

Exercise 2: Calculate 2^n

1. Algorithm 1: Use the defined linear search : $2^n = 2^{n-1} * 2$

a. Pseudo-code:

```
result = 1
for i from 1 to n:
    result = result * 2
```

b. Complexity: $O(n)$

2. Algorithm 2: Use the divide and conquer:

$$2^n = (2^{n/2} * 2^{n/2}) \text{ if } (n \% 2 == 0)$$

$$2^n = (2^{n/2} * 2^{n/2} * 2) \text{ if } (n \% 2 == 1)$$

a. Pseudo-code:

```
function pow(a, b):
    if b == 0 return 1
    res = pow(a, b / 2)
    res = res * res
    if b % 2 == 1:
        res = res * a
    return res

pow(2, n)
```

b. Complexity: $O(\log n)$