Research Statement of Thanh Nguyen-Tang

Machine learning has achieved remarkable breakthroughs in various Artificial Intelligence (AI) problem domains, including games, protein folding, natural language processing, drug synthesis, recommender systems, self-driving cars, and materials discovery. Despite the remarkable empirical success, we still lack a solid understanding of the capabilities and limits of such AI systems. Critical foundational gaps, if left unaddressed, will ultimately impede progress in AI and undermine its potential to meet the future needs of our society.

An overarching goal of my research is to establish **algorithmic foundations of learning for modern AI systems**, enabling next-generation AI with better *scalability*, *explainability*, and *transferability*. I have tackled among the most challenging AI systems: data-driven decision-making, in which agents are tasked with learning an optimal

Figure 1: My research is on algorithmic foundations of learning for modern AI systems.

decision-making model using data from interactions with an unknown environment. My work has so far focused on three key challenges of learning, emerged from practical data-driven decision-making, (1) **offline (reinforcement) learning**: learning from pre-collected offline data to mitigate expensive online interaction, (2) **multi-agent learning**: learning in the presence of multiple strategic agents, and (3) **trustworthy learning**: learning safe and robust models for adversarial environments. My approach emphasizes understanding learning through the lens of critical resources (e.g., data and computation) needed for learning, as well as designing optimal algorithms that use these resources efficiently.
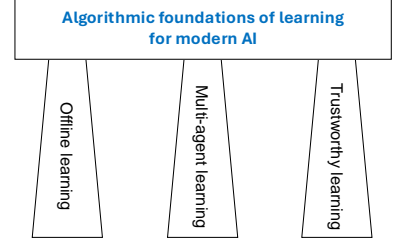
1. Offline (reinforcement) learning

The growth in scale of pre-collected data suggests that data-driven decision-making should take advantage of such offline data for learning. In many cases, such offline learning is not even a choice but mandatory, due to the prohibitive costs, safety concerns, and ethical issues of *online* data collection. However, a key challenge is that the offline data distribution differs from the distribution that is induced by the target policy to be learned. Additionally, offline data often lives in high dimensions, leading to an exponentially large state space. I've established fundamental limits and capabilities of offline learning for data-driven decision-making in large state spaces, using bounded-complexity function approximation (e.g., neural networks) and novel algorithmic design.

Neural networks for offline learning of large-scale problems
Neural networks are often used to approximate state value functions and generalize across large state spaces of large-scale problems. However, it remains elusive what natural problems benefit from offline data using neural networks and to what extent. In many large-scale decision-making problems, transition dynamics exhibit similarity between states, allowing for a smoothness assumption to relate these dynamics. In [1], I model this similarity using Besov smoothness–a general smoothness condition that generalizes both Lipschitz and Sobolev smoothness, and show that deep neural networks can exploit this property to learn provably near-optimal policies from uniformly covered offline data, with accuracy independent of the number of states and actions. My research got the attention from other machine learning experts who built on my work and studied other

Figure 2: Learnable problem classes characterized by different notions of data coverage.

dynamic structures to improve sample complexity of offline decision-making using neural networks [2].

Driven by real-world needs and advances in deep learning theory, I've developed provably optimal and efficient learning algorithms for offline decision-making using neural networks and gradient-based optimization. These algorithms handle offline data with partial coverage and apply to both contextual bandits [3] and Markov decision processes (MDPs) [4], achieving competitive performance on a large-scale benchmark.

A general theory and algorithmic framework for large-scale offline decision-making Despite its significance, understanding offline decision-making in large state spaces with general function approximation remains limited. In [5, 6], I show that offline decision-making is possible for a wide and novel range
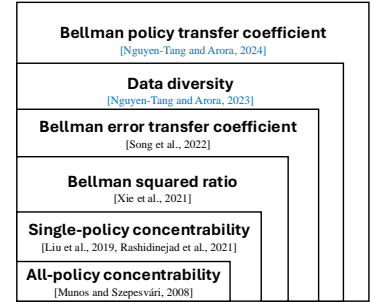
of distribution shift regimes under function approximation with bounded ℓ_1-covering numbers, the most general complexity condition thus far in the offline decision-making literature. The new regimes are captured by new notions of data coverage, including data diversity [5] and Bellman policy transfer coefficient [6], which strictly subsume previous notions (Figure 2). I also show a generic algorithmic framework that offers state-of-the-art error bounds for general bounded-complexity function approximation and, in particular, nearly minimax-optimal bounds for finite pseudo-dimension function classes. This framework unifies existing algorithms and facilitates the design of novel algorithms that use posterior sampling, providing practitioners with better insights, stronger guarantees, and more practical algorithms.

2. Multi-agent learning

Most challenging AI problems can be systematically framed as multi-agent learning, wherein multiple agents learn to act in a shared environment. Learning to make decisions in a static yet unknown environment is already hard, and harder still when multiple agents influence each other's learning outcomes and actions. A key challenge for multi-agent learning is non-stationarity, which is faced from the learning agent's perspective when the other agents react strategically. I've established fundamental limits and algorithmic principles of multi-agent learning in both cooperative and competitive settings, using novel analysis and algorithms built upon advances in reinforcement learning and game theory.

Learning against adaptive opponents While most of the literature focuses on learning equilibria, equilibria are not all we need [7]. In reactive systems (e.g., stock markets) where the opponent is adaptive to the learner's past strategies, the learner needs to exploit the opponent to maximize their return. For adaptive opponents, perhaps the only performance measure that makes sense is policy regret [8], a counterfactual notion that evaluates a competing strategy on the sequence of events that would have been generated if the competing strategy were followed. In [9], I initialize the first study on learning against adaptive opponents in Markov games using policy regret. I establish statistical limits for exploiting an adaptive opponent in games by showing the necessity to impose constraints on memory, stationarity, or regularity in the opponent's response. I showcase an algorithmic principle to exploit the weakness of an opponent who adapts more structurally. My work will benefit various learning-based systems with hierarchy information, such as human-robot collaboration, autonomous systems, and mechanism design.

