

SECURITY IN COMPUTING, FIFTH EDITION

Chapter 12: Details of Cryptography

Chapter 12 Objectives

- Learn basic terms and primitives of cryptography
- Deep dive into how symmetric encryption algorithms work
- Study the RSA asymmetric encryption algorithm
- Compare message digest algorithms
- Explain the math behind digital signatures
- Learn the concepts behind quantum cryptography

Methods of Cryptanalysis

- Break (decrypt) a single message
- Recognize patterns in encrypted messages
- Infer some meaning without even breaking the encryption, such as from the length or frequency of messages
- Easily deduce the key to break one message and perhaps subsequent ones

Methods of Cryptanalysis

- Find weaknesses in the implementation or environment of use of encryption by the sender
- Find general weaknesses in an encryption algorithm

Methods of Cryptanalysis

- We start with a brief discussion of cryptanalysis
- How can we protect data from attackers?
 - Understand what attackers are trying to accomplish
 - How they are trying to accomplish it

Methods of Cryptanalysis

- Different methods are not mutually exclusive
- Which ones are applied will depend on:
 - Expertise of the attacker
 - What information is available to the attacker
 - What access is available to the attacker
 - Other constraints, such as time

Cryptanalysis Inputs

- Ciphertext only
 - Look for patterns, similarities, and discontinuities among many messages that are encrypted alike
 - Known ciphertext
 - Chosen ciphertext
- Plaintext and ciphertext, so the cryptanalyst can see what transformations occurred
 - Known plaintext
 - Probable plaintext
 - Chosen plaintext

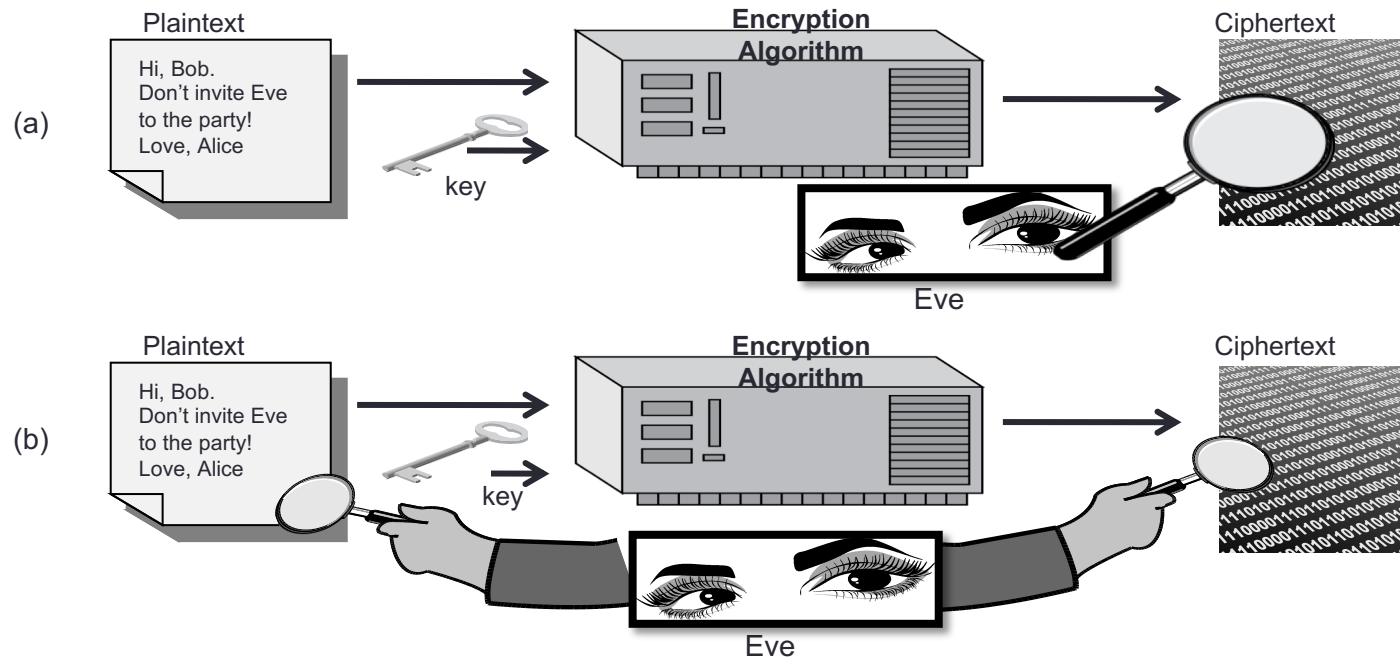
Cryptanalysis Inputs

- Plaintext and ciphertext attacks:
 - Known plaintext:
 - the analyst has an exact copy of the plaintext and ciphertext
 - Probable plaintext:
 - message is very likely to have certain content, such as a date header
 - Chosen plaintext:
 - the attacker gains sufficient access to the system to generate ciphertext from arbitrary plaintext inputs

Attacks

- Attacker may have
 - collection of ciphertexts (***ciphertext only attack***)
 - collection of plaintext/ciphertext pairs (***known plaintext attack***)

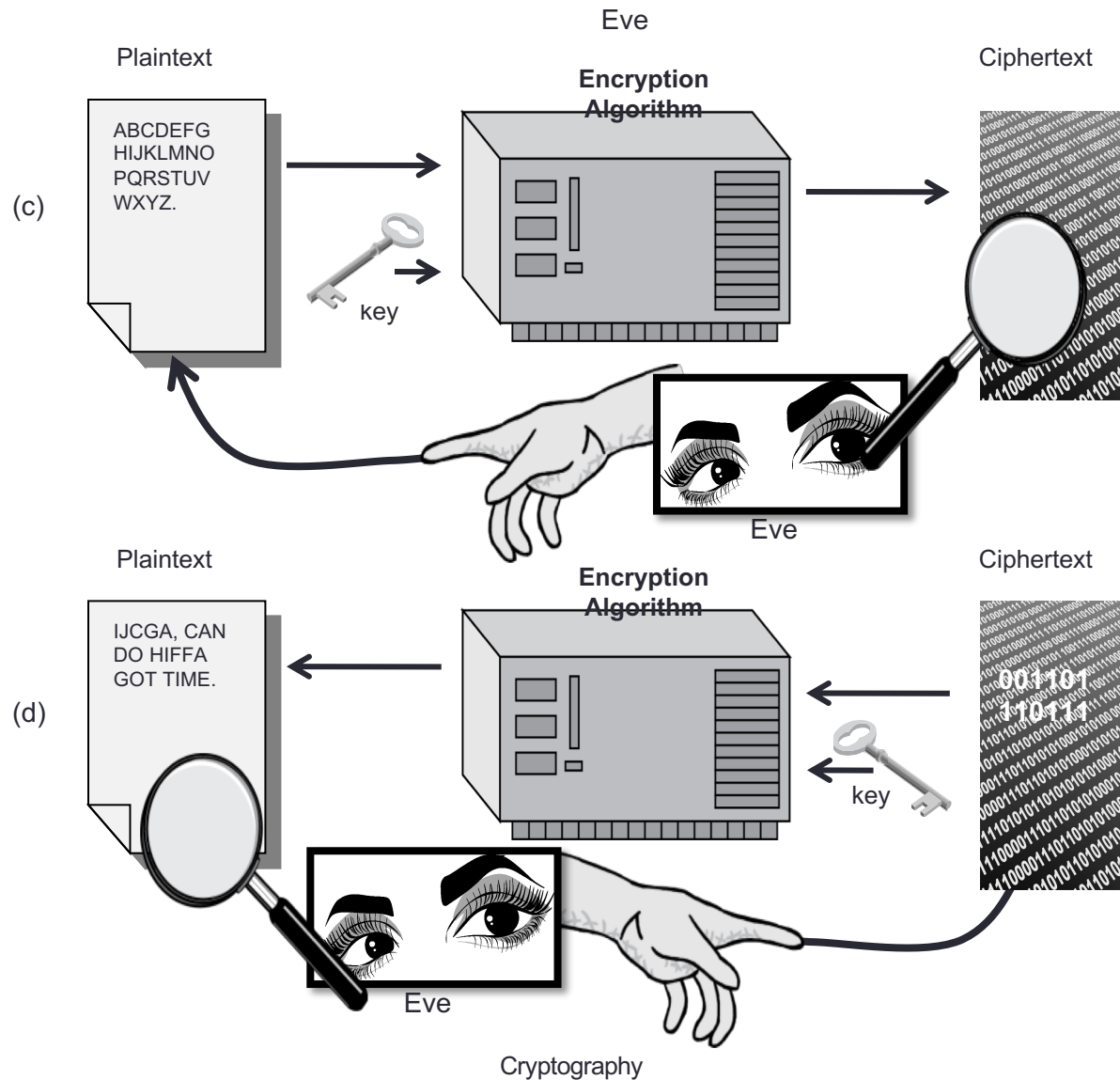
Attacks



Attacks

- Attacker may have
 - collection of plaintext/ciphertext pairs for plaintexts selected by the attacker (***chosen plaintext attack***)
 - collection of plaintext/ciphertext pairs for ciphertexts selected by the attacker (***chosen ciphertext attack***)

