

Bsp 4

a) $v = (2, -1, 2)$

$$\|v\| = \sqrt{2^2 + (-1)^2 + 2^2} = \sqrt{9} = 3$$

b) $v = 2(1, 1, -1) = (2, 2, -2)$

$$= \sqrt{2^2 + 2^2 + (-2)^2} = 2\sqrt{3}$$

c) $v = -3(1, 1, 2)$

$$= \sqrt{9 + 9 + 36} = \sqrt{54} \approx 7.35$$

d)

$$v = (1, 2, 3) - (4, 1, 2)$$

$$= \sqrt{9 + 1 + 1} = \sqrt{11}$$

Bsp 5: $A = (5, -1, 4)$, $B = (1, 5, 5)$

$$\vec{d} = (1-5; 4-(-1); 1-4)$$

$$= (-4, 5, -3)$$

$$\|\vec{d}\| = \sqrt{16 + 25 + 9} = \sqrt{50}$$

$$\vec{u} = \frac{1}{\sqrt{50}} \cdot (-4, 5, -3) = \left(\frac{-4}{\sqrt{50}}, \frac{5}{\sqrt{50}}, \frac{-3}{\sqrt{50}} \right)$$

Bsp 6:

$$A = \|\vec{v} - 3\vec{w}\| = ?$$

$$\|\vec{v}\| = 2$$

$$\|\vec{w}\| = 1$$

$$\vec{v} \cdot \vec{w} = 2$$

$$A^2 = \|\vec{v} - 3\vec{w}\|^2$$

$$A^2 = (\vec{v} - 3\vec{w}) \cdot (\vec{v} - 3\vec{w})$$

$$A^2 = \vec{v} \cdot \vec{v} - 6\vec{v} \cdot \vec{w} + 9\vec{w} \cdot \vec{w}$$

$$A^2 = 4 - 6 \cdot 2 + 9 \cdot 1$$

$$A^2 = 4 - 12 + 9 = 1$$

$$\Rightarrow A = \sqrt{1} = 1$$