Learning to collaborate to solve similar tasks faster One of the main advantages of multi-agent learning emerges in collaborative settings, where agents can share their experiences to learn their similar tasks faster and better. Despite the ubiquity of collaborative settings, a formal understanding of how and when learners of similar tasks benefit from sharing their respective experiences is still in its infancy. In [10], I formulate this question in the context of contextual linear bandits. I design a novel, computationally efficient, and nearly minimax-optimal distributed learning algorithm based on upper confidence bounds, that adaptively coordinates a set of agents to share their respective experiences while the agents are solving their own tasks. This paper will benefit federated learning and distributed collaborative systems.

3. Trustworthy learning

A key challenge in modern AI systems is ensuring generalization across diverse environments. Existing methods often lack robustness to variations in the test environments. To address this challenge, several recent works leverage adversarial training to optimize for worst-case scenarios, which often exhibit poor average-case performance, limiting their practical utility. I've developed scalable algorithms that better balance robust and average performance for data-driven decision-making, using distributionally robust optimization and distributional reinforcement learning (RL).

Robust decision-making under uncertainty Decision-making problems often assume that the training environment matches the deployment environment, which is unrealistic in many practical settings. In [11], I address this by introducing a robust regret objective, aimed at maximizing expected return against the most adversarial distributions over environments. Given the continuous action space, I model reward similarity using Gaussian processes, solve a tractable distributionally robust optimization problem with Thompson sampling on the surrogate reward, and show that this approach converges to an ϵ-suboptimal robust policy in a finite number of steps, despite the continuous action space. This work establishes the first framework for computing distributionally robust policies under uncertainty in continuous action spaces.

Scalable methods for distributional RL Distributional RL learns the full return distribution for each policy, enabling the use of risk-sensitive measures (e.g., CVaR, CPT) for robust generalization. Existing methods represent the return distribution via order statistics but fail to account for their properties during learning. In [12], I introduce a novel method using free particles to simulate return distribution samples based on statistical hypothesis testing. My algorithm sets a new record in the Atari game benchmark, is widely adopted by RL practitioners, and is featured as an exercise in the distributional RL textbook [13].

4. Future directions

I've made significant contributions to the foundations of previous learning settings, though we have only scratched the surface of these areas, and there is much more to be done. Beyond these ongoing topics, I'll describe my new research agenda, which fits well within my expertise, inspires multi-disciplinary collaborations (including fellow faculties, postdocs, graduate students, undergraduate students, and high school students), and expands over 2-year, 5-year, and 10-year research plans.

Transfer learning The techniques I've developed in offline learning apply to harness pre-collected data to improve the decision-making performance for the *same* task. While this fundamental setting is already challenging, a generalized paradigm emerges in practice and awaits further research. Moving forward, I will focus on the fundamental question of using data from a source task to improve the decision-making performance w.r.t. a target task for which (active) data collection is limited or unavailable. Answering this question will benefit application domains where it is costly to acquire new data (e.g., AI in medicine, genomics, insurance industry, smart cities), and offer opportunities to re-think many fundamental aspects of machine learning from modern challenges. Building on my previous work, I aim to tackle this research question by exploring the role of task similarity and function approximation for transfer learnability. The emphasis will be on adaptivity, i.e., how to design a learning algorithm that automatically adapts to all task similarity scenarios instead of specifically designing for different scenarios. Algorithmic approaches to transfer learning, such as representation learning [14, 15, 16] and test-time adaptation [17] that I've developed, will also be useful to study transfer learning for decision-making.

Learning meets games The world is moving toward the coexistence of multiple agents that learn from their interactions. Data input to machine learning algorithms can be generated by self-interested agents and machine learning is used to solve complex data-driven decision-making problems in economics (e.g., mechanism design). The theoretical foundations of these problems lie at the intersection of learning and game theory. With my future lab, I will continue to contribute to bridging the gap between machine learning and game theory. Five research agendas to fill this gap were put forth by other experts in the field 17 years ago [7]. Despite numerous developments ever since, the field is still in its infancy. For example, we lack a solid understanding of how to act optimally in the presence of other agents who can adapt and learn. This question underlies much of the applications in collaborative settings, where multiple agents are centralized and coordinated to achieve a team goal, or in strategic settings, where agents have their own interests and behaviors. My work [9] has provided an initial yet important step to understanding this question, by studying the algorithmic performance using a counterfactual notion of regret, and providing statistical limits and algorithmic design. One next important step is to think through what properties of the opponent's learning algorithm (e.g., algorithmic stability) are general enough yet exploitable by a learner, and how to learn in large-scale problems using function approximation.

Capabilities and limits of foundation models My previous research has taught me the crucial role of function approximation (e.g., deep networks and complexity-bounded function classes) in dealing with generalization for large-scale learning problems. Recently, a class of special neural networks known as foundation models, such as transformers, have shown remarkable performance in large-scale domains of language, image, and video. It is thus crucial and timely to unveil the mechanism behind how foundation models facilitate learning for modern AI systems, by leveraging the special connectivity in the model (e.g., attention layers). I will investigate this problem from the perspective of communication complexity theory, to understand what kind of problems foundation models are capable of computing, and an optimization perspective, to understand how and what training methods give rise to a model that generalizes well.

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