



Computer Vision

Ch (part 2): Object recognition

Contents

- Overview of ‘semantic vision’?
- Image classification/ recognition
- Bag-of-words
 - Recall
 - Vocabulary tree
- Classification
 - K nearest neighbors
 - Naïve Bayes
 - Support vector machine (previous lecture)



Overview of 'semantic vision'?



SCHOOL OF INFORMATION AND COMMUNICATION TECHNOLOGY

3

**Is this a street light?
(Recognition / classification)**



4

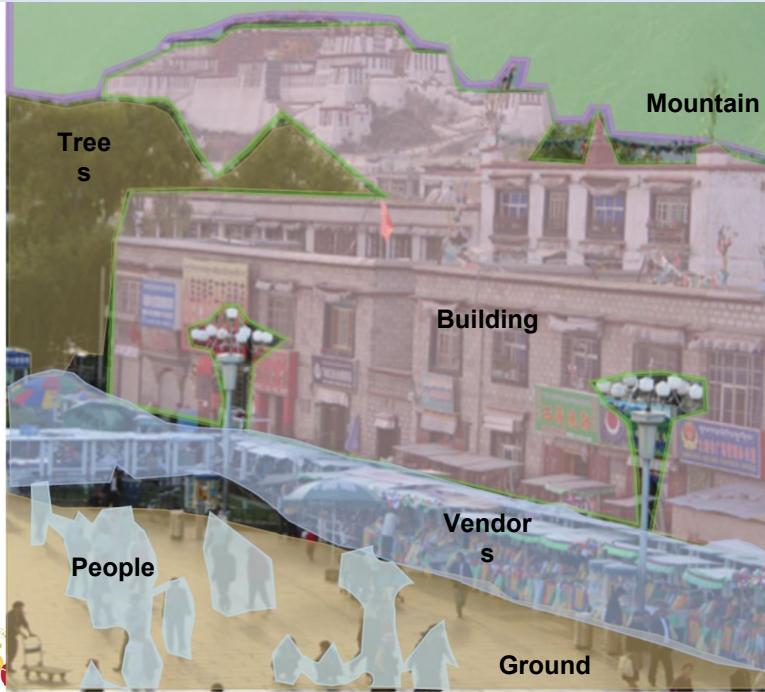
Where are the people? (Detection)



Is that Potala palace? (Identification)

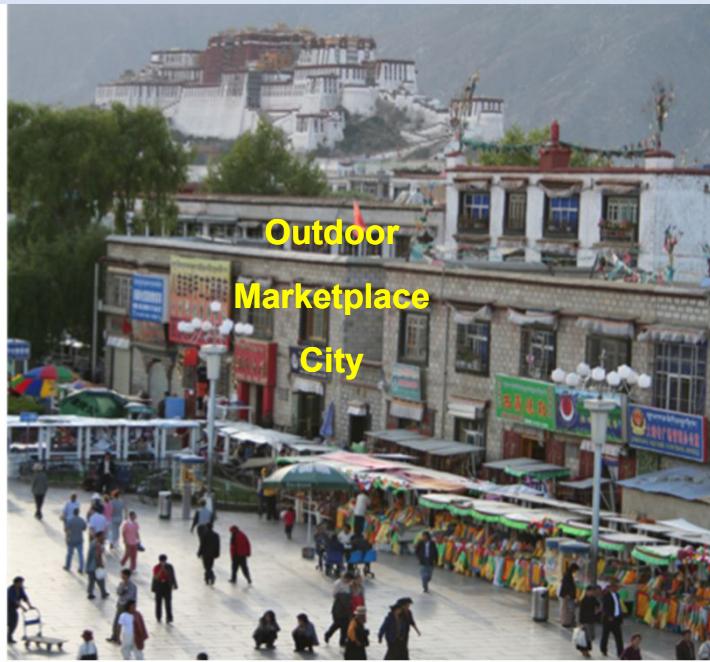


What's in the scene? (semantic segmentation)



7

What type of scene is it? (Scene categorization)



8

What are these people doing? (Activity / Event Recognition)



SCHOOL OF INFORMATION AND COMMUNICATION TECHNOLOGY

9

Object recognition Is it really so hard?

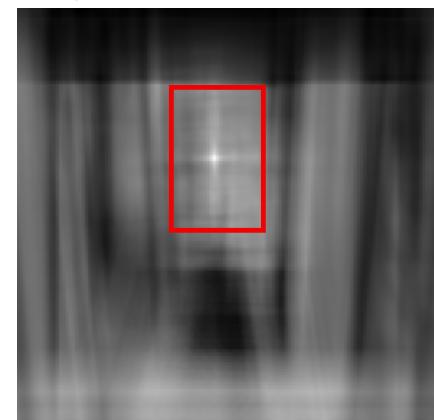
This is a chair



Find the chair in this image



Output of normalized correlation



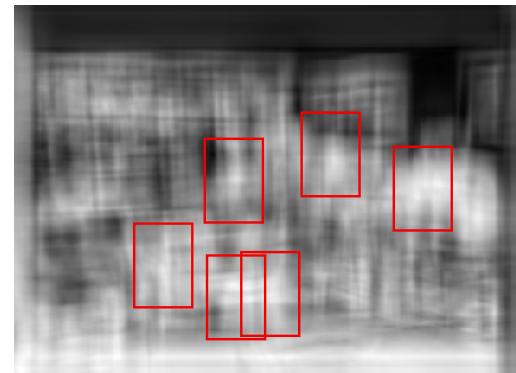
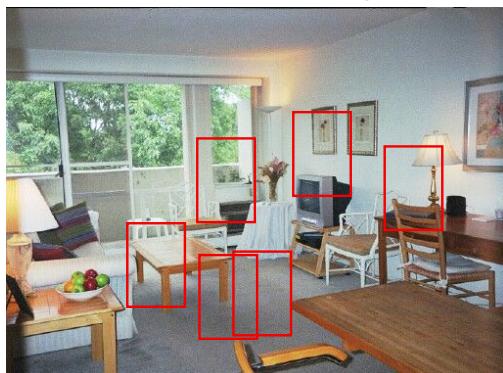
SCHOOL OF INFORMATION AND COMMUNICATION TECHNOLOGY

10

Object recognition Is it really so hard?



Find the chair in this image



Pretty much garbage

Simple template matching is not going to make it

A “popular method is that of template matching, by point to point correlation of a model pattern with the image pattern. These techniques are inadequate for three-dimensional scene analysis for many reasons, such as occlusion, changes in viewing angle, and articulation of parts.” Nivat & Binford, 1977



SCHOOL OF INFORMATION AND COMMUNICATION TECHNOLOGY

11

And it can get a lot harder



Brady, M. J., & Kersten, D. (2003). Bootstrapped learning of novel objects. *J Vis*, 3(6), 413-422

SCHOOL OF INFORMATION AND COMMUNICATION TECHNOLOGY

12

Why is this hard?

Variability: Camera position
Illumination
Shape parameters

 SCHOOL OF INFORMATION AND COMMUNICATION TECHNOLOGY

13



Challenge: variable viewpoint



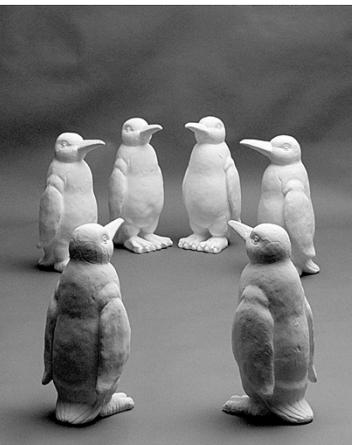
Michelangelo 1475-1564



SCHOOL OF INFORMATION AND

15

Challenge: variable illumination



SCHOOL OF INFORMATION AND COMMUNICATION TECHNOLOGY

image credit: J. Koenderink

16

Challenge: scale

and small things
from Apple.
(Actual size)



SOICT SCHOOL OF INFORMATION AND COMMUNICATION TECHNOLOGY

17

Challenge: deformation

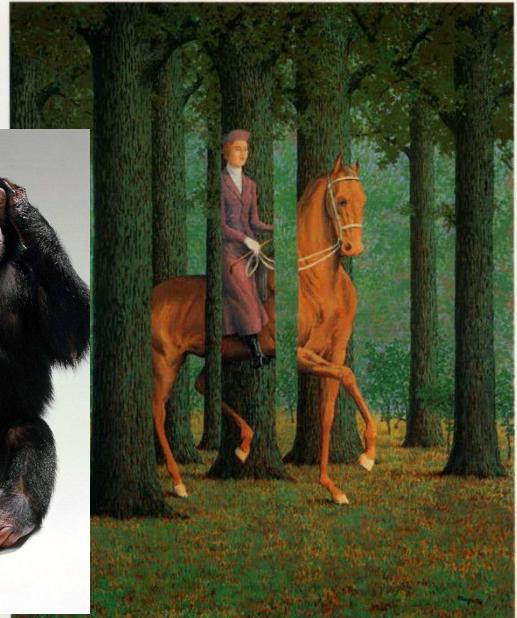
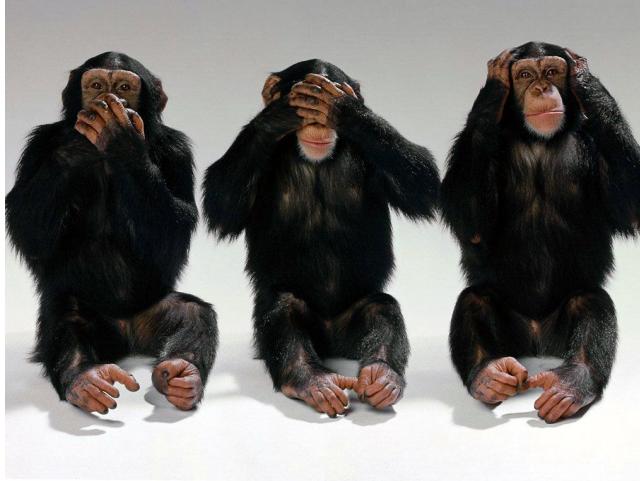




