

Chương 6

1. Hand simulate the Viterbi algorithm using the data and probability estimates in Figures 7.4- 7.6 on the sentence *Flower flowers like flowers*. Draw transition network as in Figure 7.10-7.12 for the problem, and identify what part of speech the algorithm identifies for each word.

Giải

Flower flowers like flowers

L = V, N, ART, P

category	Count at i	pair	Count at i,i+1	bigram	estimate
O	300	O, ART	213	PROB(ART/O)	0.71
O	300	O, N	87	PROB(N/O)	0.29
ART	558	ART, N	558	PROB(N/ART)	1.0
N	833	N, V	258	PROB(V/N)	0.43
N	833	N, N	108	PROB(N/N)	0.13
N	833	N, P	366	PROB(P/N)	0.44
V	300	V, N	75	PROB(N/V)	0.35
V	300	V, ART	194	PROB(ART/V)	0.65
P	307	P, ART	226	PROB(ART/P)	0.74
P	307	P, N	81	PROB(N/P)	0.26

$PROB(the ART)$.54	$PROB(a ART)$.360
$PROB(flies N)$.025	$PROB(a N)$.001
$PROB(flies V)$.076	$PROB(flower N)$.063
$PROB(like V)$.1	$PROB(flower V)$.05
$PROB(like P)$.068	$PROB(birds N)$.076
$PROB(like N)$.012		

Figure 7.6 The lexical-generation probabilities

i=1 to N	SEQ(1,1) = PROB(Flower/V) * PROB (V/O) SEQ(2,1) = PROB(Flower/N) * PROB (N/O) SEQ(3,1) = PROB(Flower/ART) * PROB (ART/O) SEQ(4,1) = PROB(Flower/P) * PROB (P/O)	$= 0.05 * 10^{-4} = 5 * 10^{-6}$ $= \mathbf{0.063 * 0.29 = 0.01827}$ $= 0$ $= 0$
t=2 to 4 i=1 to 4	SEQ(1,2) = max _{j=1,4} (SEQ(1,1) * PROB(V/V), SEQ (2,1) * PROB(V/N)) * PROB(flowers/V) SEQ(2,2) = max _{j=1,4} (SEQ(1,1) * PROB(N/V), SEQ (2,1) * PROB(N/N)) * PROB(flowers/N) SEQ(3,2) = max _{j=1,4} (SEQ(1,1) * PROB(ART/V), SEQ (2,1) * PROB(ART/N)) * PROB(flowers/ART) SEQ(4,2) = max _{j=1,4} (SEQ(1,1) * PROB(P/V), SEQ (2,1) * PROB(P/N)) * PROB(flowers/P)	$= \max(5 * 10^{-6} * 10^{-4}, 0.01827 * 0.43) * 0.05 =$ $\mathbf{0.000392805}$ $= \max(5 * 10^{-6} * 0.35, 0.01827 * 0.13) * 0.063 =$ 0.0001496313 $= 0$ $= 0$
t=3 to 4 i=1 to 4	SEQ(1,3) = max _{j=1,4} (SEQ(1,2) * PROB(V/V), SEQ (2,2) * PROB(V/N)) * PROB(like/V) SEQ(2,3) = max _{j=1,4} (SEQ(1,2) * PROB(N/V), SEQ (2,2) * PROB(N/N)) * PROB(like/N) SEQ(3,3) = max _{j=1,4} (SEQ(1,2) * PROB(ART/V), SEQ (2,2) * PROB(ART/N)) * PROB(like/ART) SEQ(4,3) = max _{j=1,4} (SEQ(1,2) * PROB(P/V), SEQ (2,2) * PROB(P/N)) * PROB(like/P)	$= \max(0.000392805 * 10^{-4}, 0.0001496313 * 0.43)$ $* 0.1 = \mathbf{0.0000064341459 = 6.43 * 10^{-6}}$ $= \max(0.000392805 * 0.35, 0.0001496313 * 0.13) *$ $0.012 = 0.000001649781 = 1.65 * 10^{-6}$ $= 0$ $= \max(0.000392805 * 10^{-4}, 0.0001496313 * 0.44)$ $* 0.068 = 0.000004476968496 = 4.48 * 10^{-6}$
t=4 i=1 to 4	SEQ(1,4) = max _{j=1,4} (SEQ(1,3) * PROB(V/V), SEQ(2,3) * PROB(V/N), SEQ (4,3) * PROB(V/P)) * PROB(flowers/V) SEQ(2,4) = max _{j=1,4} (SEQ(1,3) * PROB(N/V), SEQ(2,3) * PROB(N/N), SEQ (4,3) * PROB(N/P)) * PROB(flowers/N) SEQ(3,4) = max _{j=1,4} (SEQ(1,3) * PROB(ART/V), SEQ(2,3) * PROB(ART/N),	$= \max(6.43 * 10^{-6} * 10^{-4}, 1.65 * 10^{-6} * 0.43,$ $4.48 * 10^{-6} * 10^{-4}) * 0.05 = 3.5475 * 10^{-8}$ $= \max(6.43 * 10^{-6} * 0.35, 1.65 * 10^{-6} * 0.13, 4.48$ $* 10^{-6} * 0.26) * 0.063 = \mathbf{1.417815 * 10^{-7}}$ $= 0$

