

# Assignment 15

- ▼ C-13.2 Show that every language  $L$  in  $P$  is polynomial-time reducible to the language  $M=\{5\}$ , that is, the language that simply asks if the binary encoding of the input is equal to 5.

```
Algorithm f(x):  
  if A(x):  
    return "101"  
  else:  
    return "0"
```

- ▼ A. Show that the MST decision problem is polynomial-time reducible to the Subset Sum problem.

```
Algorithm MST2SS(G, max)  
  S ← new Sequence  
  S.insertLast(1)  
  if verifyMST(G, max) = YES then  
    return (S,1)  
  else  
    return (S,2)
```

```
Algorithm verifyMST(G, max)  
  edges ← MST(G)  
  sum ← 0  
  for each e in edges do  
    sum ← sum + weight(e)  
  
  if sum <= max then  
    return YES  
  else  
    return NO
```

- ▼ B. Show the shortest path decision problem is polynomial-time reducible to the MST decision problem. Hint: convert the shortest path problem to a decision problem, then reduce to MST problem.

```
Algorithm SP2MST(G, u, v, max)  
  G1 ← new Graph  
  u ← G1.insertVertex(u)  
  v ← G1.insertVertex(v)  
  G1.insertEdge(u, v, 3)  
  if verifySP(G, u, v, max) = YES then  
    return (G1, 3)  
  else  
    return (G1, 2)
```

Algorithm verifySP( $G, u, v, \text{max}$ )

$\text{cur} \leftarrow v$

  while  $\text{cur} \neq u$  do

$e \leftarrow \text{getParent}(\text{cur})$

$\text{sum} \leftarrow \text{weight}(e)$

$\text{cur} \leftarrow G.\text{opposite}(e, \text{cur})$

  if  $\text{sum} \leq \text{max}$  then

    return YES

  else

    return NO