



COMP0037

Report

Planning in Uncertain Worlds

Group AS

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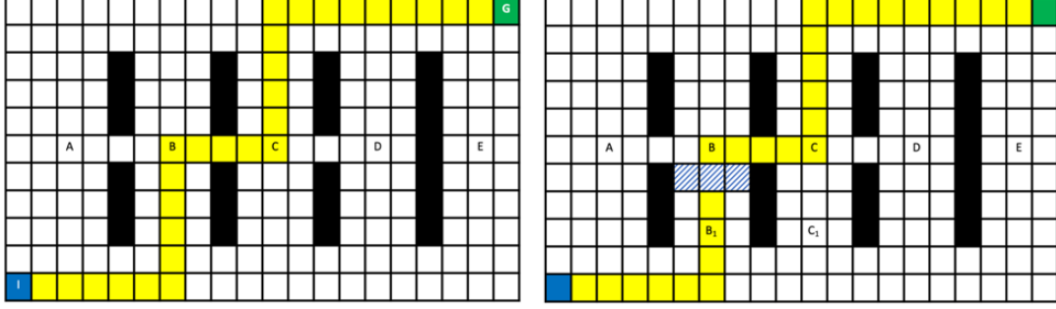
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1 Decision Re-Plan Policy

1.1 Policy Selection when Obstacle is Observed



(a) The original planned path form I to G (b) An obstacle in aisle B obstructs the going through Aisle B and C. planned path of the robot.

Figure 1: Illustration of case where robot observes an obstruction to it's planned path.

The scenario that we will be analysing is the case shown in Fig. 1a. The robot is required to go from a cell I to a cell G . These cells are marked blue and green in Fig. 1a respectively. The figure also shows the original planned path that the robot computed going down aisle B. However, once the robot turns into aisle B it observes that the aisle is blocked. This observation is done at the point when the robot reaches the cell labelled B_1 . At this point the robot can either decide to wait until the obstruction clears or it can re-plan a path. Once the robot observes the obstacle, the time the robot must wait for the obstacle to clear may be represented by the expression in Eq. 1.

$$T = \frac{0.5}{\lambda_B} + \tilde{T} \quad (1)$$

The wait time is dependent on λ_B and a random variable \tilde{T} . The random variable \tilde{T} is sampled from a exponential distribution with a rate parameter of $0.5\lambda_B$. The probability density function (PDF) for \tilde{T} is shown in Eq. 2.

$$f(t) = \begin{cases} \lambda e^{-\lambda t} & t \geq 0 \\ 0 & t < 0 \end{cases} \quad (2)$$

where, $\lambda = \frac{0.5}{\lambda_B}$.

As previously mentioned, the robot has two options to choose from: to wait for the obstacle to clear, or to re-plan and execute the new path. The two are different policies the robot must choose from. We use the symbol π to denote a policy. A policy is a mapping from the world state to an action the robot can execute.

Let us assume that if the robot decides to wait the total path length (number of cells) will be K_1 while if the robot decides to re-plan and execute the total path length will be K_2 . We let the quantity K equal to the larger value between K_1 and K_2 . Now we may write the policy for the robot to wait as π_K^1 and the policy for re-planning as π_K^2 . These policies are padded correspondingly to produce actions \mathbf{u}_K^1 and \mathbf{u}_K^2 that are padded with zero-cost state preserving actions.

To see which policy is better on average, we consider the expected value of the cost function for both cases. The case when policy π_K^1 is chosen is characterized by the inequality shown in Eq. 3.

$$\mathbb{E} [L(\pi_K^1)] \leq \mathbb{E} [L(\pi_K^2)] \quad (3)$$

Substituting the expression from Eq. 7 into Eq. 6 we obtain the expression in Eq. 8. The right-hand side of the inequality in Eq. 8 represents the smallest possible value for λ_B for which the waiting policy π_K^1 is a better option than the re-plan policy π_K^2 . The inequality also takes into consideration the constraint that $\lambda_B > 0$ and negates the solution when $\lambda_B < 0$.

$$\begin{aligned}
\frac{0.5}{\lambda_B} - 1 &\leq \frac{L_{B_1C_1} + L_{C_1C} - L_{B_1B} - L_{BC}}{L_W} \\
\frac{0.5}{\lambda_B} &\leq \frac{L_{B_1C_1} + L_{C_1C} - L_{B_1B} - L_{BC} + L_W}{L_W} \\
\lambda_B &\geq \frac{0.5L_W}{L_{B_1C_1} + L_{C_1C} - L_{B_1B} - L_{BC} + L_W}
\end{aligned} \tag{8}$$

1.2 Policy Selection at Start

1.3 Considering the Probability of the Obstacle Being Present

1.4 Considering Multiple Obstacles

2 ROS Implementation

References

Appendices