02 - Supervised Learning - Classification - Logistic Regression - Multinomial(Solution)_st122097_thantham

August 22, 2021

Lob02 Supervised Learning - Classification - Logistic Regression Multinomial

- 1.1 Name: Thantham Khamyai
- 1.2 Student ID: 122097
- 1.2.1 === Task ===
 - Doing train test split from scratch with Iris data
 - create LogisticRegression* class, giving optional training methods {'batch', 'minibatch', 'stochastic'} elsewise raise ValueError
 - Show training time for each training method
 - Perform a classification using 3 methods for {"batch", "mini-batch", "stochastic"}. Also plot training loss graph
 - Perform model evaluation using classification_report from sklearn.metrics
 - Discuss your results of **training losses** among three methods and **time taken** to fit models.

1.3 0. Import Neccessary Packages

```
[1]: import numpy as np
import matplotlib.pyplot as plt
import time
```

1.4 1. Load Dataset and Preprocessing

1.4.1 1.1 Load Iris Dataset

Iris Dataset is the dataset of dimensional measurement of each flower component. 3 dimensions of flower were measured including Sepal length, Sepal width and Petal width in unit of centimeters. These is for distinguish flower species name of Setosa, Vesicolor and Virginica.

This lab work aims to use those features to classify the flower name using Multinomial Logistic Regression because of 3 classes of target categories.

```
[2]: from sklearn import datasets iris = datasets.load_iris()
```

1.4.2 1.2 Extract X, y

This part tried to define which are X and y and examine shapes of each variable set

Warning: This Excercise solution used 3 features (in tutorial used 2 features), So Result will roughly looks quiet different

```
[3]: X = iris.data[:, :-1] # we only take the first two features.
y = iris.target #now our y is three classes thus require multinomial

print(f'Iris data features: {iris.feature_names}')
print(f'Example 5 header of X: \n {X[:5]}')

print(f'Iris target flower: {iris.target_names}')
print(f'All classes of y: \n {np.unique(y)}')

print(f'Shape of X: {X.shape} <- (m , n)')
print(f'Shape of y: {y.shape} <- (m , )')</pre>
```

```
Iris data features: ['sepal length (cm)', 'sepal width (cm)', 'petal length
(cm)', 'petal width (cm)']

Example 5 header of X:
   [[5.1 3.5 1.4]
   [4.9 3.   1.4]
   [4.7 3.2 1.3]
   [4.6 3.1 1.5]
   [5.   3.6 1.4]]

Iris target flower: ['setosa' 'versicolor' 'virginica']

All classes of y:
   [0 1 2]

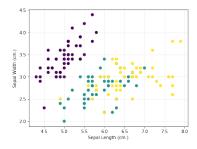
Shape of X: (150, 3) <- (m , n)

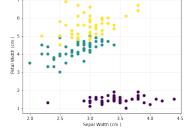
Shape of y: (150,) <- (m, )</pre>
```

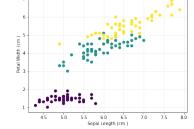
1.4.3 1.3 Show scatter plot

This block is for visualizing scatter of each feature relationship in each flower class. This will be visually observe on how the data distribution and relation between each feature looks like

```
plt1 = plt.subplot(1,3,1)
plt2 = plt.subplot(1,3,2)
plt3 = plt.subplot(1,3,3)
# Plot 1 sep len : sep wid
plt1.scatter(X[:,0], X[:,1] , c=y)
plt1.set_xlabel('Sepal Length (cm.)')
plt1.set ylabel('Sepal Width (cm.)')
plt1.grid(axis='both', alpha=.25)
# Plot 2 sep wid : pet wid
plt2.scatter(X[:,1], X[:,2], c=y)
plt2.set_xlabel('Sepal Width (cm.)')
plt2.set_ylabel('Petal Width (cm.)')
plt2.grid(axis='both', alpha=.25)
# Plot 3 sep len : pet wid
plt3.scatter(X[:,0], X[:,2] , c=y)
plt3.set_xlabel('Sepal Length (cm.)')
plt3.set_ylabel('Petal Width (cm.)')
plt3.grid(axis='both', alpha=.25)
```