Attacks



Cryptographic Primitives

- Substitution
 - One set of bits is exchanged for another
 - For example, each alphabetic letter replaced with another
 - Can also be done on data bytes or blocks
 - Involves a lookup table
 - Can be done quickly
 - Using software or optimized hardware
- Transposition
 - Rearranging the order of the ciphertext to break any repeating patterns in the underlying plaintext

Cryptographic Primitives

- Confusion
 - Good confusion: algorithm has a complex functional relationship between plaintext/key pair and ciphertext
 - => changing one character in the plaintext causes unpredictable changes to the resulting ciphertext
- Diffusion
 - Distributes the information from single plaintext characters over the entire ciphertext output
 - => even small changes to the plaintext result in broad changes to the ciphertext

Cryptographic Primitives

- These are the basic techniques that make up cryptographic algorithms
- The first two—substitution and transposition—are simple mathematical operations
 - used within complex cryptosystems.
- The latter two—confusion and diffusion—are more conceptual
 - may be accomplished in a number of different ways depending on the cryptographic algorithm.

One-time Pad

- A one-time pad is often used as an example of the perfect cipher
- Only useful as a concept
 - completely impractical.
-

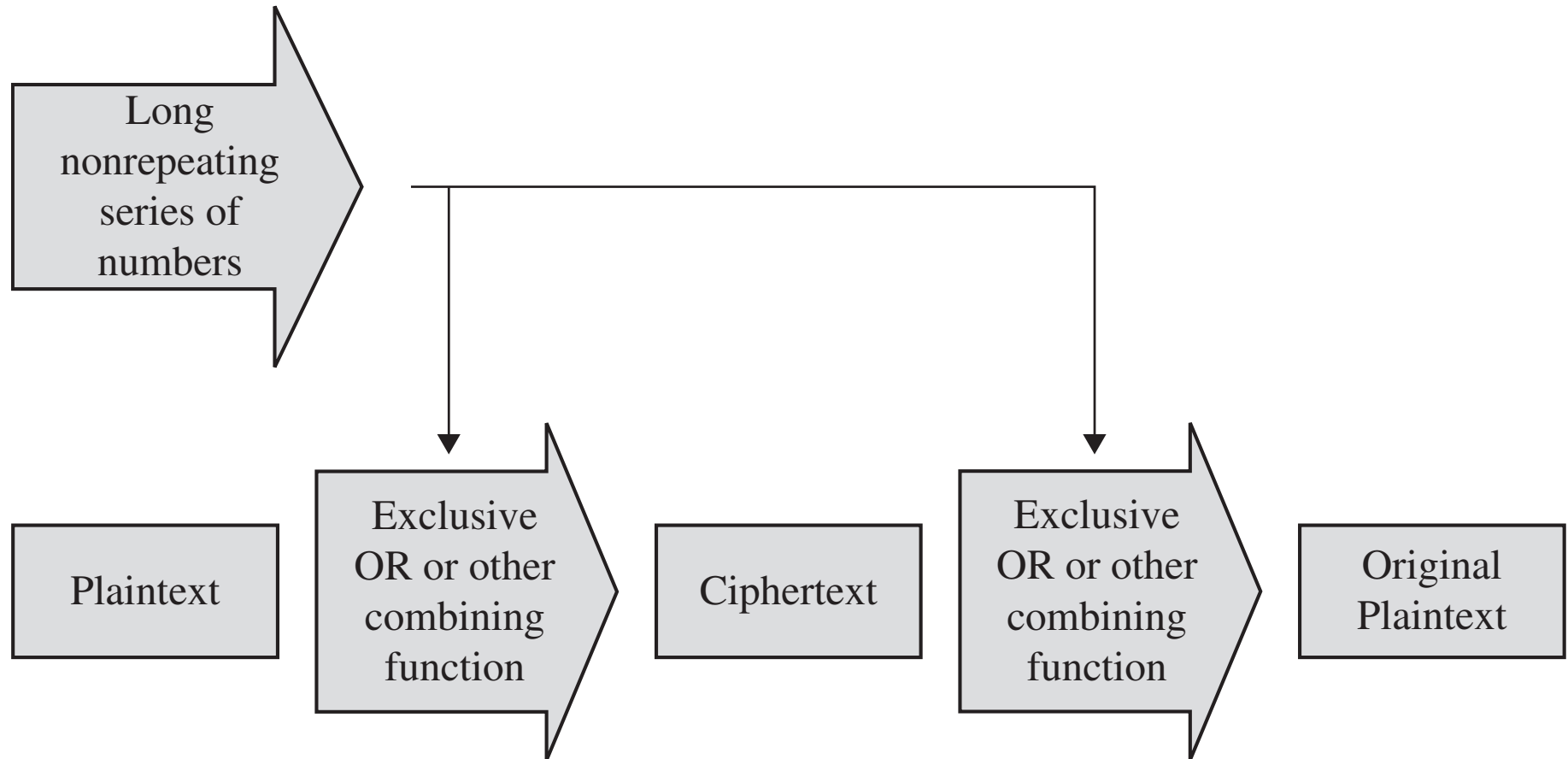
One-time Pad

- A one-time pad is a substitution cipher
 - Uses an arbitrarily large, nonrepeating set of keys
 - requires both an unlimited set of completely random keys and absolute sender and receiver synchronization
 - both of which are impractical.
- Resistance to cryptanalysis:
 - one-time pad is the gold standard against which other enc. algorithms are measured
 - offers no patterns for attackers to analyze.

One-time Pad – Vernam Cipher

- Vernam cipher, a type of one-time pad
- In the Vernam cipher, XOR is used instead of pure substitution

One-Time Pads – Vernam Cipher



Shannon's Characteristics of Good Ciphers

- The amount of secrecy needed should determine the amount of labor appropriate for the encryption and decryption
- The set of keys and the enciphering algorithm should be free from complexity
- The implementation of the process should be as simple as possible

Shannon's Characteristics of Good Ciphers

- Errors in ciphering should not propagate and cause corruption of further information in the message
- The size of the enciphered text should be no larger than the text of the original message

Shannon's Characteristics of Good Ciphers

- The amount of secrecy needed should determine the amount of labor appropriate for the encryption and decryption
 - The degree of secrecy required factors such as key length and number of rounds
 - should be based on implementation of the algorithm, current and predicted speeds of computers, and resources of likely attackers

Shannon's Characteristics of Good Ciphers

- The set of keys and the enciphering algorithm should be free from complexity
 - The process has to work on any kind of plaintext input, and keys should be easy for users to generate, transmit, and store

Shannon's Characteristics of Good Ciphers

- The implementation of the process should be as simple as possible
 - complexity is the enemy of good security analysis.
 - It is easier to identify flaws in, and to correctly implement, a simpler algorithm
 - a simpler algorithm is therefore more likely to be free of flaws

Shannon's Characteristics of Good Ciphers

- Errors in ciphering should not propagate and cause corruption of further information in the message
 - Communication errors do happen, and when they do, the need for retransmission should be as limited as possible

Shannon's Characteristics of Good Ciphers

- The size of the enciphered text should be no larger than the text of the original message
 - A ciphertext that expands in size cannot possibly carry more information than the source plaintext
 - yet gives the cryptanalyst more data from which to infer a pattern
 - Larger messages also require more transmission time and storage and are therefore less practical for users

Properties of a Trustworthy Cryptosystem

- It is based on sound mathematics
- It has been analyzed by competent experts and found to be sound
- It has stood the test of time