SOICT SCHOOL OF INFORMATION AND COMMUNICATION TECHNOLOGY

18

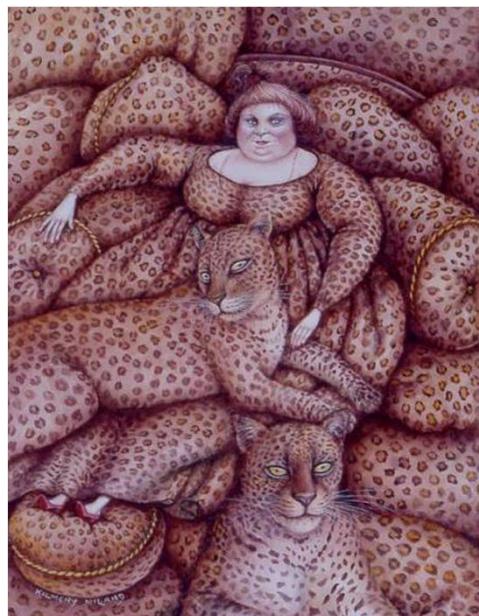
Challenge: Occlusion



Magritte, 1957

19

Challenge: background clutter



Kilmeny Niland. 1995

20



Challenge: intra-class variations



Image Classification/ Recognition



SCHOOL OF INFORMATION AND COMMUNICATION TECHNOLOGY

23

Image Classification/ Recognition



(assume given set of discrete labels)
{dog, cat, truck, plane, ...}

→ cat



SCHOOL OF INFORMATION AND COMMUNICATION TECHNOLOGY

24

Image Classification: Problem



08	02	22	97	38	15	00	40	00	75	04	05	07	78	52	12	50	77	73
49	99	40	17	81	18	57	60	87	17	40	98	43	69	91	56	62	00	
81	49	31	73	55	79	14	29	93	71	40	67	11	88	30	03	49	13	65
52	70	95	23	04	60	11	42	83	55	56	01	32	56	71	37	02	36	91
22	31	16	71	51	57	10	89	41	92	36	54	22	40	40	28	66	33	13
24	47	34	10	99	03	45	02	44	75	33	53	78	36	84	20	35	17	12
32	98	81	28	64	23	67	10	26	38	40	67	59	54	70	66	18	38	64
70	26	20	68	02	62	12	20	95	63	94	39	63	08	40	91	66	49	94
24	55	58	05	66	73	99	26	97	17	78	78	96	83	14	88	34	89	63
21	36	23	09	75	00	76	42	20	45	35	14	00	61	33	97	34	31	33
78	17	53	28	22	75	31	67	15	94	03	80	04	42	16	14	09	53	92
16	39	05	42	96	35	31	47	55	58	88	24	00	17	54	24	36	29	85
86	56	00	48	35	71	89	07	05	44	44	37	44	60	21	58	51	54	17
19	80	81	68	05	94	47	69	28	73	92	19	86	52	17	77	04	89	55
04	52	08	63	97	35	99	16	07	97	57	32	16	26	26	79	33	27	98
04	42	16	73	35	10	11	24	94	72	18	08	46	29	32	40	62	76	36
20	69	36	41	72	30	23	88	31	39	69	82	67	59	85	74	04	36	16
20	73	35	29	78	31	90	01	74	31	49	71	48	84	01	16	23	57	05
01	70	54	71	83	51	54	69	16	92	33	45	61	43	52	01	89	19	48

What the computer sees

image classification →
 82% cat
 15% dog
 2% hat
 1% mug



SCHOOL OF INFORMATION AND COMMUNICATION TECHNOLOGY

25

Data-driven approach

- Collect a database of images with labels
- Use ML to train an image classifier
- Evaluate the classifier on test images

Example training set



SCHOOL OF INFORMATION AND COMMUNICATION TECHNOLOGY

26

A simple pipeline - Training

Training
Images



Image
Features

A simple pipeline - Training

Training
Images

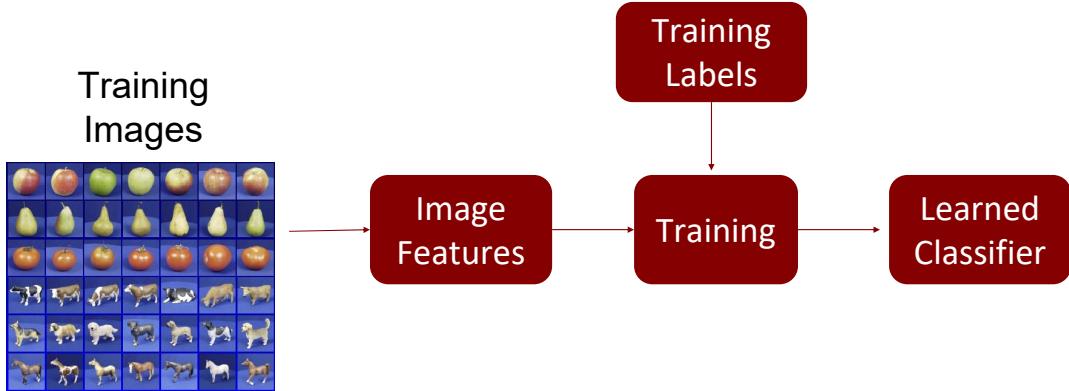


Image
Features

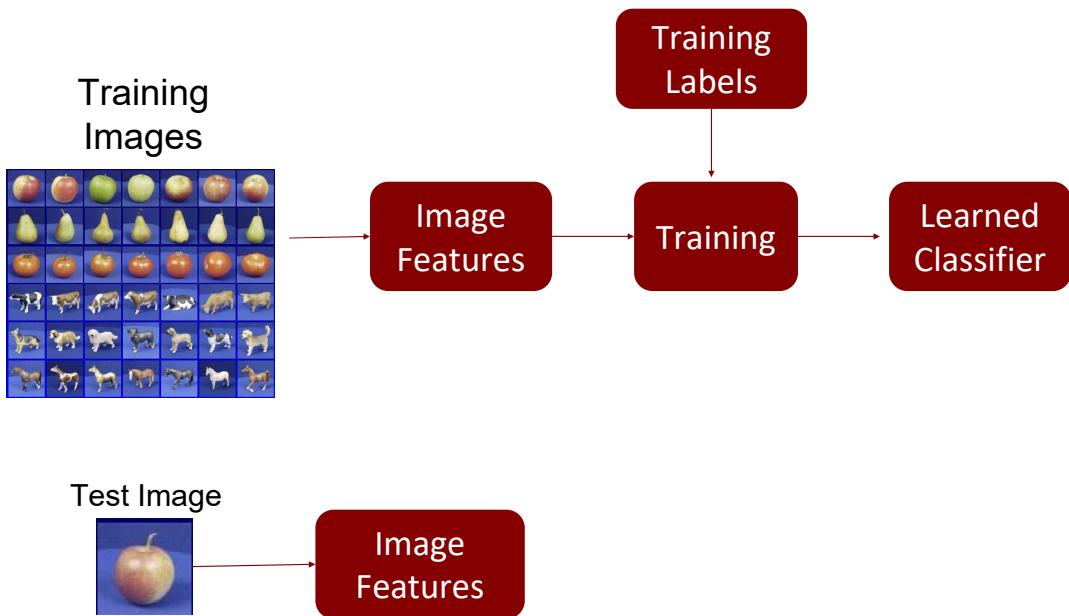
Training
Labels

Training

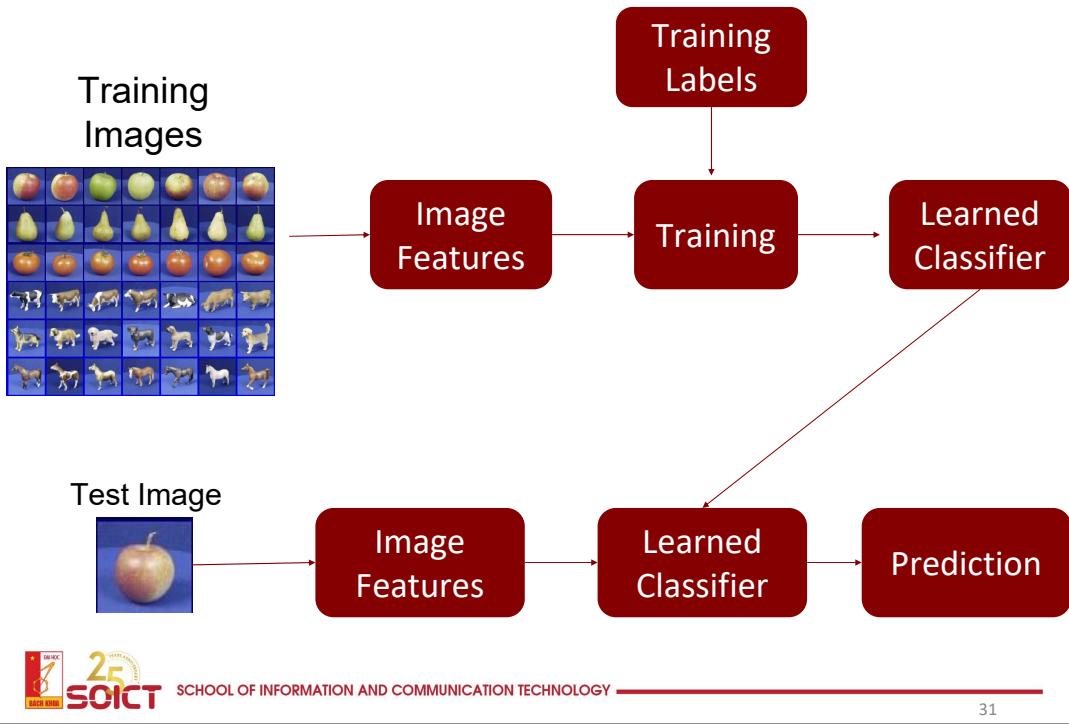
A simple pipeline - Training



A simple pipeline - Training



A simple pipeline - Training

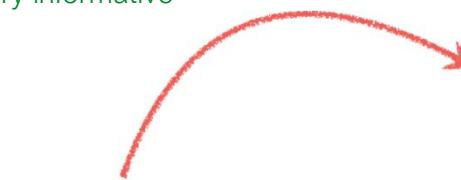
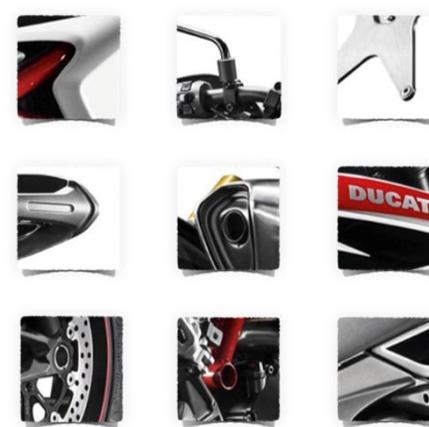


Bag of words

Basic model: recall
Vocabulary tree

Some local feature are very informative

An object as

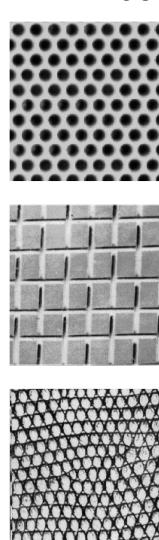
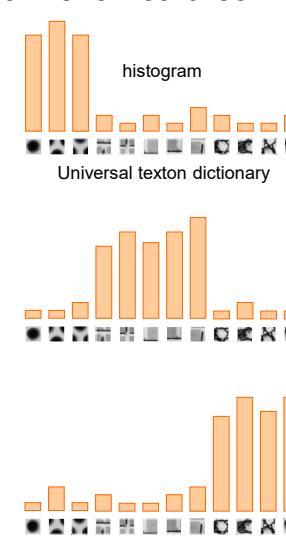
a collection of local features (bag-of-features)

- deals well with occlusion
- scale invariant
- rotation invariant

33

Bag-of-features

represent a data item (document, texture, image) as a histogram over features

25 SOICT SCHOOL OF INFORMATION AND COMMUNICATION TECHNOLOGY

34

Standard BOW pipeline

(for image classification)