1.4.4 1.4 Standardize X

For better convergenced capability in term of timing, Scaling will be performed

```
[5]: from sklearn.preprocessing import StandardScaler
scaler = StandardScaler()
X = scaler.fit_transform(X)

print(f'X after scaling: \n {X[:5]}')

X after scaling:
```

```
[[-0.90068117 1.01900435 -1.34022653]
[-1.14301691 -0.13197948 -1.34022653]
[-1.38535265 0.32841405 -1.39706395]
```

```
[-1.50652052  0.09821729 -1.2833891 ]
[-1.02184904  1.24920112 -1.34022653]]
```

1.4.5 1.5 Adding Intercept term and checking shape of X, Y

Add Intercept term using np.insert which insert '1' at 'index 0' in 'axis = 1' to X matrix

Then we will see new column for intercept 1 at index 0 columns

Also, shape of X will be (m, n+1) after adding intercept

```
[6]: X = np.insert(X, 0, 1, axis=1)
     print(f'Shape of X: {X.shape} <- (m , n+1)')</pre>
     print(f'Shape of y: {y.shape} <- (m, )')</pre>
     print(f'Example 5 header of X: \n {X[:5]}')
    Shape of X: (150, 4) \leftarrow (m, n+1)
    Shape of y: (150,) <- (m,)
    Example 5 header of X:
     [[ 1.
                   -0.90068117 1.01900435 -1.34022653]
     [ 1.
                  -1.14301691 -0.13197948 -1.34022653]
     [ 1.
                  -1.38535265 0.32841405 -1.39706395]
     [ 1.
                   -1.50652052 0.09821729 -1.2833891 ]
     [ 1.
                   -1.02184904 1.24920112 -1.34022653]]
```

1.4.6 1.6 Perform Train Test Split from scratch and Check shape of data

Expected Algorithm:

Then implementing train_test_split function. we will see new shape for each X and y

```
#create idx of test data
idx_test = np.array([i for i in range(X.shape[0]) if i not in idx_train])

#split X, Y
X_train = X[idx_train]
X_test = X[idx_test]
Y_train = Y[idx_train]
Y_test = Y[idx_test]

return X_train, X_test, Y_train, Y_test

# Perform splitting from created function
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.3)

print(f'Shape of X_train: {X_train.shape} <- (m , n+1)')
print(f'Shape of Y_train: {y_train.shape} <- (m , n+1)')
print(f'Shape of Y_test: {X_test.shape} <- (m , n+1)')
print(f'Shape of Y_test: {Y_test.shape} <- (m , n+1)')
print(f'Shape of Y_test: {y_test.shape} <- (m , n+1)')</pre>
```

```
Shape of X_train: (105, 4) <- (m , n+1)
Shape of Y_train: (105,) <- (m, )
Shape of X_test: (45, 4) <- (m , n+1)
Shape of Y_test: (45,) <- (m, )
```

1.4.7 1.3 Define function for One-Hot Encoding and Encode

In Multinomial Logistic Regression, y is multiple classes of integer. to classify this by logistic regression, It should be encoded using** One-Hot Encoding** to make it be probabilistic target in Y shape of (m, k) whether m =sample and k =number of probabilistic multi-class of flower target

Remark: One-Hot Encoding **implement only y_train** for fitting, **classification report needs y_test as interger form** (y_predicted will be output as interger form)

```
[8]: def OneHotEncoding(y, n_feature):
    k = len(set(y))
    m = len(y)
    n = n_feature
    y_encode = np.zeros((m, k))
    for class_i in range(k):
        row_idx = y==class_i
        y_encode[np.where(row_idx), class_i] = 1
    return y_encode

Y_train = OneHotEncoding(y_train, X.shape[1])

print(f'y before encode has shape {y_train.shape}')
```

```
print(f'Y after encode has shape {Y_train.shape}')
print(f'y before encode are {y_train[:5]}')
print(f'Y after encode are {Y_train[:5]}')

y before encode has shape (105,)
Y after encode has shape (105, 3)
y before encode are [0 2 0 1 0]
Y after encode are [[1. 0. 0.]

[0. 0. 1.]
[1. 0. 0.]
[0. 1. 0.]
[1. 0. 0.]]
```

