



FPT SCHOOL OF BUSINESS
& TECHNOLOGY

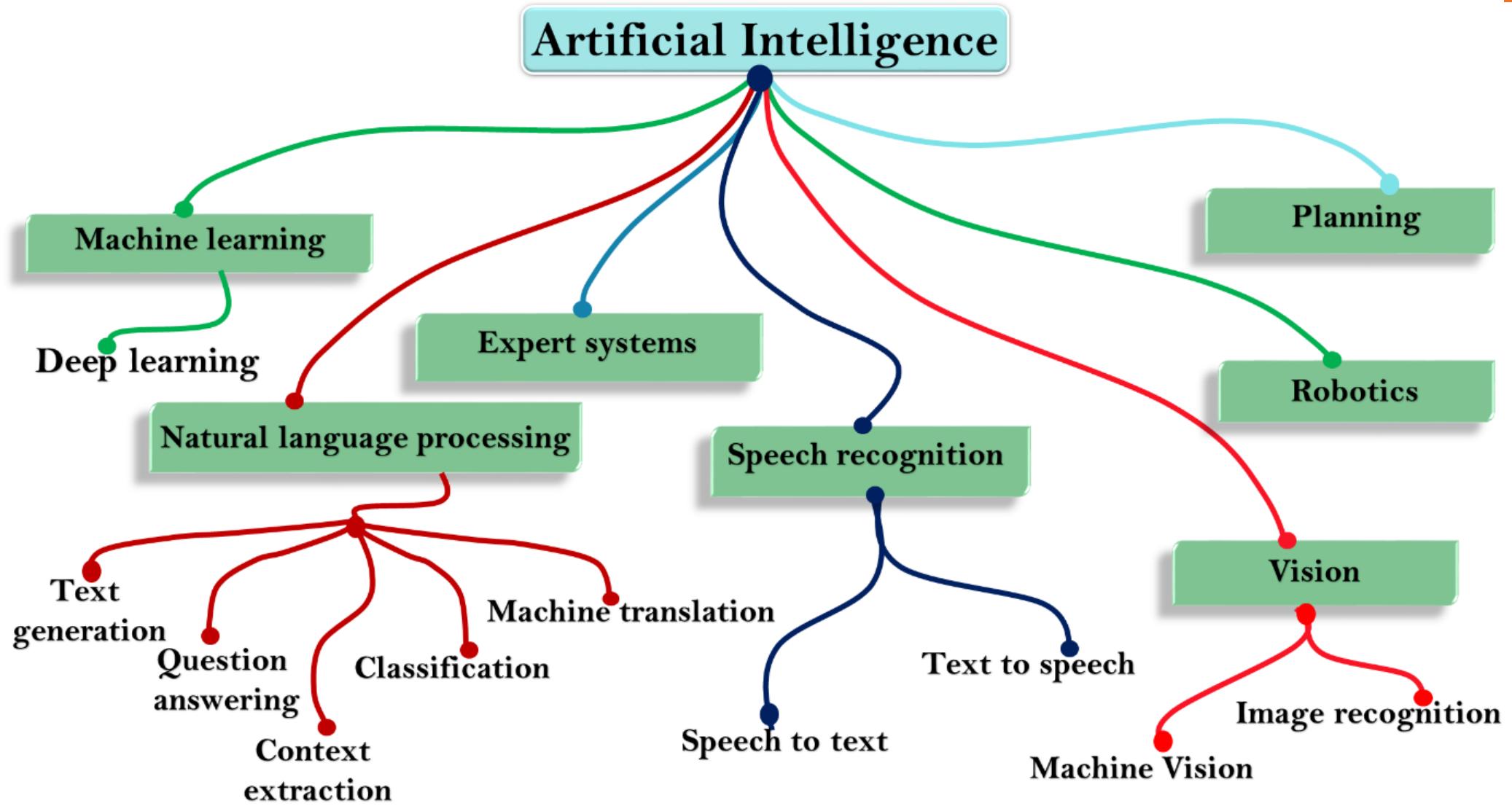
Digital Signal Processing

Giới thiệu về mạng CNN

Phd. Trần Thanh Trúc

RECAP

RECAP - AI



RECAP: AI

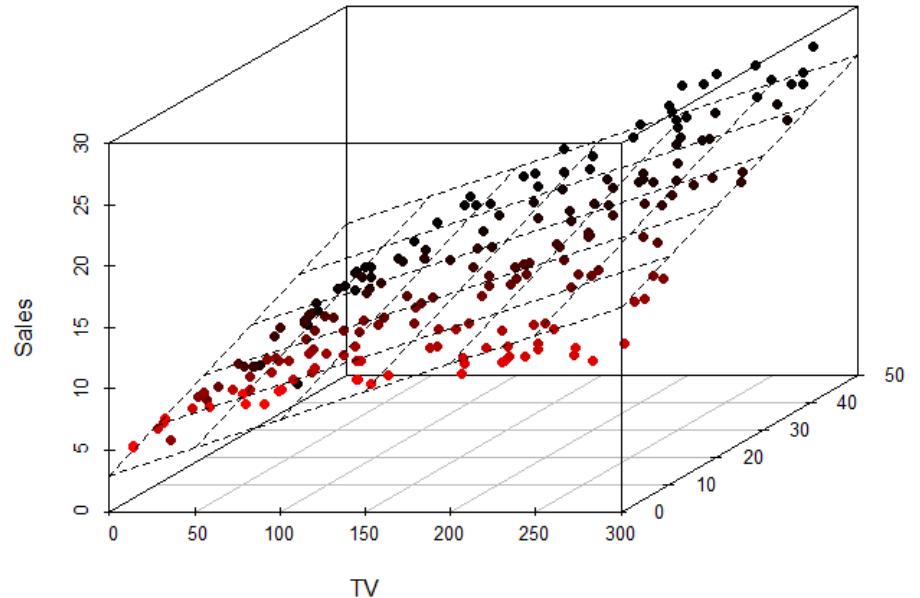
AI approaching includes 3 parts:

1. Machine Learning
2. Expert System
3. Evolution Algorithm

RECAP: LR

$$\mathbf{y} = X\boldsymbol{\beta} + \boldsymbol{\varepsilon}$$

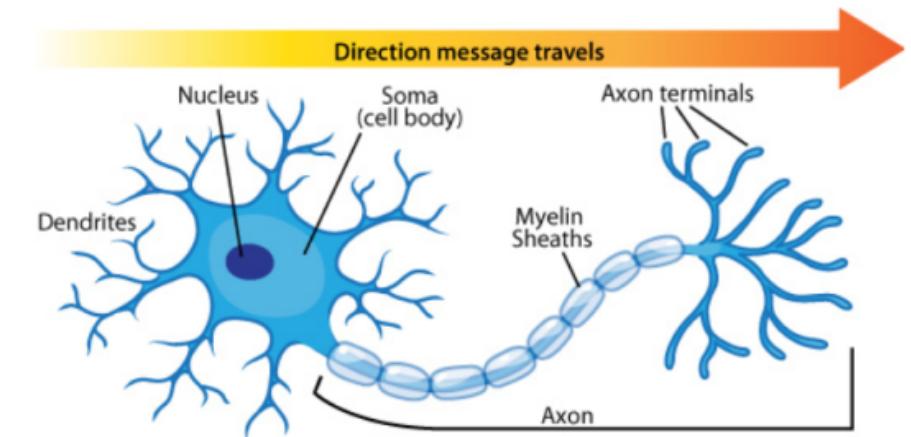
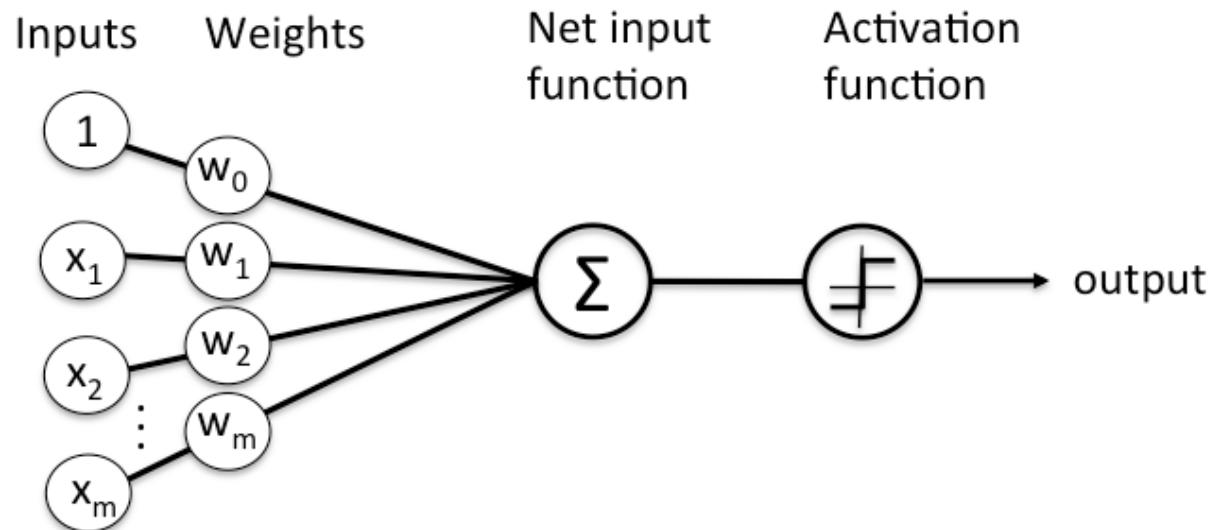
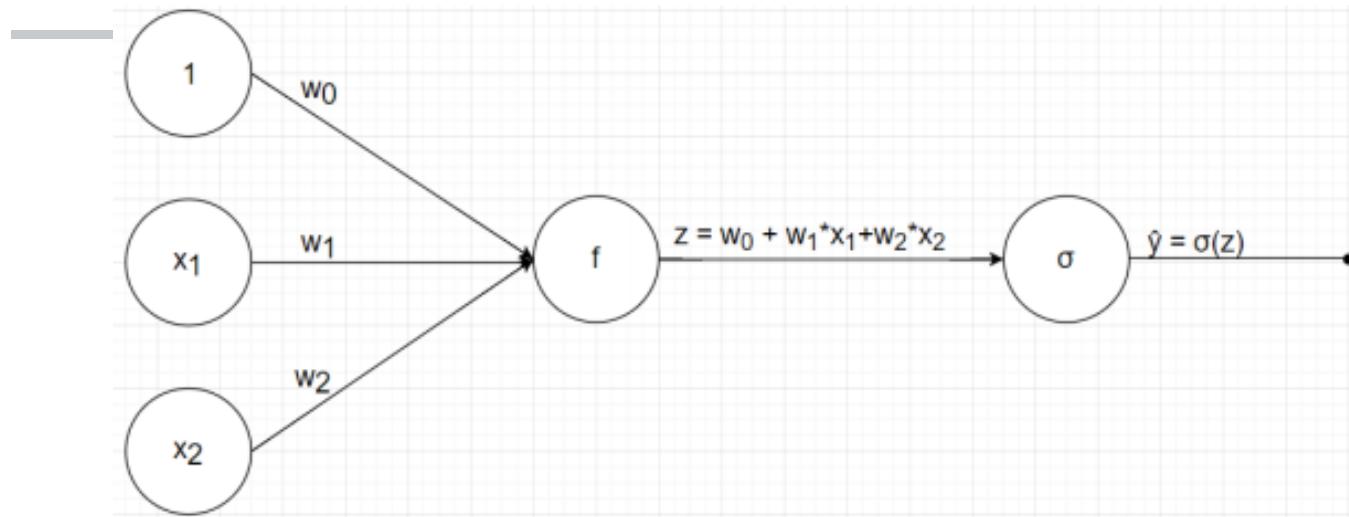
$$\mathbf{y} = \begin{pmatrix} y_1 \\ y_2 \\ \vdots \\ y_n \end{pmatrix} - X = \begin{pmatrix} \mathbf{x}_1^\top \\ \mathbf{x}_2^\top \\ \vdots \\ \mathbf{x}_n^\top \end{pmatrix} = \begin{pmatrix} 1 & x_{11} & \cdots & x_{1p} \\ 1 & x_{21} & \cdots & x_{2p} \\ \vdots & \vdots & \ddots & \vdots \\ 1 & x_{n1} & \cdots & x_{np} \end{pmatrix} -$$



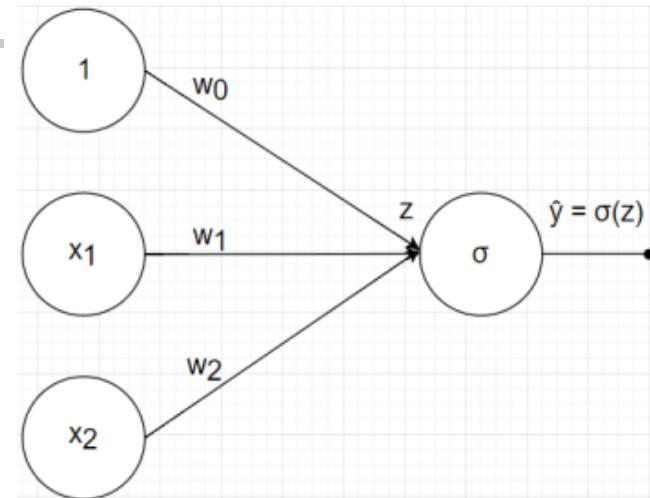
$$\boldsymbol{\beta} = \begin{pmatrix} \beta_0 \\ \beta_1 \\ \beta_2 \\ \vdots \\ \beta_p \end{pmatrix}, \quad \boldsymbol{\varepsilon} = \begin{pmatrix} \varepsilon_1 \\ \varepsilon_2 \\ \vdots \\ \varepsilon_n \end{pmatrix}$$

$$y_i = \beta_0 + \beta_1 x_{i1} + \cdots + \beta_p x_{ip} + \varepsilon_i = \mathbf{x}_i^\top \boldsymbol{\beta} + \varepsilon_i, \quad i = 1, \dots, n,$$

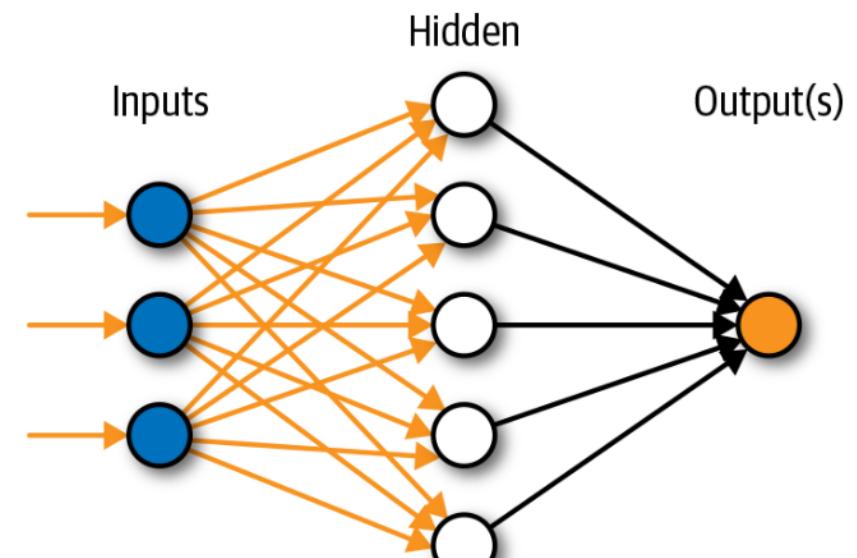
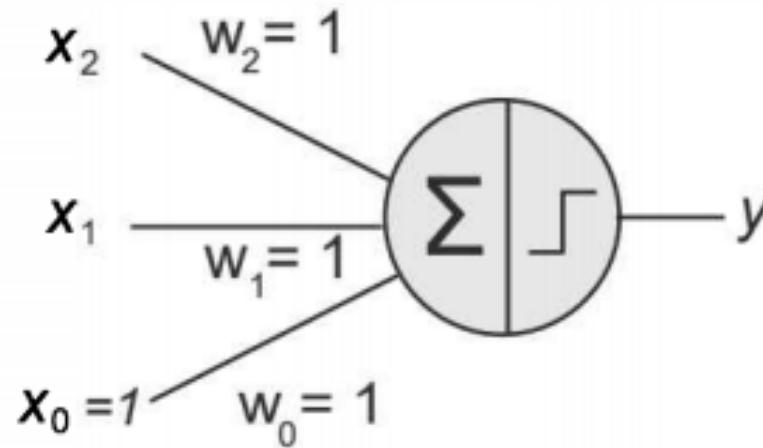
RECAP : ANN



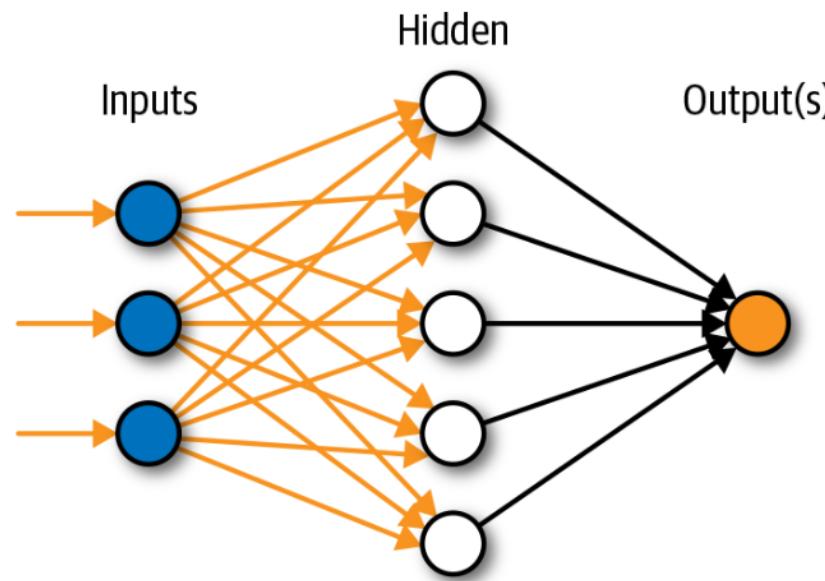
RECAP : ANN



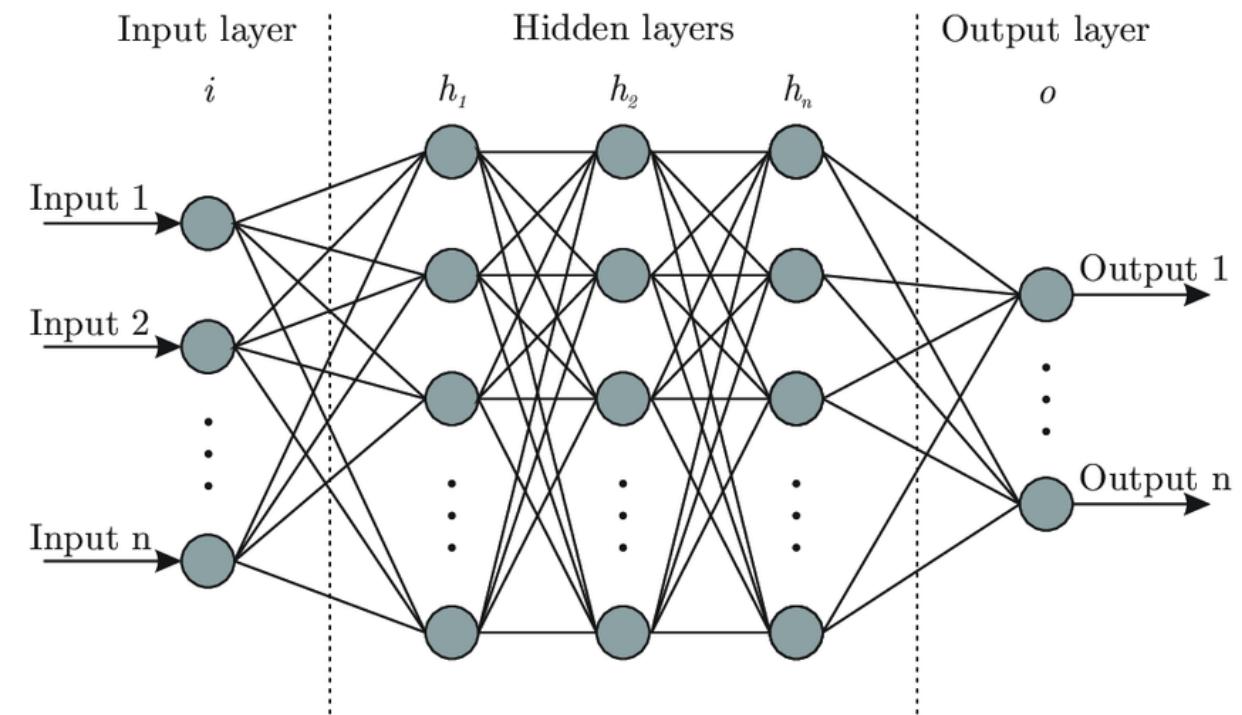
A. McCulloch-Pitts neuron



RECAP : ANN

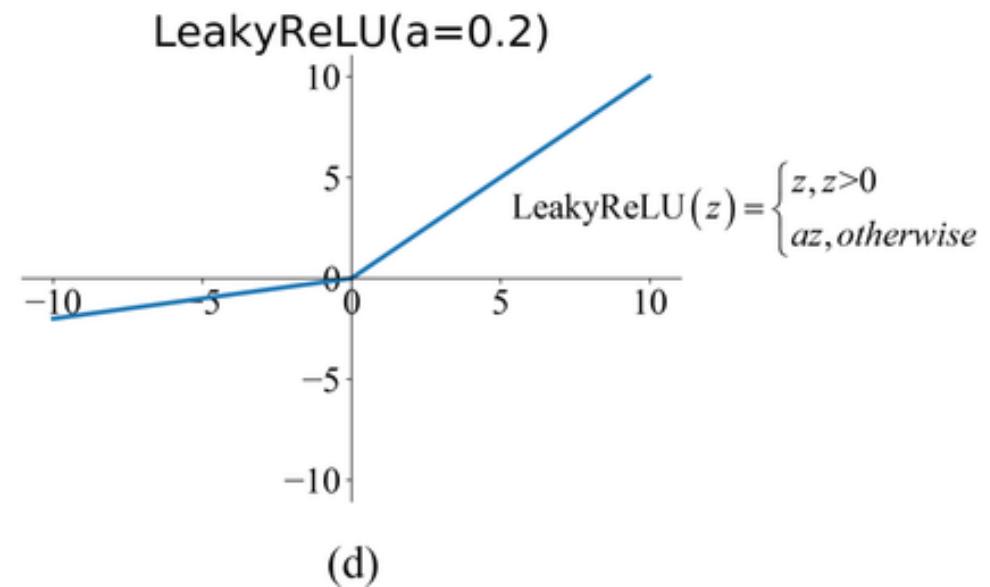
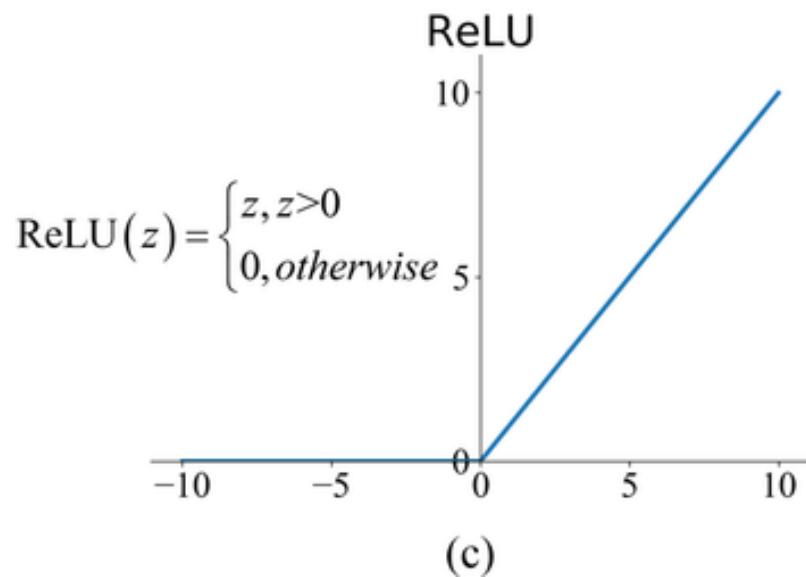
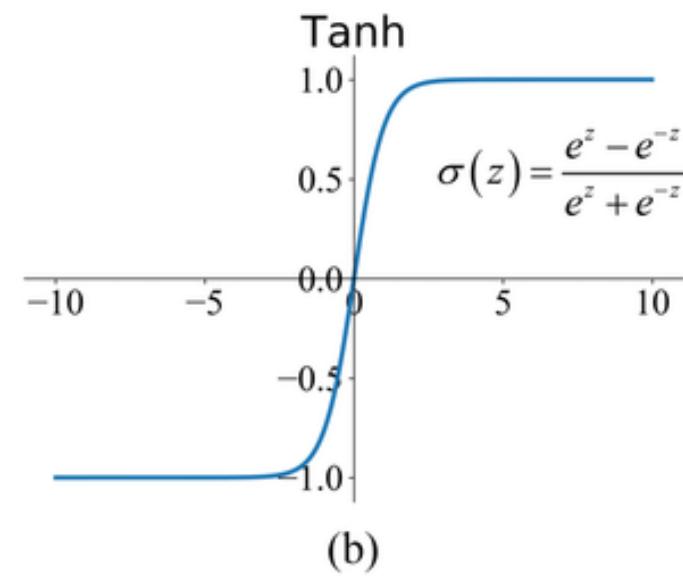
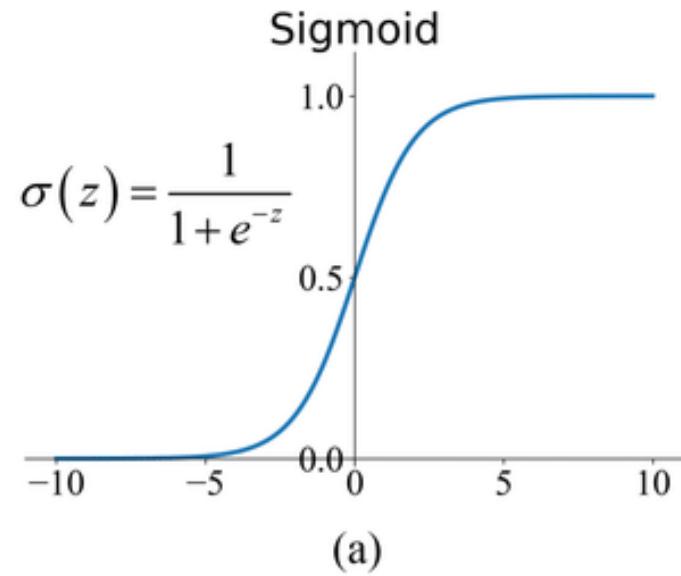


Single hidden layer ANN



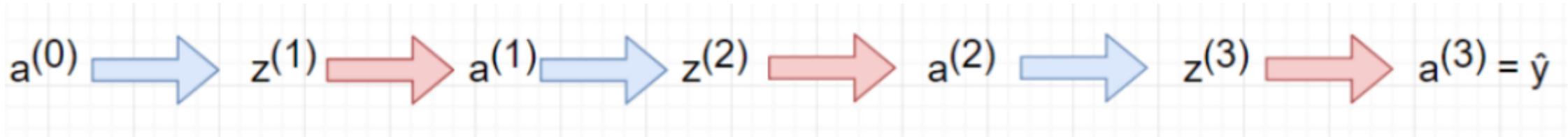
Multiple hidden layers ANN

RECAP: ACTIVATION FUNCTION

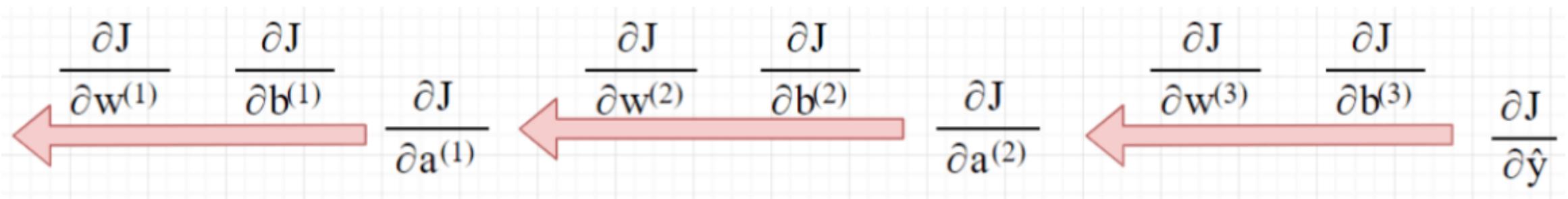


RECAP: BACKPROPAGATION

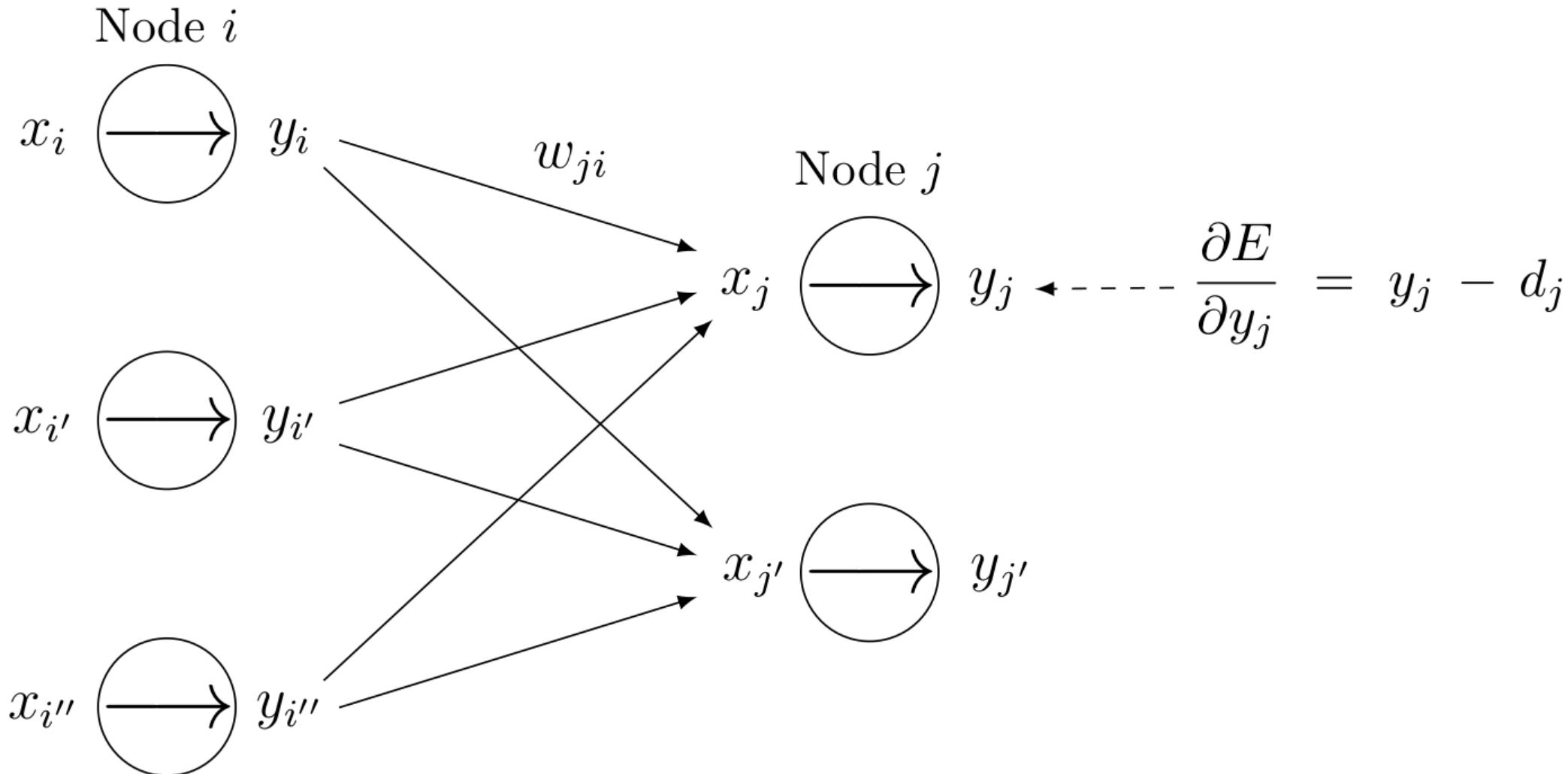
Forward pass: Compute outputs



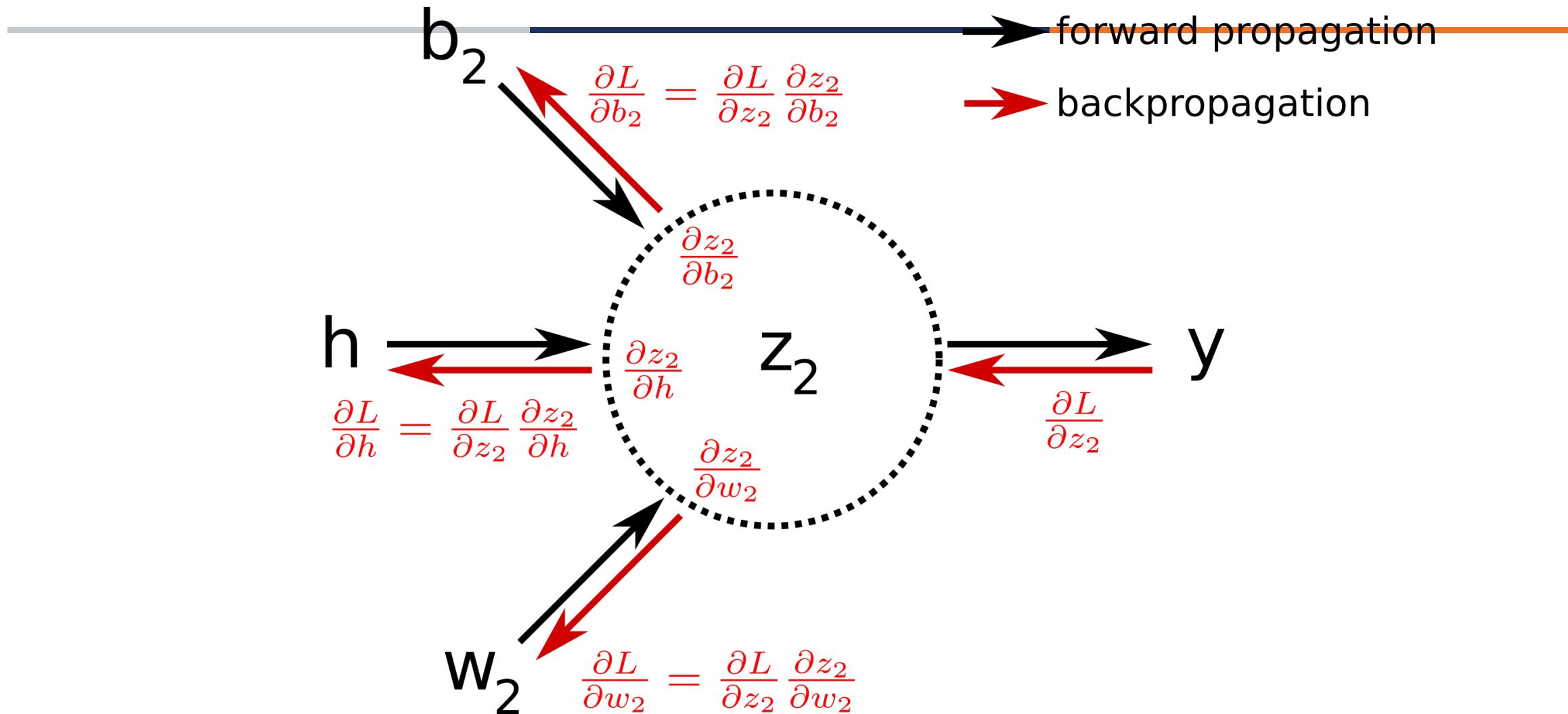
Backward pass: Compute gradients



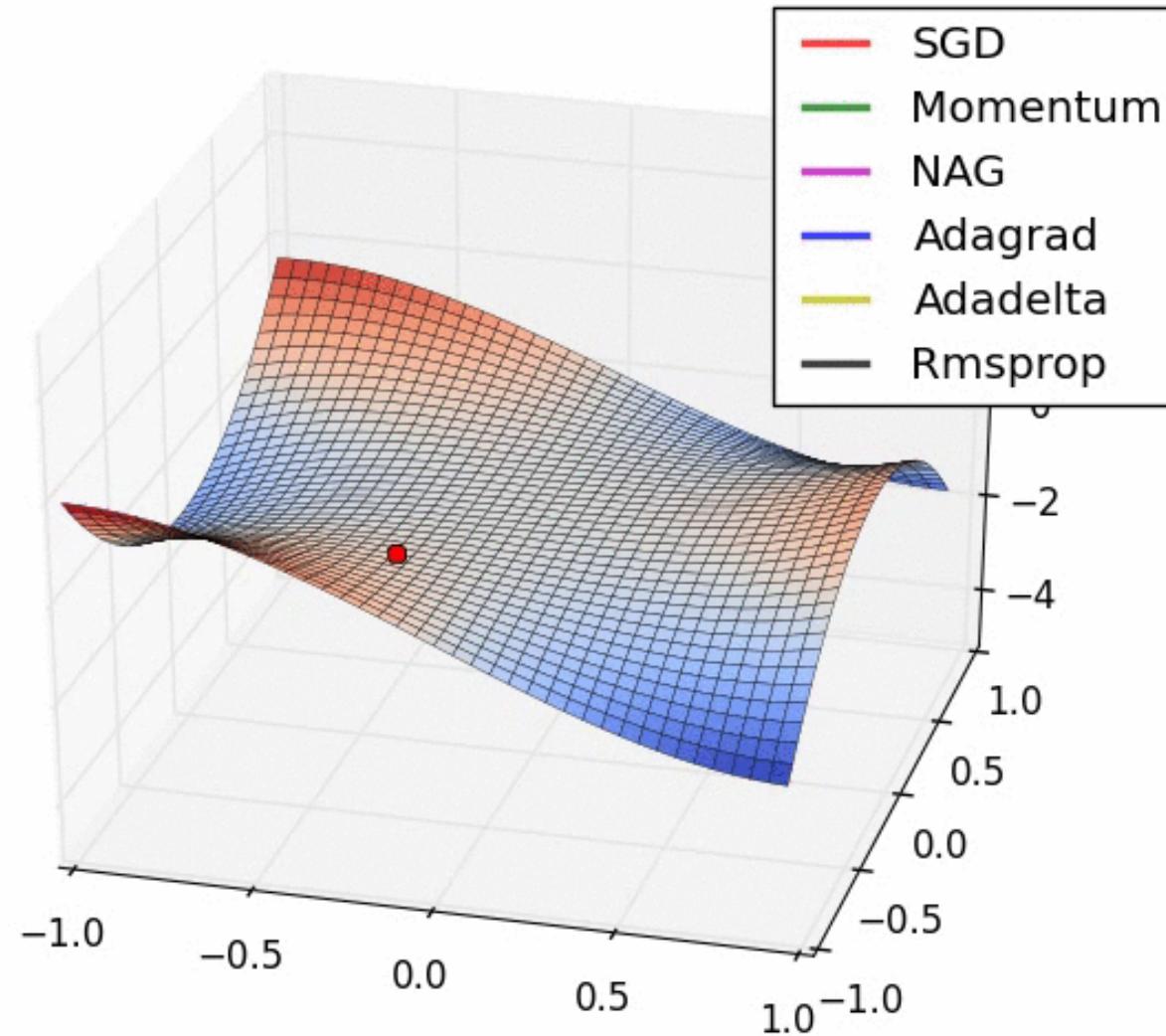
RECAP: BACKPROPAGATION



RECAP: BACKPROPAGATION



RECAP: OPTIMIZER



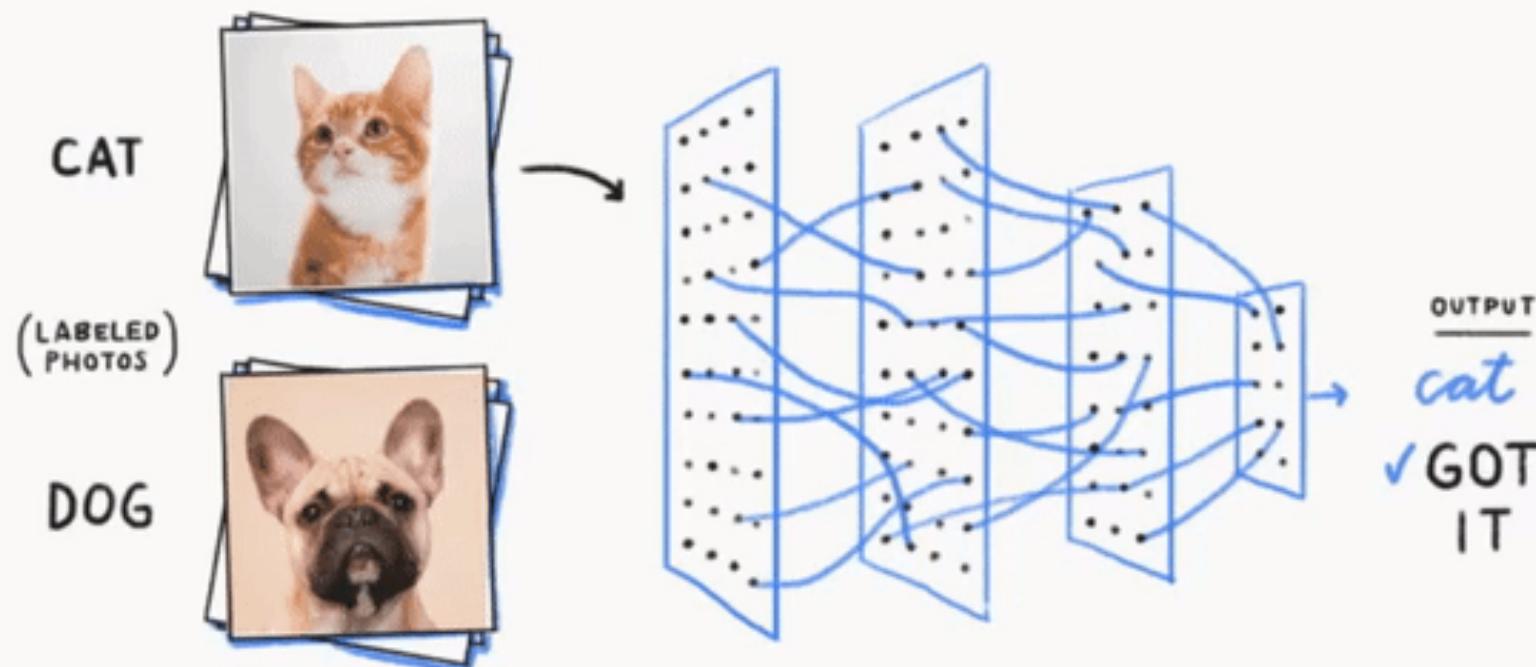
CNN – Convolution Neural Network

Content

- Understand about CNN and its component
- Understand CNN architecture and how it works
- Build a simple CNN model
- Practice based on your project dataset

What is CNN?

A Neural Network is a function that can learn



COMPUTER VISION - COLORS

- RGB: is primary colors of light including Red, Green, and Blue
- RGB are combined in various ways to create a broad spectrum of colors
- Number of colors?

COMPUTER VISION - PIXELS

800x600 pixels



800x600 matrix

$$\begin{bmatrix} w_{1,1} & w_{1,2} & \dots & w_{1,800} \\ w_{2,1} & w_{2,2} & \dots & w_{2,800} \\ \dots & \dots & \dots & \dots \\ w_{600,1} & w_{600,2} & \dots & w_{600,800} \end{bmatrix}$$

Each $w_{ij} = (r, g, b)$ is a pixel in computer vision

COMPUTER VISION - PIXELS

Pixels data storing

$$\begin{bmatrix} 100 & 101 & 131 \\ 150 & 10 & 111 \\ 10 & 200 & 100 \end{bmatrix} \begin{bmatrix} 100 & 112 & 20 \\ 210 & 120 & 120 \\ 260 & 20 & 20 \end{bmatrix} \begin{bmatrix} 50 & 3 & 80 \\ 130 & 130 & 130 \\ 30 & 30 & 3 \end{bmatrix}$$

R G B

COMPUTER VISION - PIXELS

Image in computer vision is a 3D Tensor

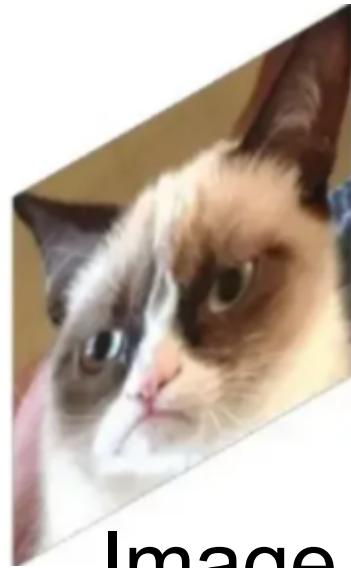
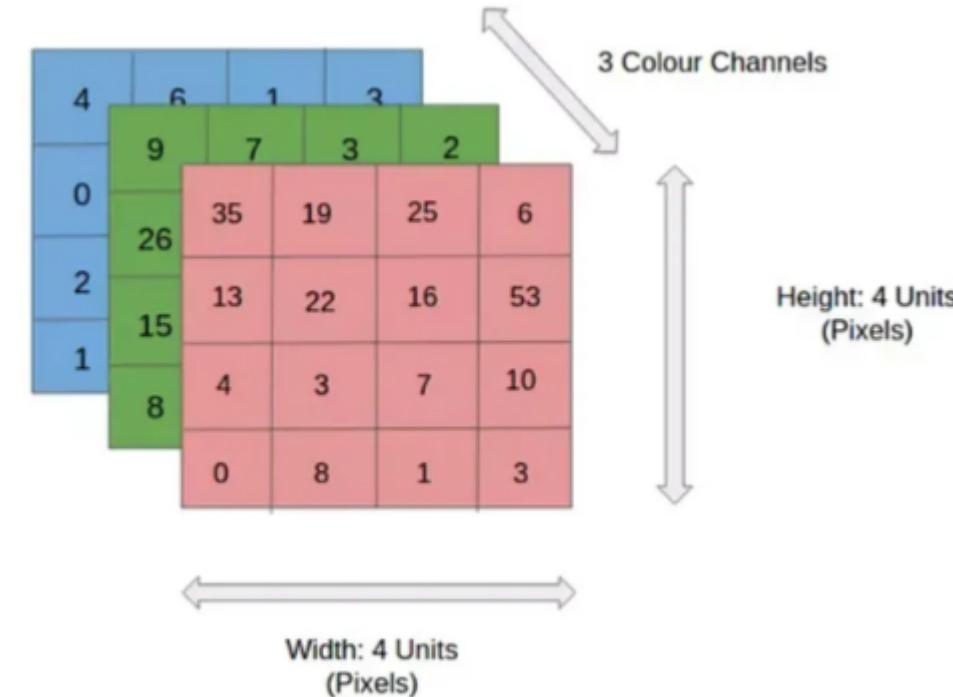


Image
(RGB)



COMPUTER VISION – Grey Scale

Convert formula: $w = r*0.299 + g*0.587 + b*0.114$



Image
(RGB)



Image
(Grey scale)

What is Convolution?

0	0	0	0	0	0	0	...
0	156	155	156	158	158	158	...
0	153	154	157	159	159	159	...
0	149	151	155	158	159	159	...
0	146	146	149	153	158	158	...
0	145	143	143	148	158	158	...
...

Input Channel #1 (Red)

0	0	0	0	0	0	0	...
0	167	166	167	169	169	169	...
0	164	165	168	170	170	170	...
0	160	162	166	169	170	170	...
0	156	156	159	163	168	168	...
0	155	153	153	158	168	168	...
...

Input Channel #2 (Green)

0	0	0	0	0	0	0	...
0	163	162	163	165	165	165	...
0	160	161	164	166	166	166	...
0	156	158	162	165	166	166	...
0	155	155	158	162	167	167	...
0	154	152	152	157	167	167	...
...

Input Channel #3 (Blue)

-1	-1	1
0	1	-1
0	1	1

Kernel Channel #1



308

+

1	0	0
1	-1	-1
1	0	-1

Kernel Channel #2



-498

0	1	1
0	1	0
1	-1	1

Kernel Channel #3



164

+

+ 1 = -25



Bias = 1

-25				...
				...
				...
				...
...

Output

What is Convolution?

Input Image

0	0	0	0	0	0	0
0	1	1	1	1	1	0
0	1	0	0	1	0	0
0	1	0	1	0	0	0
0	1	1	0	0	0	0
0	1	0	0	0	0	0
0	0	0	0	0	0	0

Convolution

0	0	0
0	1	1
0	1	0

Convolved Image

3	2	2	3	1
2	0	2	1	0
2	2	1	0	0
3	1	0	0	0
1	0	0	0	0

What is Convolution?

Input Image

0	0	0	0	0	0	0
1	1	1	1	1	1	0
1	0	1	0	0	0	0
0	1	0	1	0	0	0
0	1	1	0	0	0	0
0	1	0	0	0	0	0
0	0	0	0	0	0	0

Convolution

0	0	0
0	1	1
0	1	0

Convolved Image

3				

What is Convolution?

Input Image

0	1	1	1	0	0	0
0	1	1	1	1	1	0
0	0	0	1	0	0	0
0	1	0	1	0	0	0
0	1	1	0	0	0	0
0	1	0	0	0	0	0
0	0	0	0	0	0	0

What is Convolution?

Convolution

0	0	0
0	1	1
0	1	0

Convolved Image

3	2			

What is Convolution?

Input Image

0	0	0	0	0	0	0
0	0	0	1	1	1	0
1	0	0	0	1	0	0
1	1	0	1	0	0	0
0	1	1	0	0	0	0
0	1	0	0	0	0	0
0	0	0	0	0	0	0

Convolution

0	0	0
0	1	1
0	1	0

Convolved Image

3	2	2	3	1
2				

Convolution and Image processing

- A convolution matrix is used in image processing for tasks such as edge detection, blurring, sharpening, ...

Convolution and Image processing - Identity

Input Image

0	0	0	0	0	0	0
0	1	1	1	1	1	0
0	1	0	0	1	0	0
0	1	0	1	0	0	0
0	1	1	0	0	0	0
0	1	0	0	0	0	0
0	0	0	0	0	0	0

Identity
Convolution

0	0	0
0	1	0
0	0	0

Convolved Image

1	1	1	1	1
1	0	0	1	0
1	0	1	0	0
1	1	0	0	0
1	0	0	0	0

Convolution and Image processing - Blurring

Input Image

0	0	0	0	0	0	0
0	1	1	1	1	1	0
0	1	0	0	1	0	0
0	1	0	1	0	0	0
0	1	1	0	0	0	0
0	1	0	0	0	0	0
0	0	0	0	0	0	0

Blurring
Convolution

.1	.1	.1
.1	.2	.1
.1	.1	.1

Convolved Image

.4	.5	.5	.5	.4
.4	.2	.3	.6	.3
.5	.4	.4	.2	.1
.5	.6	.2	.1	0
.4	.3	.1	0	0

Convolution – Downsampling (Stride)

- **Stride** refers to the number of pixels by which the filter (or kernel) moves across the input image during the convolution operation.
- $\text{Output_size} = (\text{input_size} - \text{kernel_size})/\text{stride} + 1$

Convolution – Downsampling (Stride)

Input Image

1	1	1	1	1	0
1	0	0	1	0	0
1	0	1	0	0	0
1	1	0	0	0	0
1	0	0	0	0	0
0	0	0	0	0	0

Convolution

1	1
1	1

Convolved Image

3		

Convolution – Downsampling (Stride)

Input Image

1	1	1	1	1	0
1	0	0	1	0	0
1	0	1	0	0	0
1	1	0	0	0	0
1	0	0	0	0	0
0	0	0	0	0	0

Convolution

1	1
1	1

Convolved Image

3	3	

Convolution – Downsampling (Stride)

Input Image

1	1	1	1	1	0
1	0	0	1	0	0
1	0	1	0	0	0
1	1	0	0	0	0
1	0	0	0	0	0
0	0	0	0	0	0

Convolution

1	1
1	1

Convolved Image

3	3	1

Convolution – Downsampling (Stride)

Input Image

1	1	1	1	1	0
1	0	0	1	0	0
1	0	1	0	0	0
1	1	0	0	0	0
1	0	0	0	0	0
0	0	0	0	0	0

Convolution

1	1
1	1

Convolved Image

3	3	1

Convolution – Downsampling (Stride)

Input Image

1	1	1	1	1	0
1	0	0	1	0	0
1	0	1	0	0	0
1	1	0	0	0	0
1	0	0	0	0	0
0	0	0	0	0	0

Convolution

1	1
1	1

Convolved Image

3	3	1
3		

Convolution – Downsampling (Stride)

Input Image

1	1	1	1	1	0
1	0	0	1	0	0
1	0	1	0	0	0
1	1	0	0	0	0
1	0	0	0	0	0
0	0	0	0	0	0

Convolution

1	1
1	1

Convolved Image

3	3	1
3	1	

Convolution – Downsampling (Stride)

Input Image

1	1	1	1	1	0
1	0	0	1	0	0
1	0	1	0	0	0
1	1	0	0	0	0
1	0	0	0	0	0
0	0	0	0	0	0

Convolution

1	1
1	1

Convolved Image

3	3	1
3	1	

Convolution – Downsampling (Stride)

Input Image

1	1	1	1	1	0
1	0	0	1	0	0
1	0	1	0	0	0
1	1	0	0	0	0
1	0	0	0	0	0
0	0	0	0	0	0

Convolution

1	1
1	1

Convolved Image

3	3	1
3	1	0
1	0	0

Convolution – Padding

- **Padding** is the process of adding extra pixels around the border of an input image before applying a convolutional filter
- Example of zero padding:

Image						
0	0	0	0	0	0	0
0						0
0						0
0						0
0						0
0						0
0	0	0	0	0	0	0

Convolution – Padding

- Preserves Edge Information: Without padding, the pixels at the edges and corners of the image are used less frequently, leading to loss of information.
- Controls Output Size: Padding allows control over the output size for designing deep networks.
- Prevents Shrinking: Successive convolutions without padding would continuously reduce the size of the feature maps, eventually making them too small

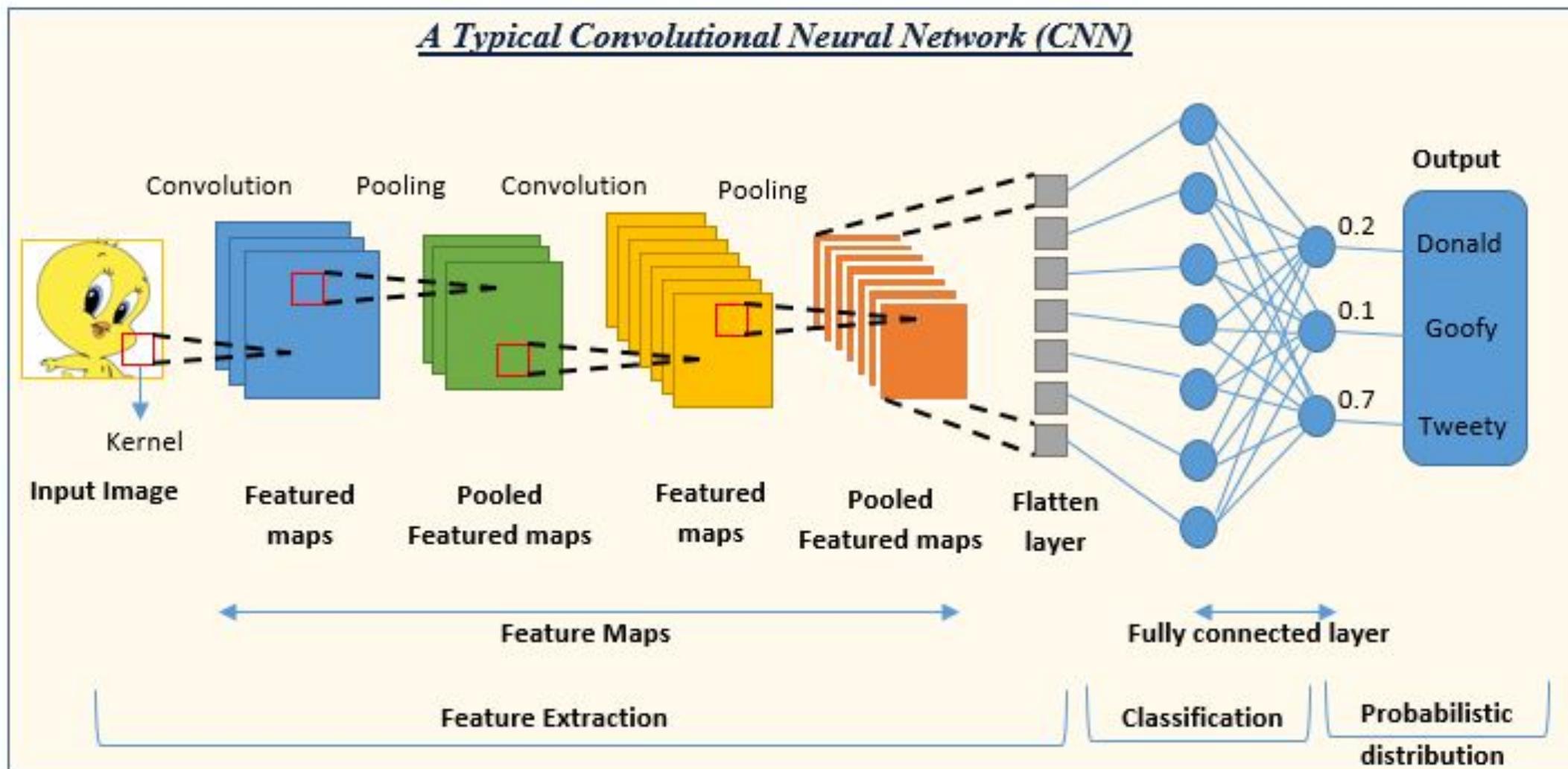
Convolution – Padding

$$\bullet \text{ } outputsize = \frac{inputsize - kernel + 2 * padding}{stride} + 1$$

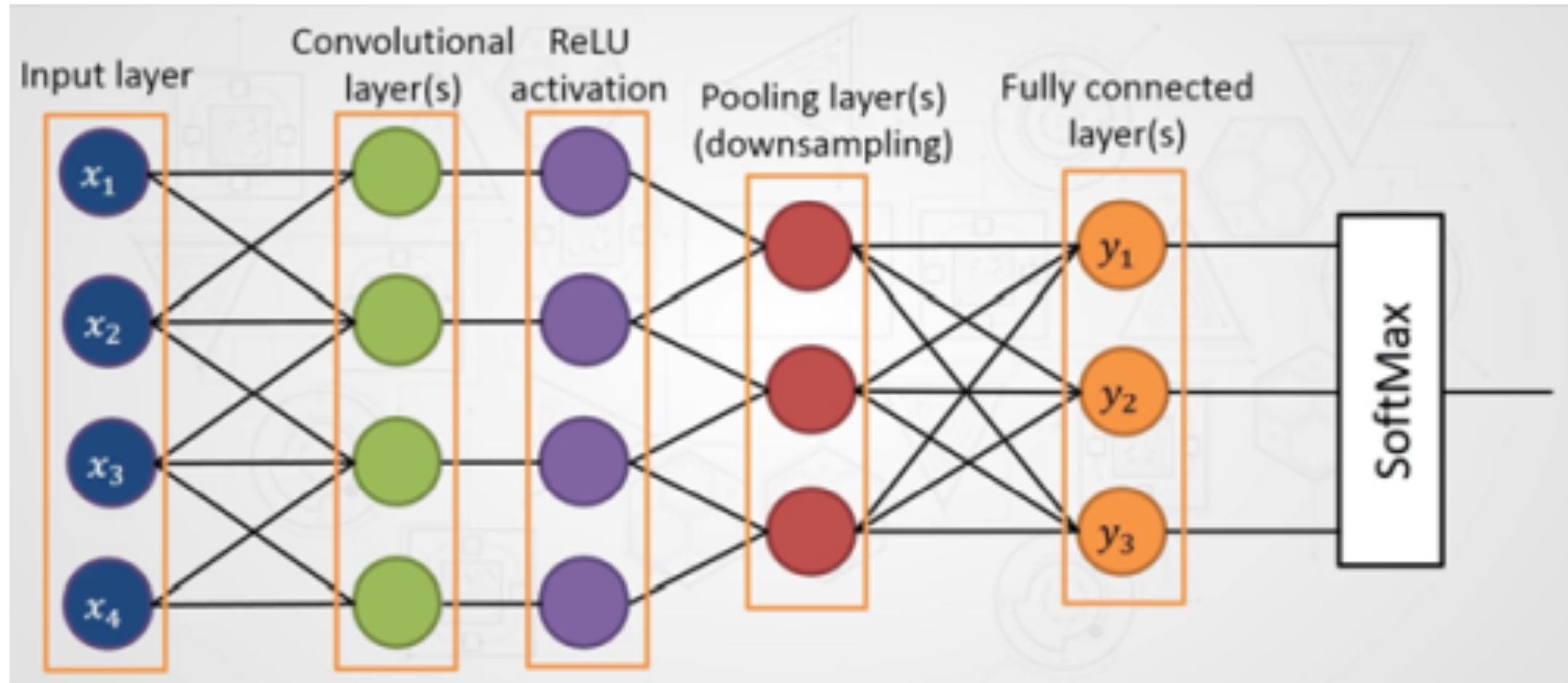
Convolution Neural Network - CNN

- A Convolutional Neural Network (CNN) is a specialized type of artificial neural network (ANN).
- CNN was designed to process and analyze visual data with some convolution layers.
- CNNs are widely used in computer vision applications such as image classification, object detection, and image segmentation.

A typical CNN



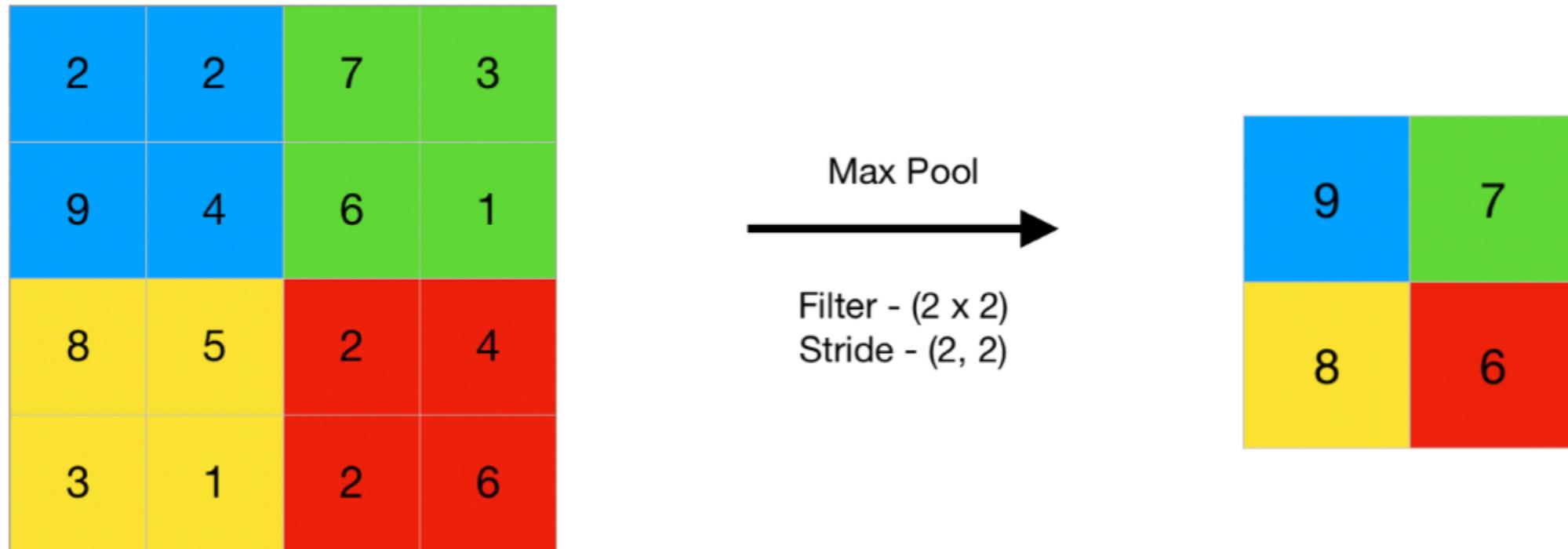
A typical CNN



CNN - Key Components

- **Convolutional Layers:** extract features such as edges, textures, and patterns.
- **Pooling Layers:** reduce the spatial dimensions, decrease the computational load and control overfitting. Common types include max pooling and average pooling.
- **Fully Connected Layers:** similar to traditional neural networks and are used to make the final classification or prediction based on the extracted features.
- **Activation Functions:** Functions like ReLU, Softmax.

CNN – Pooling layer



Max pooling with 2x2 matrix

CNN – Pooling layer

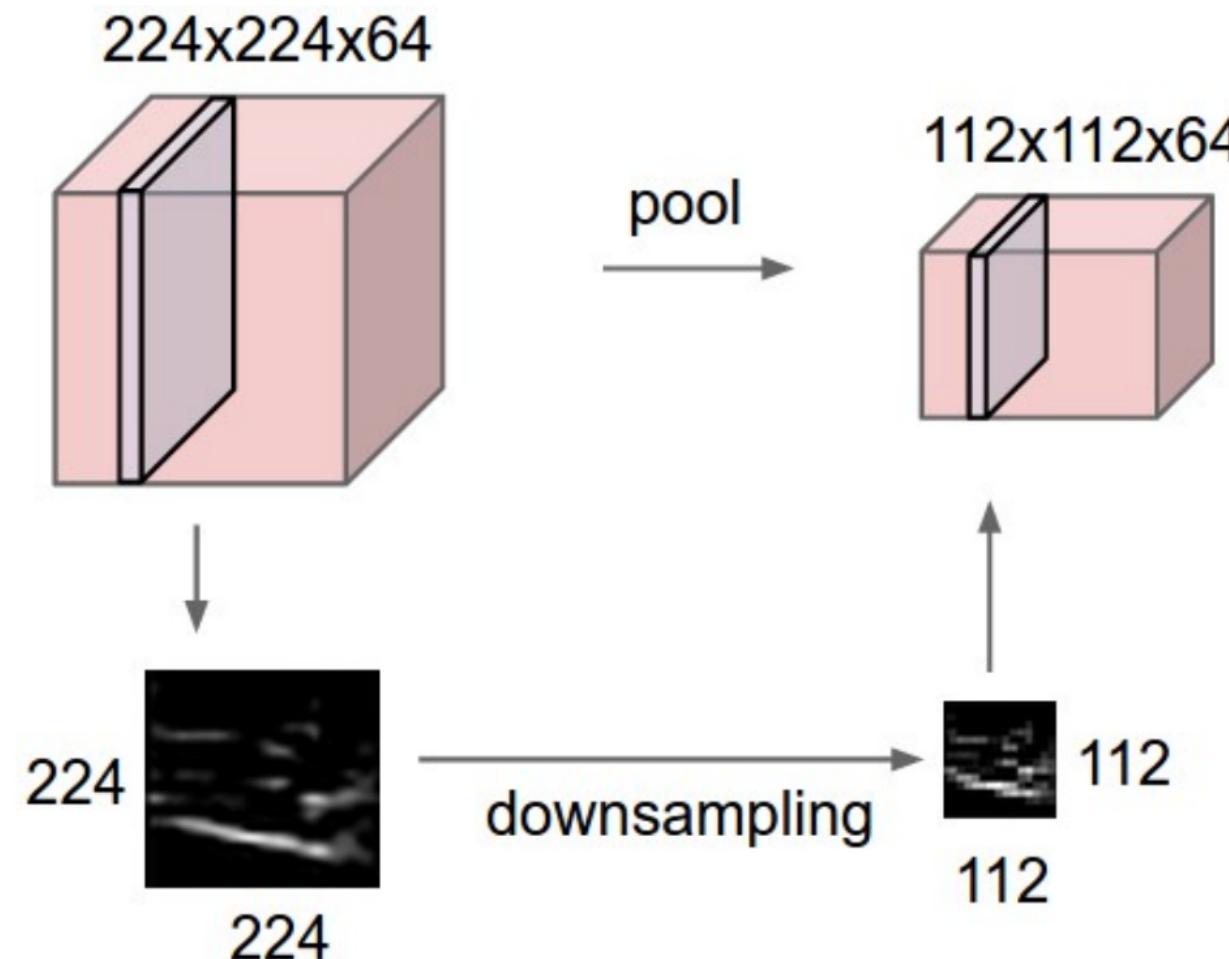
2	2	7	3
9	4	6	1
8	5	2	4
3	1	2	6

Average Pool
Filter - (2 x 2)
Stride - (2, 2)

4.25	4.25
4.25	3.5

Average pooling with 2x2 matrix

CNN – Pooling layer



Pooling layer with 2×2 matrix

CNN – Pooling layer

- A pooling layer is used to:
 - Reduce the spatial dimensions (width and height) while preserving the depth (number of channels) and important features.
 - Down sample the feature maps, making the network more computationally efficient.

