Purpose

This document is meant to explain PST additions and alterations created to accommodate VTS (variable time stepping). While the current method works, it may change in the future.

Solution Control Array

Between each sw_con entry, a *time block* is created that is then solved using a user defined solution method. As such, the solver_con array has 1 less row than the sw_con array. An example solver con array is shown below.

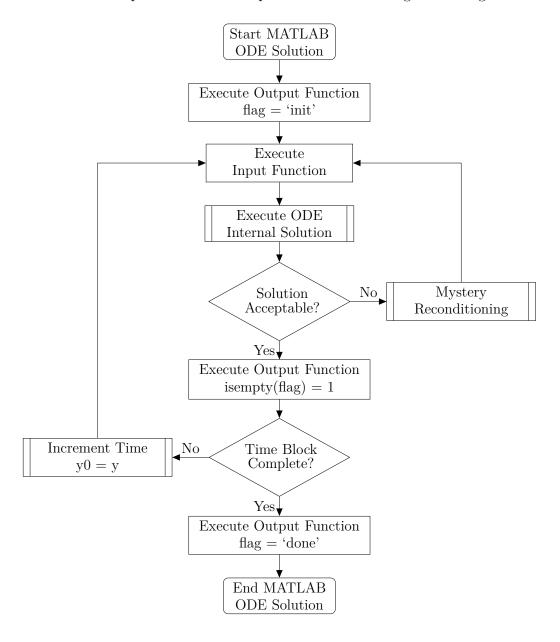
```
%% solver_con format
% A cell with a solver method in each row corresponding to the specified
% 'time blocks' defined in sw_con
%
% Valid solver names:
% huens - Fixed time step default to PST
% ode113 - works well during transients, consistent # of slns, time step stays relatively
\hookrightarrow small
\% ode15s - large number of slns during init, time step increases to reasonable size
% ode23 - realtively consisten # of required slns, timstep doesn't get very large
% ode23s - many iterations per step - not efficient...
% ode23t - occasionally hundereds of iterations, sometimes not... decent
% ode23tb - similar to 23t, sometimes more large solution counts
solver_con ={ ...
    'huens'; % pre fault - fault
    'huens'; % fault - post fault 1
    'huens'; % post fault 1 - post fault 2
    'huens'; % post fault 2 - sw_con row 5
    'huens'; % sw_con row 5 - sw_con row 6
    'ode23t'; % sw_con row 6 - sw_con row 7 (end)
    };
```

As of this writing, the pstSETO version uses the s_simu_BatchVTS script to perform variable time stepping methods. This script will likely replace the s_simu script in the main PST4 folder after versioning is complete.

Theoretically, a user would only have to add a solver_con to a data file to use variable time step methods. If one is not specified, Huen's method is used for all time blocks (i.e. default PST behavior).

MATLAB ODE solver

The variable time step implementation in PST revolves around using the built in MATLAB ODE solvers. All these methods perform actions depicted in the following block diagram.



The input to an ODE solver include, an input function, a time interval (time block), initial conditions, and solver options. The current options used for VTS are shown below and deal with error tolerance levels, initial step size, max step size, and an Output function.

```
% Configure ODE settings
%options = odeset('RelTol',1e-3,'AbsTol',1e-6); % default settings
options = odeset('RelTol',1e-3,'AbsTol',1e-6, ...
    'InitialStep', 1/60/4, ...
    'MaxStep',60, ...
    'OutputFcn',outputFcn); % set 'OutputFcn' to function handle
```

vtsInputFcn

The slightly abbreviated input function is shown below.

```
function [dxVec] = vtsInputFcn(t, y)
% VTSINPUTFCN passed to ODE solver to perfrom required step operations
%
  NOTES: Updates g.vts.dxVec, and returns values
%
%
  Input:
%
  t - simulation time
%
  y - solution vector (initial conditions)
%
%
  Output:
   dxVec - requried derivative vector for ODE solver
global g
%% call handleStDx with flag==2 to update global states with newest passed in soln.
\% i.e. update states at g.vts.dataN with newest solution
handleStDx(g.vts.dataN, y, 2)
initStep(g.vts.dataN)
networkSolutionVTS(g.vts.dataN, t)
dynamicSolution(g.vts.dataN )
dcSolution(g.vts.dataN )
%% call handleStDx with flag==1 to update global dxVec
handleStDx(g.vts.dataN , [], 1) % update g.vts.dxVec (solution vector not needed)
dxVec = g.vts.dxVec; % return for ODE fcn requirements
if g.vts.iter == 0
   % save initial network solution
  handleNetworkSln(g.vts.dataN ,1)
end
g.vts.iter = g.vts.iter + 1; % increment iteration number
end % end vtsInputFcn
```

vtsOutputFcn

The slightly abbreviated output function is shown below.

```
function status = vtsOutputFcn(t,y,flag)
% VTSOUTPUTFCN performs associated flag actions with ODE solvers.
%
  Input:
%
  t - simulation time
%
   y - solution vector
%
   flag - dictate function action
%
%
   Output:
   status - required for normal operation (return 1 to stop)
global g
status = 0; % required for normal operation
if isempty(flag) % normal step completion
   % restore network to initial solution
   handleNetworkSln(g.vts.dataN ,2) % may cause issues with DC.
   monitorSolution(g.vts.dataN); % Perform Line Monitoring and Area Calculations
   %% Live plot call
   if g.sys.livePlotFlag
       livePlot(g.vts.dataN)
   end
   % after each successful integration step by ODE solver:
   % log step time
   g.sys.t(g.vts.dataN) = t;
   g.vts.stVec = y;
                              % update state vector
   handleStDx(g.vts.dataN, y, 2) % place new solution results into associated globals
   g.vts.slns(g.vts.dataN) = g.vts.iter;
                                            % log solution step iterations
                                            % reset iteration counter
   g.vts.iter = 0;
elseif flag(1) == 'i'
   % init solver for new time block
   handleStDx(g.vts.dataN, y, 2) % log initial conditions
elseif flag(1) == 'd'
   % only debug screen output at the moment
end % end if
end % end function
```

