

Problem 1: $f(x) = 3x^2 + 5x - 7$

$$f(x) = 3x^2 + 5x - 7$$

$$f'(x) = 6x + 5$$

Problem 2: $f(x) = \sqrt{x}$

$$f(x) = \sqrt{x} = x^{\frac{1}{2}}$$

$$f'(x) = \frac{1}{2} \cdot x^{\frac{1}{2}-1}$$

$$= \frac{1}{2} \cdot x^{-\frac{1}{2}}$$

$$= \frac{1}{2} \cdot \frac{1}{x^{\frac{1}{2}}}$$

$$= \frac{1}{2} \cdot \frac{1}{\sqrt{x}}$$

$$= \frac{1}{2\sqrt{x}}$$

Problem 3: $f(x) = x^2 \sin(x)$

$$f(x) = x^2 \sin(x)$$

$$f'(x) = (x^2)' \sin(x) + x^2 \sin'(x)$$

$$= 2x \sin(x) + x^2 \cos(x)$$

Problem 4: $f(x) = \sin(3x^2 + 2x)$

Set $g(x) = 3x^2 + 2x$

$$g'(x) = (3x^2 + 2x)' = 6x + 2$$

$$f(x) = \sin(3x^2 + 2x) = \sin(g(x))$$

$$f'(x) = f'(g(x)) \cdot g'(x)$$

$$= \sin'(g(x)) \cdot g'(x)$$

$$= \cos(3x^2 + 2x) \cdot 6x + 2$$