	$\text{SEQ}(4,3) * \text{PROB}(\text{ART}/P) * \text{PROB}(\text{flowers}/\text{ART})$ $\text{SEQ}(4,4) = \max_{j=1,4} (\text{SEQ}(1,3) * \text{PROB}(P/V), \text{SEQ}(2,3) * \text{PROB}(P/N), \text{SEQ}(4,3) * \text{PROB}(P/P) * \text{PROB}(\text{flowers}/P))$	= 0
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Xác định chuỗi từ loại:

C(4) = 2, C(3) = 1, C(2) = 1, C(1) = 2

Vậy chuỗi từ loại là **N V V N**

2. Using the bigram and lexical generation probabilities given in this chapter, calculate the word probabilities using the forward algorithm for the sentence *The a flies like flower* (involving a very rare use of the word a as a noun, as in the a flies, the b flies, and so on). Remember to use 0.0001 as a probability for any bigram not in the table. Are the results you get reasonable? If not, what is the problem and how might it be fixed ?

Giải

The a flies like flower

L = ART, N, V, P

	N	V	ART	P	TOTAL
flies	21	23	0	0	44
fruit	49	5	1	0	55
lik	10	30	0	21	61
a	1	0	201	0	202
the	1	0	300	2	303
flower	53	15	0	0	68
flowers	42	16	0	0	58
birds	64	1	0	0	65
others	592	210	56	284	1142
TOTAL	833	300	558	307	1998

t=1

$$\text{SEQSUM}(1,1) = \text{PROB}(\text{The}/\text{ART}) * \text{PROB}(\text{ART}/\text{O}) = 0.54 * 0.71 = 0.3834$$

$$\text{SEQSUM}(2,1) = \text{PROB}(\text{The}/\text{N}) * \text{PROB}(\text{N}/\text{O}) = 1/833 * 0.29 = 3.4814 * 10^{-4}$$

$$\text{SEQSUM}(3,1) = \text{PROB}(\text{The}/\text{V}) * \text{PROB}(\text{V}/\text{O}) = 0 * 10^{-4} = 0$$

$$\text{SEQSUM}(4,1) = \text{PROB}(\text{The}/\text{P}) * \text{PROB}(\text{P}/\text{O}) = 2/307 * 10^{-4} = 6.5147 * 10^{-7}$$

t=2

$$\text{SEQSUM}(1,2) =$$

$$(\text{PROB}(\text{ART}/\text{ART}) * \text{SEQSUM}(1,1) + \text{PROB}(\text{ART}/\text{N}) * \text{SEQSUM}(2,1) + \text{PROB}(\text{ART}/\text{V}) * \text{SEQSUM}(3,1) + \text{PROB}(\text{ART}/\text{P}) * \text{SEQSUM}(4,1))$$

$$* \text{PROB}(a/\text{ART})$$

$$= (10^{-4} * 0.3834 + 10^{-4} * 3.4814 * 10^{-4} + 0 + 0.74 * 6.5147 * 10^{-7}) * 0.36$$

$$= 1.3988 * 10^{-5}$$

$$\text{SEQSUM}(2,2) =$$

$$(\text{PROB}(N/\text{ART}) * \text{SEQSUM}(1,1) + \text{PROB}(N/N) * \text{SEQSUM}(2,1) +$$

$$\text{PROB}(N/V) * \text{SEQSUM}(3,1) + \text{PROB}(N/P) * \text{SEQSUM}(4,1)) * \text{PROB}(a/N) =$$

$$= (1 * 0.3834 + 0.13 * 3.4814 * 10^{-4} + 0 + 0.26 * 6.5147 * 10^{-7}) * 0.001$$

$$= 3.8346 * 10^{-4}$$

$$\text{SEQSUM}(3,2) =$$

$$(\text{PROB}(V/\text{ART}) * \text{SEQSUM}(1,1) + \text{PROB}(V/N) * \text{SEQSUM}(2,1) +$$

$$\text{PROB}(V/V) * \text{SEQSUM}(3,1) + \text{PROB}(V/P) * \text{SEQSUM}(4,1)) * \text{PROB}(a/V) = 0$$

$$\text{SEQSUM}(4,2) =$$

$$(\text{PROB}(P/\text{ART}) * \text{SEQSUM}(1,1) + \text{PROB}(P/N) * \text{SEQSUM}(2,1) +$$

$$\text{PROB}(P/V) * \text{SEQSUM}(3,1) + \text{PROB}(P/P) * \text{SEQSUM}(4,1)) * \text{PROB}(a/P) = 0$$

$$t=3$$

$$\text{SEQSUM}(1,3) =$$

$$(\text{PROB}(\text{ART}/\text{ART}) * \text{SEQSUM}(1,2) + \text{PROB}(\text{ART}/N) * \text{SEQSUM}(2,2) +$$