Simulation Loop The complete simulation loop code is shown below. This code was copied from s simu BatchVTS with corresponding line numbers.

```
%% Simulation loop start
362
     warning('*** Simulation Loop Start')
363
     for simTblock = 1:size(g.vts.t_block)
364
365
         g.vts.t_blockN = simTblock;
366
         g.k.ks = simTblock; % required for huen's solution method.
367
368
         if ~isempty(g.vts.solver_con)
369
              odeName = g.vts.solver_con{g.vts.t_blockN};
370
         else
371
              odeName = 'huens'; % default PST solver
372
373
         end
374
         if strcmp( odeName, 'huens')
375
              % use standard PST huens method
376
              fprintf('*** Using Huen''s integration method for time block %d\n*** t=[%7.4f,
377
              \rightarrow %7.4f]\n', ...
                  g.vts.t_blockN, ...
378
                  g.vts.fts{g.vts.t_blockN}(1), g.vts.fts{g.vts.t_blockN}(end))
379
380
              % add fixed time vector to system time vector
381
              nSteps = length(g.vts.fts{g.vts.t_blockN});
382
              g.sys.t(g.vts.dataN:g.vts.dataN+nSteps-1) = g.vts.fts{g.vts.t_blockN};
383
              % account for pretictor last step time check
385
386
              g.sys.t(g.vts.dataN+nSteps) = g.sys.t(g.vts.dataN+nSteps-1)+
                  g.sys.sw_con(g.vts.t_blockN,7);
387
              for fStep = 1:nSteps
388
                  k = g.vts.dataN;
389
                  j = k+1;
390
391
                  % display k and t at every first, last, and 50th step
392
                  if (mod(k,50)==0) \mid | fStep == 1 \mid | fStep == nSteps
393
                      fprintf('*** k = \%5d, \tt(k) = \%7.4f\n',k,g.sys.t(k)) \% DEBUG
394
                  end
395
396
                  %% Time step start
397
                  initStep(k)
398
399
                  %% Predictor Solution =========
400
                  networkSolutionVTS(k, g.sys.t(g.vts.dataN))
401
                  monitorSolution(k);
402
                  dynamicSolution(k)
403
                  dcSolution(k)
404
```

```
predictorIntegration(k, j, g.k.h_sol)
405
406
                 407
                 networkSolutionVTS(j, g.sys.t(g.vts.dataN+1))
408
                 dynamicSolution(j)
409
                 dcSolution(j)
410
                 correctorIntegration(k, j, g.k.h_sol)
411
412
                 \% most recent network solution based on completely calculated states is k
413
                 monitorSolution(k);
414
                 %% Live plot call
415
                 if g.sys.livePlotFlag
416
                     livePlot(k)
417
                 end
418
419
                 % index handling
420
                 g.vts.dataN = g.vts.dataN + 1;
421
                 g.vts.tot_iter = g.vts.tot_iter + 2;
422
                 g.vts.slns(g.vts.dataN) = 2;
423
             end
424
             handleStDx(j, [], 3) % update g.vts.stVec to initial conditions of states
425
             handleStDx(k, [], 1) % update q.vts.dxVec to initial conditions of derivatives
426
             handleNetworkSln(k, 1) % update saved network solution
427
428
         else % use given variable method
429
             fprintf('*** Using %s integration method for time block %d\n*** t=[%7.4f, %7.4f]\n',
430
                 odeName, g.vts.t_blockN, ...
431
                 g.vts.t_block(g.vts.t_blockN, 1), g.vts.t_block(g.vts.t_blockN, 2))
432
             feval(odeName, inputFcn, g.vts.t_block(simTblock,:), g.vts.stVec , options);
433
434
             % Alternative example of using actual function name:
435
             % (13(inputFcn, q.vts.t_block(q.vts.t_blockN,:), q.vts.stVec, options);
436
             % feval used for now, could be replaced with if statements.
437
         end
438
439
     end% end simulation loop
440
```

Place holders for function explanations / real basic explanations of some VTS functions.

initTblocks

Analyzes sw_con and solver_con to create appropriate time blocks that are used in simulation.

handleStDx

Function to handle the collecting, indexing, and updating ALL states and derivatives. It uses dynamic field names and seems like a pretty slick solution to a very annoying problem.

handleNetworkSln

Saves the initial network solution and ensures it is restored after a variable step solution where many network solutions may overwrite the first (and correct) solution.

networkSolutionVTS

A function that solves the system network at the passed in data index. Essentially the same as the networkSolution function, except instead of relying on index number to switch Y-matricies, the switching is done based on passed in simulation time.