1.5 2. LogisticRegression Class Creation

Referring to previous Logistic Regression Class structure, This class also looks similar, but what changes are new use **W** matrix instead of theta vector, change h_theta function to implement softmax function in multinomial probabilistic for each prediction and cost function to conclude loss value

```
[9]: class LogisticRegression:
         def __init__(self,method= 'mini-batch',max_iterations=100000, alpha=0.001,_
      →early_stopping=False, tol = 0.0001,
                     mini_batch_size = 10, record_history_every = 100, __
      →print_loss_every=500):
             self.training_method = method
             self.alpha = alpha
             self.tol = tol
             self.early_stopping = early_stopping
             self.max_iterations = max_iterations
             self.training_history = []
             self.batch_size = mini_batch_size
             self.epoch_to_record_history = record_history_every
             self.epoch_to_print = print_loss_every
             self.previous_loss = 10000
             self.stop_epoch = 0
             self.fitting_time = 0
             if self.training_method not in ['batch', 'mini-batch', 'stochastic']:
                 raise ValueError('''method defined not match any available:
     →'batch','mini-batch','stchastic' ''')
         def fit(self, X, Y):
             # 1 initiaite W, idx for stochastic, and time
             self.W = self.initiate_W(X.shape[1], Y.shape[1])
             idx_used = []
```

```
time_start = time.time()
       # 2 Perform Looping learning
       for i in range(self.max_iterations):
           # 2.1 condition to choose method
           if self.training method=='batch':
               # pass all samples
               x_to_train = X # dump all x
               y_to_train = Y # dump sll y
           elif self.training_method=='stochastic': # <= With Replacement</pre>
               # randomly select 1 sample
               select_idx = np.random.randint(X.shape[0])# random idx
               while select_idx in idx_used:
                    select_idx = np.random.randint(X.shape[0])# random idx
               x_to_train = np.array([X[select_idx, :]]) # extract one X by_
\hookrightarrow i dx
               y_to_train = np.array([Y[select_idx]]) # extract one y by idx
               idx_used.append(select_idx)
               if len(idx_used) == X.shape[0]:
                    idx_used = []
           elif self.training_method=='mini-batch':
                # randomly select portion of samples following predefined mini_{\sqcup}
\rightarrowbatch size
               select_start_idx = np.random.randint(X.shape[0] - self.
→batch_size) # random starting idx
               x_to_train = X[select_start_idx:select_start_idx + self.
→batch_size, :] # extract portion of X
               y_to_train = Y[select_start_idx:select_start_idx + self.
→batch_size] # extract portion of y
           else:
               raise ValueError('''method defined not match any available:
⇔'batch','mini-batch','stochastic' ''')
           # 2.3 calculate gradient and loss of current iteration
           current_loss, grad = self.gradient(x_to_train, y_to_train)
           # 2.4 if diffence of current and previous loss less than tolerance
\hookrightarrow -> stop fitting
```

```
if self.early_stopping & (np.abs(self.previous_loss - current_loss)__

< self.tol):</pre>
               self.stop_epoch = i # keep early stopping iteration in_
⇒stop epoch variable
               # print early stopped epoch and exit loop
               print(f'early_stopped at epoch: {i+1}')
               print(f'training latest loss: {self.previous_loss}')
               break
           # 2.5 record current loss to be precious loss
           self.previous_loss = current_loss
           # 2.6 Update W
           self.W = self.W - self.alpha * grad
           # add history loss
           if i % self.epoch_to_record_history == 0: # if this iteration is_
→every ... for recording loss
               self.training_history.append(current_loss) # save this loss
           # print current loss
           if i % self.epoch_to_print == 0: # if this iteration is every ...
→ for printing loss
               print(f'loss at epoch {i}: {current_loss}') # print current_
\rightarrow iteration loss'
       self.fitting_time = time.time() - time_start
       self.stop_epoch = i # if no early stopping -> keep last iteration_
→ number to stop_epoch
       print(f'fitting model completed by loss: {current_loss}')
       print(f'fitting time: {round(self.fitting_time, 3)} seconds')
   def gradient(self, X, Y):
       h = self.h_theta(X) # predict h_theta
       cost = - np.sum(Y * np.log(h)) / X.shape[0] # calculate cost -> - sum(_
\hookrightarrow Y - log(h) ) / m
       error = h - Y # calcualte error (yhat - y)
       grad = self.softmax grad(X, error) # calculate gradient to optimize W
       return cost, grad
   def softmax(self, X_dot_W):
       return np.exp(X_dot_W) / np.sum(np.exp(X_dot_W), axis=1, keepdims=True)__
\rightarrow# e^h / sum( e^h )
```

```
def softmax_grad(self, X, error):
       return np.dot(X.T, error) # (yhat - y)x
   def h_theta(self, X):
       return self.softmax(np.dot(X, self.W)) # X dot W and pass to softmax
\hookrightarrow function
   def initiate_W(self, n, k):
       return np.zeros((n, k)) # make W matrix of full of O
   def predict(self, X_test):
       return np.argmax(self.h_theta(X_test), axis=1) # reverse interger class_
→ from one-hot classes
   def show_learning_graph(self):
       if len(self.training_history) == 0: # if no loss in history list
           print('hitory is empty!, fit model before!')
       else: # else show learning curve
           plt.plot(np.arange(start = 1, stop = self.stop_epoch, step=self.
→epoch_to_record_history) , self.training_history, label = "Train Losses")
           plt.title("Losses thourgh learning curve")
           plt.xlabel("number of epoch")
           plt.ylabel("losses")
           plt.legend()
```