$$\text{PROB}(\text{ART}/V) * \text{SEQSUM}(3,2) + \text{PROB}(\text{ART}/P) * \text{SEQSUM}(4,2))$$

$$* \text{PROB}(\text{flies}/\text{ART}) = 0$$

$$\text{SEQSUM}(2,3) =$$

$$(\text{PROB}(N/\text{ART}) * \text{SEQSUM}(1,2) + \text{PROB}(N/N) * \text{SEQSUM}(2,2) +$$

$$\text{PROB}(N/V) * \text{SEQSUM}(3,2) + \text{PROB}(N/P) * \text{SEQSUM}(4,2)) * \text{PROB}(\text{flies}/N)$$

$$= (1 * 1.3988 * 10^{-5} + 0.13 * 3.8346 * 10^{-4} + 0 + 0) * 0.025 = 1.5959 * 10^{-6}$$

$$\text{SEQSUM}(3,3) =$$

$$(\text{PROB}(V/\text{ART}) * \text{SEQSUM}(1,2) + \text{PROB}(V/N) * \text{SEQSUM}(2,2) +$$

$$\text{PROB}(V/V) * \text{SEQSUM}(3,2) + \text{PROB}(V/P) * \text{SEQSUM}(4,2)) * \text{PROB}(\text{flies}/V) \\ = (10^{-4} * 1.3988 * 10^{-5} + 0.43 * 3.8346 * 10^{-4} + 0 + 0) * 0.076 = 1.2532 * 10^{-5}$$

$$\text{SEQSUM}(4,3) =$$

$$(\text{PROB}(P/\text{ART}) * \text{SEQSUM}(1,2) + \text{PROB}(P/N) * \text{SEQSUM}(2,2) + \\ \text{PROB}(P/V) * \text{SEQSUM}(3,2) + \text{PROB}(P/P) * \text{SEQSUM}(4,2)) * \text{PROB}(\text{flies}/P) = 0$$

$$t=4$$

$$\text{SEQSUM}(1,4) =$$

$$(\text{PROB}(\text{ART}/\text{ART}) * \text{SEQSUM}(1,3) + \text{PROB}(\text{ART}/N) * \text{SEQSUM}(2,3) + \\ \text{PROB}(\text{ART}/V) * \text{SEQSUM}(3,3) + \text{PROB}(\text{ART}/P) * \text{SEQSUM}(4,3)) \\ * \text{PROB}(\text{like}/\text{ART}) = 0$$

$$\text{SEQSUM}(2,4) =$$

$$(\text{PROB}(N/\text{ART}) * \text{SEQSUM}(1,3) + \text{PROB}(N/N) * \text{SEQSUM}(2,3) + \\ \text{PROB}(N/V) * \text{SEQSUM}(3,3) + \text{PROB}(N/P) * \text{SEQSUM}(4,3)) * \text{PROB}(\text{like}/N) \\ = (0 + 0.13 * 1.5959 * 10^{-6} + 0.35 * 1.2532 * 10^{-5} + 0) * 0.012 \\ = 5.5124 * 10^{-8}$$

$$\text{SEQSUM}(3,4) =$$

$$(\text{PROB}(V/\text{ART}) * \text{SEQSUM}(1,3) + \text{PROB}(V/N) * \text{SEQSUM}(2,3) + \\ \text{PROB}(V/V) * \text{SEQSUM}(3,3) + \text{PROB}(V/P) * \text{SEQSUM}(4,3)) * \text{PROB}(\text{like}/V) \\ = (0 + 0.43 * 1.5959 * 10^{-6} + 10^{-4} * 1.2532 * 10^{-5} + 0) * 0.1 \\ = 6.8749 * 10^{-8}$$

$$\text{SEQSUM}(4,4) =$$

$$(\text{PROB}(P/\text{ART}) * \text{SEQSUM}(1,3) + \text{PROB}(P/N) * \text{SEQSUM}(2,3) + \\ \text{PROB}(P/V) * \text{SEQSUM}(3,3) + \text{PROB}(P/P) * \text{SEQSUM}(4,3)) * \text{PROB}(\text{like}/P) \\ = (0 + 0.44 * 1.5959 * 10^{-6} + 10^{-4} * 1.2532 * 10^{-5} + 0) * 0.068 \\ = 4.7835 * 10^{-8}$$

t=5

SEQSUM(1,5) =

$$\begin{aligned} & (\text{PROB}(\text{ART}/\text{ART}) * \text{SEQSUM}(1,4) + \text{PROB}(\text{ART}/\text{N}) * \text{SEQSUM}(2,4) + \\ & \text{PROB}(\text{ART}/\text{V}) * \text{SEQSUM}(3,4) + \text{PROB}(\text{ART}/\text{P}) * \text{SEQSUM}(4,4)) \\ & * \text{PROB}(\text{flower}/\text{ART}) = 0 \end{aligned}$$

