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, 2015





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# Περίληψη

Η παρούσα εργασία ασχολείται με την μελέτη της συμπεριφοράς των συναρτήσεων  $f(x)$  και  $g(x)$  για μεγάλα  $x$ . Οι συναρτήσεις αυτές ορίζονται ως  $f(x) = \sum_{n \leq x} \lambda(n)$  και  $g(x) = \sum_{n \leq x} \mu(n)$ , όπου  $\lambda(n)$  και  $\mu(n)$  είναι οι συνάρτησεις Liouville και Möbius αντίστοιχα. Η μελέτη αυτή βασίζεται στην θεωρία των αριθμών και στην ανάλυση. Οι κύριες ενότητες της εργασίας είναι:

- 1. Εισαγωγή
- 2. Ορισμοί και βασικές ιδιότητες
- 3. Αξιωματική θεωρία
- 4. Αποδείξεις
- 5. Συμπεράσματα



# Abstract

The purpose of this diploma thesis is to develop and implement an algorithm for most likely nearest neighbors monitoring from specific focal points in a hypothetical service for smartphone users. Whenever a user submits a most likely nearest neighbors query, sets three criteria: (i) a focal point of interest  $q$ , (ii) the desired number  $k$  of nearest neighbors, and (iii) a probability threshold  $\theta$ .

Because of privacy protection reasons, no user compromises their geographical position to the rest, but declares a wider *uncertainty region*. In this case, these regions are modelled according to the bivariate Gaussian distribution. Of course, uncertainty can acquire different parameters, expressing different scales of privacy. By using the term “*most likely nearest neighbors*”, we mean that in a certain search region around point  $q$ ,  $k$  moving users with probabilistic coverage above a certain threshold  $\theta$  have been found.

This thesis mainly focuses on developing indexing, filtering and pruning techniques which will enable us to reduce the cost and processing time of data. The suggested algorithm is deliberately chosen to be approximate in the calculation of probabilistic coverage of uncertain regions and provides a solution to the problem of answering probabilistic nearest neighbor queries for uncertain positions of moving objects. By utilizing the above techniques, an experimental study was conducted against synthetic datasets generated using the map of Athens. In addition, the expected performance on the execution times and accuracy of answers was confirmed. The overall conclusion of this thesis is that the algorithm is suitable for real time problems, where some accuracy may be sacrificed for the benefit of timely response.

## Keywords

Uncertainty, Probabilistic nearest neighbor queries, bivariate Gaussian distribution, moving objects, data streams.



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# Κατάλογος Σχημάτων

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6.1	. . . . .	24





# Κατάλογος Πινάκων

6.1	.....	23
-----	-------	----



# Κεφάλαιο 1

· · · , · ·

## 1.1

· ) ( ), ) · , · ·

### 1.1.1

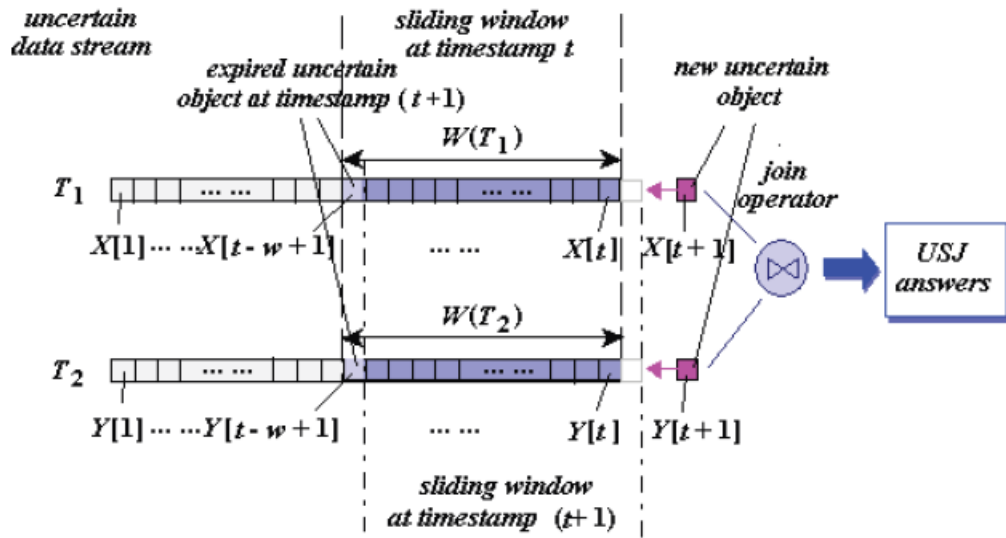
// · :  
:

- 1. ...
- 2. ...
- 3. ...
- 4. ...
- 5. ...

## 1.2

: · ( ):  
2. 3 . 4 ...  
( ), · , ·





Σχήμα 2.1: (: [1])

## Κεφάλαιο 2

### 2.1

, , , .

### 2.2 ' 1'

// 1 . , , . 2.1.

, , , . :

\* : [8]

\* : [1, 2, 3]

\* : [4, 5, 7]

\* : [6]

\* : [9]

**2.3**     $\epsilon$     **2'**

...

## Κεφάλαιο 3

### 3.1

// . // . //

### 3.2 ‘ , , 1’

...

### 3.3 ‘ , , 2’

...





## Κεφάλαιο 4

‘ ’, ...: *k*-

4.1

2-3 .

4.2 ‘ ’, ...: ’

.

4.3 ‘ ’, ...: ’

, , ...



## Κεφάλαιο 5

‘ , ...:  $k$ -

### 5.1

, .

### 5.2 ‘ / 1, ...: ’

, 1 . .. . /, .

---

#### Algorithm 1 Probabilistic $k\theta NN$ Monitoring

---

- 1: **Procedure** *VerifyCandidate* (focal query point  $q$ , threshold  $\theta$ , object  $o$ , list of auxiliary objects  $P$ , distance  $kMAXDIST$ )
  - 2: **if**  $\Phi(o, kMAXDIST) \geq \theta$  **and**  $L_2(q, o) \leq L_2(q, P.top())$  **then**
  - 3:    $P.pop()$ ;       //Replace the most extreme element in  $P$ , since candidate  $o$  ...
  - 4:    $P.push(o)$ ;    //... has enough probability and has its mean closer to focal  $q$
  - 5: **end if**
  - 6: **End Procedure**
- 

### 5.3 ‘ / 2, ...: ’

...



# Κεφάλαιο 6

## 6.1

## 6.2

## 6.3

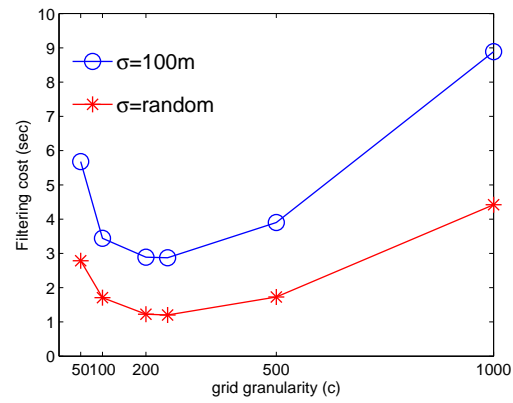
... ) ( , ) ) , ...  
... .. 6.1:

$c \times c$	$50 \times 50, 100 \times 100, 200 \times 200, \mathbf{250 \times 250},$ $500 \times 500, 1000 \times 1000$
$\sigma$	25m, 50m, 75m, <b>100m</b> , 150m, 200m
$k$	1, 2, <b>3</b> , 4, 5, 10, 20
$\theta$	50%, 60%, 70%, <b>75%</b> , 80%, 90%, 99%

Πίνακας 6.1:

### 6.3.1

...



Σχήμα 6.1:

## 6.4

, . 6.1. , . ( ) , .. .

## 6.5

. , .. 1. , 2. , ...

## Κεφάλαιο 7

.

### 7.1

· , · , · · ·

#### 7.1.1 ° 1°

...

#### 7.1.2 ° 1°

...

### 7.2

· , · , ηαρδωαρε, ... , · , ·





## Κεφάλαιο 8

### 8.1

, .

### 8.2

.



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uncertainty  
cumulative distribution function  
query evaluation  
sampling  
indexing  
continuous query  
nearest-neighbor query  
privacy  
grid  
moving object  
window  
multiplexing  
data stream  
focal point  
aggregation  
join  
filtering  
timestamp