1.6 3. Performing Classification

1.6.1 3.1 Instantiate LosgisticRegression Model

This part is just for performing classification using create class with class parameters of 'mini-batch' training method and activate early stopping

```
[10]: model = LogisticRegression(method= 'mini-batch',max_iterations=150000, alpha=0.

→0003, early_stopping=True, tol = 1e-6,

mini_batch_size = 30, record_history_every = 100,

→print_loss_every=2000)
```

1.6.2 3.2 Fitting Model

The fitting has set to print loss every 1000 epochs and record training history every 100 epochs. Then show training graph

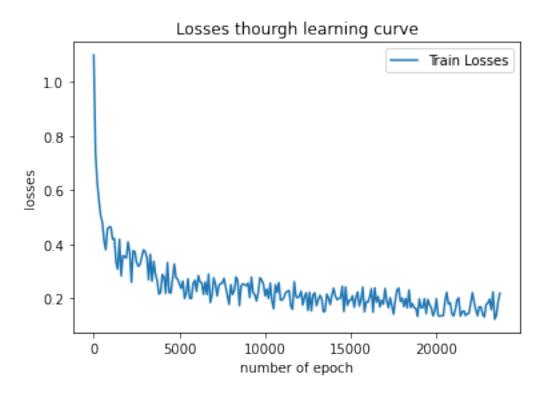
```
[11]: model.fit(X_train, Y_train) # fitting
model.show_learning_graph() # call show history function (make this to callable
→in the main class)
```

loss at epoch 0: 1.0986122886681098 loss at epoch 2000: 0.40906677513520295 loss at epoch 4000: 0.2892397566000717 loss at epoch 6000: 0.22616889546888305 loss at epoch 8000: 0.251494875546524 loss at epoch 10000: 0.20995420210353946 loss at epoch 12000: 0.20966936508959882 loss at epoch 14000: 0.2384083484729111 loss at epoch 16000: 0.1866146080975442 loss at epoch 18000: 0.20127134934113475 loss at epoch 20000: 0.19953259524448694 loss at epoch 22000: 0.18267796925119073 early_stopped at epoch: 23723

training latest loss: 0.14728151534939263

fitting model completed by loss: 0.14728086923093822

fitting time: 1.887 seconds



From training, The training was fitting stopped at epoch which different loss not over than tolerance value