SEQSUM(2,5) =

$$\begin{aligned} & (\text{PROB}(\text{N}/\text{ART}) * \text{SEQSUM}(1,4) + \text{PROB}(\text{N}/\text{N}) * \text{SEQSUM}(2,4) + \\ & \text{PROB}(\text{N}/\text{V}) * \text{SEQSUM}(3,4) + \text{PROB}(\text{N}/\text{P}) * \text{SEQSUM}(4,4)) * \text{PROB}(\text{flower}/\text{N}) \\ & = (0 + 0.13 * 5.5124 * 10^{-8} + 0.35 * 6.8749 * 10^{-8} + 0.26 * 4.7835 * 10^{-8}) * 0.063 \\ & = 2.7509 * 10^{-9} \end{aligned}$$

SEQSUM(3,5) =

$$\begin{aligned} & (\text{PROB}(\text{V}/\text{ART}) * \text{SEQSUM}(1,4) + \text{PROB}(\text{V}/\text{N}) * \text{SEQSUM}(2,4) + \\ & \text{PROB}(\text{V}/\text{V}) * \text{SEQSUM}(3,4) + \text{PROB}(\text{V}/\text{P}) * \text{SEQSUM}(4,4)) * \text{PROB}(\text{flower}/\text{V}) \\ & = (0 + 0.43 * 5.5124 * 10^{-8} + 10^{-4} * 6.8749 * 10^{-8} + 10^{-4} * 4.7835 * 10^{-8}) * 0.05 \\ & = 1.1857 * 10^{-9} \end{aligned}$$

SEQSUM(4,5) =

$$\begin{aligned} & (\text{PROB}(\text{P}/\text{ART}) * \text{SEQSUM}(1,4) + \text{PROB}(\text{P}/\text{N}) * \text{SEQSUM}(2,4) + \\ & \text{PROB}(\text{P}/\text{V}) * \text{SEQSUM}(3,4) + \text{PROB}(\text{P}/\text{P}) * \text{SEQSUM}(4,4)) * \text{PROB}(\text{flower}/\text{P}) = 0 \end{aligned}$$

Tính xác suất từ vựng

$$1. \text{SEQSUM}(1,1) + \text{SEQSUM}(2,1) + \text{SEQSUM}(3,1) + \text{SEQSUM}(4,1) = 0.3837$$

$$\text{PROB}(\text{the}|\text{ART}|\text{the}) = \text{SEQSUM}(1,1) / 0.3837 = 0.9992$$

$$\text{PROB}(\text{the}|\text{N}|\text{the}) = \text{SEQSUM}(2,1) / 0.3837 = 0.00091$$

$$\text{PROB}(\text{the}|\text{V}|\text{the}) = \text{SEQSUM}(3,1) / 0.3837 = 0$$

$$\text{PROB}(\text{the}|\text{P}|\text{the}) = \text{SEQSUM}(4,1) / 0.3837 = 0.0000017$$

$$2. \text{SEQSUM}(1,2) + \text{SEQSUM}(2,2) + \text{SEQSUM}(3,2) + \text{SEQSUM}(4,2) = 3.9745 * 10^{-4}$$

$$\text{PROB}(a|\text{ART}|\text{the } a) = \text{SEQSUM}(1,2) / (3.9745 * 10^{-4}) = 0.0352$$

$$\text{PROB}(a|\text{N}|\text{the } a) = \text{SEQSUM}(2,2) / (3.9745 * 10^{-4}) = \mathbf{0.9648}$$

$$\text{PROB}(a|\text{V}|\text{the } a) = \text{SEQSUM}(3,2) / (3.9745 * 10^{-4}) = 0$$

$$\text{PROB}(a|\text{P}|\text{the } a) = \text{SEQSUM}(4,2) / (3.9745 * 10^{-4}) = 0$$

$$3. \text{SEQSUM}(1,3) + \text{SEQSUM}(2,3) + \text{SEQSUM}(3,3) + \text{SEQSUM}(4,3) = 1.4128 * 10^{-5}$$

$$\text{PROB}(\text{flies}|\text{ART}|\text{the } a \text{ flies}) = \text{SEQSUM}(1,3) / (1.4128 * 10^{-5}) = 0$$

$$\text{PROB}(\text{flies}|\text{N}|\text{the } a \text{ flies}) = \text{SEQSUM}(2,3) / (1.4128 * 10^{-5}) = 0.1130$$

$$\text{PROB}(\text{flies}|\text{V}|\text{the } a \text{ flies}) = \text{SEQSUM}(3,3) / (1.4128 * 10^{-5}) = \mathbf{0.8870}$$

$$\text{PROB}(\text{flies}|\text{P}|\text{the } a \text{ flies}) = \text{SEQSUM}(4,3) / (1.4128 * 10^{-5}) = 0$$

$$4. \text{SEQSUM}(1,4) + \text{SEQSUM}(2,4) + \text{SEQSUM}(3,4) + \text{SEQSUM}(4,4) = 1.7171 * 10^{-7}$$

$$\text{PROB}(\text{like}|\text{ART}|\text{the } a \text{ flies like}) = \text{SEQSUM}(1,4) / (1.7171 * 10^{-7}) = 0$$

$$\text{PROB}(\text{like}|\text{N}|\text{the } a \text{ flies like}) = \text{SEQSUM}(2,4) / (1.7171 * 10^{-7}) = 0.3210$$

$$\text{PROB}(\text{like}|\text{V}|\text{the } a \text{ flies like}) = \text{SEQSUM}(3,4) / (1.7171 * 10^{-7}) = \mathbf{0.4004}$$

$$\text{PROB}(\text{like}|\text{P}|\text{the } a \text{ flies like}) = \text{SEQSUM}(4,4) / (1.7171 * 10^{-7}) = 0.2786$$

$$5. \text{SEQSUM}(1,5) + \text{SEQSUM}(2,5) + \text{SEQSUM}(3,5) + \text{SEQSUM}(4,5) = 3.9366 * 10^{-9}$$

$$\text{PROB}(\text{flowers}|\text{ART}|\text{the } a \text{ flies like flowers}) = \text{SEQSUM}(1,5) / (3.9366 * 10^{-9}) = 0$$

$$\text{PROB}(\text{flowers}|\text{N}|\text{the } a \text{ flies like flowers}) = \text{SEQSUM}(2,5) / (3.9366 * 10^{-9}) = \mathbf{0.6988}$$

$$\text{PROB}(\text{flowers}|\text{V}|\text{the } a \text{ flies like flowers}) = \text{SEQSUM}(3,5) / (3.9366 * 10^{-9}) = 0.3012$$

$$\text{PROB}(\text{flowers}|\text{P}|\text{the } a \text{ flies like flowers}) = \text{SEQSUM}(4,5) / (3.9366 * 10^{-9}) = 0$$

Như vậy **the a flies like flowers** là **ART N V V N**.

Kết quả trên không hợp lý, khi từ loại của flies như ta mong muốn là N, như kết quả phân tích lại thu được flies có từ loại là V.

Lý do có thể vì kích thước tập mẫu dữ liệu đầu vào chưa đủ lớn.

Cách giải quyết dễ thấy nhất là tăng kích thước tập mẫu lên.

3. 3. Consider an extended version of Grammar 7.17 with the additional rule:

$$10. VP \rightarrow V PP$$

The revised rule probabilities are shown here (Any not mentioned are the same as in Grammar 7.17):

$$VP \rightarrow V \quad 0.32 \quad VP \rightarrow V NP PP \quad 0.20$$

$$VP \rightarrow V NP \quad 0.33 \quad VP \rightarrow V PP \quad 0.15$$

In addition, the following bigram probabilities differ from those in Figure 7.4:

$$PROB(N/V) = 0.53 \quad PROB(ART/V) = 0.32 \quad PROB(P/V) = 0.15$$

a) Hand simulate (or implement) the forward algorithm on *Fruit flies like birds* to produce the lexical probabilities.

b) Draw out the full chart for *Fruit flies like birds*, showing the probabilities of each constituent.

Giải

a) L = ART, N, V, P

	N	V	ART	P	TOTAL
<u>flies</u>	21	23	0	0	44
<u>fruit</u>	49	5	1	0	55
<u>lik</u>	10	30	0	21	61
<u>a</u>	1	0	201	0	202
<u>the</u>	1	0	300	2	303
<u>flower</u>	53	15	0	0	68
<u>flowers</u>	42	16	0	0	58
<u>birds</u>	64	1	0	0	65
<u>others</u>	592	210	56	284	1142
TOTAL	833	300	558	307	1998

t=1

$$SEQSUM(1,1) = PROB(fruit/ART) * PROB(ART/O) = 1/558 * 0.71 = 1.2724 * 10^{-3}$$

$$SEQSUM(2,1) = PROB(fruit/N) * PROB(N/O) = 49/833 * 0.29 = 0.0171$$

$$SEQSUM(3,1) = PROB(fruit/V) * PROB(V/O) = 5/300 * 10^{-4} = 1.6667 * 10^{-6}$$

$$SEQSUM(4,1) = PROB(fruit/P) * PROB(P/O) = 0$$

t=2

SEQSUM(1,2) =

$$\begin{aligned} & (\text{PROB}(\text{ART}/\text{ART}) * \text{SEQSUM}(1,1) + \text{PROB}(\text{ART}/\text{N}) * \text{SEQSUM}(2,1) + \\ & \text{PROB}(\text{ART}/\text{V}) * \text{SEQSUM}(3,1) + \text{PROB}(\text{ART}/\text{P}) * \text{SEQSUM}(4,1)) \\ & * \text{PROB}(\text{flies}/\text{ART}) \end{aligned}$$

$$= 0$$

SEQSUM(2,2) =

$$\begin{aligned} & (\text{PROB}(\text{N}/\text{ART}) * \text{SEQSUM}(1,1) + \text{PROB}(\text{N}/\text{N}) * \text{SEQSUM}(2,1) + \\ & \text{PROB}(\text{N}/\text{V}) * \text{SEQSUM}(3,1) + \text{PROB}(\text{N}/\text{P}) * \text{SEQSUM}(4,1)) \\ & * \text{PROB}(\text{flies}/\text{N}) \end{aligned}$$

$$= (1 * 1.2724 * 10^{-3} + 0.13 * 0.0171 + 0.53 * 1.6667 * 10^{-6} + 0) * 0.025$$

$$= 8.7407 * 10^{-5}$$

SEQSUM(3,2) =

$$\begin{aligned} & (\text{PROB}(\text{V}/\text{ART}) * \text{SEQSUM}(1,1) + \text{PROB}(\text{V}/\text{N}) * \text{SEQSUM}(2,1) + \\ & \text{PROB}(\text{V}/\text{V}) * \text{SEQSUM}(3,1) + \text{PROB}(\text{V}/\text{P}) * \text{SEQSUM}(4,1)) * \text{PROB}(\text{flies}/\text{V}) \end{aligned}$$

$$= (10^{-4} * 1.2724 * 10^{-3} + 0.43 * 0.0171 + 10^{-4} * 1.6667 * 10^{-6} + 0) * 0.076$$

$$= 5.5884 * 10^{-4}$$

SEQSUM(4,2) =

$$\begin{aligned} & (\text{PROB}(\text{P}/\text{ART}) * \text{SEQSUM}(1,1) + \text{PROB}(\text{P}/\text{N}) * \text{SEQSUM}(2,1) + \\ & \text{PROB}(\text{P}/\text{V}) * \text{SEQSUM}(3,1) + \text{PROB}(\text{P}/\text{P}) * \text{SEQSUM}(4,1)) * \text{PROB}(\text{flies}/\text{P}) \end{aligned}$$

$$= 0$$

t=3

SEQSUM(1,3) =

$$\begin{aligned} & (\text{PROB}(\text{ART}/\text{ART}) * \text{SEQSUM}(1,2) + \text{PROB}(\text{ART}/\text{N}) * \text{SEQSUM}(2,2) + \\ & \text{PROB}(\text{ART}/\text{V}) * \text{SEQSUM}(3,2) + \text{PROB}(\text{ART}/\text{P}) * \text{SEQSUM}(4,2)) \\ & * \text{PROB}(\text{like}/\text{ART}) \end{aligned}$$

$$= 0$$

SEQSUM(2,3) =

$$\begin{aligned}
& (\text{PROB}(\text{N}/\text{ART}) * \text{SEQSUM}(1,2) + \text{PROB}(\text{N}/\text{N}) * \text{SEQSUM}(2,2) + \\
& \text{PROB}(\text{N}/\text{V}) * \text{SEQSUM}(3,2) + \text{PROB}(\text{N}/\text{P}) * \text{SEQSUM}(4,2)) \\
& * \text{PROB}(\text{like}/\text{N}) \\
& = (0 + 0.13 * 8.7407 * 10^{-5} + 0.53 * 5.5884 * 10^{-4} + 0) * 0.012 \\
& = 3.6906 * 10^{-6}
\end{aligned}$$

$$\text{SEQSUM}(3,3) =$$

$$\begin{aligned}
& (\text{PROB}(\text{V}/\text{ART}) * \text{SEQSUM}(1,2) + \text{PROB}(\text{V}/\text{N}) * \text{SEQSUM}(2,2) + \\
& \text{PROB}(\text{V}/\text{V}) * \text{SEQSUM}(3,2) + \text{PROB}(\text{V}/\text{P}) * \text{SEQSUM}(4,2)) \\
& * \text{PROB}(\text{like}/\text{V}) \\
& = (0 + 0.43 * 8.7407 * 10^{-5} + 10^{-4} * 5.5884 * 10^{-4} + 0) * 0.1 \\
& = 3.7641 * 10^{-6}
\end{aligned}$$

$$\text{SEQSUM}(4,3) =$$

$$\begin{aligned}
& (\text{PROB}(\text{P}/\text{ART}) * \text{SEQSUM}(1,2) + \text{PROB}(\text{P}/\text{N}) * \text{SEQSUM}(2,2) + \\
& \text{PROB}(\text{P}/\text{V}) * \text{SEQSUM}(3,2) + \text{PROB}(\text{P}/\text{P}) * \text{SEQSUM}(4,2)) \\
& * \text{PROB}(\text{like}/\text{P}) \\
& = (0 + 0.44 * 8.7407 * 10^{-5} + 0.15 * 5.5884 * 10^{-4} + 0) * 0.068 \\
& = 8.3154 * 10^{-6}
\end{aligned}$$

t=4

$$\text{SEQSUM}(1,4) =$$

$$\begin{aligned}
& (\text{PROB}(\text{ART}/\text{ART}) * \text{SEQSUM}(1,3) + \text{PROB}(\text{ART}/\text{N}) * \text{SEQSUM}(2,3) + \\
& \text{PROB}(\text{ART}/\text{V}) * \text{SEQSUM}(3,3) + \text{PROB}(\text{ART}/\text{P}) * \text{SEQSUM}(4,3)) \\
& * \text{PROB}(\text{birds}/\text{ART}) \\
& = 0
\end{aligned}$$

$$\text{SEQSUM}(2,4) =$$

$$\begin{aligned}
& (\text{PROB}(\text{N}/\text{ART}) * \text{SEQSUM}(1,3) + \text{PROB}(\text{N}/\text{N}) * \text{SEQSUM}(2,3) + \\
& \text{PROB}(\text{N}/\text{V}) * \text{SEQSUM}(3,3) + \text{PROB}(\text{N}/\text{P}) * \text{SEQSUM}(4,3)) \\
& * \text{PROB}(\text{birds}/\text{N})
\end{aligned}$$

$$= (0 + 0.13 * 3.6906 * 10^{-6} + 0.53 * 3.7641 * 10^{-6} + 0.26 * 8.3154 * 10^{-6}) * 0.076$$

$$= 3.5239 * 10^{-7}$$

$$\text{SEQSUM}(3,4) =$$

$$(\text{PROB}(V/\text{ART}) * \text{SEQSUM}(1,3) + \text{PROB}(V/N) * \text{SEQSUM}(2,3) +$$

$$\text{PROB}(V/V) * \text{SEQSUM}(3,3) + \text{PROB}(V/P) * \text{SEQSUM}(4,3))$$

$$* \text{PROB}(\text{birds}/V)$$

$$= (0 + 0.43 * 3.6906 * 10^{-6} + 10^{-4} * 3.7641 * 10^{-6} + 10^{-4} * 8.3154 * 10^{-6}) * 1/300$$

$$= 5.2939 * 10^{-9}$$

$$\text{SEQSUM}(4,4) =$$

$$(\text{PROB}(P/\text{ART}) * \text{SEQSUM}(1,3) + \text{PROB}(P/N) * \text{SEQSUM}(2,3) +$$

$$\text{PROB}(P/V) * \text{SEQSUM}(3,3) + \text{PROB}(P/P) * \text{SEQSUM}(4,3))$$

$$* \text{PROB}(\text{birds}/P)$$

$$= 0$$

Tính xác suất từ vựng

$$1. \text{SEQSUM}(1,1) + \text{SEQSUM}(2,1) + \text{SEQSUM}(3,1) + \text{SEQSUM}(4,1) = 0.0184$$

$$\text{PROB}(\text{fruit}|\text{ART}|\text{fruit}) = \text{SEQSUM}(1,1) / 0.0184 = 0.069152173913$$

$$\text{PROB}(\text{fruit}|N|\text{fruit}) = \text{SEQSUM}(2,1) / 0.0184 = 0.929347826087$$

$$\text{PROB}(\text{fruit}|V|\text{fruit}) = \text{SEQSUM}(3,1) / 0.0184 = 0.0000905815217391$$

$$\text{PROB}(\text{fruit}|P|\text{fruit}) = \text{SEQSUM}(4,1) / 0.0184 = 0$$

$$2. \text{SEQSUM}(1,2) + \text{SEQSUM}(2,2) + \text{SEQSUM}(3,2) + \text{SEQSUM}(4,2) = 0.000647$$

$$\text{PROB}(\text{flies}|\text{ART}|\text{fruit flies}) = 0$$

$$\text{PROB}(\text{flies}|N|\text{fruit flies}) = \text{SEQSUM}(2,2) / 0.000647 = 0.1363$$

$$\text{PROB}(\text{flies}|V|\text{fruit flies}) = \text{SEQSUM}(3,2) / 0.000647 = 0.8637$$

$$\text{PROB}(\text{flies}|P|\text{fruit flies}) = 0$$

$$3. \text{SEQSUM}(1,3) + \text{SEQSUM}(2,3) + \text{SEQSUM}(3,3) + \text{SEQSUM}(4,3) = 0.00001577$$

$$\text{PROB}(\text{like}|\text{ART}|\text{fruit flies like}) = 0$$

$$\text{PROB}(\text{like}|\text{N}|\text{fruit flies like}) = \text{SEQSUM}(2,3) / 0.00001577 = 0.2340$$

$$\text{PROB}(\text{like}|\text{V}|\text{fruit flies like}) = \text{SEQSUM}(3,3) / 0.00001577 = 0.2387$$

$$\text{PROB}(\text{like}|\text{P}|\text{fruit flies like}) = \text{SEQSUM}(4,3) / 0.00001577 = 0.5273$$

$$4. \text{SEQSUM}(1,4) + \text{SEQSUM}(2,4) + \text{SEQSUM}(3,4) + \text{SEQSUM}(4,4) = 3.5768 * 10^{-7}$$

$$\text{PROB}(\text{birds}|\text{ART}|\text{fruit flies like birds}) = 0$$

$$\text{PROB}(\text{birds}|\text{N}|\text{fruit flies like birds}) = \text{SEQSUM}(2,4) / (3.5768 * 10^{-7}) = 0.9852$$

$$\text{PROB}(\text{birds}|\text{V}|\text{fruit flies like birds}) = \text{SEQSUM}(3,4) / (3.5768 * 10^{-7}) = 0.0148$$

$$\text{PROB}(\text{birds}|\text{P}|\text{fruit flies like birds}) = 0$$

Như vậy **fruit flies like birds** là **N V P N**.