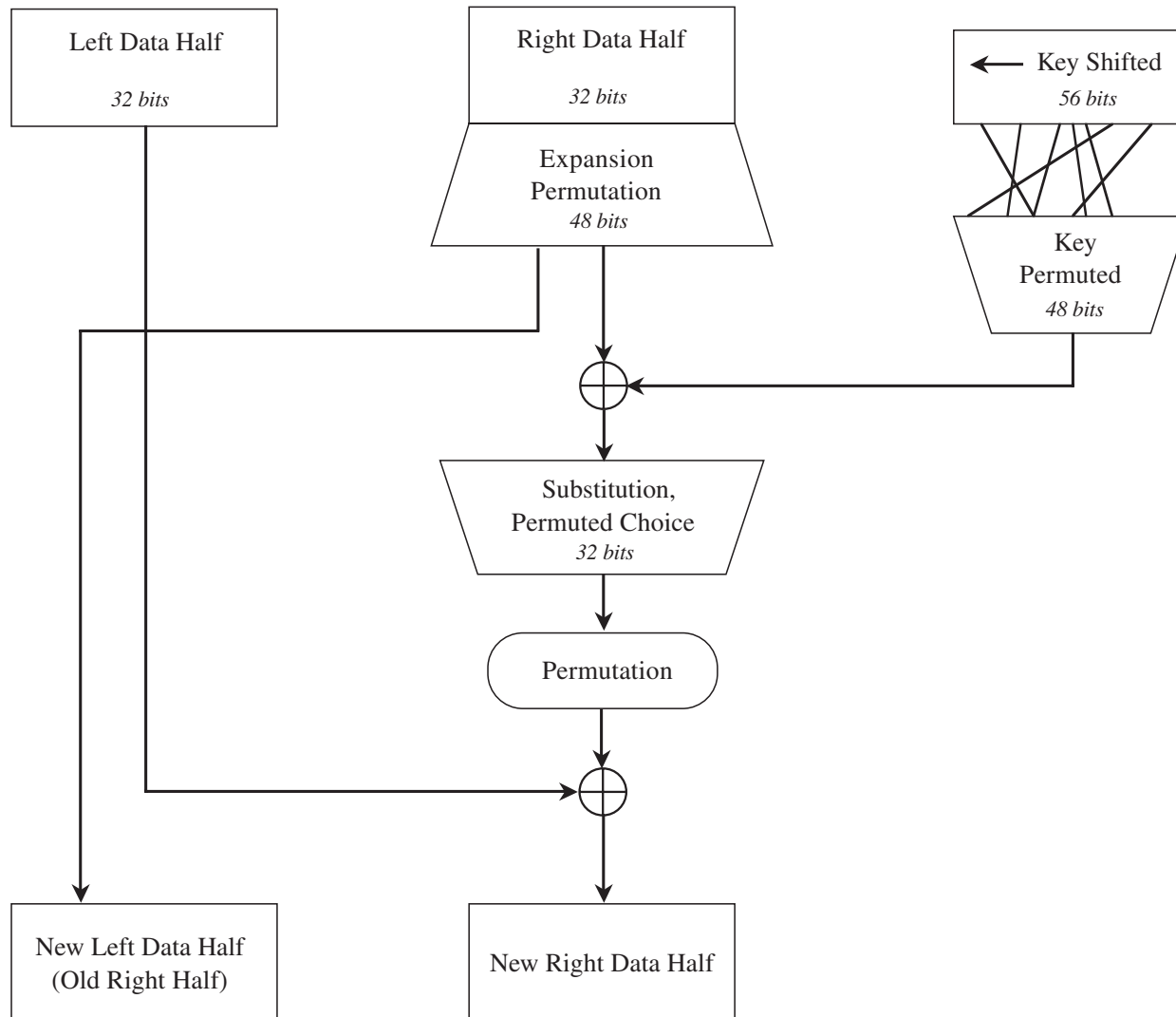
Properties of a Trustworthy Cryptosystem

- Good cryptographic algorithms are derived from sound principles and have security properties that are proven by expert mathematicians.
- Historically, algorithms that have not met this standard have been easily broken.
- Because cryptographic algorithms are complex, it can take years of analysis
 - before serious flaws are identified

DES Algorithm

- Symmetric cryptography algorithm
- No longer practical for use against modern technology
 - However, algorithm has a combination of strong fundamentals and relative simplicity
 - useful for demonstrating how symmetric encryption works

DES Algorithm – Single Cycle



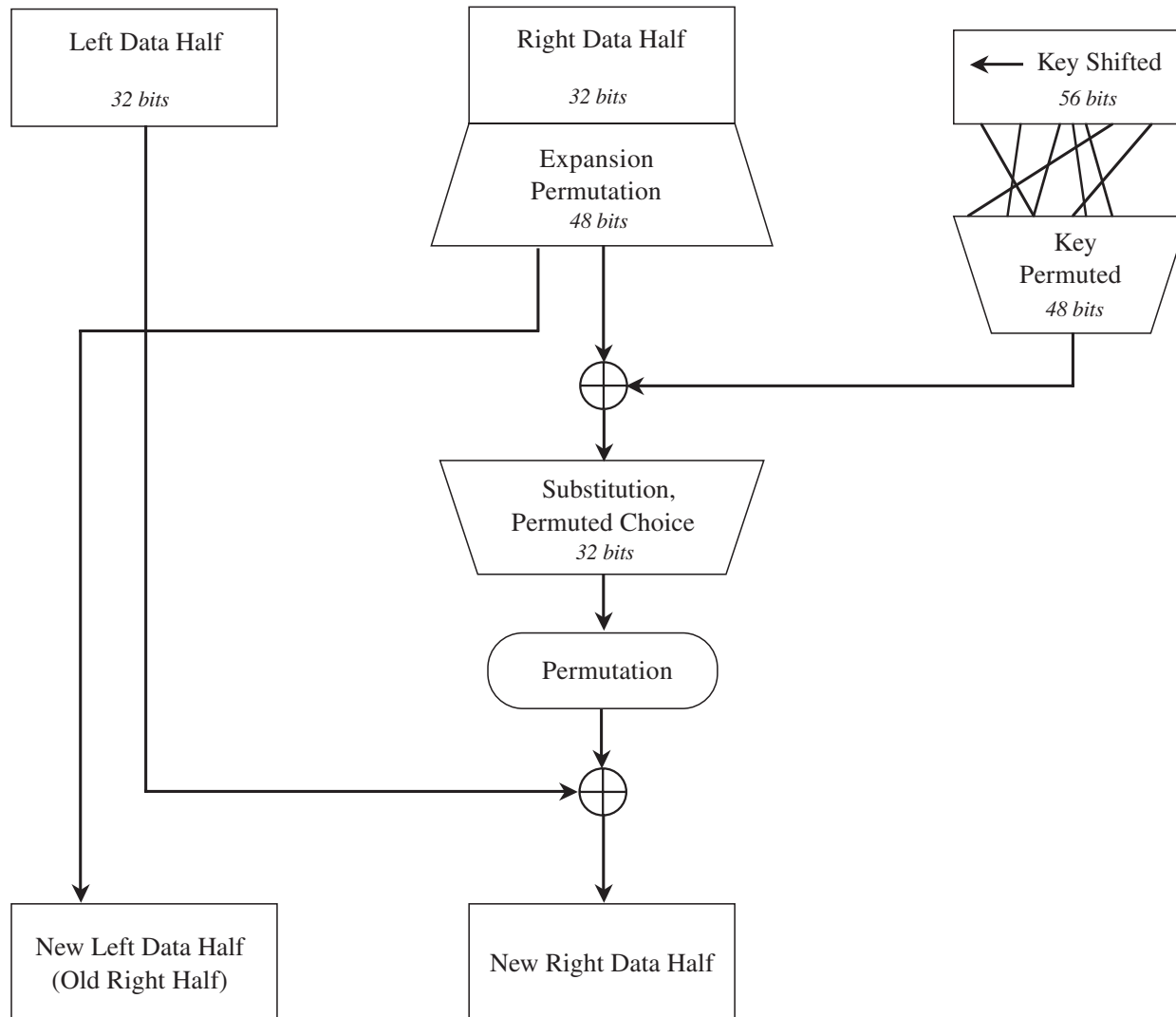
DES Algorithm – Single Cycle

- Input to DES is divided into blocks of 64 bits
- The data bits are permuted by an “initial permutation”
- The key is reduced from 64 bits to 56 bits
 - parity bits are removed)
- The 64 permuted data bits are broken into a left half and right half
- The 32-bit right half is expanded to 58 bits
 - by repeating certain bits

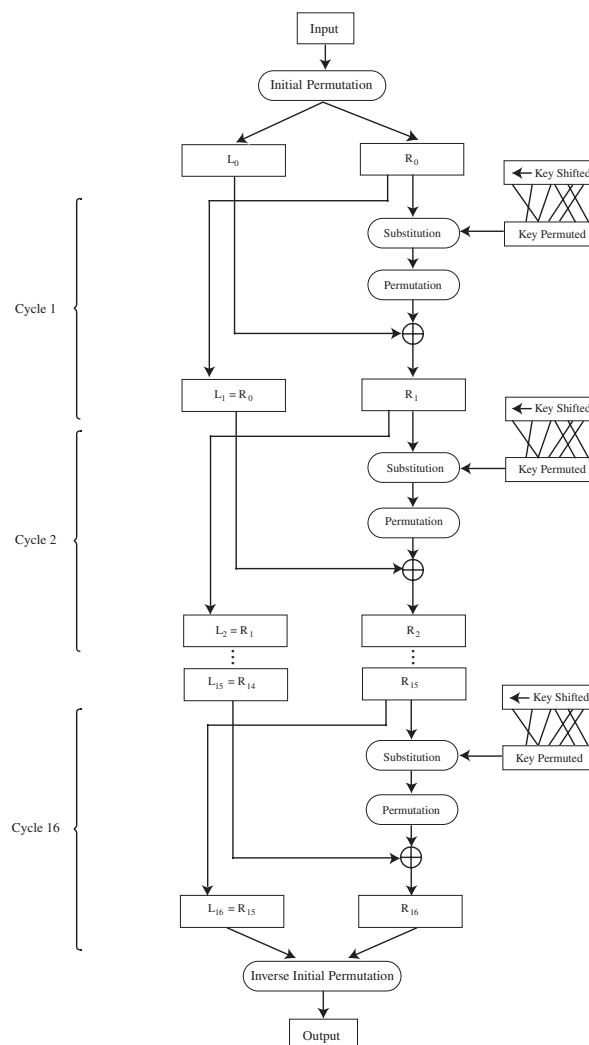
DES Algorithm – Single Cycle (cont.)

- The key is reduced to 48 bits
 - by choosing only certain bits according to tables called S-boxes
- The key is shifted left by a number of bits and also permuted
- The key is combined with the right half, which is then combined with the left half
- The result of these combinations becomes the new right half
 - while the old right half becomes the new left half

DES Algorithm – Single Cycle

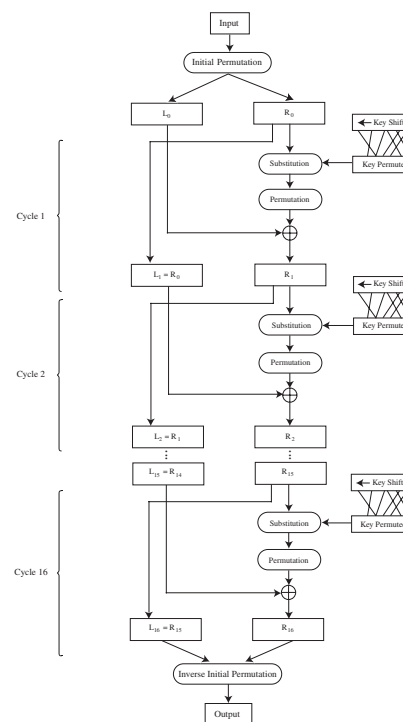


DES Algorithm (cont.)

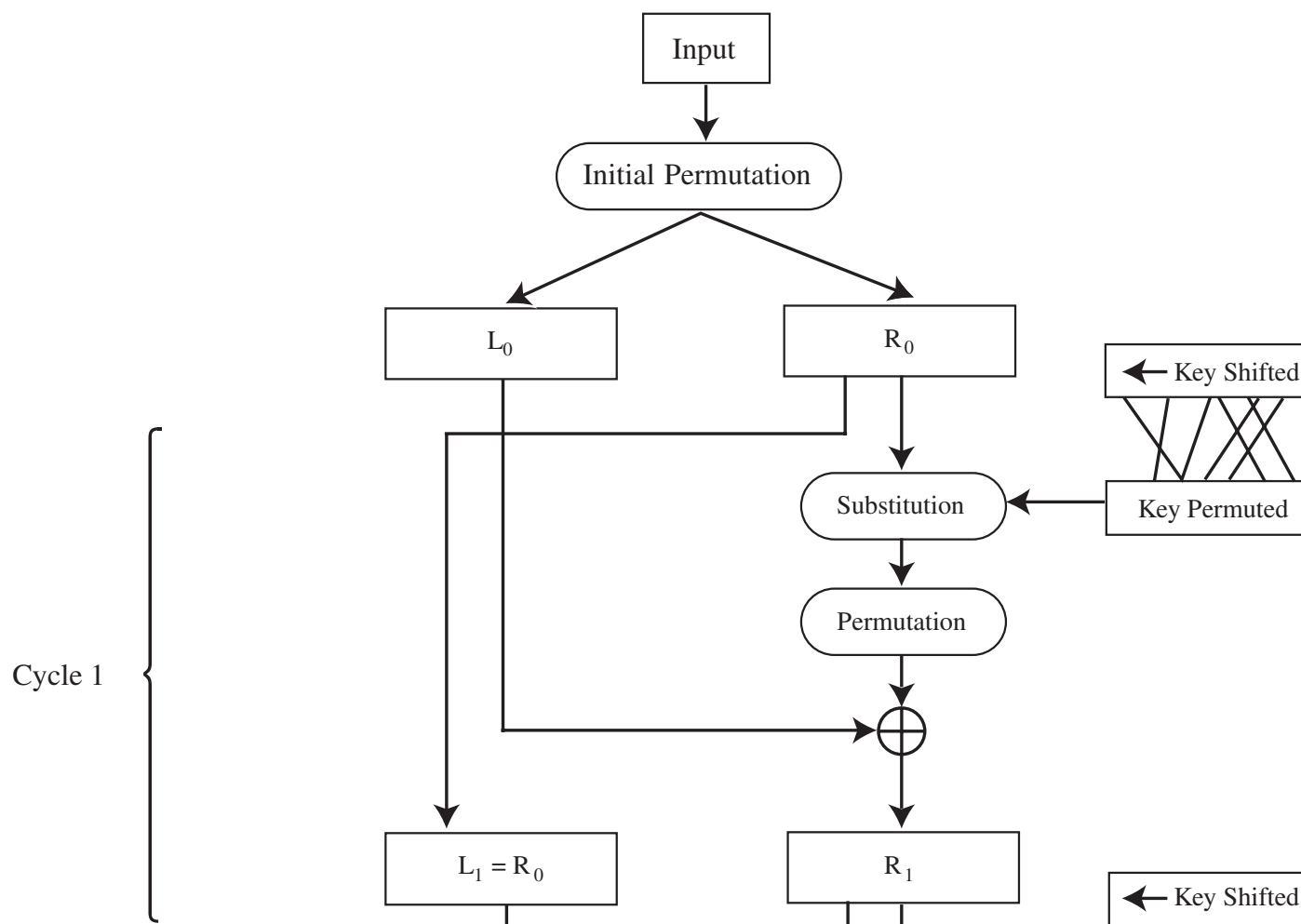


DES Algorithm (cont.)

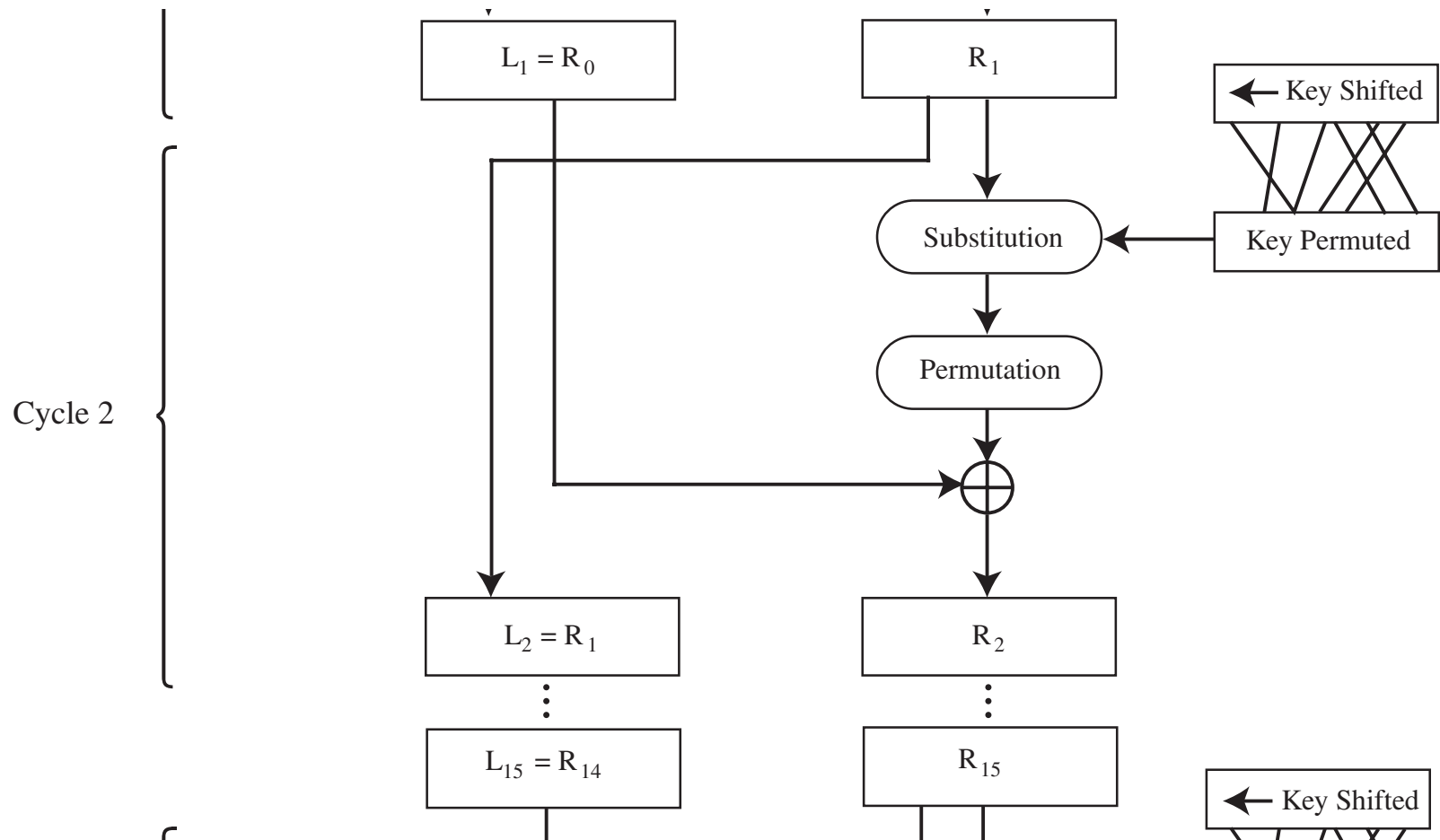
three cycles along with the initial permutation and the final permutation:



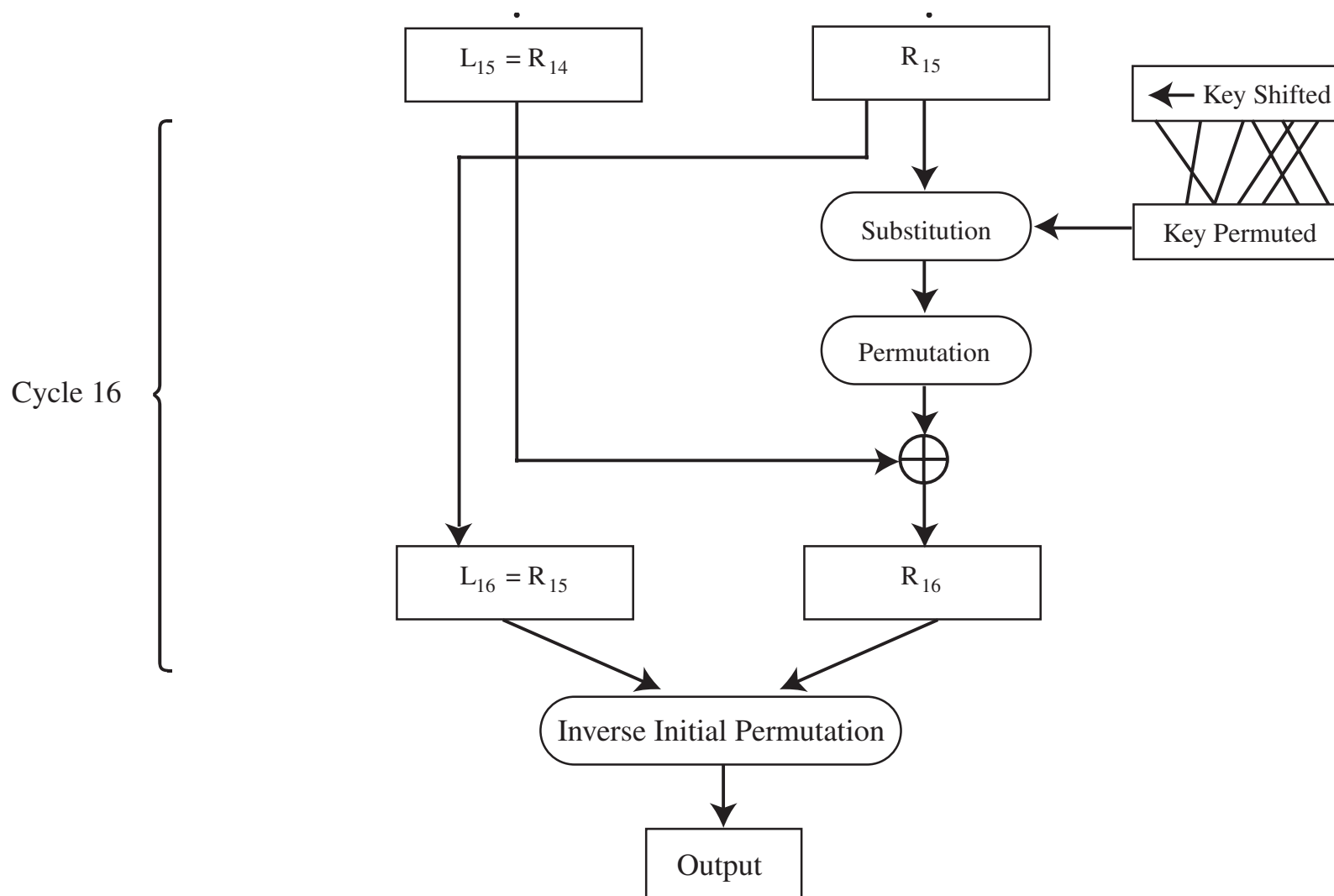
DES Algorithm (cont.) – initial permutation



DES Algorithm (cont.) – Single Cycle



DES Algorithm (cont.) – Final Permutation



DES Decryption

$$L_j = R_{j-1} \quad (1)$$

$$R_j = L_{j-1} \oplus f(R_{j-1}, k_j) \quad (2)$$

By rewriting these equations in terms of R_{j-1} and L_{j-1} , we get

$$R_{j-1} = L_j \quad (3)$$

and

$$L_{j-1} = R_j \oplus f(R_{j-1}, k_j) \quad (4)$$

Substituting (3) into (4) gives

$$L_{j-1} = R_j \oplus f(L_j, k_j) \quad (5)$$

DES Decryption

- a single algorithm is used for both encryption and decryption.
 - L is the left-half input
 - R is the right-half input
 - j is the current cycle
 - k is the key for the current cycle
 - f is the function computed in an expand-shift-substitute-permute cycle.

DES Decryption

- Equations (3) and (5) show that R and L for the previous cycle can be derived entirely from R and L of the current cycle
 - demonstrating that the DES algorithm can work in reverse

DES Decryption

$$L_j = R_{j-1} \quad (1)$$

$$R_j = L_{j-1} \oplus f(R_{j-1}, k_j) \quad (2)$$

By rewriting these equations in terms of R_{j-1} and L_{j-1} , we get

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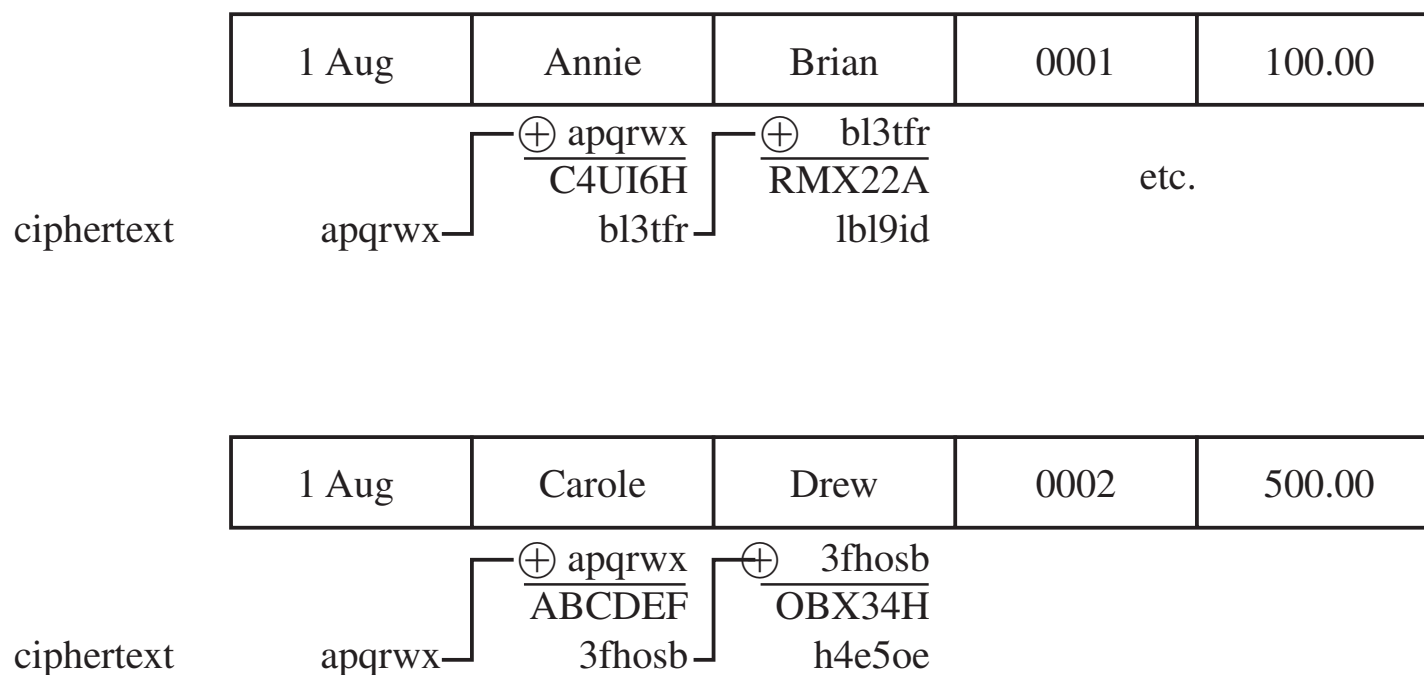
Substituting (3) into (4) gives

$$L_{j-1} = R_j \oplus f(L_j, k_j) \quad (5)$$

Chaining

- DES uses the same process for each 64-bit block
 - => two identical blocks encrypted with the same key will have identical output
- This provides too much information to an attacker
 - Data may be commonly reused in real life:
 - messages that have common beginnings or endings
 - reuse of a single key over a series of transactions
- The solution to this problem is chaining
 - makes the encryption of each block dependent on the content of the previous block as well as its own content

Simple Chaining Example



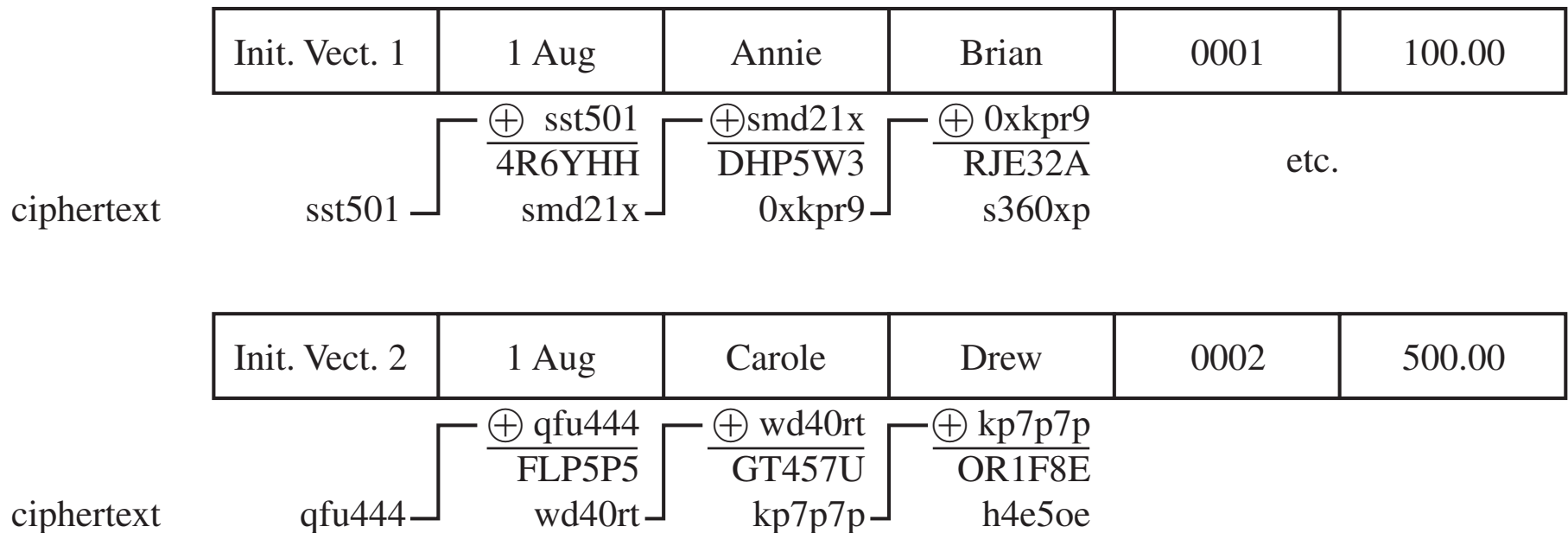
Simple Chaining Example

- the input of the second block is an XOR of the output of the first block and the plaintext of the second block.
- This has the effect of making identical plaintext in two different messages produce completely different ciphertext.
- But what about the first block?

Initialization Vectors

- To protect against the problem of identical first blocks, we start with an initialization vector:
 - an unpredictable (usually random) value that changes for each message
 - => the positive effect of chaining can be useful even for the first block of data

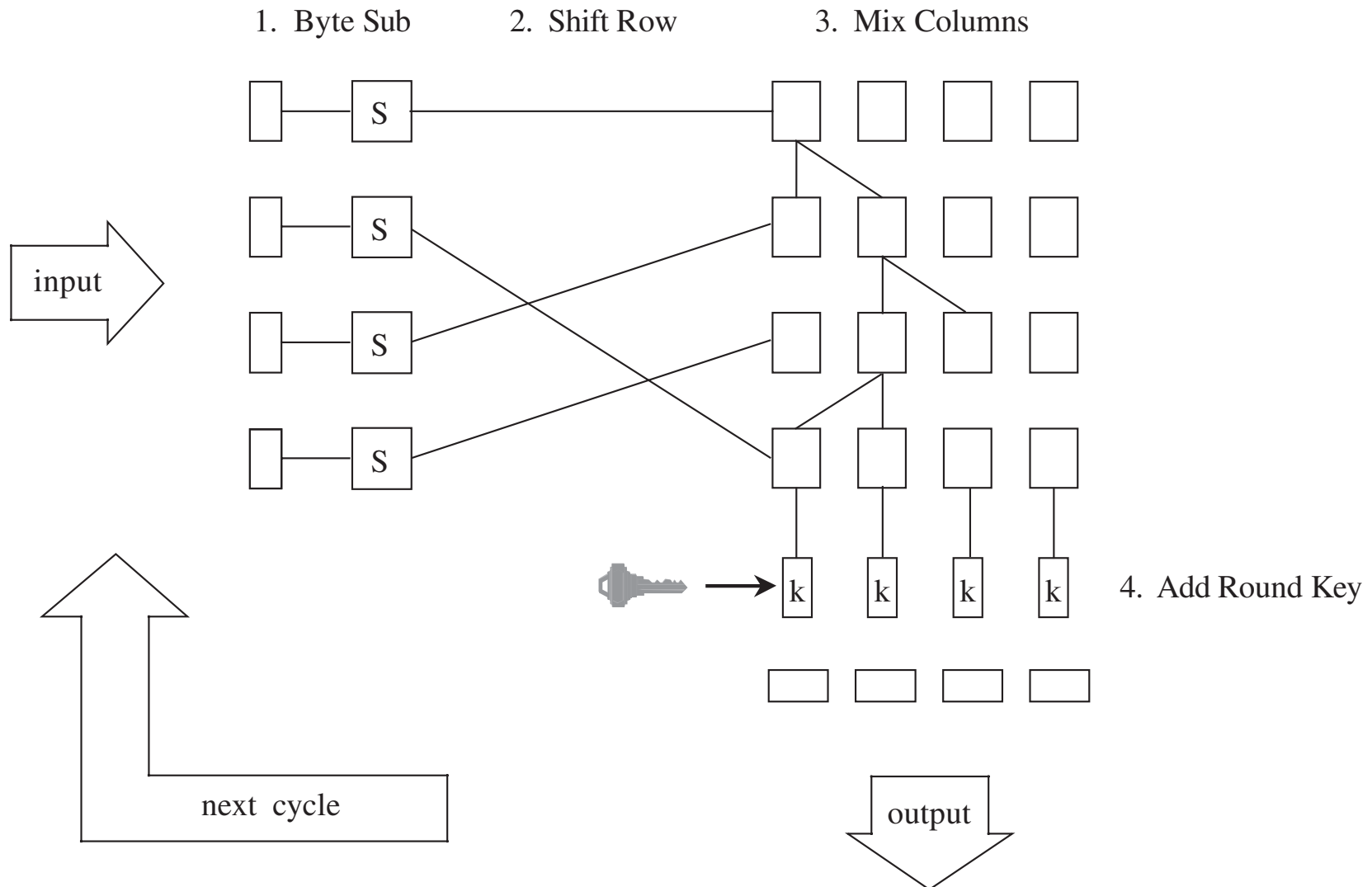
Initialization Vectors



AES

- Symmetric cryptography algorithm
- Successor of DES
- Still considered secure

Structure of AES



Structure of AES

- AES is much more complex than DES
- The algorithm consists of 10, 12, or 14 cycles, for a 128-, 192-, or 256-bit key, respectively.
- Each cycle consists of four steps:
 - Byte substitution, shift row, mix column and add subkey
- Each cycle performs both confusion and diffusion as well as blends the key into the result