SCHOOL OF INFORMATION AND COMMUNICATION TECHNOLOGY

35

Dictionary Learning:

Learn Visual Words using clustering

Encode:

build Bags-of-Words (BOW) vectors
for each image

Classify:

Train and test data using BOWs



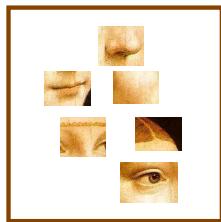
SCHOOL OF INFORMATION AND COMMUNICATION TECHNOLOGY

36

Dictionary Learning:

Learn Visual Words using clustering

1. extract features (e.g., SIFT) from images



Dictionary Learning:

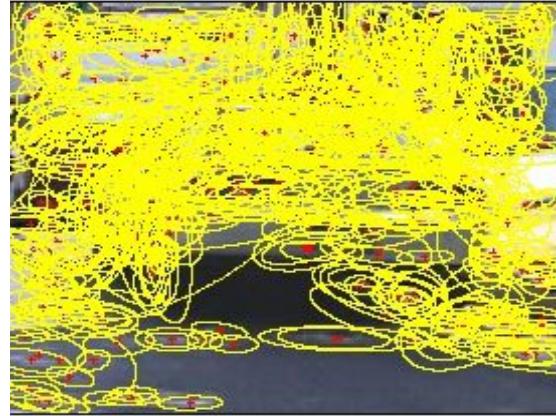
Learn Visual Words using clustering

2. Learn visual dictionary (e.g., K-means clustering)

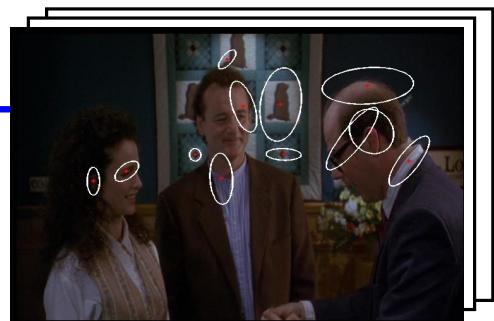


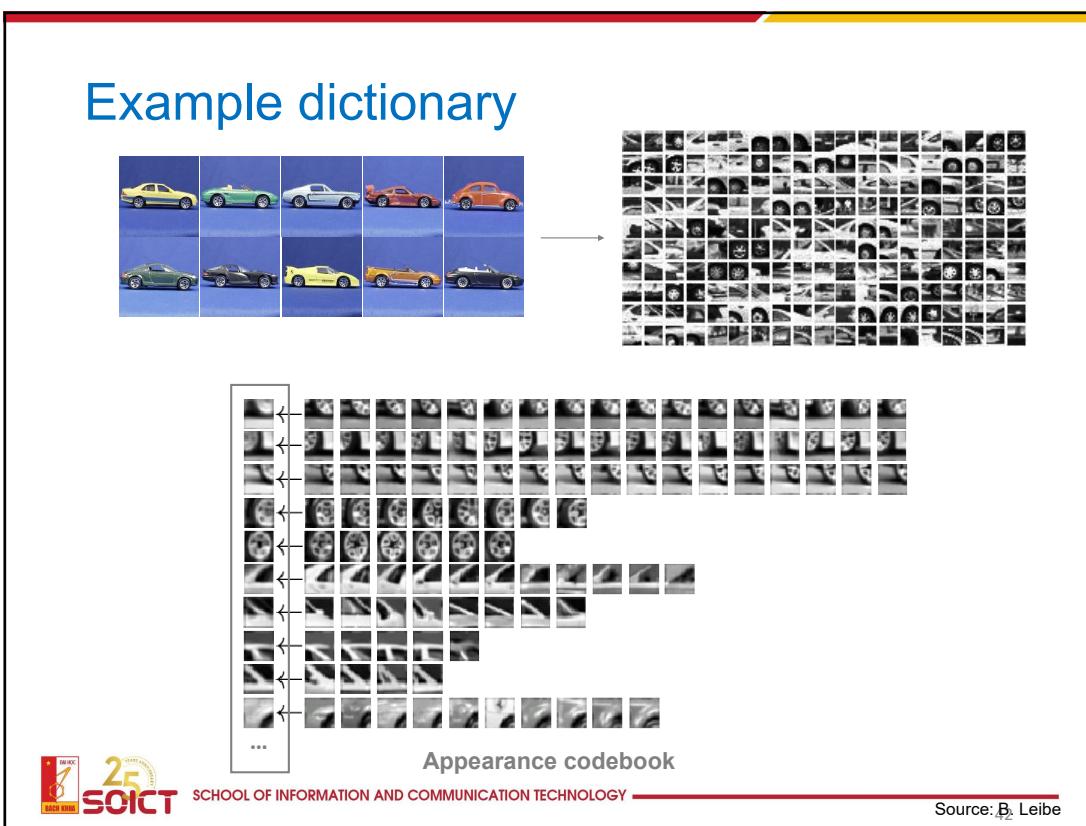
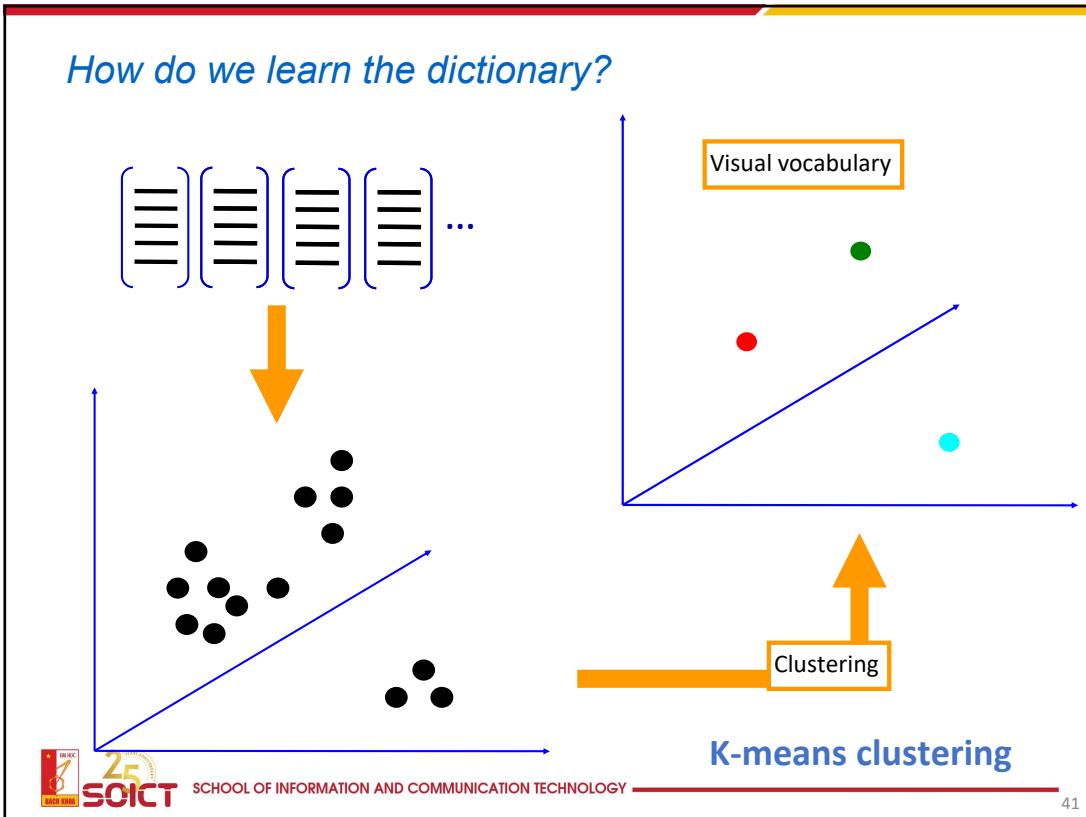
What kinds of features can we extract?

- Regular grid
 - Vogel & Schiele, 2003
 - Fei-Fei & Perona, 2005
- Interest point detector
 - Csurka et al. 2004
 - Fei-Fei & Perona, 2005
 - Sivic et al. 2005
- Other methods
 - Random sampling (Vidal-Naquet & Ullman, 2002)
 - Segmentation-based patches (Barnard et al. 2003)



$$\left[\begin{array}{c} \parallel \\ \parallel \\ \parallel \\ \parallel \end{array} \right] \left[\begin{array}{c} \parallel \\ \parallel \\ \parallel \\ \parallel \end{array} \right] \left[\begin{array}{c} \parallel \\ \parallel \\ \parallel \\ \parallel \end{array} \right] \left[\begin{array}{c} \parallel \\ \parallel \\ \parallel \\ \parallel \end{array} \right] \dots$$





Dictionary Learning:

Learn Visual Words using clustering

Encode:

build Bags-of-Words (BOW) vectors
for each image

Classify:

Train and test data using BOWs



1. Quantization: image features gets associated to a visual word (nearest cluster center)

Encode:

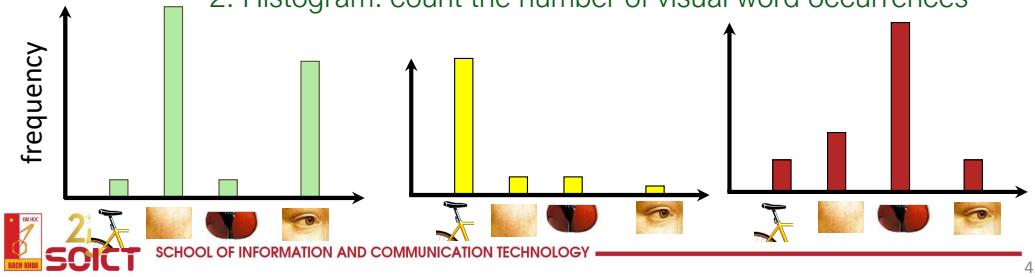
build Bags-of-Words (BOW) vectors
for each image



Encode:

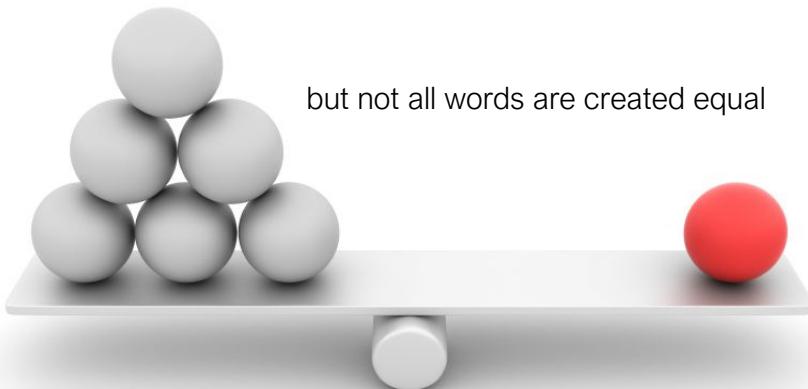
build Bags-of-Words (BOW) vectors
for each image