1.7 4. Model Evaluation

1.7.1 4.1 Predict y_predicted

From model created, predict function was made for **predict output of interger form** (not one-hot form) because when we check metrics, classes should be interger indicator classes (should not be one-hot class indicator)

We can see how reverse One-Hot encoded back to interger class in predict function which use np.argmax to return the index of max probability value from predicted output in h theta function

```
[12]: y_pred = model.predict(X_test) # This will return integer form of classes
print(f'result of y_predicted: \n {y_pred[:]}')
```

```
result of y_predicted:
```

1.7.2 4.2 Evaluate Result using classification_report imported from sklearn.metrics

Shortly, we use classification report from sklearn.metrics package. However, in code, we just put y_test to compare with y_pred which they are interger form of classes because in step of OneHot encoding, we encodeed only y_train (m,) to be Y_train (m, k), not for y_test

So that,we can put y_test directly to classification report function, then we will see class labels as 0,1,2 which stand for ['setosa' 'versicolor' 'virginica']

```
[13]: from sklearn.metrics import classification_report

print(f'Classification Report: \n {classification_report(y_test, y_pred)}')
```

Classification Report:

		precision	recall	f1-score	support
	0	1.00	1.00	1.00	13
	1	0.94	0.94	0.94	16
	2	0.94	0.94	0.94	16
accura	CV			0.96	45
macro av	•	0.96	0.96	0.96	45
weighted av	vg	0.96	0.96	0.96	45

1.8 5. Implement Training model for different method and Discussion

This section will perform classification following Lab work Tasks to do as

- Perform 3 training method classification 'batch', 'mini-batch', 'stochastic'
- use train_test_split implemented X_train, X_test, Y_train (encoded) and y_test from previous execution

- Show Classification Report, Fitting time and Plot training losses for each training method
- Dicussion on result and what are considerations

Remark: To dicuss result among 3 models, early_stopping will not be set, other training parameters will be the same except training method

1.8.1 5.1 Instantiate models for different training method

Training method are separated, and iterations is 30,000 with alpha.0003, deactivated early stopping option altough tol has set, record history every 30 iterations and print loss evenly 2,000 iterations

1.8.2 In case of method is not match any

```
[14]: model_batch = LogisticRegression(method= 'batch is the

→best',max_iterations=30000, alpha=0.0003, early_stopping=False, tol = 1e-6,

record_history_every =30, print_loss_every=2000)
```

```
ValueError
                                                  Traceback (most recent call
→last)
       <ipython-input-14-c60c2484719f> in <module>
   ---> 1 model_batch = LogisticRegression(method= 'batch is the_
⇒best', max iterations=30000, alpha=0.0003, early stopping=False, tol = 1e-6,
         2
                           record_history_every =30, print_loss_every=2000)
       <ipython-input-9-cb6e9192da08> in __init__(self, method, max_iterations,_
→alpha, early_stopping, tol, mini_batch_size, record_history_every, __
→print_loss_every)
        17
        18
                   if self.training_method not in ['batch', 'mini-batch',
→'stochastic']:
                       raise ValueError('''method defined not match any \Box
  ---> 19
→available: 'batch', 'mini-batch', 'stchastic' ''')
        21
               def fit(self, X, Y):
       ValueError: method defined not match any available:
→ 'batch', 'mini-batch', 'stchastic'
```

