

**ECE 166 – Microwave Circuits and Systems**  
**Homework #5– Friday December 3, 2021 - In the Review Session**  
**(Low-Noise Amplifier Design, High-Gain Amplifier Design)**  
**Counts as 1.5Hwks**

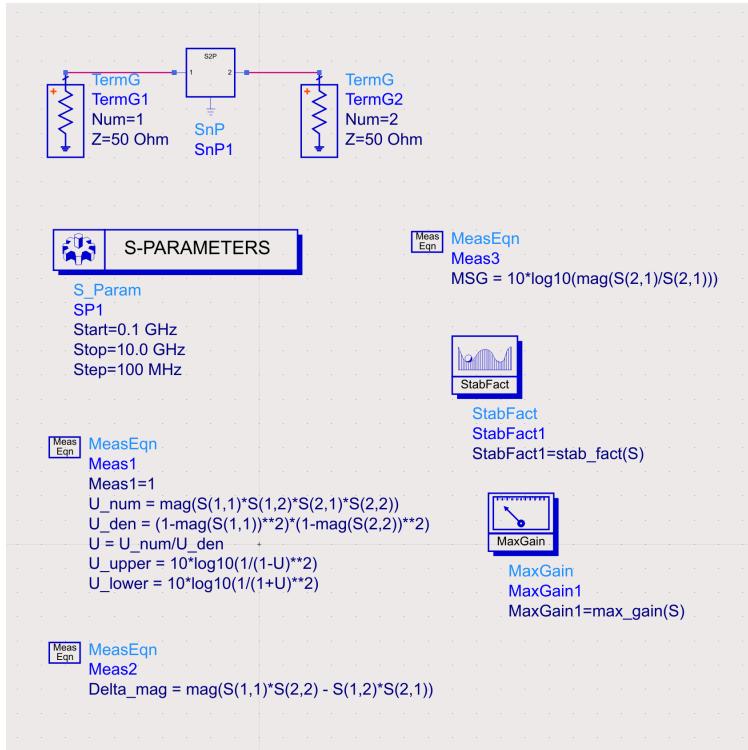
You will be designing a low noise and a high gain amplifier using the Avago ATF 34143 amplifier. This is a high-performance GaAs amplifier with a  $NF_{min}$  of 0.1-0.3 dB at 500 MHz to 3 GHz (all for 20 cents, amazing!). *All simulations and plots are to be done in ADS.* The S-parameters are given on the website.

*Note: ADS can plot many of these parameters for you. See ECE 166 website.*

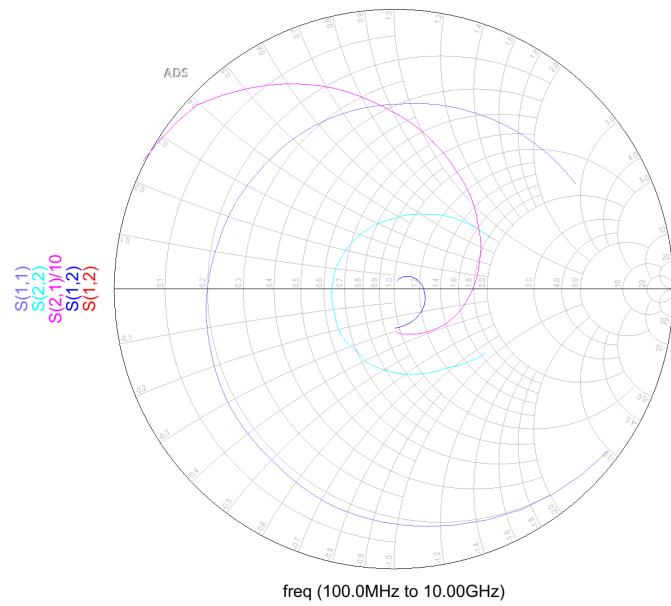
- 1) Using the S-parameters for 3 V, 20 mA bias (page 7 in the data sheet), calculate and plot at 0.1-10 GHz:
  - a) S-parameters (for  $S_{21}$ , you can plot  $S_{21}/10$  so that it is mostly in the Smith Chart).
  - b) The unilateral coefficient ( $U$ ), and the upper and lower bounds of the gain in dB (centered at 0 dB). In which frequency region is the unilateral approximation valid?
  - c) The Stability Factor,  $k$  and  $\Delta$ . In which frequency region is the transistor unconditionally stable?
  - d) The maximum transducer gain in dB (MSG or MAG depending on  $k$ ) that can be attained using this device. Compare with  $S_{21}$ . This is basically Fig. 23 in the data sheet.
- 2) Using the S-parameters at 3 V, 20 mA, and the noise parameters, design a low-noise amplifier at 2.5 GHz for WLAN base-stations. Clearly write  $\Gamma_{opt}$ ,  $\Gamma_s$ ,  $\Gamma_o$ ,  $\Gamma_i$  and  $\Gamma_l$  at 2.5 GHz, the matching networks used (ideal components but with  $Q=40$  for the inductor and  $Q=100$  for the capacitor), and the simulated S-parameters and noise figure (plot from 0.1-5 GHz). Use LC matching. Label the gain, the output match level (must be good), the input match level (should not be *that* good but OK), and the noise figure at 1-4 GHz. Check that the LNA is stable at all frequencies by plotting the input and output stability circles, and  $\Gamma_s$  and  $\Gamma_l$  (again, ADS does this automatically). Make sure that  $\Gamma_s$  and  $\Gamma_l$  do not enter the un-stable regions at their respective frequencies. Make sure that  $S_{11}$  and  $S_{22}$  for the entire amplifier are  $< 1$  at all frequencies (for stability). Clearly plot the S-parameters and NF of the entire amplifier. Clearly state how you stabilized it.
- 3) Using the same S-parameters at 3 V, 20 mA, design a high-gain amplifier at 5.5 GHz. You will see that the transistor is still not stable but  $U$  is  $\sim 0.1$ , and that one can use a unilateral gain approximation. However, the transistor is greatly unstable at  $< 4$  GHz and your wonderful design at 5.5 GHz may lead to oscillations at lower frequencies. Make sure to avoid the bad regions on the Smith chart for both  $\Gamma_s$  and  $\Gamma_l$ . Clearly show the LC matching networks used (ideal components but with  $Q=40$  for the inductor and  $Q=100$  for the capacitor). Plot the S-parameters and NF of the amplifier from 1 to 10 GHz (but check stability at all frequencies). Clearly state how you stabilized it. What is the achieved gain at 5.5 GHz as compared to the unilateral gain?

Thao Nguyen  
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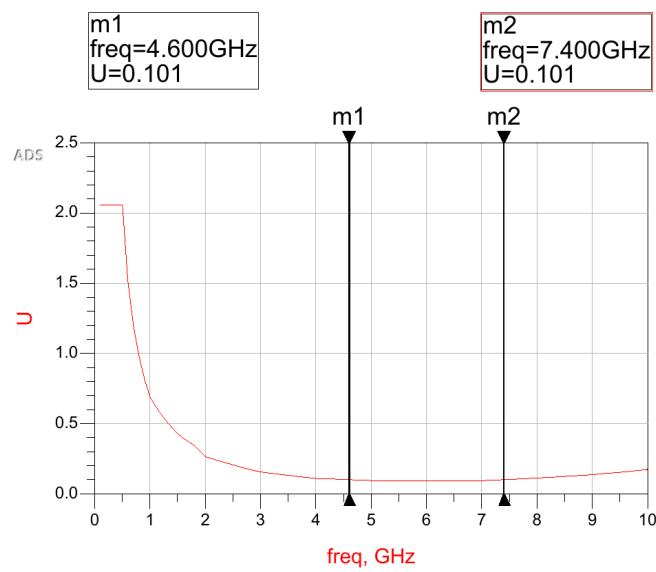
### Problem 1

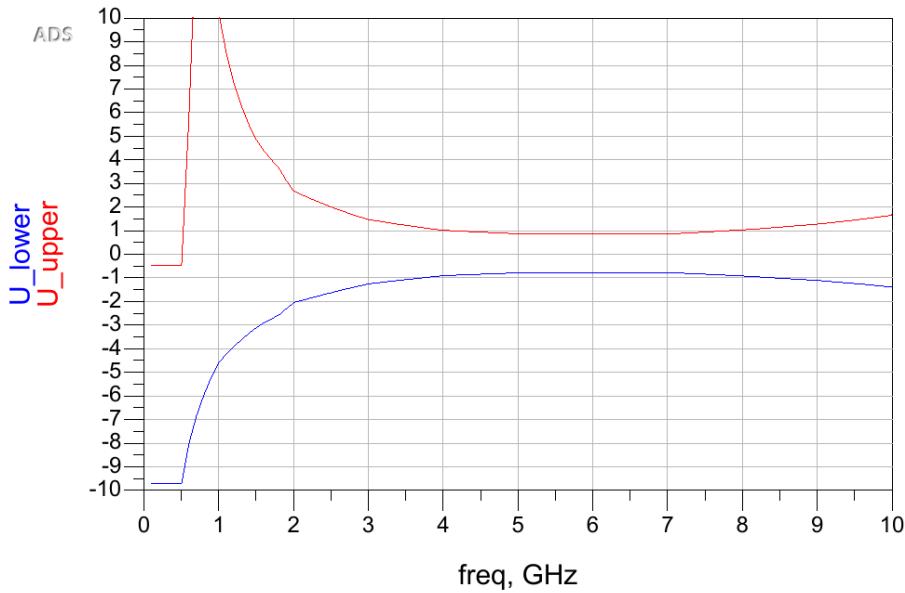


a)



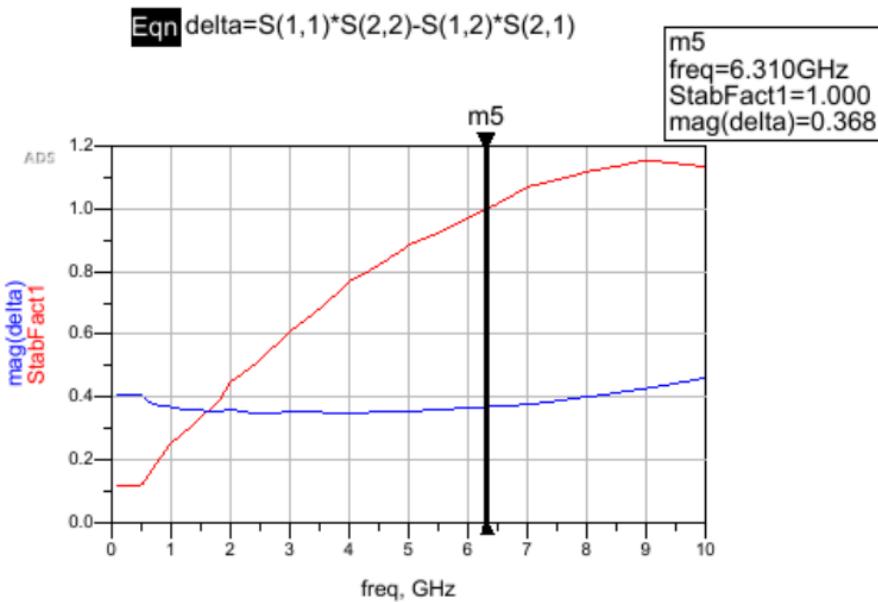
b)





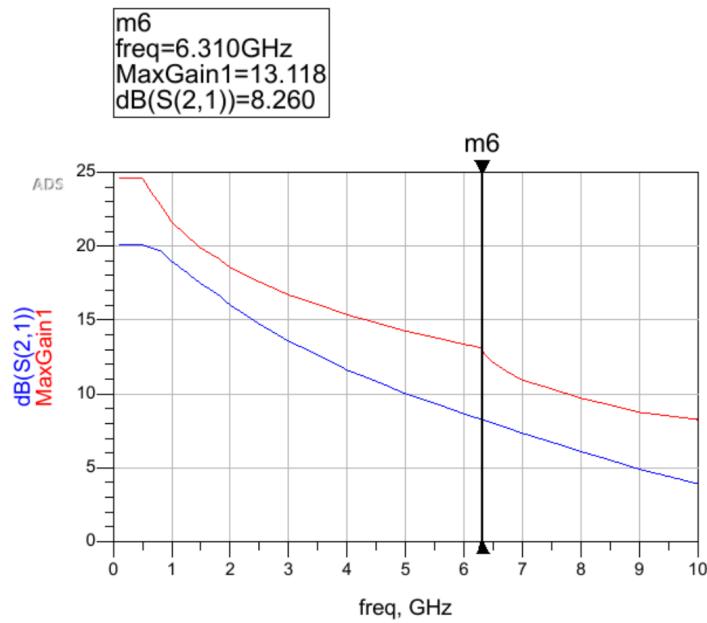
The unilateral approximation is valid when  $u < 0.1$ , which is frequency range 4.6 GHz - 7.4 GHz. This is when the effect of  $S_{12}$  can be ignored.

c)



The amplifier is unconditionally stable when  $|k| > 1$ ,  $|\delta| < 1$ .

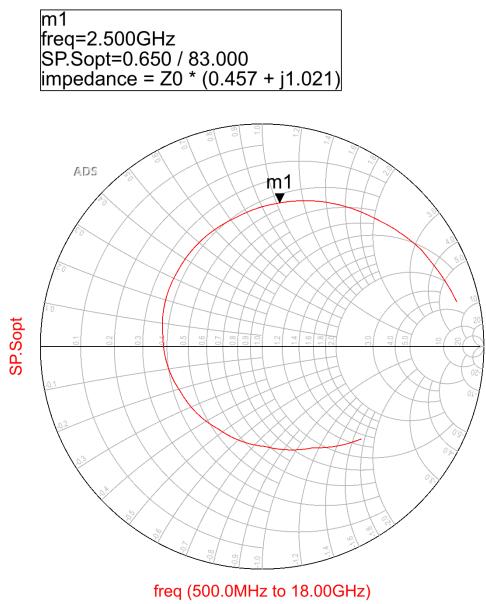
d)



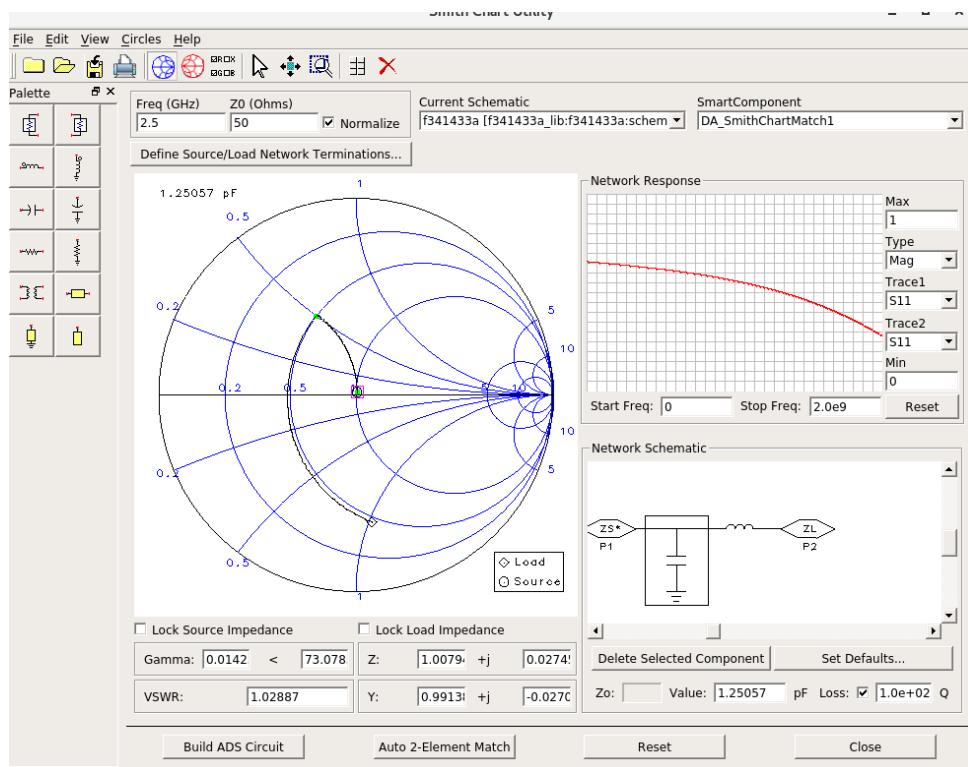
Frequencies lower than 6.31 GHz are unstable. Higher frequencies are stable.

## Problem 2: Low-Noise Amplifier

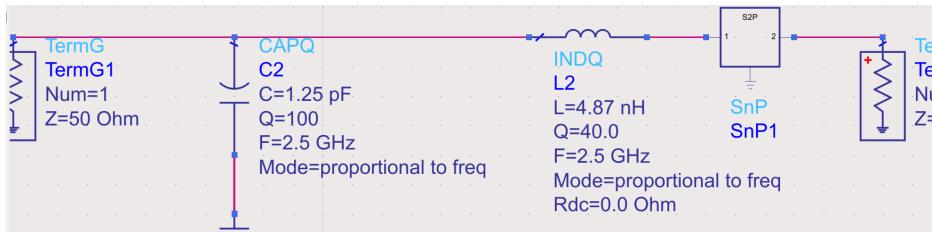
Finding gamma opt for the ATF-34143 at 2.4 GHz:



The above shows the  $Z_s$  that correspond to  $\gamma_{\text{opt}}$ . Below, the smith chart is used to match  $Z_s^*$  to  $Z_0$ . For  $Q(\text{ind}) = 40$  and  $Q(\text{cap}) = 100$ ,  $L = 4.87 \text{ nH}$  and  $C = 1.25 \text{ pF}$ .

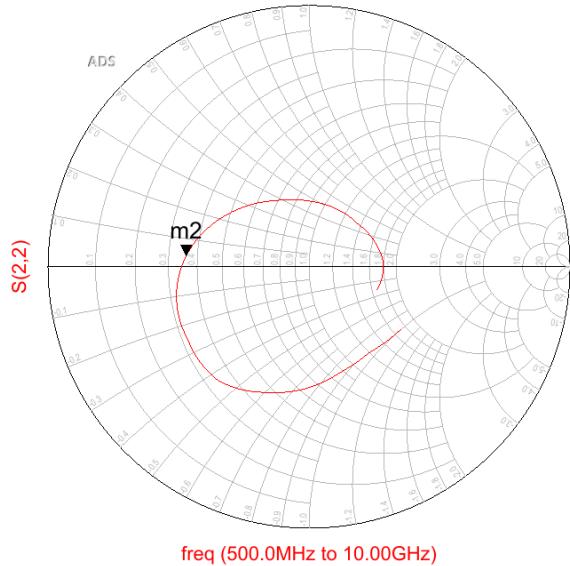


The circuit now looks like:

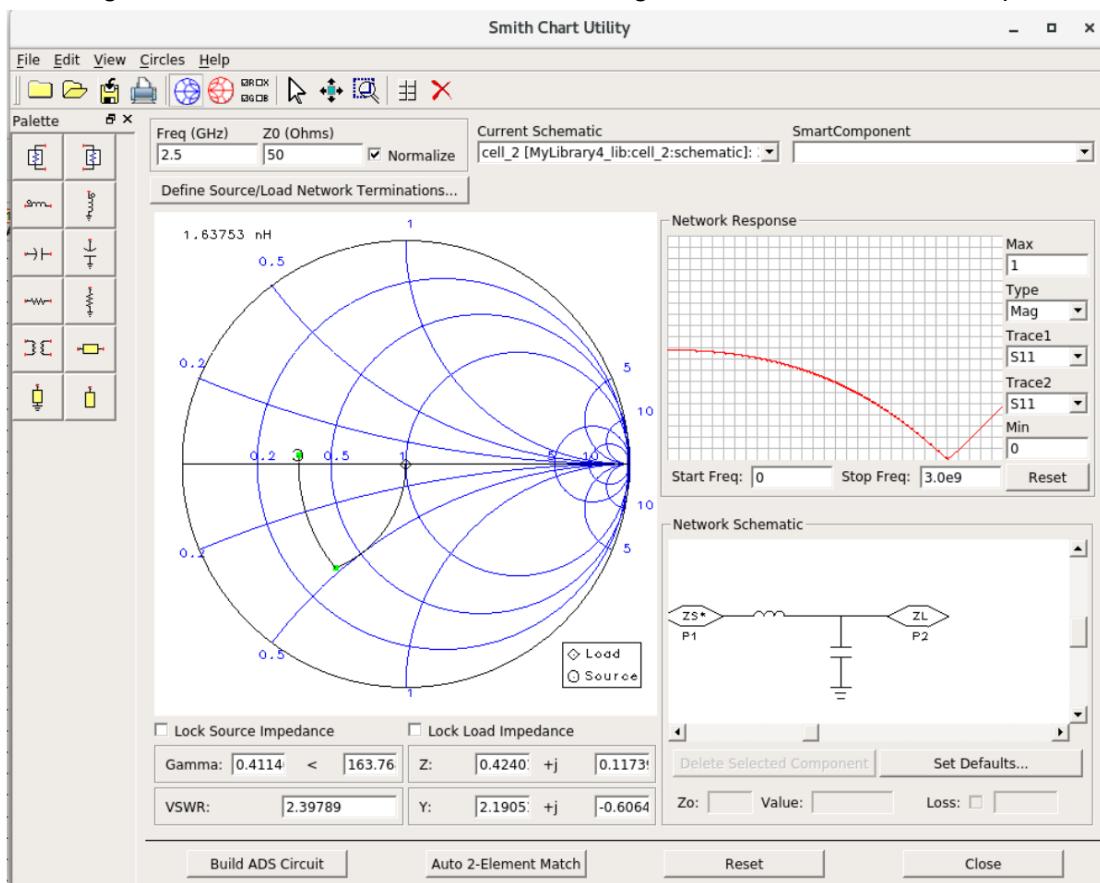


Next, we need to design a matching network for the output. Finding Gamma(out) and the corresponding Zout:

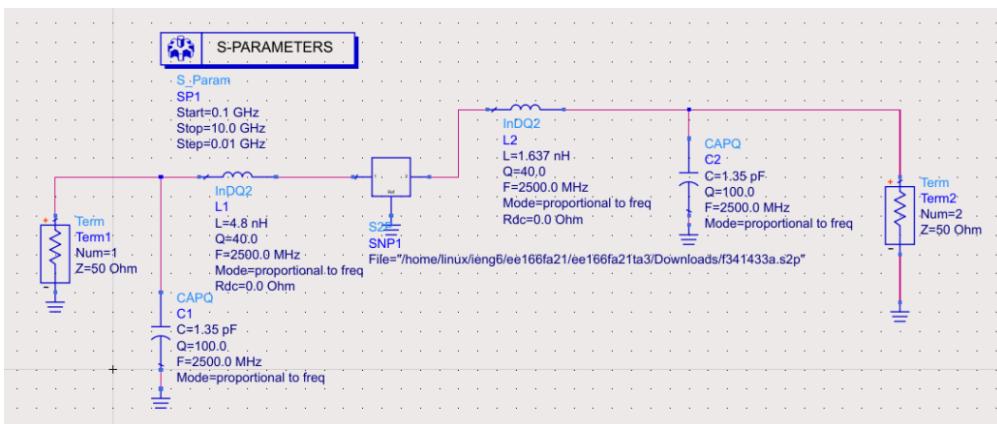
```
m2
freq=2.500GHz
S(2,2)=0.473 / 174.827
impedance = Z0 * (0.359 + j0.039)
```



Matching  $Z_{out}^*$  to  $Z_0$  with finite Q's included, we get  $L = 1.637 \text{ nH}$ ,  $C = 1.735 \text{ pF}$

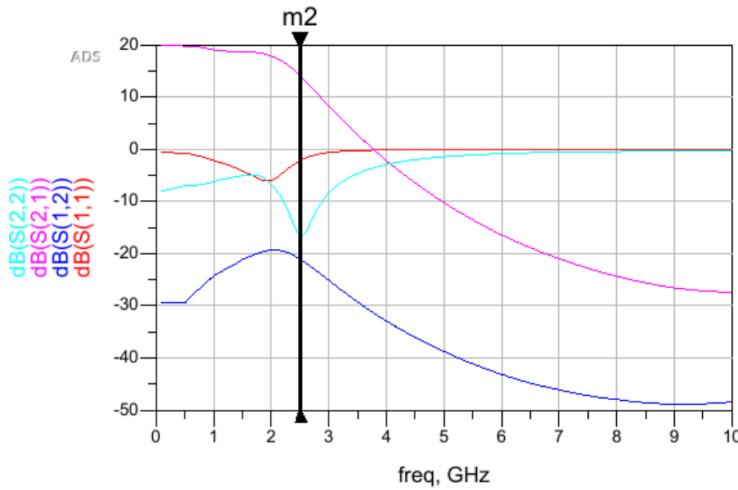


Final circuit is now:



The S-parameters are:

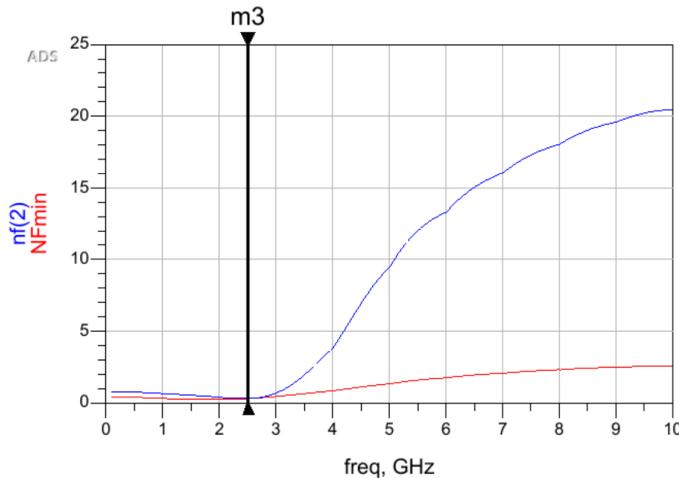
|                    |
|--------------------|
| m2                 |
| freq=2.500GHz      |
| dB(S(1,1))=-2.112  |
| dB(S(1,2))=-21.055 |
| dB(S(2,1))=14.099  |
| dB(S(2,2))=-16.587 |

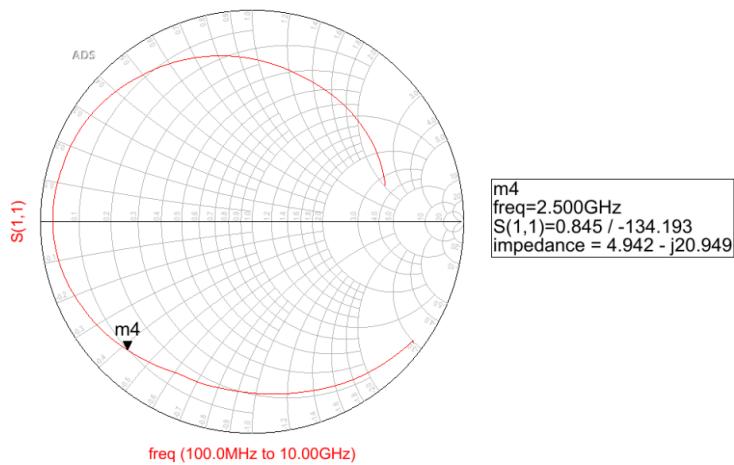
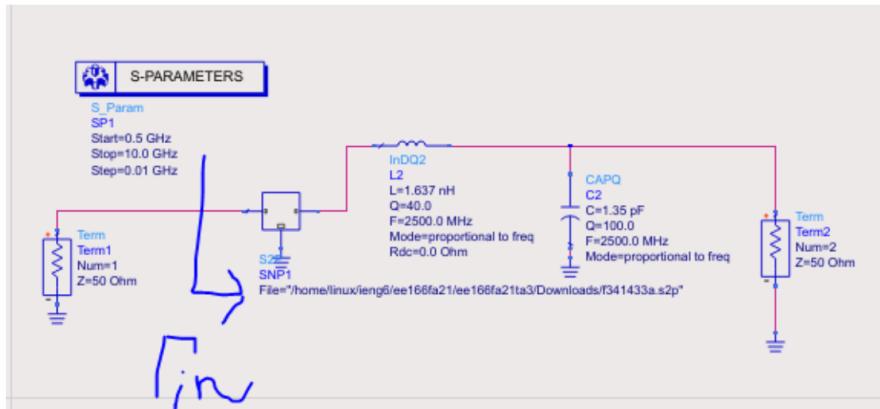


This is close to what the data sheet parameters are, so the amplifier is correctly designed. S21 is the gain, 14 dB at 2.5 GHz which agrees with Ga on the datasheet. The output match level is S22 @2.5GHz = -16.59 dB. The input match level is S11 @2.5GHz = -2.11 dB.

NF:

|               |
|---------------|
| m3            |
| freq=2.500GHz |
| NFmin=0.294   |
| nf(2)=0.298   |



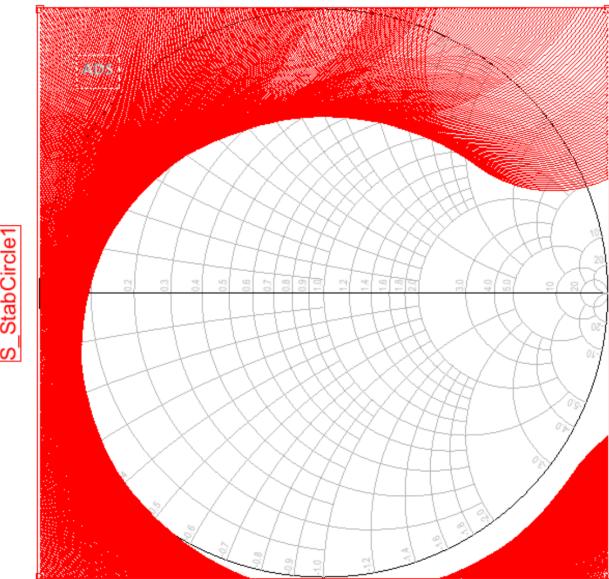
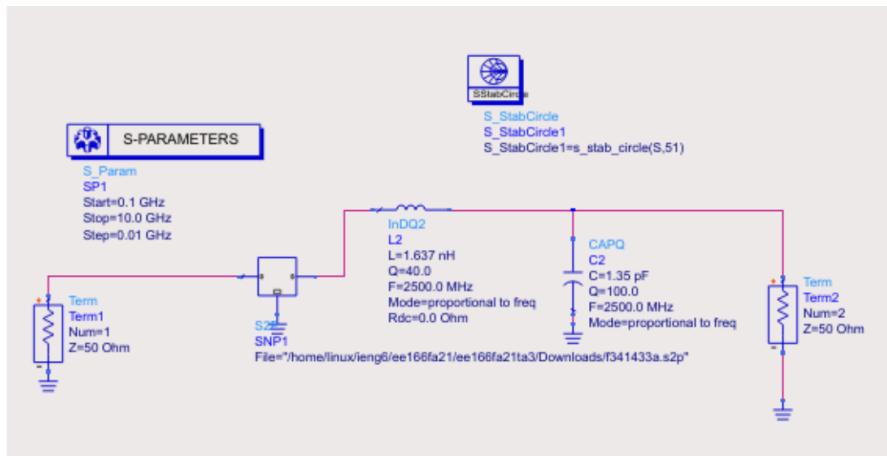


Above is gamma\_in @2.5GHz. Gamma\_I is the conjugate of gamma\_out, which was measured earlier. Therefore, gamma\_I is  $0.489\exp(-1i*174\text{deg})$ . We now know gamma\_in, gamma\_out, gamma\_I, and gamma\_opt.

Now, we need to check that the LNA is stable at all frequencies.

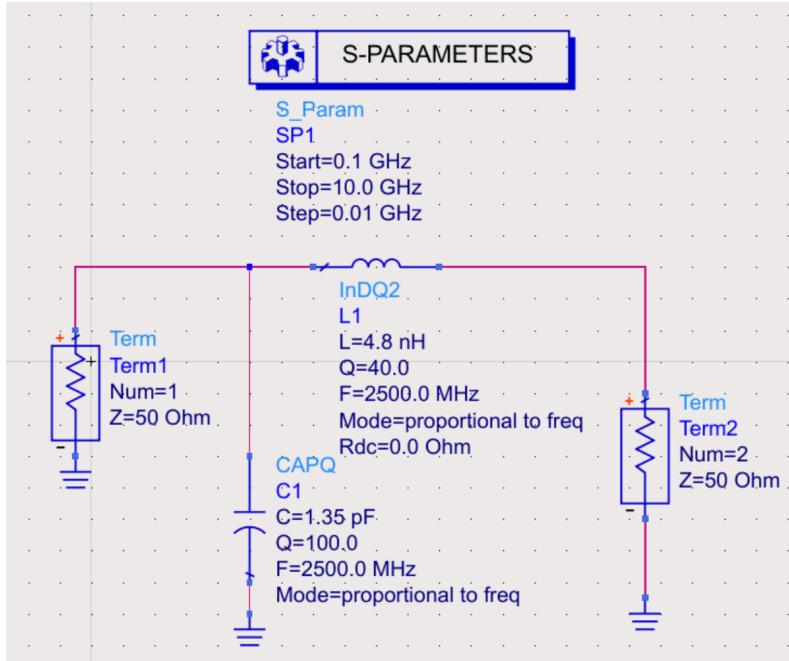
## Stability Adjustments

A source stability circle is generated to find the region where gamma\_s will be stable.

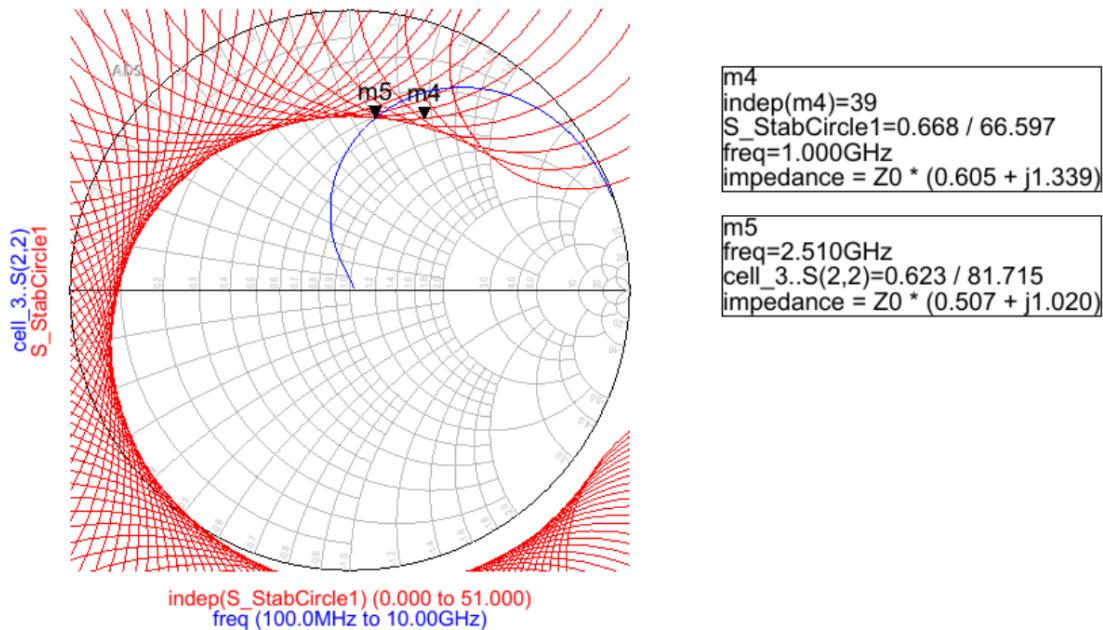


Indep(S\_StabCircle1) (0.000 to 51.000)

For stability, the S22 curve of the input matching network must not intersect at the same frequency of the red region above.

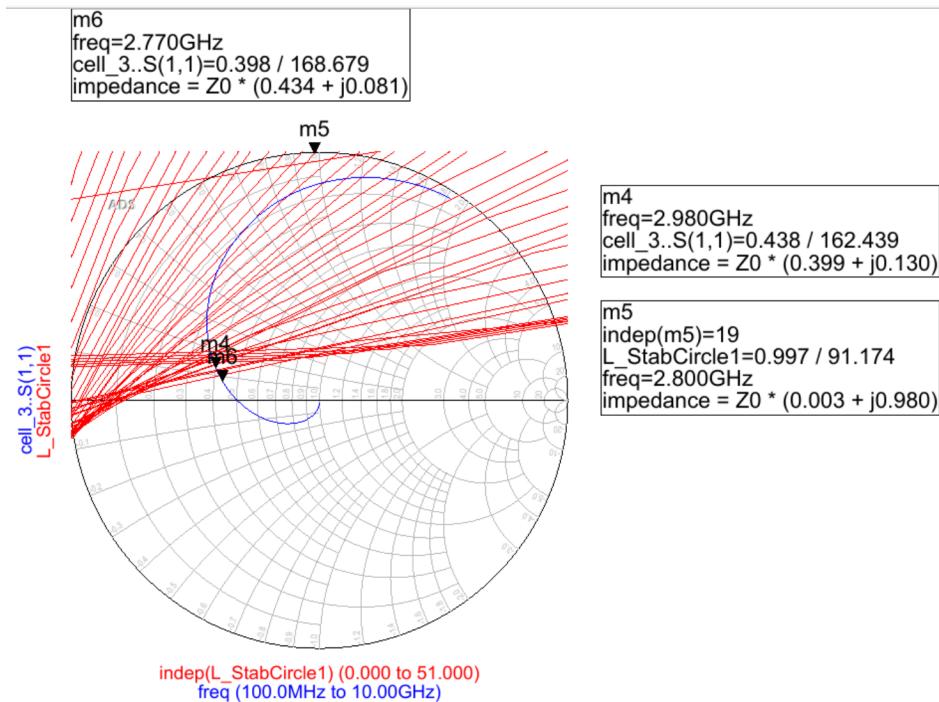
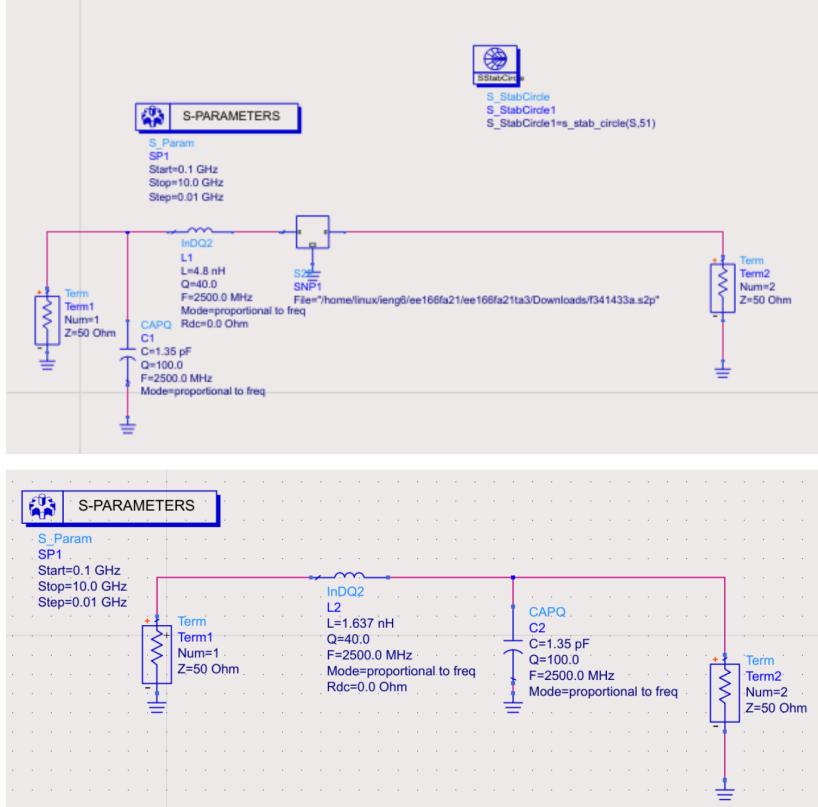


Plotting with less curves to make it more clear:



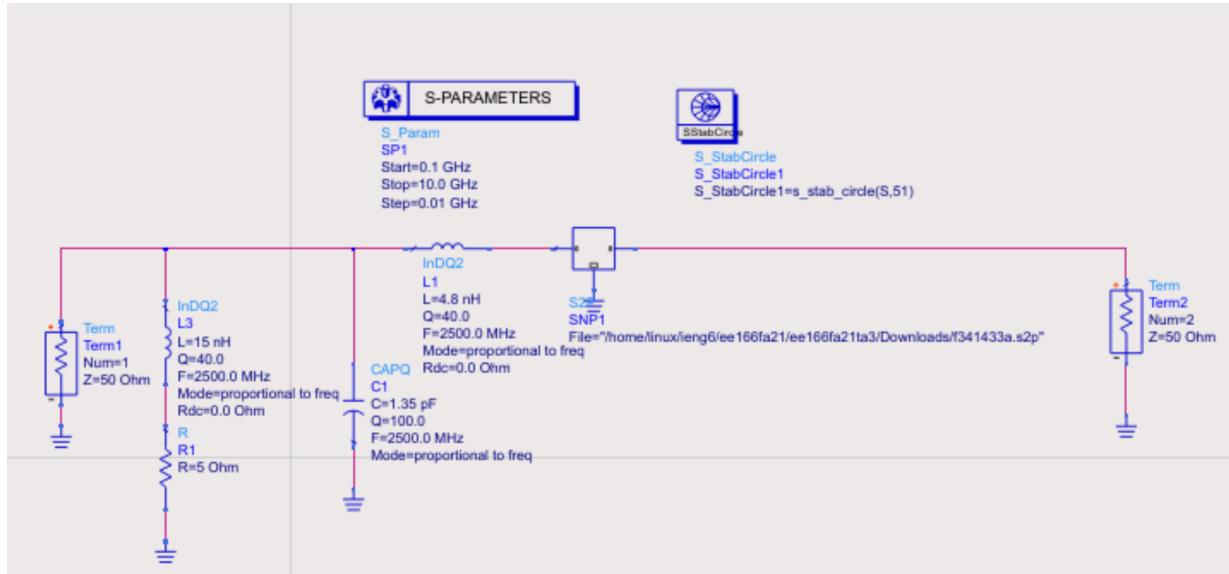
The red curve which intersects with m5 is the highest frequency of the stability circle. This is much lower than the S22 circle frequencies in that region, so it will be conditionally stable. This is different from unconditionally stable, in which all the red circles would be outside the smith chart. This only happens when  $k>1$ .

Doing the same for the output network, we use L\_StabCircle to generate load stability circles.

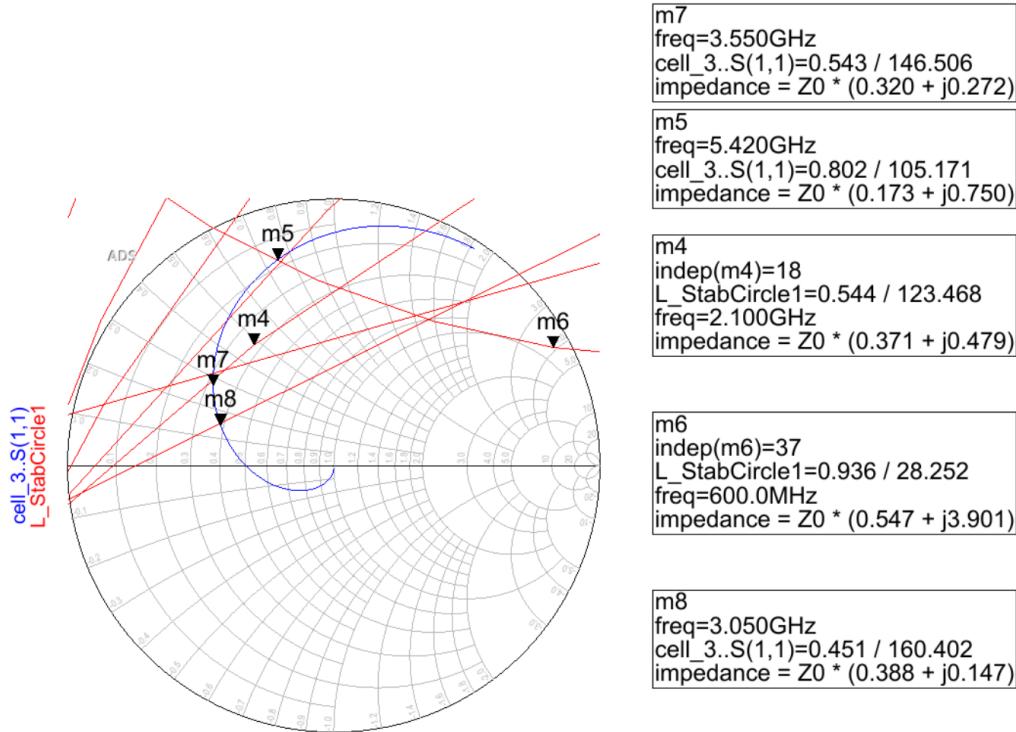


This is clearly unstable because some of the curves are very close to each other in frequency on their intersection.

To fix this, we introduce a large shunt inductor in series with a small resistor.

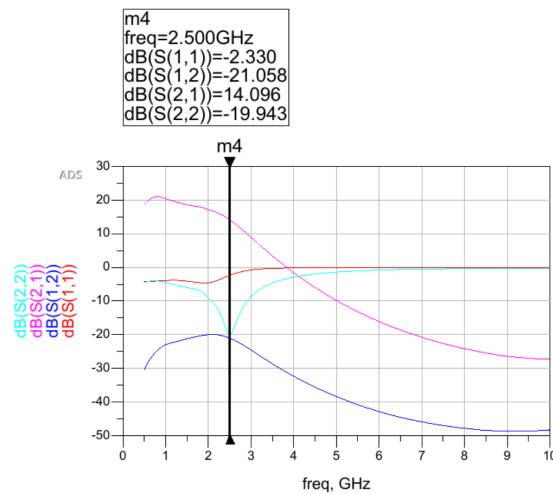
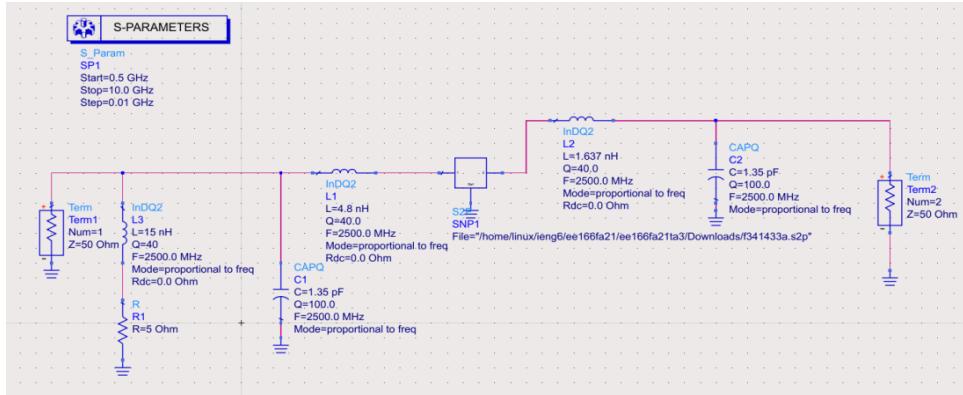


Taking a look at the stability circles again:

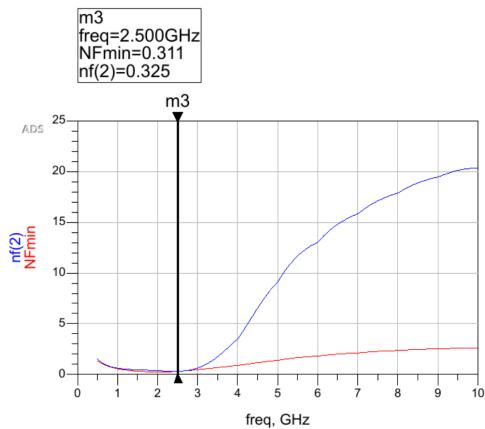


The amplifier is now clearly conditionally stable, as there is plenty of headroom in frequency between the red curves and blue curves.

Now, we will plot the S-parameters again to see what effect the stability adjustments had. This effect should be negligible. The final circuit is below:



The noise figure is slightly worse because of the addition of a resistor, but it is still within acceptable range. The amplifier design is complete.



### Problem 3: High-Gain Amplifier

The S parameters of the amplifier @5.5GHz are below:

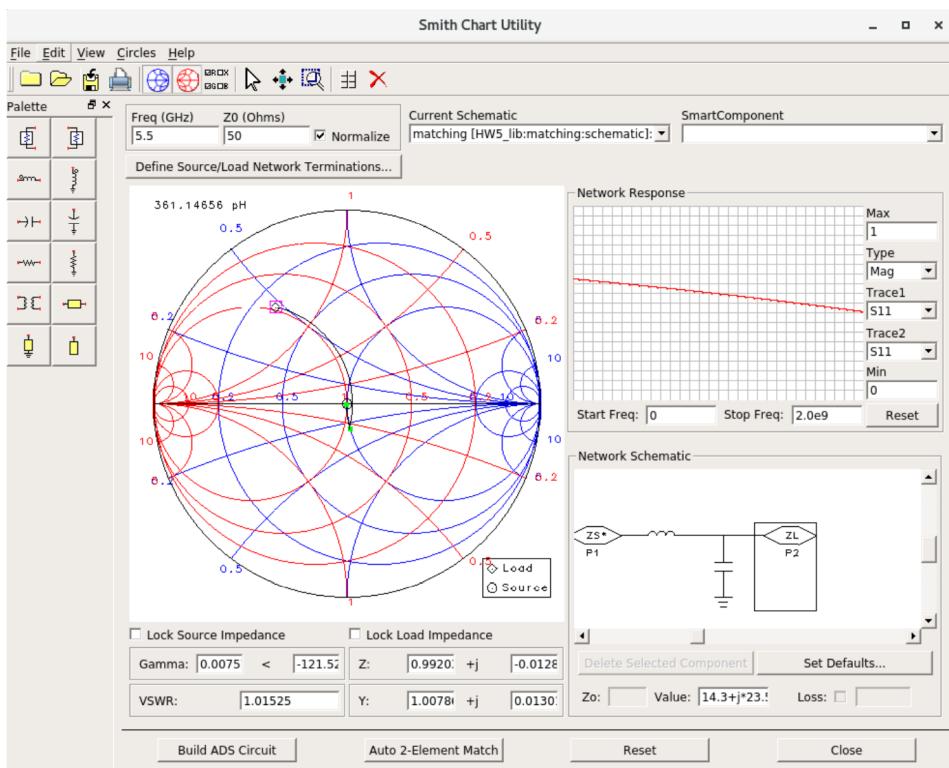
| freq      | S(1,1)          | S(1,2)          | S(2,1)        | S(2,2)          | u     |
|-----------|-----------------|-----------------|---------------|-----------------|-------|
| 5.500 GHz | 0.645 / 126.500 | 0.122 / -28.000 | 2.936 / 5.500 | 0.225 / 132.000 | 0.094 |

$$\text{Eqn } u = (\text{mag}(S(1,1)) * \text{mag}(S(2,1)) * \text{mag}(S(1,2)) * \text{mag}(S(2,2))) / ((1 - \text{pow}(\text{mag}(S(1,1)), 2)) * (1 - \text{pow}(\text{mag}(S(2,2)), 2)))$$

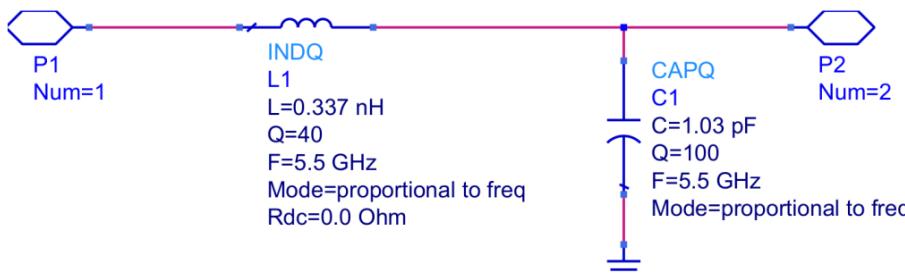
u is around 0.1, so we can use the unilateral approximation for matching:

Gamma\_s = S(1,1)\* and Gamma\_l = S(2,2)\*

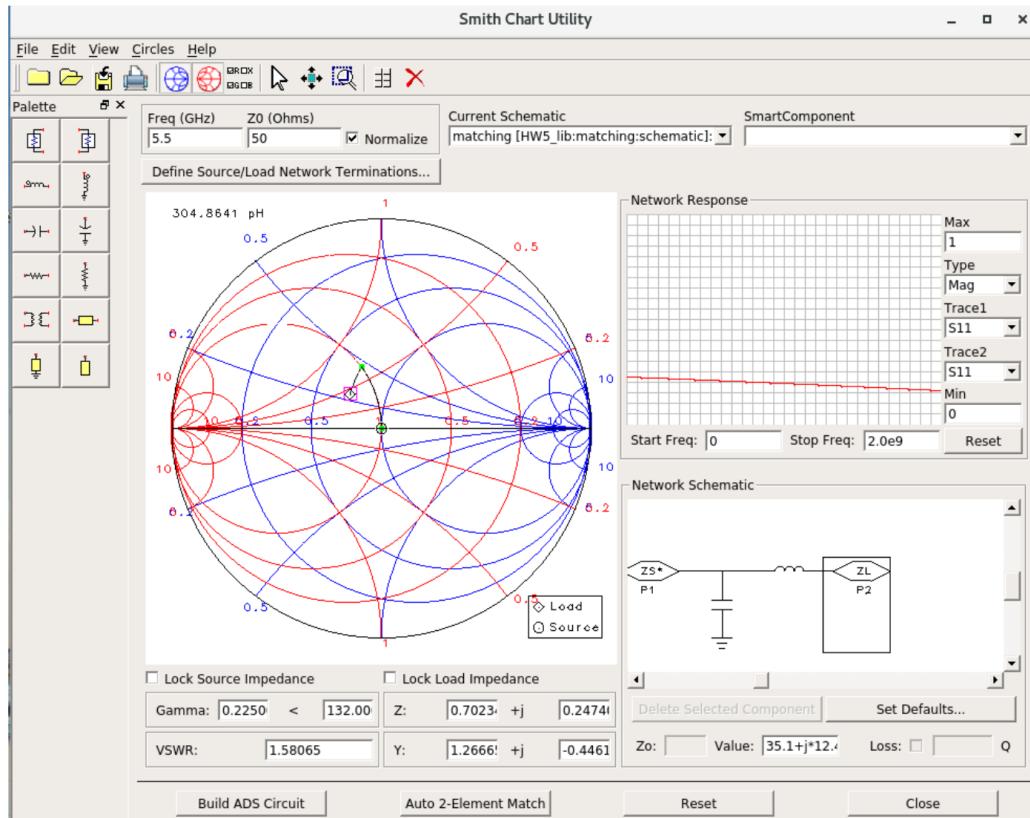
Matching gamma\_s with S(1,1):



We get the matching network for the source below:

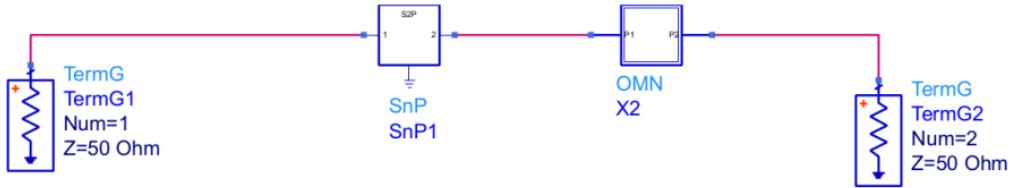


Next we match gamma\_I to get the load matching network:



Now, we look at the stability for 0.1GHz to 10GHz.

First, the s stab circles for gamma\_s:



### S-PARAMETERS

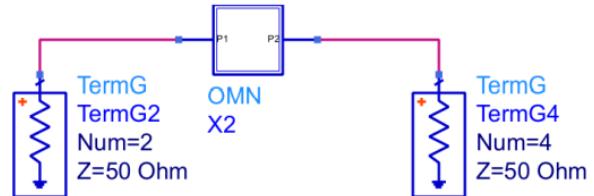
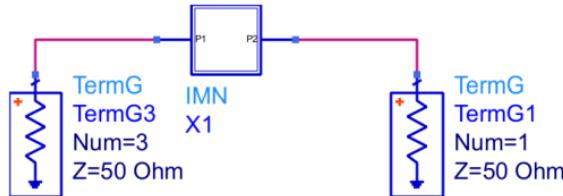
```
S_Param
SP1
Start=0 GHz
Stop=10.0 GHz
Step=0.5 GHz
```

### SStabCircle

```
S_StabCircle
S_StabCircle1
S_StabCircle1=s_stab_circle(S,51)
```

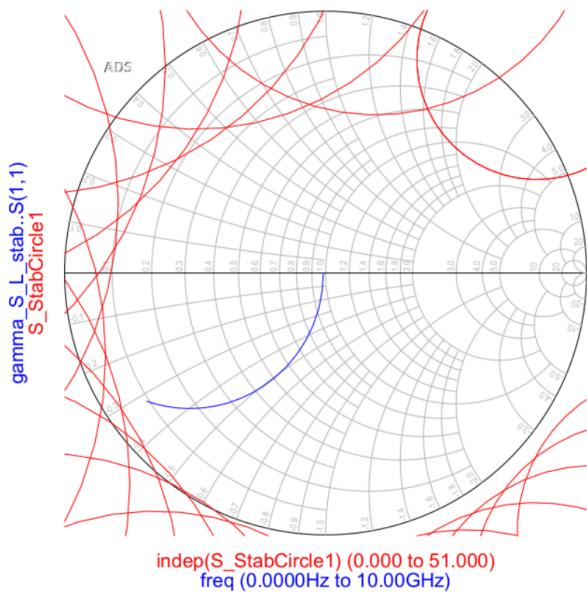
### SStabRegion

```
S_StabRegion
S_StabRegion1
S_StabRegion1=s_stab_region(S)
```



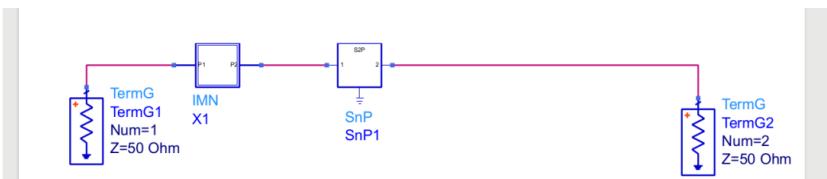
### S-PARAMETERS

```
S_Param
SP1
Start=0 GHz
Stop=10.0 GHz
Step=0.5 GHz
```



The network is stable for gamma\_s.

Now, the L stab circles for gamma\_l:

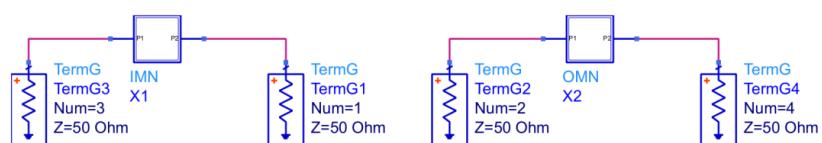


**S-PARAMETERS**

S\_Param  
SP1  
Start=0 GHz  
Stop=10.0 GHz  
Step=0.5 GHz

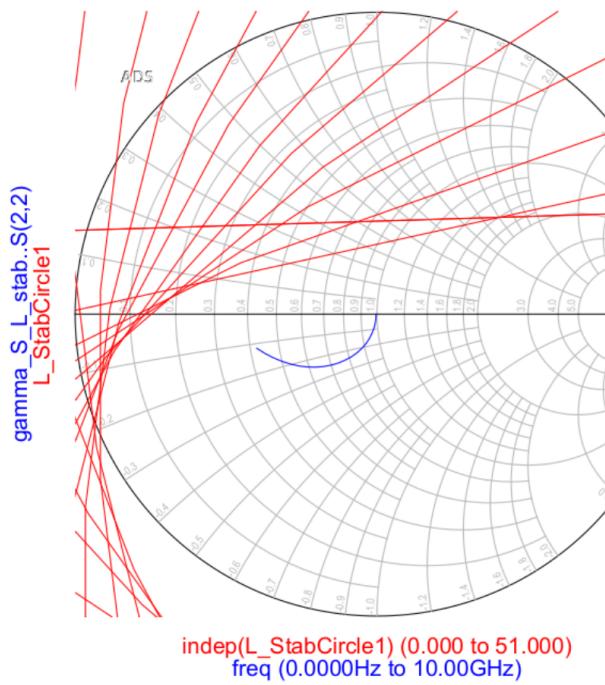
**LStabCircle**  
L\_StabCircle  
L\_StabCircle1  
L\_StabCircle1=l\_stab\_circle(S,51)

**LStabRegion**  
L\_StabRegion  
L\_StabRegion1  
L\_StabRegion1=l\_stab\_region(S)



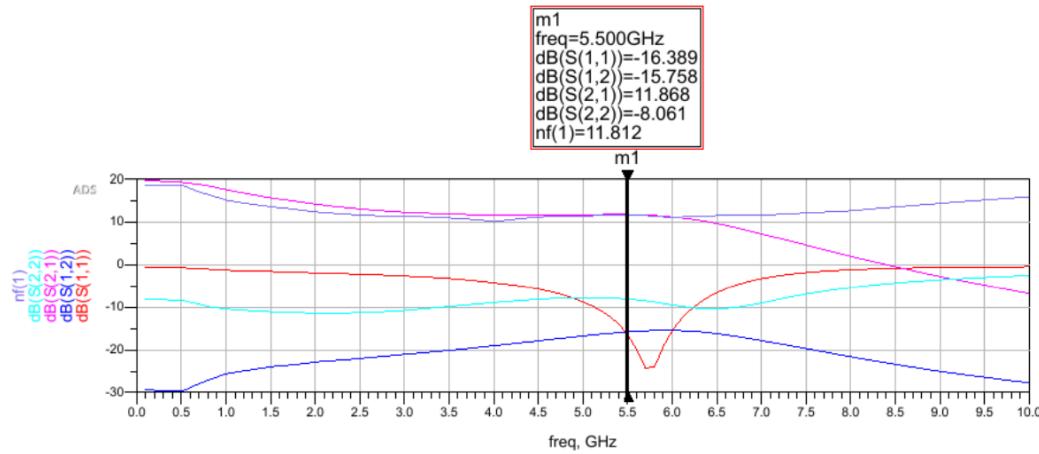
**S-PARAMETERS**

S\_Param  
SP1  
Start=0 GHz  
Stop=10.0 GHz  
Step=0.5 GHz



Gamma\_I is also stable.

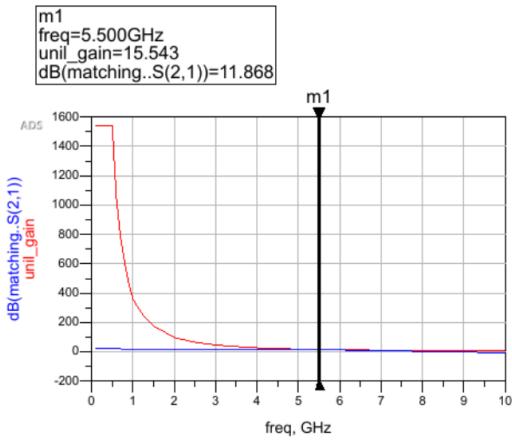
Below is the NF and gain comparison to the unilateral approximation:



We can see that this is not designed for low noise and for matching since we are using a non-ideal inductor and capacitor. It is not a perfect match for S11 and S22.

Comparing the gains:

Eqn unil\_gain =  $\text{pow}(\text{mag}(S(2,1)), 2) / (((1 - \text{pow}(\text{mag}(S(1,1)), 2)) * (1 - \text{pow}(\text{mag}(S(2,2)), 2))))$  using the S parameters of the amplifier before matching



It is 4dB lower than max unilateral gain.