2. Histogram: count the number of visual word occurrences



45

but not all words are created equal



TF-IDF

Term Frequency Inverse Document Frequency

$$\mathbf{v}_d = [n(w_{1,d}) \ n(w_{2,d}) \ \cdots \ n(w_{T,d})]$$

weigh each word by a heuristic

$$\mathbf{v}_d = [n(w_{1,d})\alpha_1 \ n(w_{2,d})\alpha_2 \ \cdots \ n(w_{T,d})\alpha_T]$$

$$n(w_{i,d})\alpha_i = n(w_{i,d}) \log \left\{ \frac{D}{\sum_{d'} \mathbf{1}[w_i \in d']} \right\}$$

term frequency inverse document frequency

(down-weights **common** terms)



SCHOOL OF INFORMATION AND COMMUNICATION TECHNOLOGY

47

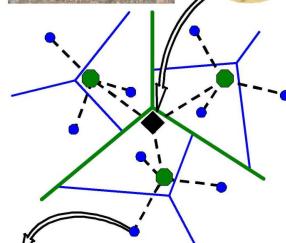
Scalability: Alignment to large databases

- What if we need to align a test image with thousands or millions of images in a model database?
 - Efficient putative match generation
 - Fast nearest neighbor search, inverted indexes

Test image



Vocabulary tree with inverted index



Database



D. Nistér and H. Stewénius, [Scalable Recognition with a Vocabulary Tree](#),
CVPR 2006



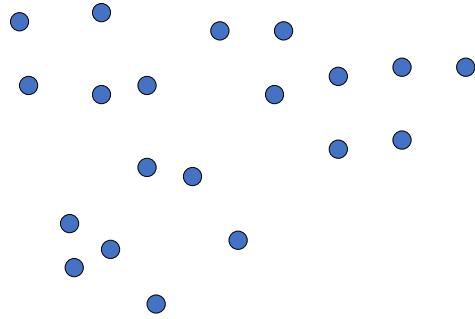
SCHOOL OF II

slide: S. Lazebnik

48

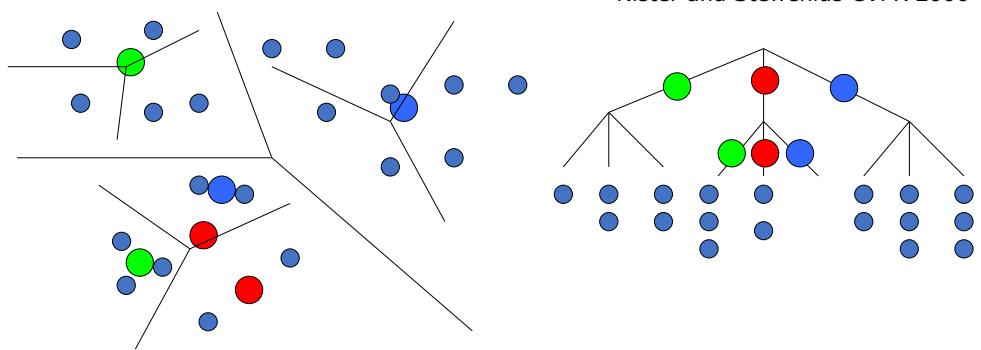
What is a Vocabulary Tree?

Nister and Stewenius CVPR 2006

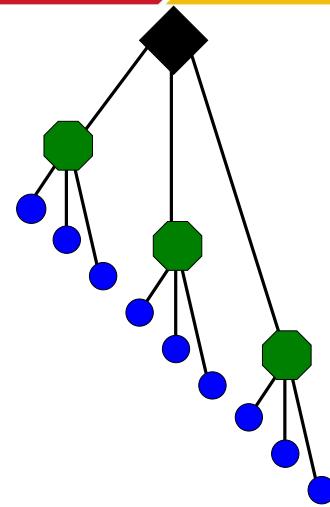


What is a Vocabulary Tree?

Nister and Stewenius CVPR 2006

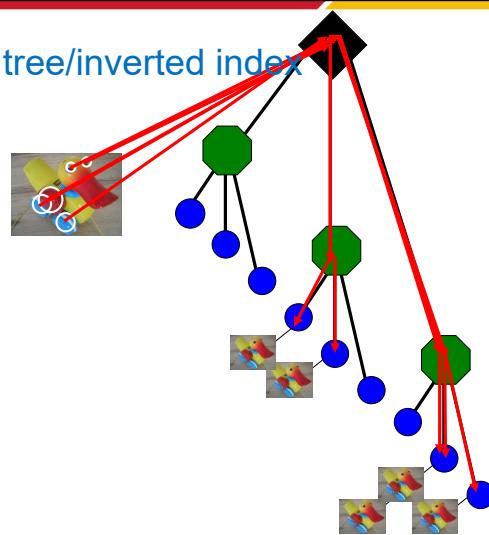


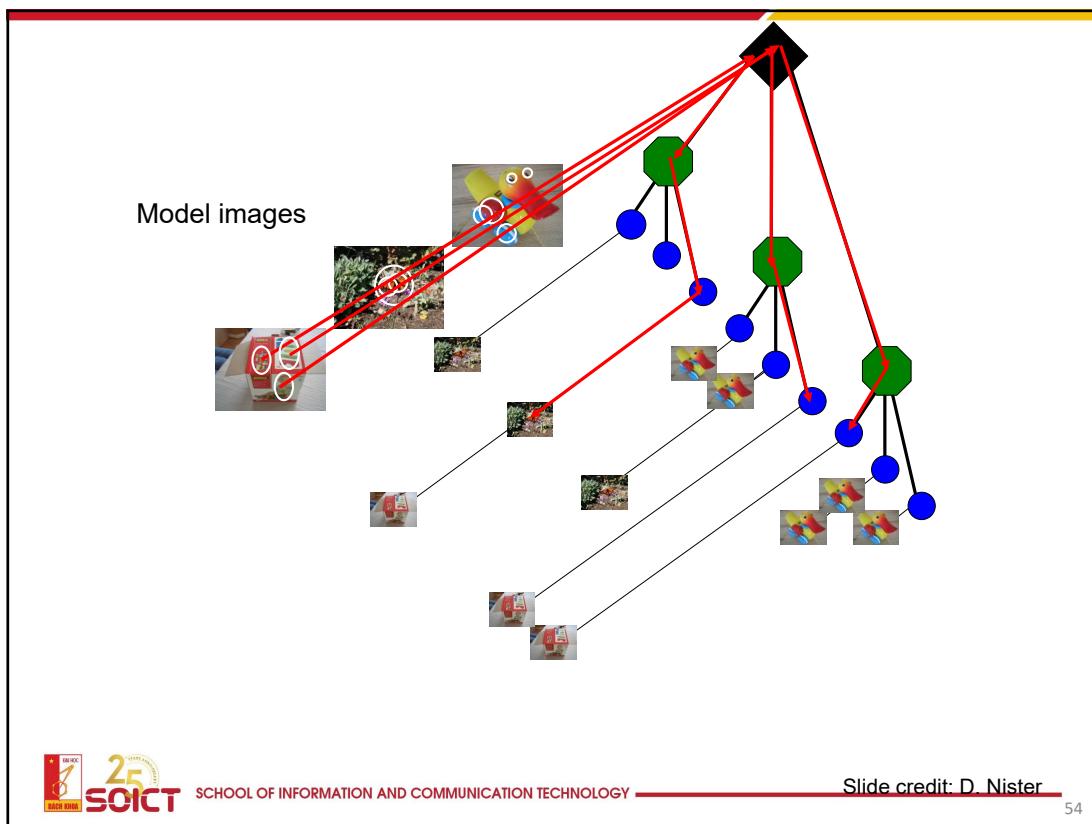
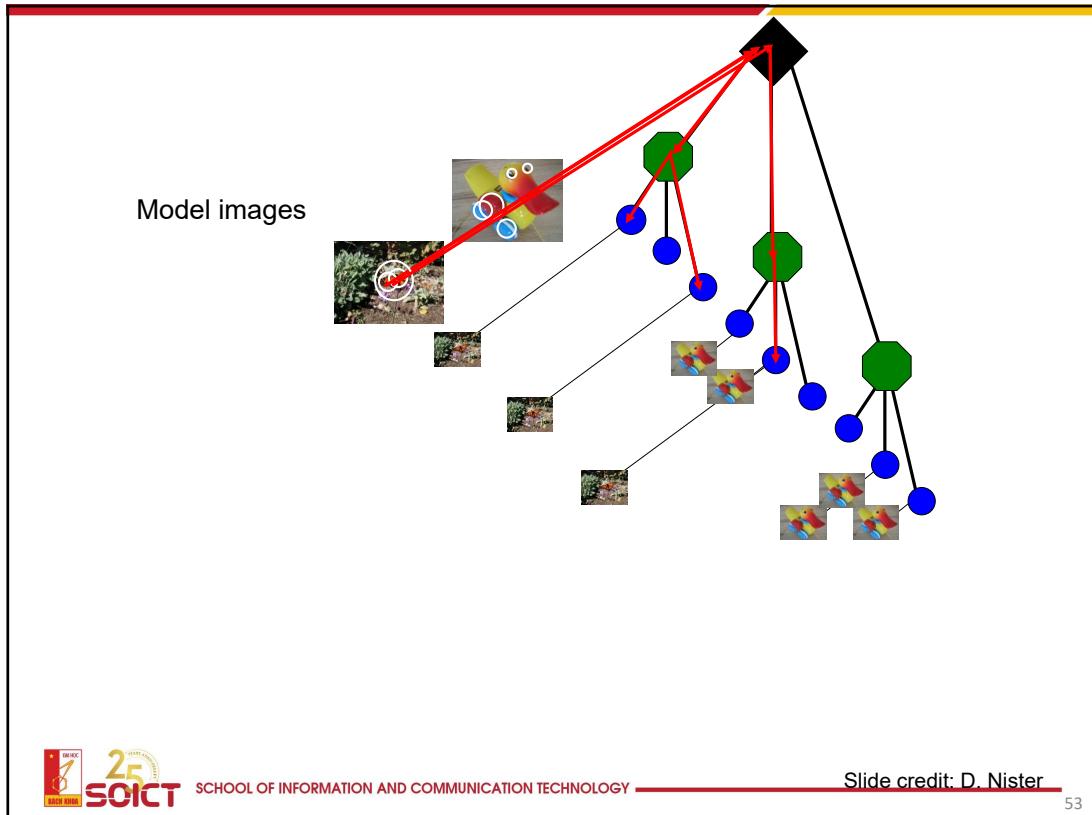
- Multiple rounds of K-Means to compute decision tree (offline)
- Fill and query tree online