1.8.3 Doing instantiate model properly

1.8.4 5.2 Fitting all models

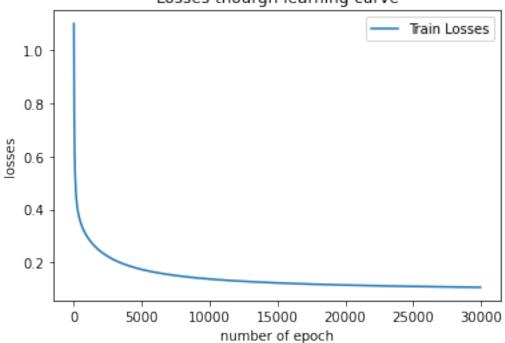
5.2.1 batch gradient descent training

loss at epoch 0: 1.0986122886681098

```
loss at epoch 2000: 0.24108792783538632
loss at epoch 4000: 0.18914022062561545
loss at epoch 6000: 0.16366906552249325
loss at epoch 8000: 0.1485563706592071
loss at epoch 10000: 0.13854785325087238
loss at epoch 12000: 0.13142223548445509
loss at epoch 14000: 0.12608428945636388
loss at epoch 16000: 0.12193261664275053
loss at epoch 18000: 0.1186095354224878
loss at epoch 20000: 0.11588883051542406
loss at epoch 22000: 0.11362029511513998
loss at epoch 24000: 0.1117001772468021
loss at epoch 26000: 0.11005443738950418
loss at epoch 28000: 0.10862877334949496
fitting model completed by loss: 0.10738300437126652
fitting time: 2.224 seconds
Classification Report:
               precision
                           recall f1-score
                                               support
           0
                   1.00
                             1.00
                                       1.00
                                                   13
           1
                   0.94
                             0.94
                                       0.94
                                                   16
```

2	0.94	0.94	0.94	16
accuracy			0.96	45
macro avg	0.96	0.96	0.96	45
weighted avg	0.96	0.96	0.96	45





Batch gradient descent

Considerations:

- 1) Completed 30,000 iterations within \sim 2 seconds
- 2) Training curve graph looks very stable and not much significant change of loss after 5000-10,000 iterations
- 3) Classification metrics showed very good for classifying Iris data

5.2.2 mini-batch gradient descent training

loss at epoch 0: 1.0986122886681098 loss at epoch 2000: 0.38118508555870023

loss at epoch 4000: 0.3339954037950777 loss at epoch 6000: 0.2898274061381072 loss at epoch 8000: 0.2550817976736971 loss at epoch 10000: 0.2335809845057702 loss at epoch 12000: 0.16982528846403336 loss at epoch 14000: 0.2489227747896376 loss at epoch 16000: 0.2072602339044721 loss at epoch 18000: 0.18407942127084506 loss at epoch 20000: 0.19575099336686075 loss at epoch 22000: 0.14712695874098725 loss at epoch 24000: 0.18047368916633688 loss at epoch 26000: 0.19331784421774179 loss at epoch 28000: 0.13349112390686113

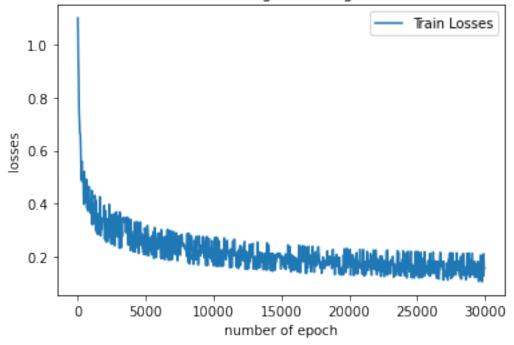
fitting model completed by loss: 0.13054515421077967

fitting time: 2.455 seconds

Classification Report:

	precision	recall	f1-score	support
0 1	1.00 0.94	1.00 0.94	1.00 0.94	13 16
2	0.94	0.94	0.94	16
accuracy			0.96	45
macro avg	0.96	0.96	0.96	45
weighted avg	0.96	0.96	0.96	45

Losses thourgh learning curve



Mini-Batch gradient descent

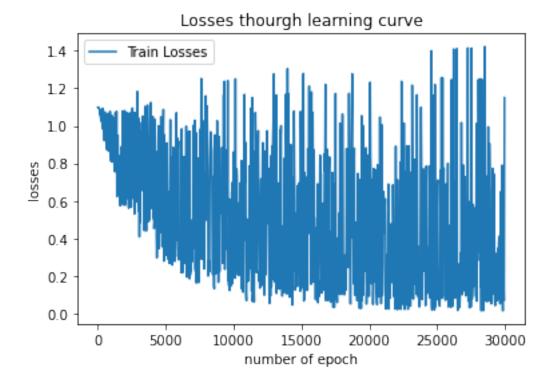
Considerations:

- 1) Completed 30,000 iterations within \sim 2 seconds
- 2) Training curve graph looks potentially unstable after decreasing loss lower than 0.4 and not much significant change of loss after 10,000 iterations
- 3) Classification metrics showed statifying for classifying Iris data

5.2.3 stochastic gradient descent training

```
loss at epoch 0: 1.0986122886681098
loss at epoch 2000: 0.795158239821472
loss at epoch 4000: 0.3968420485933217
loss at epoch 6000: 0.2936914559509471
loss at epoch 8000: 1.254790291144449
loss at epoch 10000: 0.9685951784756022
loss at epoch 12000: 0.5989177159576209
loss at epoch 14000: 0.747127601771642
loss at epoch 16000: 1.025354939262359
loss at epoch 18000: 0.8533788330946587
loss at epoch 20000: 0.11589390037509577
loss at epoch 22000: 0.6902137440545962
loss at epoch 24000: 0.7697735210210093
loss at epoch 26000: 0.01705642436993027
loss at epoch 28000: 0.5429699154054477
fitting model completed by loss: 0.7333574981107482
fitting time: 3.274 seconds
Classification Report:
```

	precision	recall	II-score	support
0	1.00	1.00	1.00	13
1	0.75	0.56	0.64	16
2	0.65	0.81	0.72	16
accuracy			0.78	45
macro avg	0.80	0.79	0.79	45
weighted avg	0.79	0.78	0.77	45



Stochastic gradient descent

Considerations:

- 1) Completed 30,000 iterations within ~3 seconds
- 2) Training curve graph looks dramatically variant and difficult to stably converged even through 30,000 eiterations
- 3) Classification metrics showed fair for classifying Iris data

1.8.5 Result Discussion among training method for Multinomial Logistic Regression by Iris Data

- Clasification Result
 - The overall we can roughly looks is Accuracy. Batch training method showed very good result at ~0.9 even Precision, Recall and F1 score. next 1st runner-up is Mini-Batch method which provided ~0.9 Accuracy, but it performed not good as best one. This is because we did not take all training X to perform minimize loss, so some training X set might be repeatitively taken to tune up W, but some X very less times to be calculate new W. This is one of a bias aspect to train the model. Nevertheless, stochastic gave considerable result. This is because although no replacement implemented a sample took to calculate new W is less times. So, if we want to make stochastic converge properly, it needs to be more iterations to reach that point.
- Time to fit
 - Although Batch method provided fastest training time but Mini-Batch also perform approximately around ~2-3 second with Iris data which has 105 training data (70:30

split). This may be because process will spend some time to execute splitting X data to train despite no splitting process for Batch. In constrast, Stochastic performed taking time more than others (>3 seconds) because no replacement approach to select training X, and it also need to do several steps before excecute gradient function

• Training loss Gragh

— It is true that Batch method should provide best stability of curve due to taking all training to tune W. However, Stochastic method should be therotical better, but it visually perform very variant during training because it has to select only 1 training X to tune whole W set. This cause difficulty to converged good result in less number of training. If it perform on large dataset, it could be better in term of training time and converged cost (computational cost). For Mini-Batch, it took both advantages from Batch and Stochastic to select a portion of training X set to tune W up properly. This brings about decrease computaional cost and suitable convergence cappability comparing to the bad aspect of Batch method and good aspect of Stchastic method

• Overall and conclusion

- Even though all method have thier own issues to consider, we should realzie the capability of them and select the best one for better study. For practical study, large dataset will cause directly to the reason to choose training method. Eventually, Mini-Batch should be prioritized to be a choice to perform in any ML problem. To decrease bad side of Batch, and rise good side of stochastic. We should think suitable one to be used

[]: