

$$a/. \det(2A^{-1}) = 2^4 \cdot \frac{1}{\det A} = 16 \cdot \frac{1}{-4} = -4$$

$$b/. |A \cdot A^T| = (|A| \cdot |A|) = |A|^2 = 16$$

$$c/. |\text{adj} A| = |\det A \cdot A^{-1}|$$

$$= \det A \cdot \det A^{-1}$$

$$= \det A \cdot \frac{1}{\det A} = \det A^3 = (-4)^3 = -64$$

$$d/. |I - A^3| = |-I \cdot A^3| = (-1)^4 \cdot \det A^3 = 1 \cdot (-4)^3 = -64$$

$$e/. |(2A)^{-1}|$$

$$= \frac{1}{\det(2A)} = \frac{1}{2^4 \cdot \det A} = \frac{1}{16 \cdot (-4)} = \frac{1}{-64}$$

$$f/. \det(A^{-1} - 2 \text{adj} A)$$

$$= \det\left(\frac{1}{\det A} \cdot \text{adj} A - 2(\text{adj} A)\right)$$

$$= \det\left(\left(\frac{1}{\det A} - 2\right)(\text{adj} A)\right)$$

$$= \left(\frac{1}{-4} - 2\right)^4 \cdot -64 = \frac{-6561}{4}$$