

Clustering & PCA

```
#Load data
```

```
customers = read.csv('~/.Downloads/Mall_Customers.csv')
```

```
summary(customers)
```

```
##      CustomerID      Gender      Age      Annual.Income..k...
##  Min.       :  1.00   Length:200     Min.       :18.00   Min.       : 15.00
##  1st Qu.: 50.75   Class :character  1st Qu.:28.75   1st Qu.: 41.50
##  Median :100.50   Mode  :character  Median :36.00   Median : 61.50
##  Mean    :100.50                      Mean    :38.85   Mean     : 60.56
##  3rd Qu.:150.25                      3rd Qu.:49.00   3rd Qu.: 78.00
##  Max.     :200.00                      Max.     :70.00   Max.     :137.00
##  Spending.Score..1.100.
##  Min.       : 1.00
##  1st Qu.:34.75
##  Median :50.00
##  Mean    :50.20
##  3rd Qu.:73.00
##  Max.     :99.00
```

```
# Change name of 2 variables
```

```
names(customers)[4] <- paste('AnnualIncome')
```

```
names(customers)[5] <- paste('SpendingScore')
```

```
customers$Gender = as.factor(customers$Gender)
```

```
# Ignore customer ID since it does not have any relationship with other variables
```

```
customers <- customers[,2:5]
```

```
summary(customers)
```

```
##      Gender      Age      AnnualIncome      SpendingScore
##  Female:112   Min.       :18.00   Min.       : 15.00   Min.       : 1.00
##  Male   : 88   1st Qu.:28.75   1st Qu.: 41.50   1st Qu.:34.75
##                                     Median :36.00   Median : 61.50   Median :50.00
##                                     Mean    :38.85   Mean    : 60.56   Mean    :50.20
##                                     3rd Qu.:49.00   3rd Qu.: 78.00   3rd Qu.:73.00
```

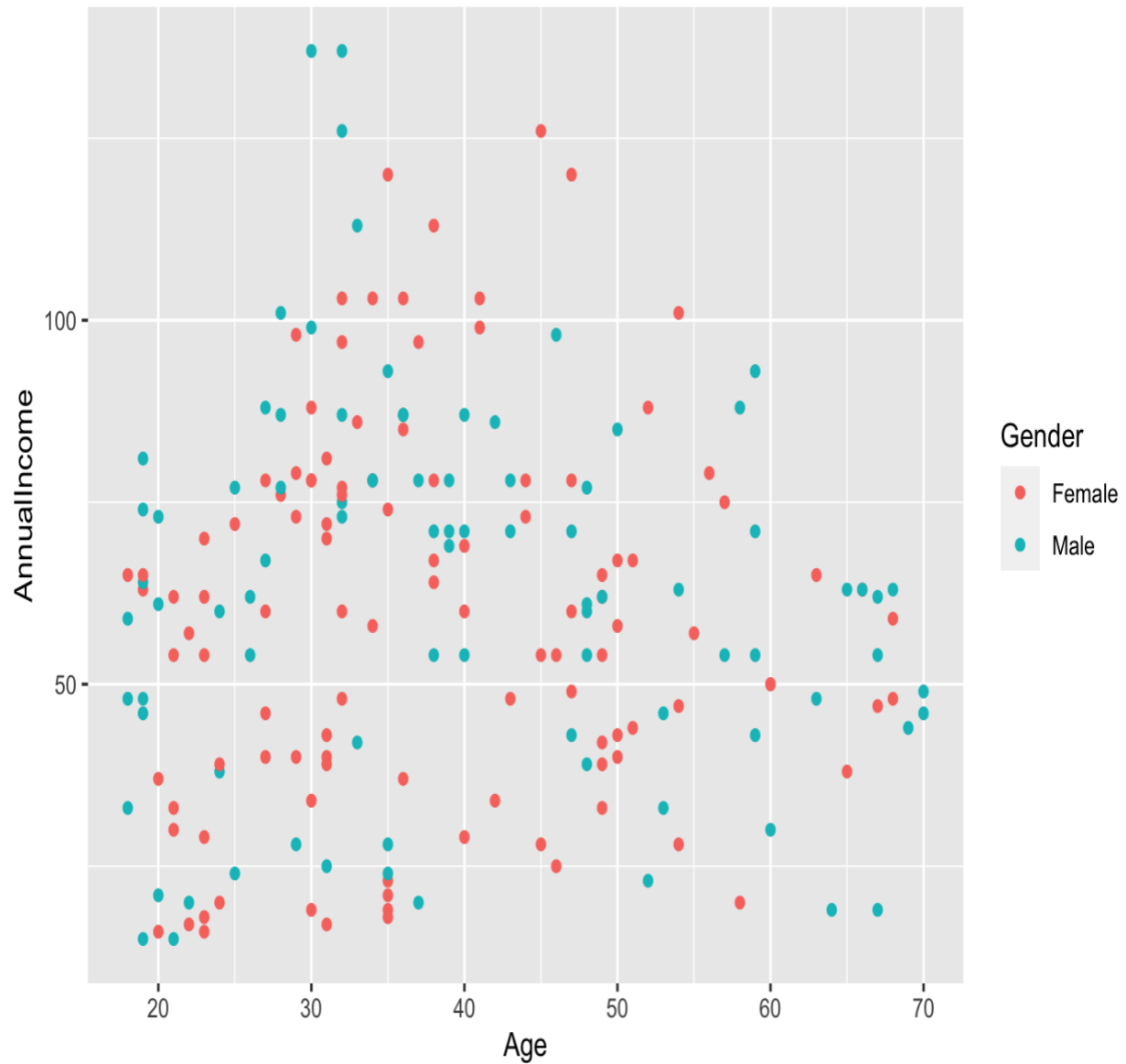
```
##                               Max.      :70.00   Max.      :137.00   Max.      :99.00
```

```
# Plot to see relationship among variables
```

```
library(ggplot2)
```

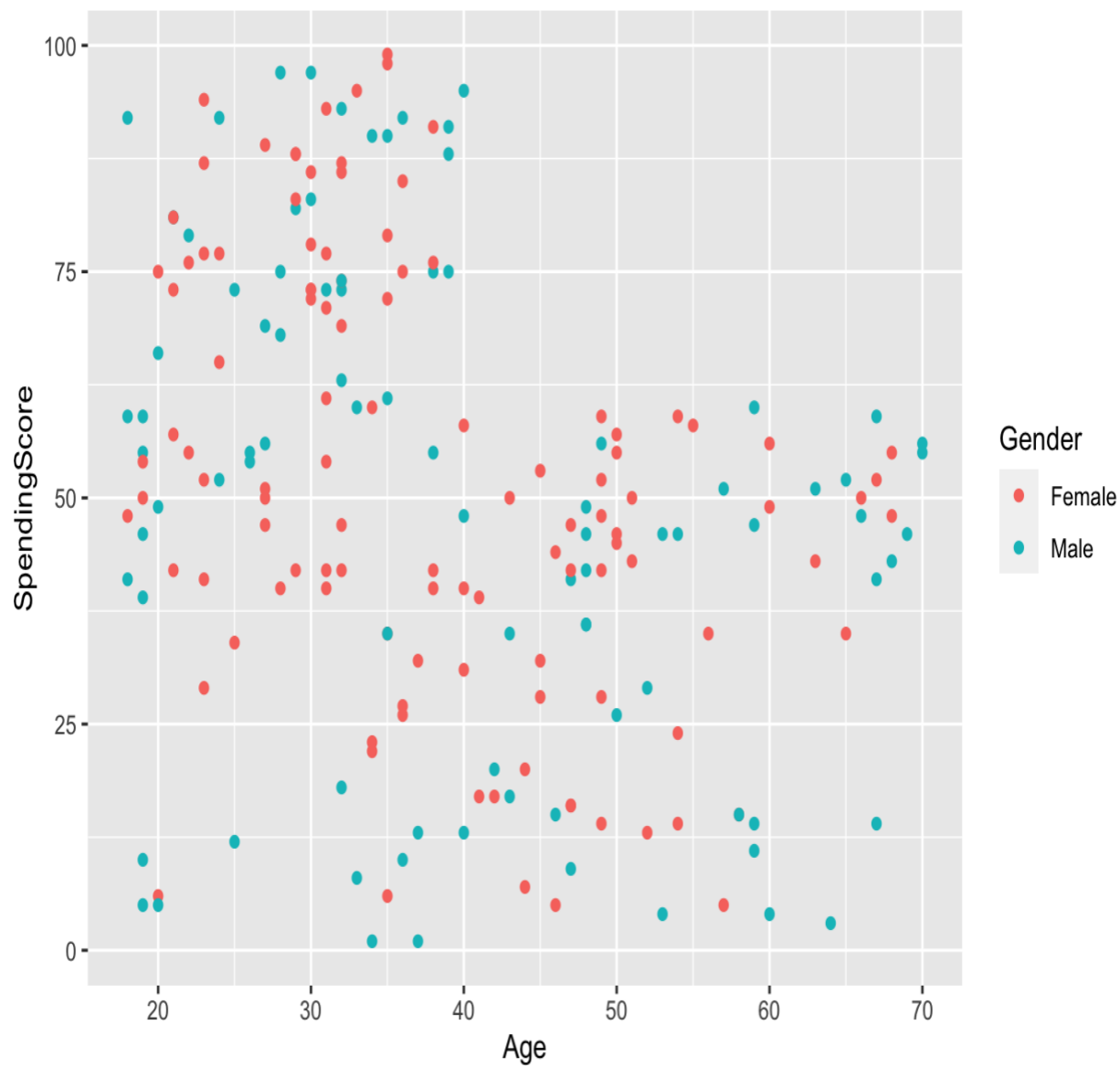
```
ggplot(customers) +
```

```
  geom_point(aes(x = Age, y = AnnualIncome, col = Gender))
```

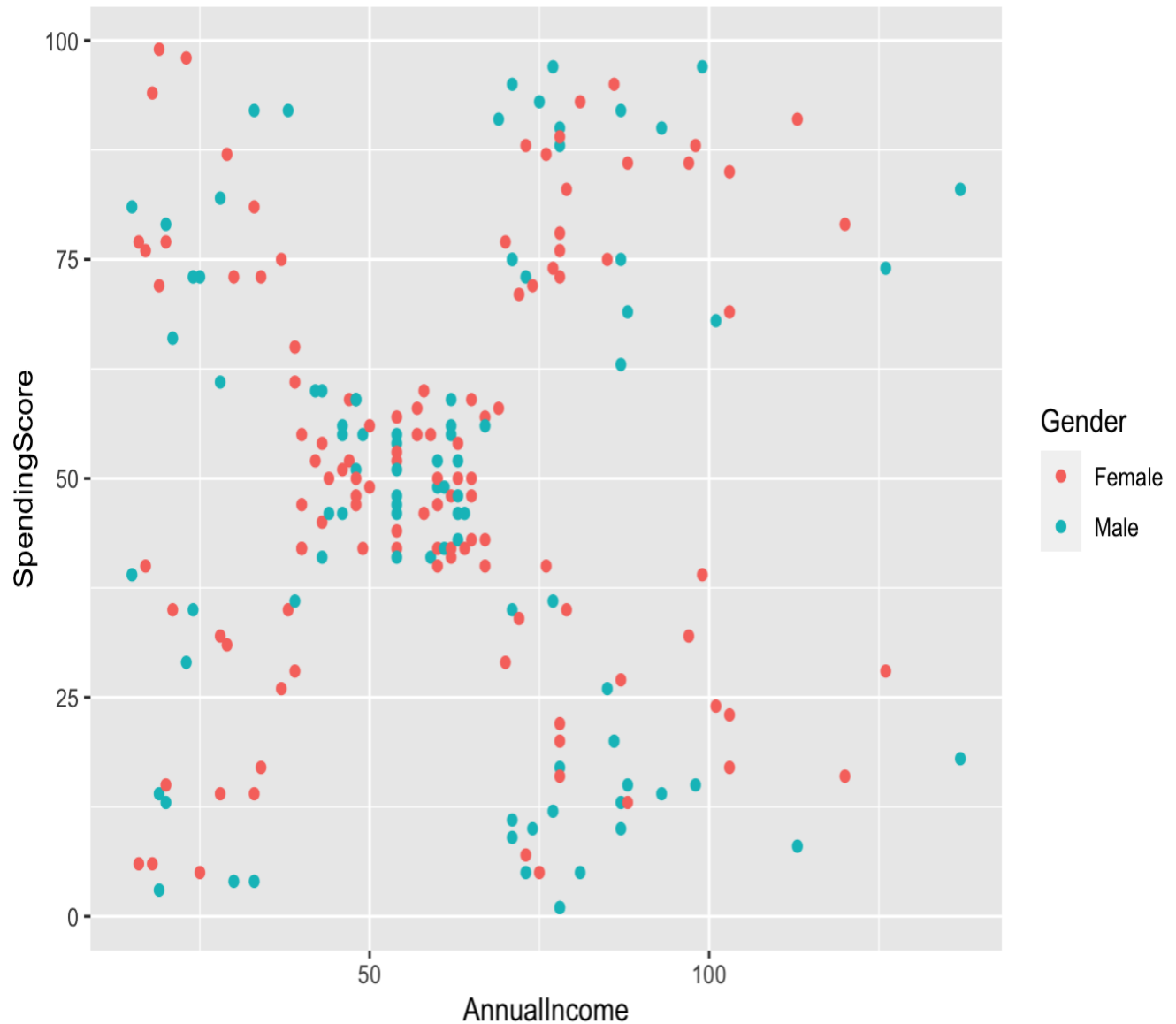


```
ggplot(customers) +
```

```
  geom_point(aes(x = Age, y = SpendingScore, col = Gender))
```



```
ggplot(customers) +  
  geom_point(aes(x = AnnualIncome, y = SpendingScore, col = Gender))
```



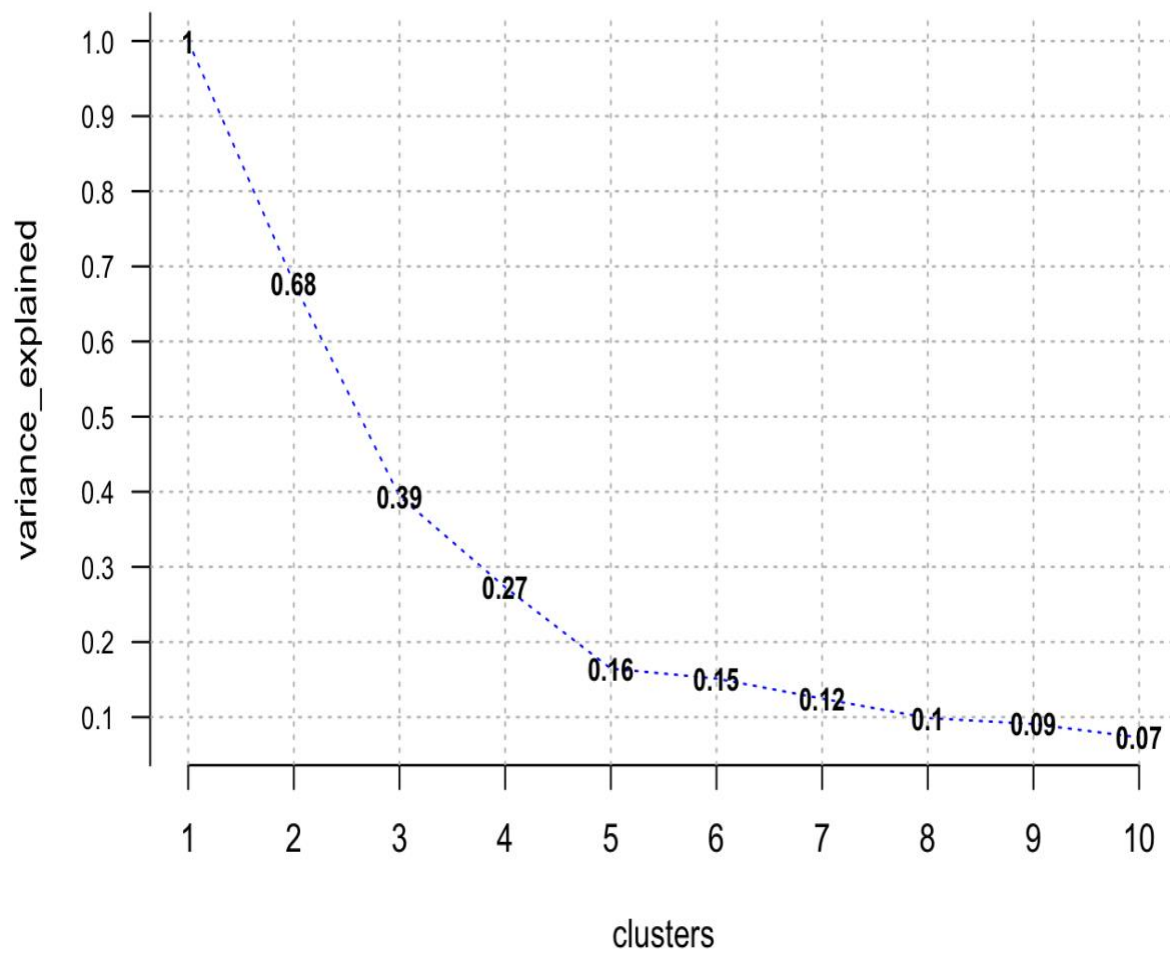
The first plot shows that the highest income are obtained by people who age from 30 to 50. The second plot demonstrates all the huge spenders are less than 40 years old. Customers above that age have the highest values of Spending Score are around 60 points. The last plot shows that observations tend to classify themselves in a couple of areas on the graph. There is a numerous group right in the middle and a few groups in the corners of the plot. Gender seems to have little effect when income and spending of customers is analysed.

7.1 Perform k-means clustering on the dataset

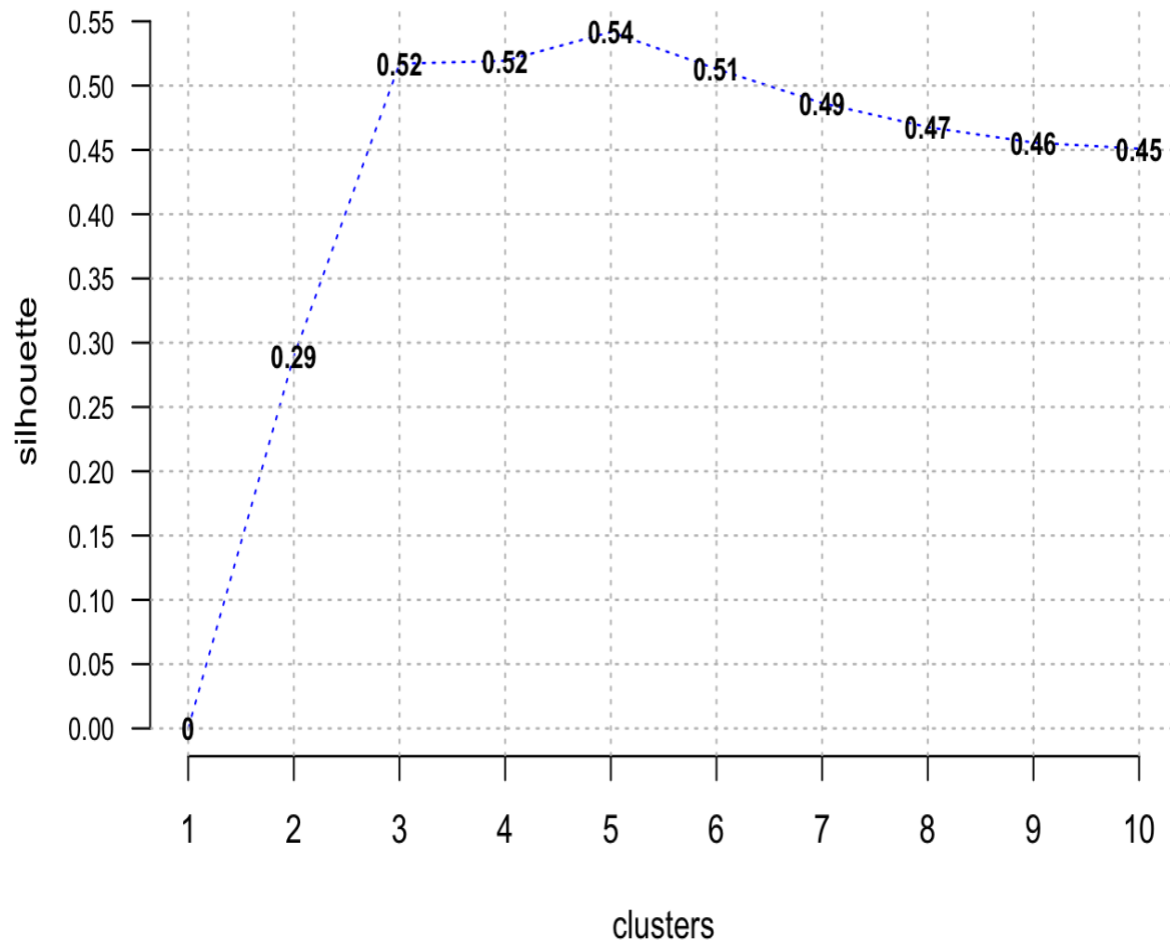
Based on the above graphs, we found out that two variables: AnnualIncome and SpendingScore are the ones that influence consumer behaviour the most. Therefore the clusters will be generated only on the basis of these two variables.

```
# Define the most optimal numbers of clusters  
library(ClusterR)
```

```
## Loading required package: gtools
##
## Attaching package: 'gtools'
## The following object is masked from 'package:e1071':
##
##      permutations
## The following object is masked from 'package:car':
##
##      logit
opt <- Optimal_Clusters_KMeans(customers[, 3:4], max_clusters = 10, plot_clusters = T)
```



```
# Use another method to define optimal number of clusters  
opt <- Optimal_Clusters_KMeans(customers[, 3:4], max_clusters = 10, plot_clusters = T, criterion = 'silhouette')
```



The highest average silhouette value (equal to 0.54) is present for $k = 5$. Therefore we should opt for 5 clusters in our further analysis with k-means algorithm.

```
set.seed(22)

# Perform k-means clustering on the dataset
km <- kmeans(customers[,3:4], 5)
customers$ClusterNumber <- km$cluster
km

## K-means clustering with 5 clusters of sizes 35, 81, 23, 22, 39
##
## Cluster means:
```

```

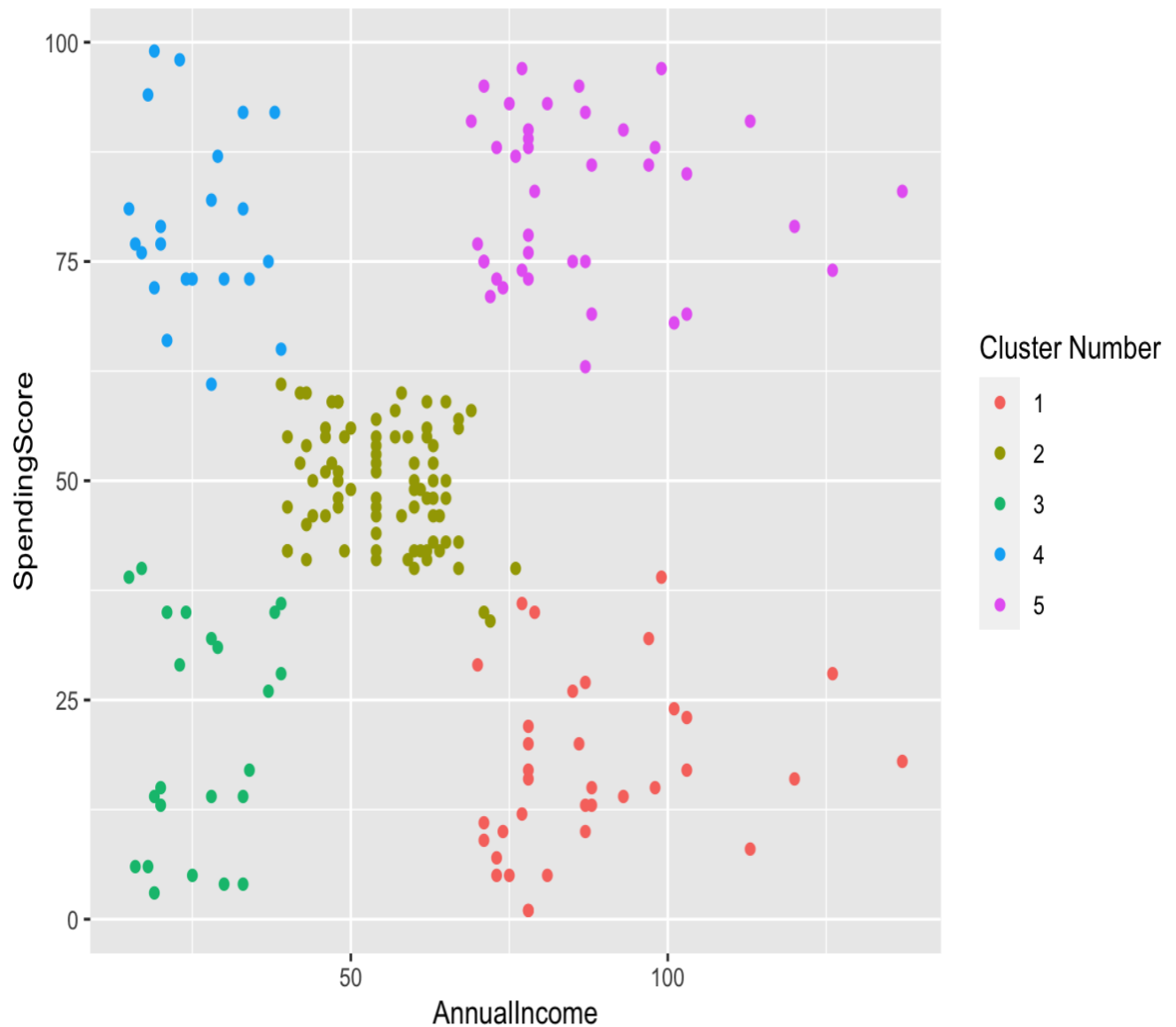
## AnnualIncome SpendingScore
## 1      88.20000      17.11429
## 2      55.29630      49.51852
## 3      26.30435      20.91304
## 4      25.72727      79.36364
## 5      86.53846      82.12821
##
## Clustering vector:
## [1] 3 4 3 4 3 4 3 4 3 4 3 4 3 4 3 4 3 4 3 4 3 4 3 4 3 4 3 4 3 4 3 4
3
## [38] 4 3 4 3 4 3 2 3 4 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
2
## [75] 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
2
## [112] 2 2 2 2 2 2 2 2 2 2 2 2 5 1 5 2 5 1 5 1 5 2 5 1 5 1 5 1 5 1 5 2 5 1 5 1
5
## [149] 1 5 1 5 1 5 1 5 1 5 1 5 1 5 1 5 1 5 1 5 1 5 1 5 1 5 1 5 1 5 1 5
1
## [186] 5 1 5 1 5 1 5 1 5 1 5 1 5 1 5 1 5
##
## Within cluster sum of squares by cluster:
## [1] 12511.143 9875.111 5098.696 3519.455 13444.051
## (between_SS / total_SS = 83.5 %)
##
## Available components:
##
## [1] "cluster"      "centers"      "totss"        "withinss"     "tot.withinss"
"
## [6] "betweenss"    "size"         "iter"         "ifault"
summary(km)
##           Length Class  Mode
## cluster      200    -none- numeric
## centers       10    -none- numeric
## totss         1    -none- numeric
## withinss      5    -none- numeric
## tot.withinss  1    -none- numeric
## betweenss    1    -none- numeric

```



```
## size          5    -none- numeric
## iter          1    -none- numeric
## ifault        1    -none- numeric

# Plot your results
ggplot(customers[,3:5]) +
  geom_point(aes(x = AnnualIncome, y = SpendingScore, col = as.factor(ClusterNumber))) +
  scale_color_discrete(name="Cluster Number")
```



7.2 Repeat the exercise from (1) using different numbers of clusters k between $\{1, \dots, 10\}$.

For each result, extract the within-cluster sum of squares using `...$tot.withinss`. Create a scree plot (i.e., plot the sum of squares against the number of clusters) to identify the ideal number of clusters. How many clusters do you suggest we should use to group our customers?

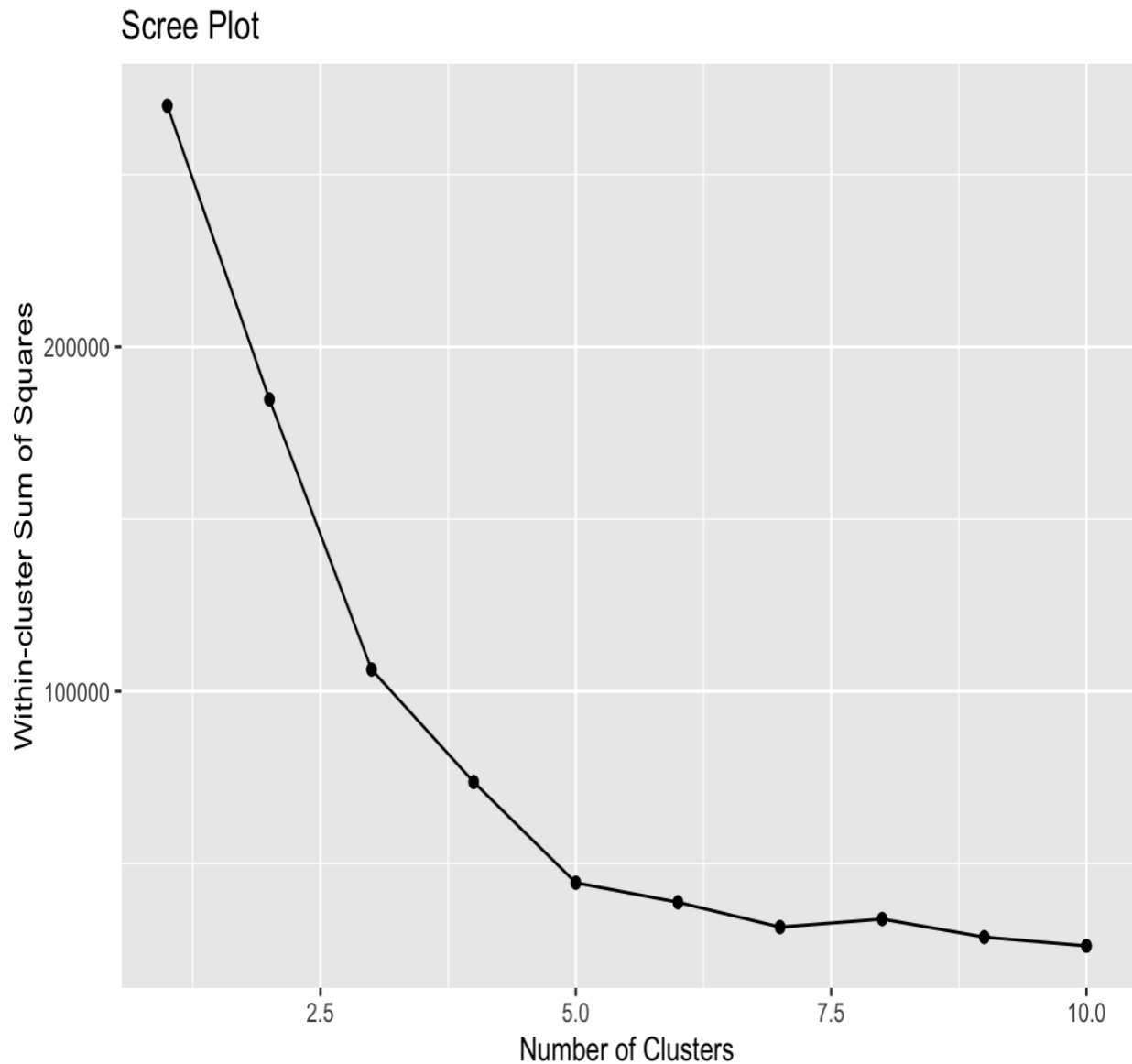
```
set.seed(1)

# Create an empty vector
wss = 0

# Use for loop to aggregate the sum of squares for 1 - 10 cluster centers
for(i in 1:10) {
  km.out <- kmeans(customers[,3:4], centers = i , nstart=1)
  #Save total within sum of squares to wss variable
  wss[i] = km.out$tot.withinss
  # For each clusters k from 1 to 10, extract the within-cluster sum of square
  s
  print(wss[i])}

## [1] 269981.3
## [1] 184740.4
## [1] 106348.4
## [1] 73679.79
## [1] 44448.46
## [1] 38788.46
## [1] 31573.82
## [1] 33908.15
## [1] 28662.93
## [1] 26115.87

# Plot a scree plot shows the total within sum of squares vs. number of clusters
qplot(1:10, wss) + geom_point() +
  geom_line() +
  xlab("Number of Clusters") +
  ylab("Within-cluster Sum of Squares") +
  ggtitle("Scree Plot")
```



```
# Set k equal to the number of clusters corresponding to the elbow location  
k = 5
```

The ideal number of clusters is the one that is located at the elbow location, which is 5.

Same results as we determined the most optimal number of cluster using silhouette method in 7.1, the result here is consistent. Therefore, I would highly suggest using 5 clusters to group customers.

7.3 In order to visualize clusters, we must reduce the dimensionality of the data.
Use principal

component analysis to generate two variables out of the four present in the dataset (ignore customer id as a variable). Find a suitable name for the variables you have generated

```

#Perform Principal Component Analysis
str(customers)

## 'data.frame':    200 obs. of  5 variables:
##  $ Gender      : Factor w/ 2 levels "Female","Male": 2 2 1 1 1 1 1 1 2 1 ...
##  $ Age         : int   19 21 20 23 31 22 35 23 64 30 ...
##  $ AnnualIncome : int   15 15 16 16 17 17 18 18 19 19 ...
##  $ SpendingScore: int   39 81 6 77 40 76 6 94 3 72 ...
##  $ ClusterNumber: int    3 4 3 4 3 4 3 4 3 4 ...

customers$Gender = as.numeric(customers$Gender)
pcclust<-prcomp(customers[, 1:4], scale=FALSE)

#Checking the summary of the PCA model
summary(pcclust)

## Importance of components:
##
##              PC1      PC2      PC3      PC4
## Standard deviation 26.4625 26.1597 12.9317 0.49548
## Proportion of Variance 0.4512 0.4409 0.1077 0.00016
## Cumulative Proportion 0.4512 0.8921 0.9998 1.00000

# Applying the PCA model on the data
pcclust$rotation[, 1:2]

##              PC1      PC2
## Gender      0.0003327282 0.001578712
## Age         0.1889772912 0.130961404
## AnnualIncome -0.5886227558 0.808388308
## SpendingScore -0.7860093664 -0.573894557

```

Results from the PCA show that components 1 and 2 (PC1 and PC2) contribute the most variance to the data. The high correlation between PC1 and spending score (-0.786) and PC2 and annual income (0.808) show that annual income and spending income are the 2 major components of the data.

These newly generated variables from PCA have got the new names in 7.1 which are AnnualIncome and SpendingScore.

7.4 Identify the clusters made up of the most valuable consumers.

Plot the customer segments based on results from the cluster analysis and PCA.

```

# Set seed to 1

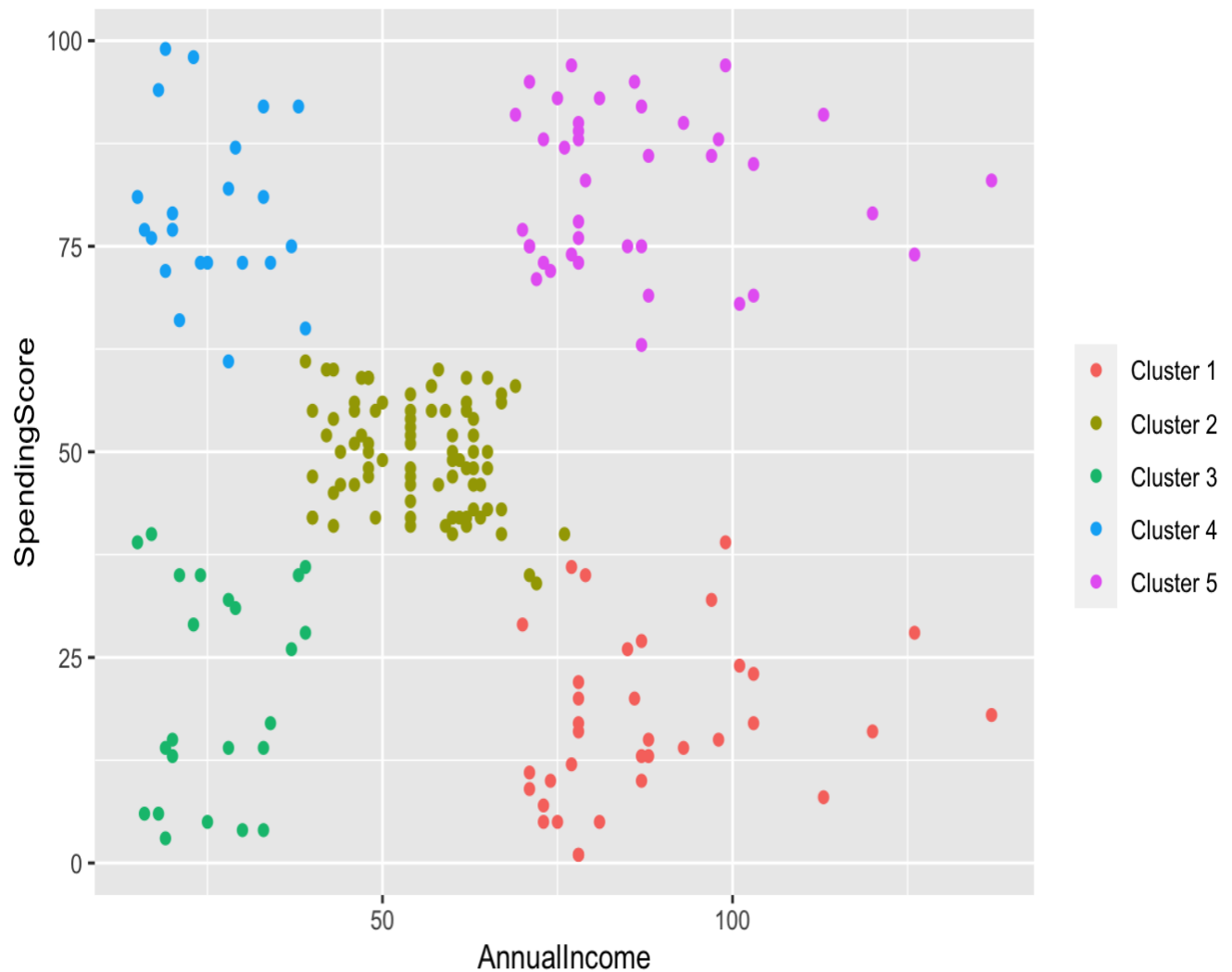
```

```
set.seed(1)

#Create a plot of the customers segments
ggplot(customers, aes(x = AnnualIncome , y = SpendingScore)) +
  geom_point(stat = "identity", aes(color = as.factor(km$cluster))) +
  scale_color_discrete(name = " ",
                       breaks=c("1", "2", "3", "4", "5"),
                       labels=c("Cluster 1", "Cluster 2", "Cluster 3",
                                "Cluster 4", "Cluster 5")) +
  ggtitle("Segments of Mall Customers",
          subtitle = "Using K-means Clustering")
```

Segments of Mall Customers

Using K-means Clustering



```
#Create a more informative plot of the customers segments
library(ggplot2)
ggplot(customers, aes(x = AnnualIncome , y = SpendingScore)) +
  geom_point(stat = "identity", aes(color = as.factor(km$cluster))) +
  scale_color_discrete(name = " ",
                        breaks=c("1", "2", "3", "4", "5"),
                        labels=c("High Income, Low Spending", "Medium Income, Medium Spending", "Low Income, Low Spending", "Low Income, High Spending", "High Income, High Spending")) +
  labs(x="Annual Income", y="Spending Score") +
  ggtitle("Segments of Mall X Customers",
```

```
subtitle = "Using K-means Clustering")
```



As the graph shown, the clusters that made up for the most valuable customers are Cluster 4,5 or the Segments “Low Income, High Spending” and “High Income, High Spending” as High Spending contributes to better revenue and profit for the business.

```
tinytex::install_tinytex()  
max_print_line = 10000
```