

Complex Adaptive Systems, Publication 4  
Cihan H. Dagli, Editor in Chief  
Conference Organized by Missouri University of Science and Technology  
2014-Philadelphia, PA

# Towards a Formal Understanding of Bateson's Rule: Chromatic Symmetry in Cyclic Boolean Networks and its Relationship to Organism Growth and Cell Differentiation

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## Abstract

There has been considerable prior research on the biological processes of morphogenesis and cellular differentiation, and the manner by which these processes give rise to symmetries in biological structures. Here we extend our previous work on thermal robustness and attractor density in cyclic formal Boolean dynamical systems, introducing a new form of spectral analysis on digital organisms at the cellular level. We interpret the phenomena of radial and bilateral symmetry in terms of spatial periodicities in the color sequences, as manifested by an organism while it orbits in its attractors. We provide new results on the influence of various organism properties on its emergent color symmetries—providing initial insights toward an eventual formal understanding of metamerism and Bateson's Rule.

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Peer-review under responsibility of scientific committee of Missouri University of Science and Technology

**Keywords:** Boolean networks; dynamical systems; chromatic, symmetry

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## 1. Introduction

Since the seminal work of Von Neumann [1], the subject of cellular automata has received considerable and continued attention (see [2, 3] for brief surveys). Understanding how the structure of a cellular network impacts its behavior as a dynamical system is crucial to determining how networks should be built, how they evolve over time, and how they can be made to grow while still exhibiting desired dynamical properties. Biological networks (e.g. neural networks) are subject to preferential selection processes, which drive evolution over long time scales. It is reasonable to expect that this selection process will be sensitive to not only the structural properties [4] of networks, but to their dynamical properties as well [5]. Previous researchers have considered measures such as landscape ruggedness [6, 7] and redundancy [8] in evaluating dynamical systems. In this paper, we extend our previous work on attractor dynamics [16] to describe *the manner in which the requirement to maintain rotational chromatic symmetries in an organism's attractor dynamics might serve to structure its growth trajectory*.

In addition to evolution over long time scales, biological networks exhibit cellular differentiation over short

function 6 organism and expanding the random sampling to include non-homogeneous organisms. The experimental data from the much larger set of non-homogeneous organisms should lead to a better understanding of cellular differentiation, symmetry, and morphogenesis.

### Acknowledgements

The authors would like to acknowledge that this project was developed during the development of the NSF Office of Behavioral, Social, and Economic Sciences, Anthropology Program Grant BCS-0752680.

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