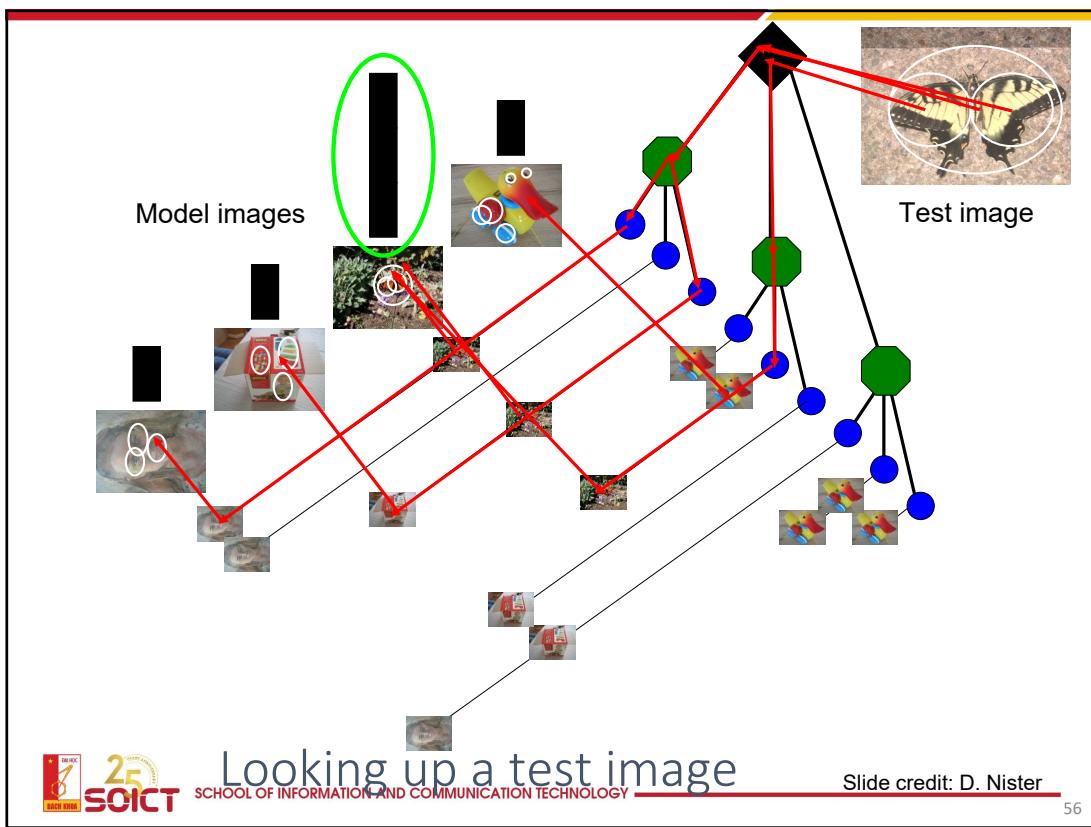
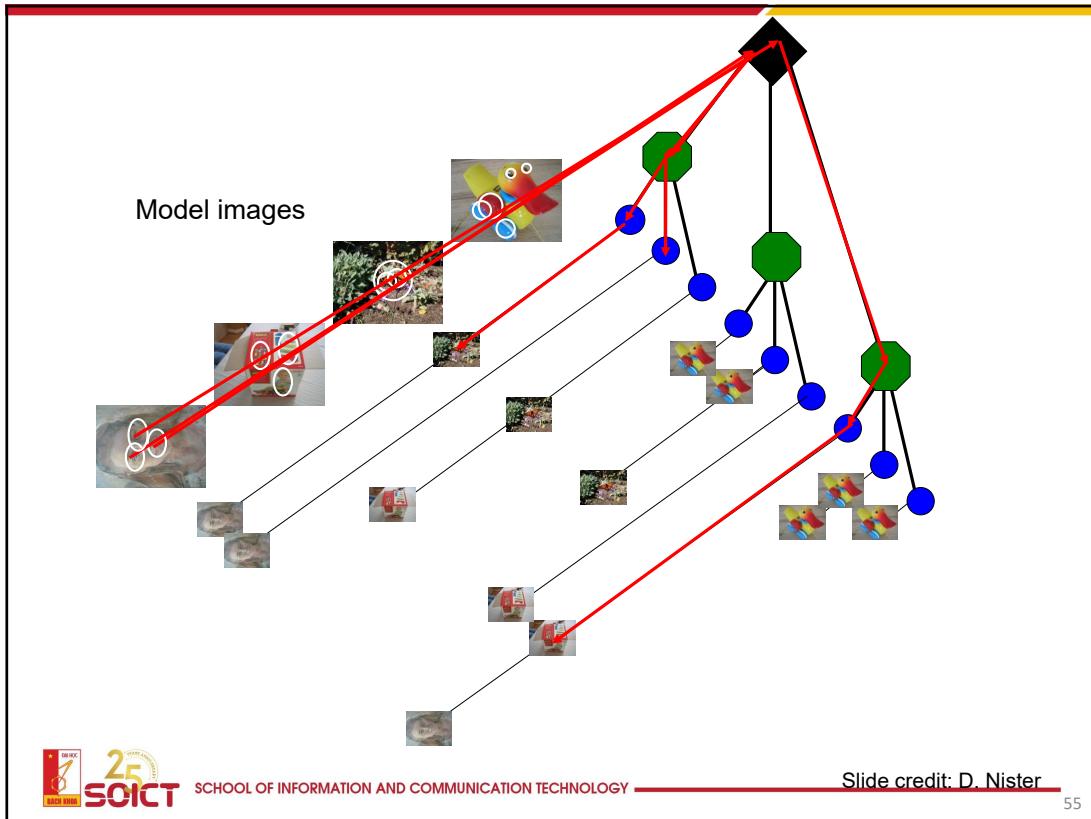


Populating the vocabulary tree/inverted index

Model images





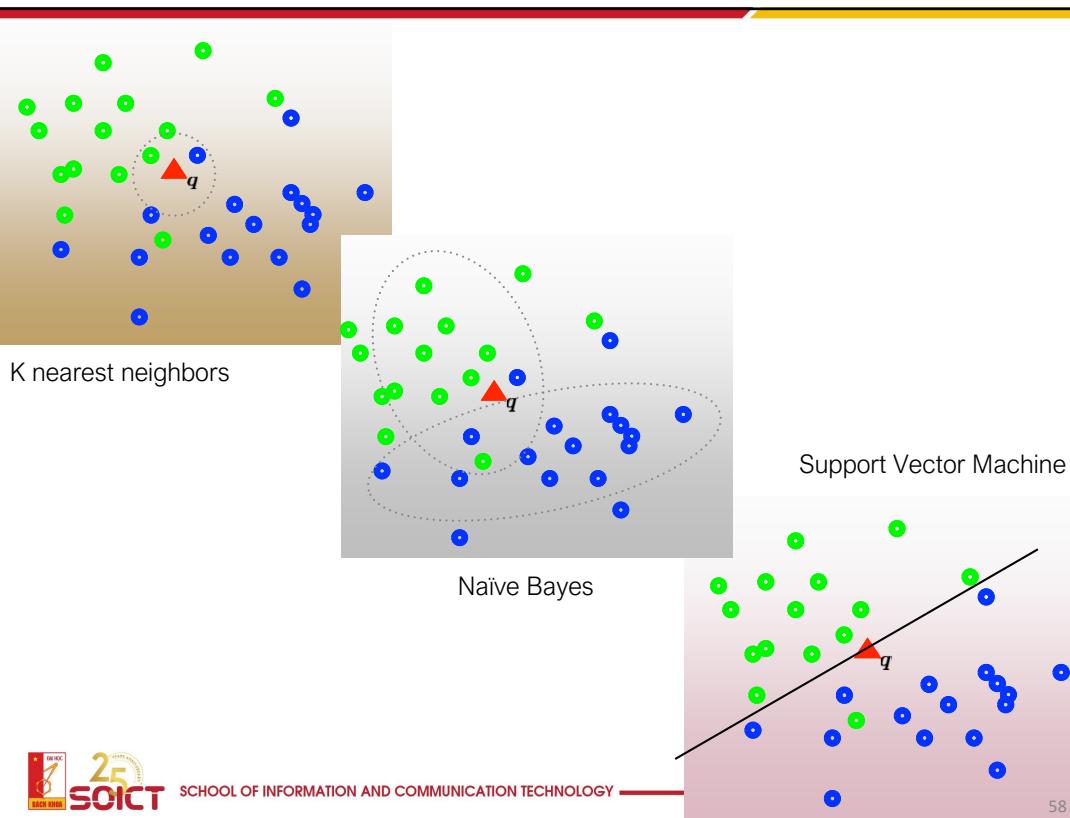


Dictionary Learning:

Learn Visual Words using clustering

Encode:
build Bags-of-Words (BOW) vectors
for each image

Classify:
Train and test data using BOWs



Classification



SCHOOL OF INFORMATION AND COMMUNICATION TECHNOLOGY

59

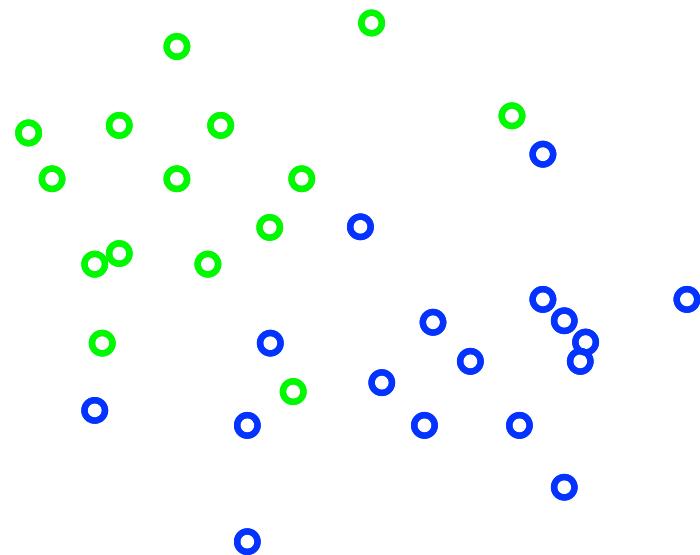
K nearest neighbors



SCHOOL OF INFORMATION AND COMMUNICATION TECHNOLOGY

60

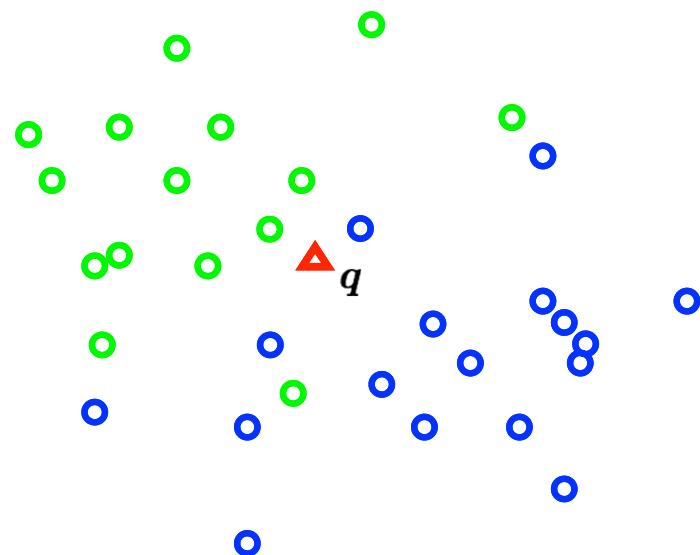
Distribution of data from two classes



SCHOOL OF INFORMATION AND COMMUNICATION TECHNOLOGY

61

Distribution of data from two classes

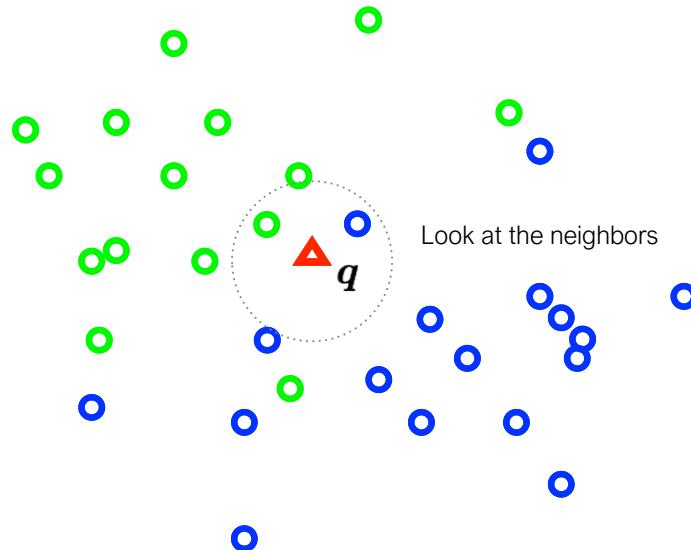


SCHOOL OF INFORMATION AND COMMUNICATION TECHNOLOGY

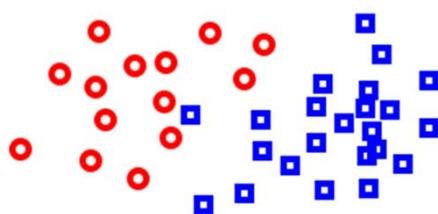
62

Which class does q belong to?

Distribution of data from two classes



K-Nearest Neighbor (KNN) Classifier

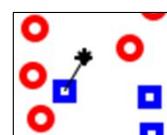


Non-parametric pattern classification approach

Consider a two class problem where each sample consists of two measurements (x,y).

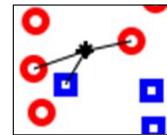
For a given query point q, assign the class of **the nearest neighbor**

$k = 1$



Compute the **k nearest neighbors** and assign the class by majority vote.

$k = 3$



Nearest Neighbor is competitive

0 0 2 9 1 5 0 8 8 0 3 2 7 7 2 6 4 9 5 5 7 2 9 2 8 2 6 8 6 5 0 0 8 7 6 / 7 1 1 2 7 4 0 0 7 2 6 3 8 6 4 2 0 1 4 0 5 7 8 2 1 4 7 1 1 3 6 6
 8 0 7 1 1 / 6 2 6 2 9 6 6 4 1 4 3 1 / 1 2 2 4 1 0 8 2 6 3 4 0 0 6 2 3 0 1 7 1 1 1 3 1 0 9 9 7 5 4 1 4 8 9 5 3 5 1 9 8 2 2 3 9 9 0 1 0 2 9
 8 4 6 8 8 2 4 6 2 9 3 3 4 3 1 / 1 4 7 0 5 9 6 0 4 4 6 1 2 3 2 6 4 / 9 6 8 5 6 0 6 4 / 3 6 5 2 1 4 5 5 4 7 7 0 7 8 2 2 3 7 0 1 8
 7 6 9 5 3 4 6 5 0 / 8 8 2 8 3 5 7 8 0 8 5 7 1 / 0 0 7 8 3 3 3 1 3 7 8 5 0 7 1 0 1 4 5 2 7 6 2 3 0 2 0 5 9 6 9 7 2 1 3 6 4 1 8 2 4 0 5 1 0 2 2 6
 9 3 7 7 1 4 0 6 1 8 4 2 7 0 2 8 / 0 0 7 8 3 3 3 1 3 7 6 1 3 1 6 0 5 7 4 7 5 8 5 4 9 9 1 5 0 1 3 2 0 3 4 8 2 2 0 2 5 5 1 4 8 8 9
 8 2 0 4 9 6 2 3 3 1 6 4 8 0 9 2 8 3 6 7 5 7 2 9 4 9 2 8 6 0 7 0 9 / 6 7 5 9 1 4 6 9 2 5 0 4 1 0 8 4 0 8 9 8 9 4 2 5 7 1 9 8 9 8 0
 3 5 5 1 7 2 1 6 9 / 9 5 5 1 6 2 8 6 7 1 4 6 0 4 0 3 3 2 7 3 6 8 9 2 5 3 9 5 4 5 2 0 5 6 3 2 8 3 9 4 5 1 0 8 6 7 3 1 3 6 6 0 9 0 /
 9 1 8 2 6 8 1 0 4 1 3 1 7 5 9 5 0 1 0 1 1 1 6 2 9 8 4 0 3 6 4 9 0 7 1 6 5 7 5 2 5 1 8 5 4 7 0 6 7 0 2 5 8 1 0 4 5 7 1 8 5 1 9 0 0 6 0 7
 8 8 5 7 3 8 9 8 8 6 8 2 3 9 7 5 6 2 9 2 8 8 1 0 7 2 0 7 5 1 9 0 2 0 9 8 6 2 3 9 3 8 0 2 1 1 4 2 9 7 4 5 / 1 2 1 9 9
 1 4 8 5 3 4 3 1 7 7 5 0 7 4 8 8 1 5 3 9 5 9 3 6 9 0 3 6 3 9 8 2 7 1 2 8 6 8 5 3 3 9 4 4 2 5 5 1 4 4 3 5 1 2 2 3 3 0 2 1 0 0 9
 2 3 7 9 0 9 7 5 4 1 2 0 1 0 5 1 4 9 3 6 1 5 2 5 0 2 6 0 0 2 6 6 0 1 2 8 7 9 8 2 0 4 7 7 5 0 5 6 4 6 7 4 3 0 7 5 0 7 4 2 0 8 1 9 4 0 4
 6 9 2 8 5 4 5 7 9 4 9 2 1 6 3 4 0 7 8 3 9 3 6 6 5 6 2 1 9 2 6 0 0 6 1 2 8 7 9 8 2 0 4 7 7 5 0 5 6 4 6 7 4 3 0 7 5 0 7 4 2 0 8 1 9 4 0 4
 1 2 8 4 5 2 7 8 1 1 3 0 3 5 7 0 3 1 9 3 6 3 1 7 7 3 0 8 4 8 2 2 6 5 2 9 4 3 9 0 9 1 6 4 2 9 2 1 1 6 7 4 7 5 9 6 8 2 1 4 4 5 1 6 1 3 2 5
 9 0 6 6 2 3 6 7 2 2 8 6 0 8 3 0 2 9 8 3 2 5 3 9 8 0 0 1 9 5 1 3 9 6 0 1 4 1 7 1 2 3 7 9 3 4 9 3 9 2 8 1 7 1 8 0 9 1 0 1 7 7 9 6 9 9 9
 2 1 0 1 0 4 5 2 8 2 8 3 5 1 7 7 1 2 1 7 8 4 0 5 7 6 8 4 7 8 5 8 4 9 8 1 3 8 0 3 1 7 7 5 6 1 6 5 7 4 9 3 5 4 7 1 2 0 8 1 6 0 7 3 4
 2 8 3 0 8 7 8 6 0 8 4 4 5 8 5 6 6 3 0 9 3 2 6 8 9 3 4 9 5 8 9 1 2 8 8 6 8 1 3 7 9 0 1 1 4 7 0 9 1 7 4 5 7 1 2 1 1 3 9 6 2 1 2 6 0 7 6 6
 4 1 9 2 2 8 0 1 3 6 1 3 4 1 1 1 5 6 0 7 0 7 2 3 2 5 2 2 9 4 9 8 1 0 / 6 1 2 7 4 0 0 8 2 2 7 2 7 4 9 2 7 5 1 3 4 9 4 1 7 5 6 2 8 3

Test Error Rate (%)

Linear classifier (1-layer NN)	12.0
K-nearest-neighbors, Euclidean	5.0
K-nearest-neighbors, Euclidean, deskewed	2.4
K-NN, Tangent Distance, 16x16	1.1
K-NN, shape context matching	0.67
1000 RBF + linear classifier	3.6
SVM deg 4 polynomial	1.1
2-layer NN, 300 hidden units	4.7
2-layer NN, 300 HU, [deskewing]	1.6
LeNet-5, [distortions]	0.8
Boosted LeNet-4, [distortions]	0.7

MNIST Digit Recognition

- Handwritten digits
 - 28x28 pixel images: $d = 784$
 - 60,000 training samples
 - 10,000 test samples
- Yann LeCunn



SCHOOL OF INFORMATION AND COMMUNICATION TECHNOLOGY

65

What is the best distance metric between data points?

- Typically Euclidean distance
- Locality sensitive distance metrics
- Important to normalize.
Dimensions have different scales

How many K?

- Typically $k=1$ is good
- Cross-validation (try different k !)



SCHOOL OF INFORMATION AND COMMUNICATION TECHNOLOGY

66

Distance metrics

$$D(\mathbf{x}, \mathbf{y}) = \sqrt{(x_1 - y_1)^2 + \cdots + (x_N - y_N)^2} \quad \text{Euclidean}$$

$$D(\mathbf{x}, \mathbf{y}) = \frac{\mathbf{x} \cdot \mathbf{y}}{\|\mathbf{x}\| \|\mathbf{y}\|} = \frac{x_1 y_1 + \cdots + x_N y_N}{\sqrt{\sum_n x_n^2} \sqrt{\sum_n y_n^2}} \quad \text{Cosine}$$

$$D(\mathbf{x}, \mathbf{y}) = \frac{1}{2} \sum_n \frac{(x_n - y_n)^2}{(x_n + y_n)} \quad \text{Chi-squared}$$

Distance metrics

L1 (Manhattan) distance

$$d_1(I_1, I_2) = \sum_p |I_1^p - I_2^p|$$

L2 (Euclidean) distance

$$d_2(I_1, I_2) = \sqrt{\sum_p (I_1^p - I_2^p)^2}$$

- Two most commonly used special cases of p -norm

$$\|\mathbf{x}\|_p = \left(|x_1|^p + \cdots + |x_n|^p \right)^{\frac{1}{p}} \quad p \geq 1, \mathbf{x} \in \mathbb{R}^n$$

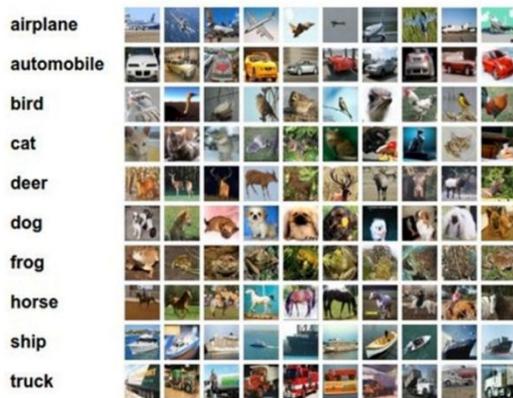
CIFAR-10 and NN results

Example dataset: **CIFAR-10**

10 labels

50,000 training images

10,000 test images.



For every test image (first column),
examples of nearest neighbors in rows

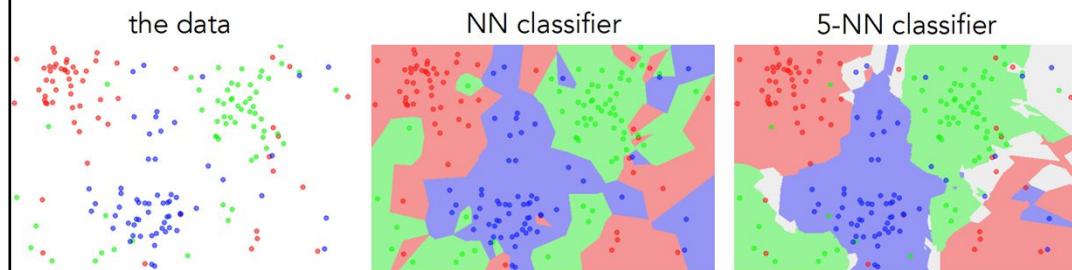


SCHOOL OF INFORMATION AND COMMUNICATION TECHNOLOGY

70

k-nearest neighbor

- Find the k closest points from training data
- Labels of the k **points** “**vote**” to classify



SCHOOL OF INFORMATION AND COMMUNICATION TECHNOLOGY

71

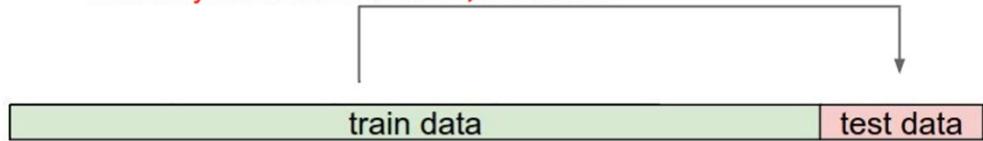
Hyperparameters

- What is the best distance to use?
- What is the best value of k to use?
- i.e., how do we set the hyperparameters?
- Very problem-dependent
- Must try them all and see what works best

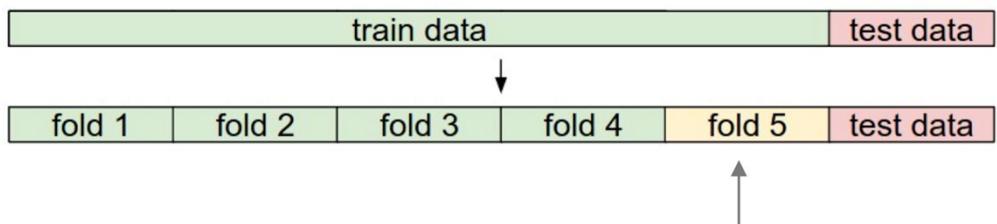
Try out what hyperparameters work best on test set.



Trying out what hyperparameters work best on test set:
Very bad idea. The test set is a proxy for the generalization performance!
 Use only **VERY SPARINGLY**, at the end.

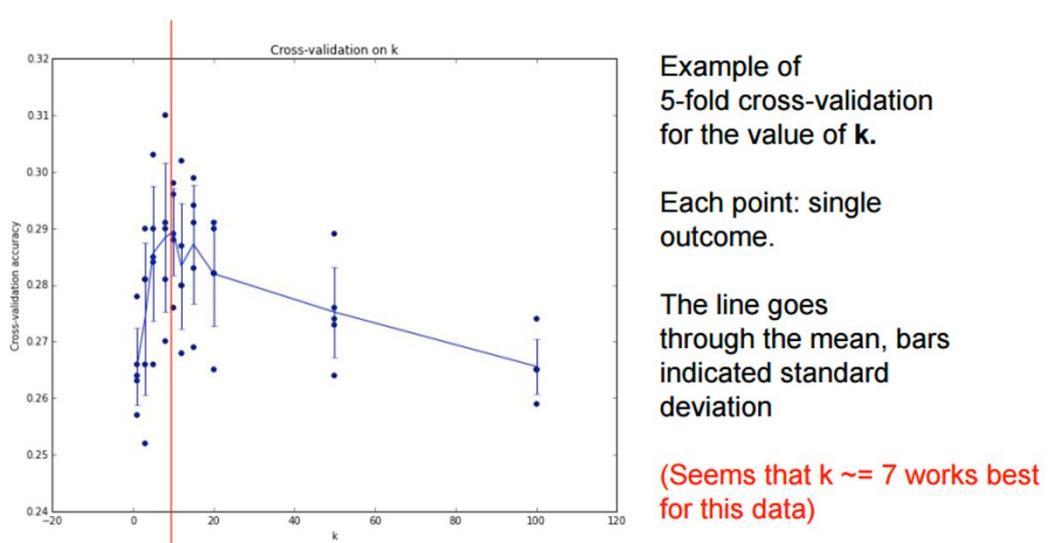
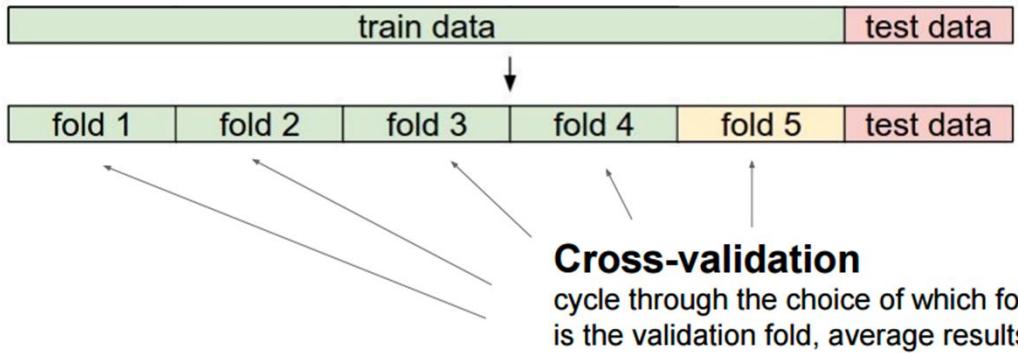


Validation



Validation data
 use to tune hyperparameters
 evaluate on test set ONCE at the end

Cross-validation



How to pick hyperparameters?

- Methodology
 - Train and test
 - Train, validate, test
- Train for original model
- Validate to find hyperparameters
- Test to understand generalizability

kNN

Pros

- simple yet effective

Cons

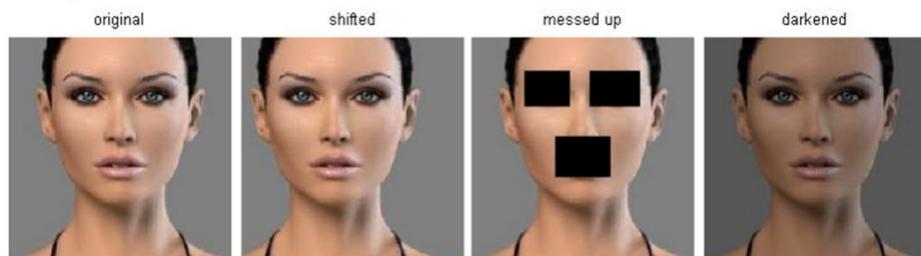
- search is expensive (can be sped-up)
- storage requirements
- difficulties with high-dimensional data

kNN -- Complexity and Storage

- N training images, M test images
- Training: $O(1)$
- Testing: $O(MN)$
- Hmm...
 - Normally need the opposite
 - Slow training (ok), fast testing (necessary)

k-Nearest Neighbor on images **never used**.

- terrible performance at test time
- distance metrics on level of whole images can be very unintuitive



(all 3 images have same L2 distance to the one on the left)

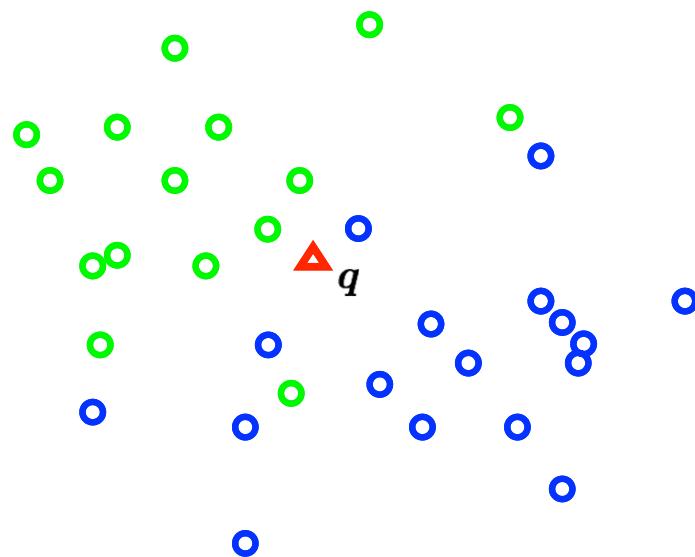
Naïve Bayes



SCHOOL OF INFORMATION AND COMMUNICATION TECHNOLOGY

82

Distribution of data from two classes



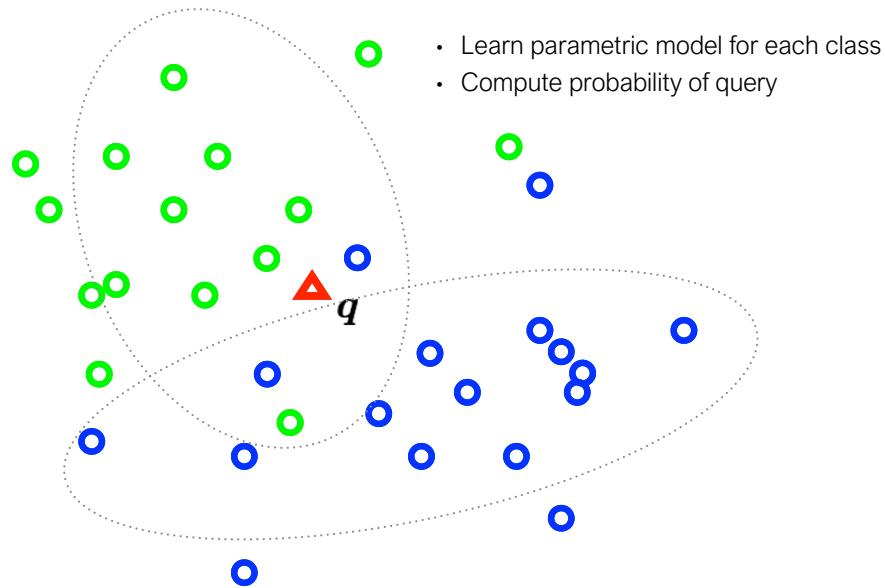
Which class does q belong to?



SCHOOL OF INFORMATION AND COMMUNICATION TECHNOLOGY

83

Distribution of data from two classes



This is called the posterior:
 the probability of a class z given the observed features X

$$p(z|X)$$

For classification, z is a
 discrete random variable
 (e.g., car, person, building)

X is a set of observed features
 (e.g., features from a single image)

(it's a function that returns a single probability value)

This is called the posterior:
the probability of a class z given the observed features X

$$p(z|x_1, \dots, x_N)$$

For classification, z is a
discrete random variable
(e.g., car, person, building)

Each x is an observed feature
(e.g., visual words)

(it's a function that returns a single probability value)



SCHOOL OF INFORMATION AND COMMUNICATION TECHNOLOGY

86

Recall:

The posterior can be decomposed according to
Bayes' Rule

$$p(A|B) = \frac{p(B|A)p(A)}{p(B)}$$

In our context...

$$p(z|x_1, \dots, x_N) = \frac{p(x_1, \dots, x_N|z)p(z)}{p(x_1, \dots, x_N)}$$



SCHOOL OF INFORMATION AND COMMUNICATION TECHNOLOGY

87

The naive Bayes' classifier is solving this optimization

$$\hat{z} = \arg \max_{z \in \mathcal{Z}} p(z | \mathbf{X})$$

MAP (maximum a posteriori) estimate

$$\hat{z} = \arg \max_{z \in \mathcal{Z}} \frac{p(\mathbf{X}|z)p(z)}{p(\mathbf{X})} \quad \text{Bayes' Rule}$$

$$\hat{z} = \arg \max_{z \in \mathcal{Z}} p(\mathbf{X}|z)p(z) \quad \text{Remove constants}$$

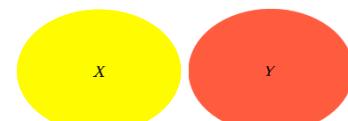
To optimize this...we need to compute this

Compute the likelihood...

A naive Bayes' classifier assumes all features are
conditionally independent

$$\begin{aligned} p(\mathbf{x}_1, \dots, \mathbf{x}_N | \mathbf{z}) &= p(\mathbf{x}_1 | \mathbf{z})p(\mathbf{x}_2, \dots, \mathbf{x}_N | \mathbf{z}) \\ &= p(\mathbf{x}_1 | \mathbf{z})p(\mathbf{x}_2 | \mathbf{z})p(\mathbf{x}_3, \dots, \mathbf{x}_N | \mathbf{z}) \\ &= p(\mathbf{x}_1 | \mathbf{z})p(\mathbf{x}_2 | \mathbf{z}) \cdots p(\mathbf{x}_N | \mathbf{z}) \end{aligned}$$

Recall:



$$p(x, y) = p(x|y)p(y) \quad p(x, y) = p(x)p(y)$$

To compute the MAP estimate

Given (1) a set of known parameters

$$p(\mathbf{z}) \quad p(\mathbf{x}|\mathbf{z})$$

(2) observations

$$\{x_1, x_2, \dots, x_N\}$$

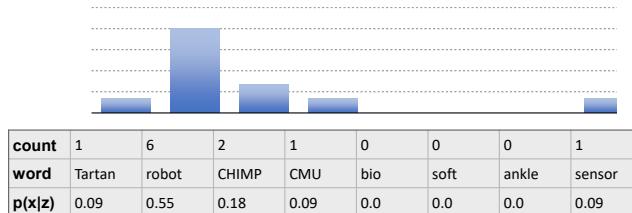
Compute which \mathbf{z} has the largest probability

$$\hat{\mathbf{z}} = \arg \max_{\mathbf{z} \in \mathbf{Z}} p(\mathbf{z}) \prod_n p(x_n | \mathbf{z})$$



SCHOOL OF INFORMATION AND COMMUNICATION TECHNOLOGY

90



$$\begin{aligned} p(X|z) &= \prod_v p(x_v|z)^{c(w_v)} \\ &= (0.09)^1 (0.55)^6 \cdots (0.09)^1 \end{aligned}$$

Numbers get really small so use log probabilities

$$\log p(X|z = \text{'grandchallenge'}) = -2.42 - 3.68 - 3.43 - 2.42 - 0.07 - 0.07 - 0.07 - 2.42 = -14.58$$

$$\log p(X|z = \text{'softrobot'}) = -7.63 - 9.37 - 15.18 - 2.97 - 0.02 - 0.01 - 0.02 - 2.27 = -37.48$$

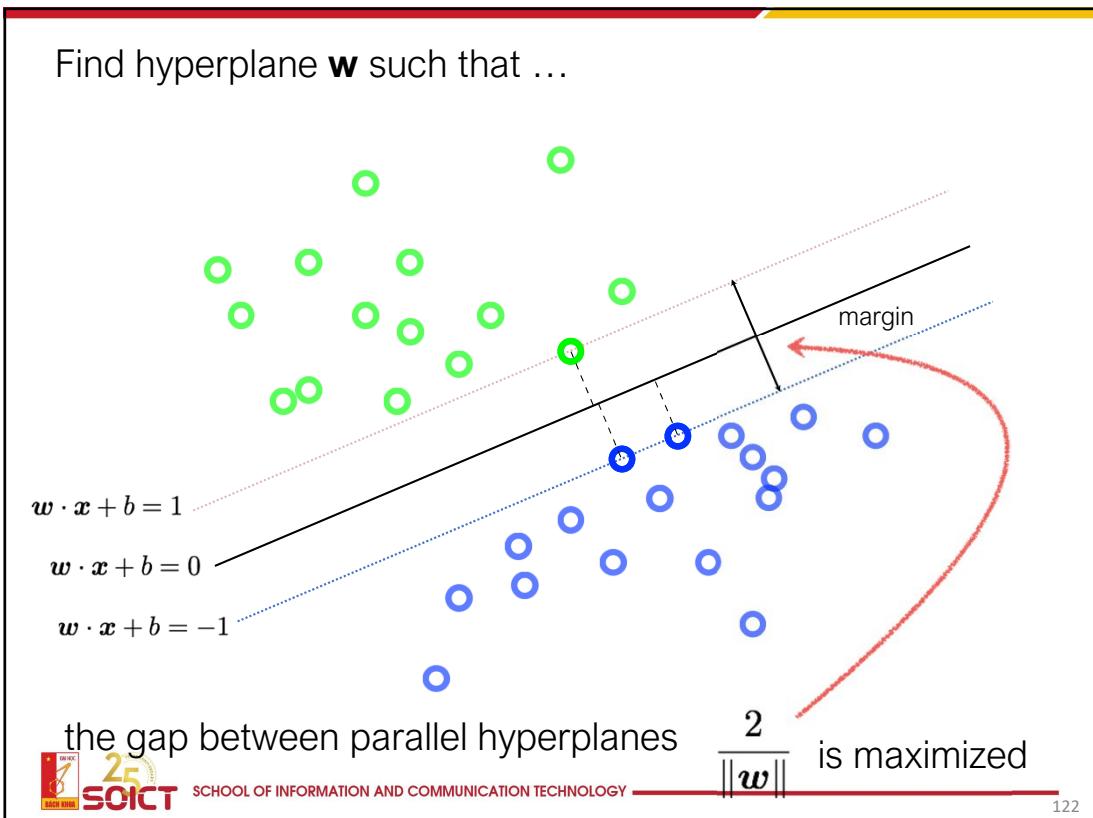
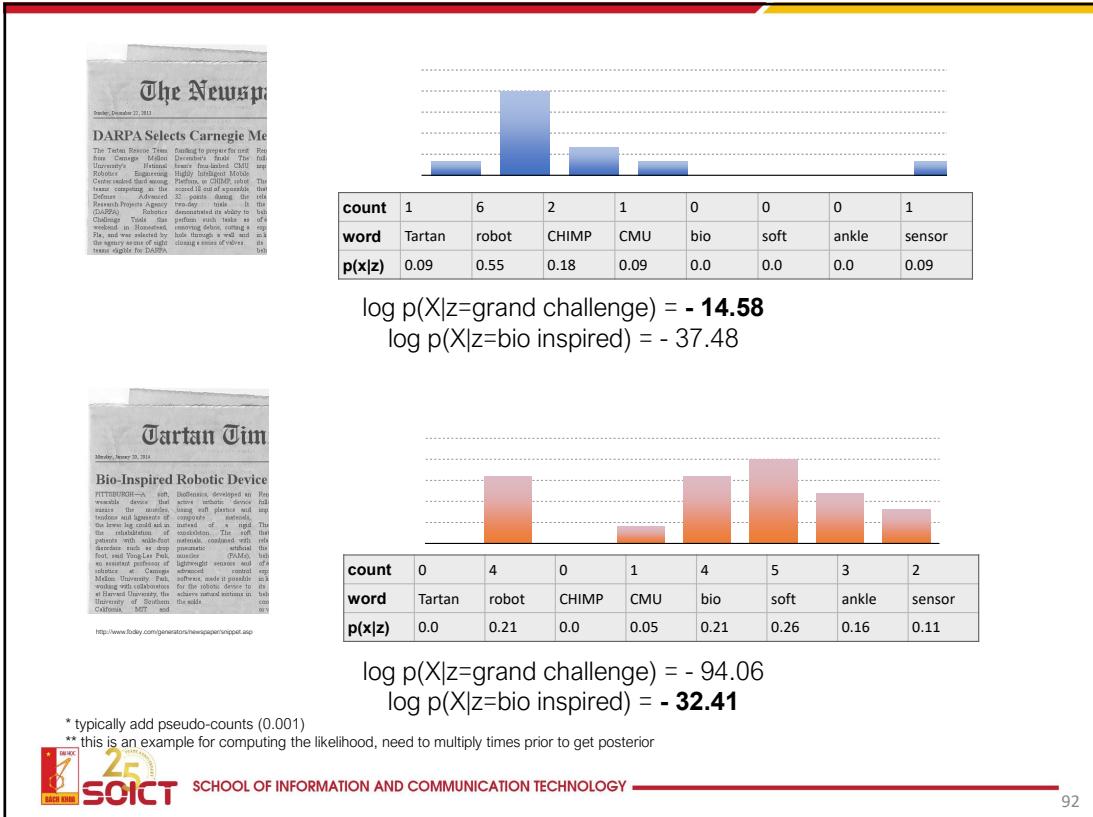
* typically add pseudo-counts (0.001)

** this is an example for computing the likelihood, need to multiply times **prior** to get posterior



SCHOOL OF INFORMATION AND COMMUNICATION TECHNOLOGY

91



References

Most of these slides were adapted from:

1. Ioannis Yannis, Gkioulekas (16-385 Computer Vision, Spring 2020, CMU)
2. Kristen Grauman (CS 376: Computer Vision, Spring 2018, The University of Texas at Austin)
3. Noah Snavely (Cornell University)
4. Fei-Fei Li (Stanford University)



SCHOOL OF INFORMATION AND COMMUNICATION TECHNOLOGY

138

Thank
you!