b)

S4

$$1 \text{ NP6}, 2 \text{ VP9}, 1 * 0.0383 * 0.33 * 30/61 * 0.1378 = 8.56 * 10^{-4}$$

S3

$$1 \text{ NP5}, 2 \text{ VP9}, 1 * 4.77 * 10^{-3} * 0.33 * 30/61 * 0.1378 = 1.07 * 10^{-4}$$

S2

$$1 \text{ NP1}, 2 \text{ VP11}, 1 * 0.14 * 49/55 * 0.15 * 23/44 * 0.0685 = 6.69 * 10^{-4}$$

S1

$$1 \text{ NP1}, 2 \text{ VP10}, 1 * 0.14 * 49/55 * 0.33 * 23/44 * 0.0145 = 3.12 * 10^{-4}$$

VP11

$$1 \text{ V2}, 2 \text{ PP1}, 0.15 * 23/44 * 0.0685$$

VP10

	1 V2, 2 NP8, $0.33 * 23/44 * 0.0145$		
		VP9 $1 V3, 2 NP4, 0.33 * 30/61 * 0.1378$	
	VP8 $1 V2, 2 NP8, 0.33 * 23/44 * 0.0145$		
	VP7 $1 V2, 2 NP3, 0.33 * 23/44 * 0.0656$		
VP6 $1 V1, 2 NP7, 0.33 * 5/55 * 7.04 * 10^{-3}$			
VP5 $1 V1, 2 NP2, 0.33 * 5/55 * 0.0668$			
		PP1 $1 P1, 2 NP4, 1 * 21/61 * 0.14 * 64/65 = 0.0685$	
		NP8 $1 N3, 2 N4, 0.09 * 10/61 * 64/65 = 0.0145$	
	NP7 $1 N2, 2 N3, 0.09 * 21/44 * 10/61 = 7.04 * 10^{-3}$		
NP6 $1 N1, 2 N2, 0.09 * 49/55 * 21/44 = 0.0383$			
NP5 $1 ART1, 2 N2, 0.55 * 1/55 * 21/44 = 4.77 * 10^{-3}$			
VP1 $1 V1, 0.32 * 5/55$	VP2 $1 V2, 0.32 * 23/44$	VP3 $1 V3, 0.32 * 30/61$	VP4 $1 V4, 0.32 * 1/65$
NP1 $1 N1$	NP2 $1 N2$	NP3 $1 N3$	NP4 $1 N4$

0.14 * 49/55	0.14 * 21/44 = 0.0668	0.14 * 10/61 = 0.0656	0.14 * 64/65 = 0.1378
ART1 1/55		P1 21/61	
V1 5/55	V2 23/44	V3 30/61	V4 1/65
N1 49/55	N2 21/44	N3 10/61	N4 64/65
Fruit	flies	like	birds

Như vậy **fruit flies like birds** là N N V N.

4. Specify PMI between two words, Positive PMI between two words in the below table

	aadvark	computer	data	pinch	result	sugar
Apricot	0	0	0	0	1	0
Pineapple	0	0	0	0	1	0
Digital	0	2	1	0	1	0
Information	0	1	6	0	4	0

Giải

$$p(w=\text{Digital} \mid c=\text{computer}) = 2/17$$

$$p(w=\text{Digital}) = 4/17$$

$$p(c=\text{computer}) = 3/17$$

Tương tự, ta có bảng sau

	p(w, c)						p(w)
	aadvark	computer	data	pinch	result	sugar	
Apricot	0	0	0	0	1/17	0	1/17
Pineapple	0	0	0	0	1/17	0	1/17
Digital	0	2/17	1/17	0	1/17	0	4/17
Information	0	1/17	6/17	0	4/17	0	11/17
p(c)	0	3/17	7/17	0	7/17	0	

Suy ra:

$$\text{pmi}(\text{Apricot}, \text{result}) = \log_2(1/17 / (7/17 * 1/17)) = 1.2801$$

Tương tự ta có bảng sau:

	pmi(w, c)
--	-----------

	aadvark	computer	data	pinch	result	sugar
Apricot					1.2801	
Pineapple					1.2801	
Digital		1.5025	-0.7199		-0.7199	
Information		-0.9569	0.4056		-0.1793	

	ppmi(w, c)					
	aadvark	computer	data	pinch	result	sugar
Apricot					1.2801	
Pineapple					1.2801	
Digital		1.5025				
Information			0.4056			