait until the last minute
  - ▶ Things usually take longer than expected
- Do not use inbuild matlab functions for the core functions (such as polyfit)
  - ▶ When we say "write a function", you have to write it
- Use backslash Matlab operator to solve linear system of equations (much faster and better)
  - ► E.g. to solve " $\vec{y} = A\vec{x}$ " for a known " $\vec{y}$ " and "A" you can use " $\vec{x} = A \setminus \vec{y}$ "

## How to write a good report

- Mimic what you see in research papers.
  - ► Use at least one figure or table to back up each point
  - Every figure and table has a descriptive caption
  - Separate out the report into logical sections
  - Use Latex to make it look decent and Submit a PDF!!!
  - ► Show Your work on how you derive EACH equation