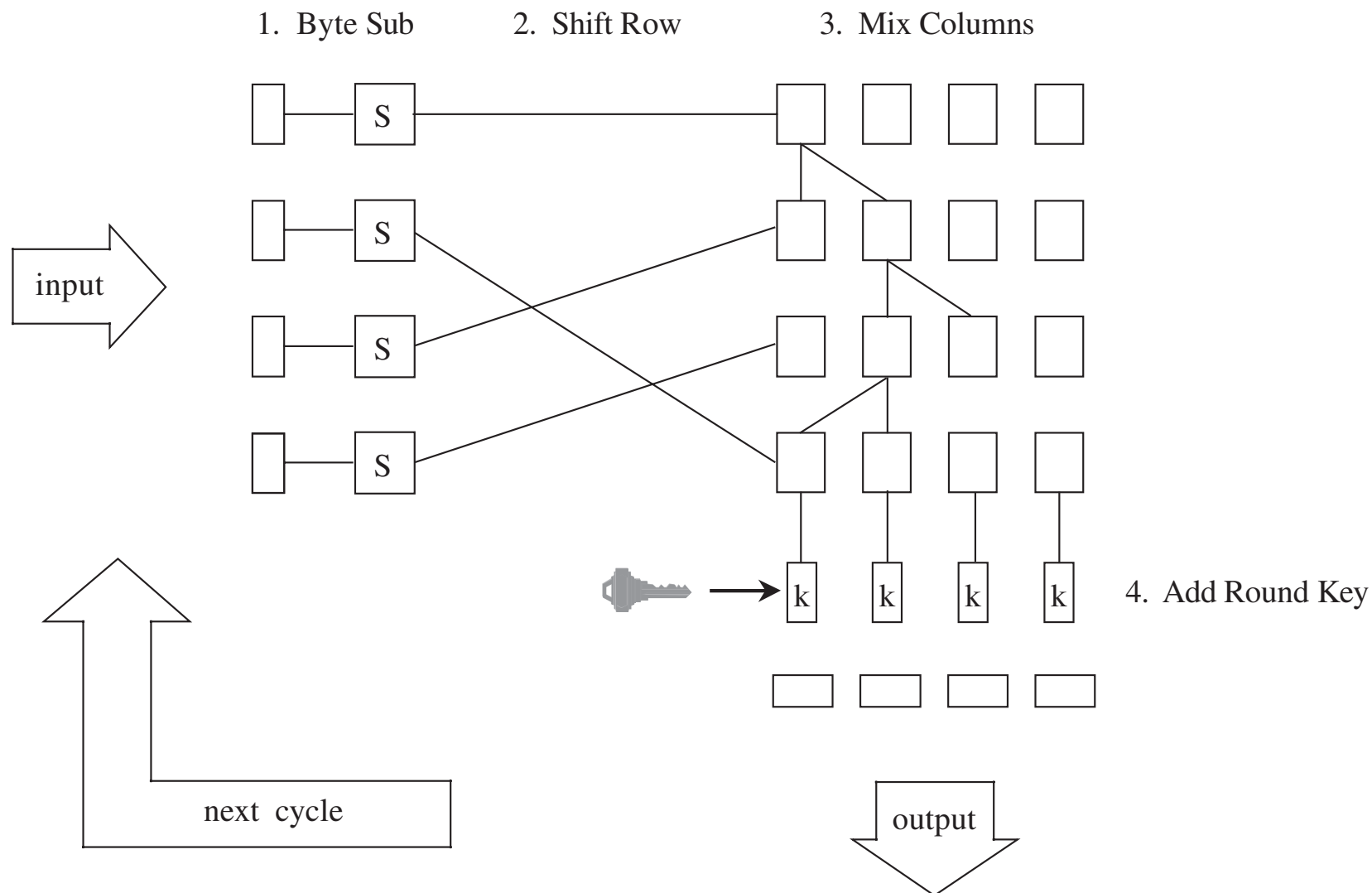
Structure of AES

- Byte substitution.
 - This step substitutes each byte of a 128-bit block according to a substitution table.
 - This is a straight diffusion operation.
- Shift row.
 - Certain bits are shifted to other positions.
 - This is a straight confusion operation.

Structure of AES

- Mix column.
 - This step involves shifting left and XORing bits with themselves.
 - These operations deliver both confusion and diffusion.
- Add subkey.
 - Here, a portion of the key unique to this cycle is XORed with the cycle result.
 - This operation delivers confusion and incorporates the key.

Structure of AES



Longevity of AES

- Since its initial publication in 1997, AES has been extensively analyzed
 - the only serious challenges to its security have been highly specialized and theoretical
- There is an evident underlying structure to AES
 - => it will be possible to use the same general approach on a slightly different underlying problem
 - to accommodate keys larger than 256 bits when necessary
- No attack to date has raised serious question as to the overall strength of AES

Additional Ciphers

- RC2, RC4, RC5, and RC6 were created by Ron Rivest
 - Creator of RSA

RC2

- RC2 is a block cipher
 - Uses a small 40 key size
 - Intended for international use by the Lotus Notes office application suite; it would use a
 - Short enough key to satisfy U.S. export restrictions to most countries
 - thereby assuring Lotus of international marketability
 - The export of cryptographic technology from the U.S. was severely restricted by law until 1992
 - gradually eased until 2000, some restrictions still remain

RC2

- RC2 consists of two operations:
 - mixing and mashing.
- In mixing, a bit stream undergoes bit shifting with concurrent substitution
 - through binary (AND, OR, NOT) operations on parts of the bits.
 - During each mixing round, a complete shuffle of bits occurs
 - from right, moving left, and cycling around to the right again.
 - There are sixteen rounds of mixing.

RC2

- RC2 consists of two operations:
 - mixing and mashing.
- The mashing round is pure substitution.
- No serious weaknesses have been discovered
 - but the 40-bit key makes brute-force key searches trivial

RC4

- RC4 is a stream cipher, widely used in wireless networks
 - WEP and WPA as well as in SSL
 - and various other products.
- RC4 was especially popular before 2000
 - like RC2, it employs a variable length key
 - => could be configured to use a 40-bit key
 - short enough to pass export restrictions

RC4

- RC4 is essentially a keyed pseudorandom number generator (PRNG)
 - generates a stream of bits in no predictable order.
- For encryption, the stream of bits is XORed with the plaintext bits

RC4

- Rc4 uses a 256-element array A containing each of the 256 possible values of an 8-bit byte
- Pointers i & j identify array bytes to be swapped.
- At each step:
 - i is incremented by 1
 - j is replaced by $j + A[i]$
 - $A[i]$ and $A[j]$ are swapped
 - byte $A[A[i]+A[j]]$ is produced as output.

RC4

- The algorithm is very efficient, especially for a software implementation
- No serious cryptanalytic weaknesses have been found in the algorithm itself.
 - However the random number sequence of an XOR stream cipher must never repeat
 - => Many implementations use it with an initialization vector (IV)
 - also called a ***nonce***

RC5

- More complex block cipher
- A data block is split in half:
 - the left half is modified
 - the halves are swapped,
 - The new left half (that is, the old right half) is modified the same way
 - the halves are swapped again.
- That sequence constitutes a full round of the algorithm.

RC5

- The modifications of each half-round involve XOR, circular shift, and addition of a portion of the key.
- The number of shifted bits depends on input data:
 - The left half is shifted by the number of bits of the value of the right half.
 - Unusual for cryptographic protocols
- No significant weaknesses have been found
 - Served as a model for AES

RC6

- RC6 is a lightly modified version of RC5
 - a proprietary product of RSA Security
 - Does not appear to be supported

Key Exchange

- Reminder: for symmetric encryption, a shared secret key is needed between each two parties
- For n parties, $(0.5 * n * n - 1) = O(N^2)$ keys are needed

Key Exchange

- Is there a more efficient method?
 - Yes, using a third trusted party
- In this case, each party will have one shared secret key with the third trusted party
 - $K_a, K_b, k_c, etc.$

Key Exchange with TTP

- What A and B want to exchange a secret key:
 - TTP picks a new secret key $K_{a,b}$
 - TTP encrypts $K_{a,b}$ with K_a and sends it to A
 - TTP encrypts $K_{a,b}$ with K_b and sends it to B
 - A and B each decrypts their respective keys
 - Using their pre-shared secret key

Key Exchange with TTP

- Disadvantage: TTP always has to be available online to perform key exchange
- Is there another method?
 - Yes, using asymmetric encryption

Key Exchange with Assymmetric Cryptography

- Alice chooses a pair of public and private keys K_{pb} and k_{pr}
- Alice distributes K_{pb} public key to all parties
- Bob chooses a secret key $K_{b,a}$ and encrypts it with K_{pb}
 - Sends $E(K_{b,a}, K_{pb})$ to Alice
- Alice uses her secret key k_{pr} to decrypt $K_{b,a}$
- Alice and Bob now share a secret key $K_{b,a}$

Asymmetric Encryption with RSA

- RSA is an Asymmetric Encryption Algorithm
- Since its introduction in 1978, RSA has been the subject of extensive cryptanalysis
 - no serious flaws have yet been found
- The encryption algorithm is based on the underlying problem of factoring large prime numbers
 - a problem for which the fastest known algorithm is exponential in time

Asymmetric Encryption with RSA

- Two keys, d and e , are used for decryption and encryption
 - they are interchangeable
- The plaintext block P is encrypted as
$$C = P^e \bmod n$$
- The decrypting key d is chosen such that:
$$(P^e)^d \bmod n = P$$

Detailed Description of RSA

The RSA algorithm uses two keys, d and e , which work in pairs, for decryption and encryption, respectively. A plaintext message P is encrypted to ciphertext C by

$$C = P^e \bmod n$$

The plaintext is recovered by

$$P = C^d \bmod n$$

Because of symmetry in modular arithmetic, encryption and decryption are mutual inverses and commutative. Therefore,

$$P = C^d \bmod n = (P^e)^d \bmod n = (P^d)^e \bmod n$$

This relationship means that one can apply the encrypting transformation and then the decrypting one, or the decrypting one followed by the encrypting one.

Deriving an RSA Key Pair

- The encryption key consists of the pair of integers (e, n) , and the decryption key is (d, n)
- The value of n should be quite large
 - a product of two primes, p and q
 - A large value inhibits factoring n to infer p and q
 - but time to encrypt increases as value of n grows larger
- Typically, p and q are nearly 100 digits each
 - $\Rightarrow n$ is approximately 200 decimal digits long
 - about 512 bits

Deriving an RSA Key Pair

- A relatively large integer e is chosen so that e is relatively prime to $(p - 1) * (q - 1)$
 - An easy way to guarantee e is relatively prime to $(p - 1) * (q - 1)$:
 - choose e as a prime that is larger than both $(p - 1)$ and $(q - 1)$
- Finally, select d such that
$$e * d = 1 \text{ mod } (p - 1) * (q - 1)$$

RSA Example

- For example, suppose the receiver selected the primes $p=11$ and $q=17$, along with $e=3$.

- The receiver calculates

$$n = p * q = 11 * 17 = 187$$

- which is half of the public key.

- The receiver also calculates

$$f(n) = (p - 1) (q - 1) = 160.$$

- $e=3$ was also chosen.

RSA Example

- For example, suppose the receiver selected the primes $p=11$ and $q=17$, along with $e=3$ (cont.).
- The receiver calculates $d=107$, since
$$d * e = 321 = 1 \text{ mod } (f(n))$$
- since The receiver distributes his public key: $n=187$ and $e=3$.

RSA Example

- Now suppose the sender wanted to send the message "HELLO"
- 'H' is 72 in ASCII
- The sender calculates $m^e = 72^3 = 183$
 - => making the ciphertext C = 183
- The receiver calculates
$$c^d = 183^{107} = 72 \pmod{187}$$
$$\Rightarrow m = 72$$
- Received translates message to 'H'
- The rest of the letters are sent the same way

RSA Encryption

- These days, 2048-bit keys are increasingly becoming a standard requirement
 - thanks to increased computing power.
- The user of RSA distributes the value of e and n and keeps d secret

How to Break Cryptography?

- [How to break cryptography](#)

Message Digests

- Message digests are ways to detect changes to a block of data
- One-way hash functions are cryptographic functions with multiple uses:
 - They are used in conjunction with public-key algorithms for both encryption and digital signatures
 - They are used in integrity checking
 - They are used in authentication
 - They are used in communications protocols

Message Digests

- Modern hash functions meet two criteria:
 - They are one-way, meaning they convert input to a digest, but it is infeasible to start with a digest value and infer the input
 - They do not have obvious collisions, meaning that it is infeasible to find a pair of inputs that produce the same digest

Properties of Current Hash Standards

Algorithm	Maximum Message Size (bits)	Block Size (bits)	Rounds	Message Digest Size (bits)
MD5	2^{64}	512	64	128
SHA-1	2^{64}	512	80	160
SHA-2-224	2^{64}	512	64	224
SHA-2-256	2^{64}	512	64	256
SHA-2-384	2^{128}	1024	80	384
SHA-2-512	2^{128}	1024	80	512
SHA-3-256	unlimited	1088	24	256
SHA-3-512	unlimited	576	24	512

Digital Signatures

- Digital signatures must meet two requirements:
 - *Unforgeable (mandatory)*: No one other than the signer can produce the signature without the signer's private key
 - *Authentic (mandatory)*: The receiver can determine that the signature really came from the signer

Digital Signatures

- Digital signatures ideally satisfy two other requirements:
 - *Not alterable (desirable)*: No signer, receiver, or any interceptor can modify the signature without the tampering being evident
 - *Not reusable (desirable)*: Any attempt to reuse a previous signature will be detected by receiver

Digital Signatures

- The general way of computing digital signatures is with public key encryption:
 - The signer computes a signature value by using a private key
 - Others can use the public key to verify that the signature came from the corresponding private key

Elliptic Curve Cryptosystems (ECC)

- While the RSA algorithm appears sufficiently strong, it has a different kind of flaw: It is patented
- An alternative form of asymmetric cryptography comes in the form of ECC
- ECC has two advantages over RSA:
 - While some technologies using ECC are patented, the general algorithm is in the public domain
 - ECC can provide similar security to RSA
 - using a shorter key length

Elliptic Curve Cryptosystems (ECC)

- ECC use very complex math
- Elliptic curve cryptography is seldom used by itself for public key encryption.
- However, it is often used as a component in digital signatures

Elliptic Curve Cryptosystems (ECC)

- In 2005 the NSA recommended set of advanced cryptography algorithms known as Suite B.
- The protocols included in Suite B are:
 - Elliptic Curve DiffieHellman (ECDH) and Elliptic Curve Menezes-Qu-Vanstone (ECMQV) for **key exchange**
 - The Elliptic Curve Digital Signature Algorithm (ECDSA) for **digital signatures**
 - AES for **symmetric encryption**
- Provides strong security, efficiency, and scalability
 - Over public-key cryptography algorithms.

Quantum Cryptography

- Based on physics, not mathematics, using light particles called photons
- It relies on our ability to measure certain properties of photons and on Heisenberg's uncertainty principle
 - Which allows senders and receivers in quantum communication to easily detect eavesdroppers

Quantum Cryptography

- Implementations of quantum cryptography remain in the prototype stage
 - creating practical photon guns and receivers is technically difficult
- While still not ready for widespread adoption, quantum cryptography may be practical within the next decade
 - would likely be a significant improvement over existing systems for encrypted communication

Quantum Cryptography

- Quantum Cryptography

Summary

- Substitution, transposition, confusion, and diffusion are the basic primitives of cryptography
- DES is a relatively simple symmetric algorithm that, although no longer practical, is useful for studying technique
- Chaining and random initialization vectors are important techniques for preventing ciphertext repetition
- AES remains the modern standard for symmetric encryption almost 20 years after its introduction

Summary

- RSA is a popular and deceptively simple algorithm for asymmetric cryptography
- Message digests use one-way cryptographic hash functions to detect message modification
- Digital signatures use asymmetric encryption to detect forged messages
- While not yet ready for mainstream use, quantum cryptography will likely be a significant improvement over modern encrypted communication

Questions?

