Swap Bits Program Explanation

Key Points:

- 1. $a ^0 = a$
- 2. a ^ a = 0
- 3. a & a = a
- 4. a & 0 = 0
- 5. 0 | 0 = 0
- 6. 0 | 1 = 1

Question:

1. Aim:

A positive number is given as input along with two positions p1, p2 and length n. Your job is to write a program that swaps 'n' bits of the number starting from positions p1, p2. p1, p2 are 0-indexed values that start from least significant bit of the number.

Use unsigned int data type.

2. Explanation:

Sample 1:

Number = 47. Its binary representation is 00101111

p1 = 1 (Start from 2nd bit from right side)

p2 = 5 (Start from 6th bit from right side)

n = 3 (No of bits to be swapped)

The 3 bits starting from p1 are 0010'111'1 and the 3 bits staring from p2 are '001'01111. After swapping these two, the resultant binary string will be 11100011 which is equal to decimal value 227.

Hence the output must be 227.

Sample 2:

Number = 28. Its binary representation is 11100

p1 = 0 (Start from 1st bit from right side)

p2 = 3 (Start from 4th bit from right side)

n = 2 (No of bits to be swapped)

The 2 bits starting from p1 are 111'00' and the 2 bits staring from p2 are '11'100. After swapping these two, the resultant binary string will be 00111 which is equal to decimal value 7.

Hence the output must be 7.

Sample 3:

Number=178. Its binary representation is 10110010.

p1 = 0 (Start from 1st bit from right side)

p2 = 30 (Start from 31st bit from right side)

n = 5 (No of bits to be swapped)

In this case, since range exceeds at position2, use 0's in that case. So, the bits starting from p1 are '10010' and the bits staring from p2 are '00000'.

Hence the output must be 2147483808.

3. Constraints:

- i. The positions and the length 'n' must always be positive.
- ii. 0<=p1<p2<=32.
- iii. If the range overflows 32, discard the extra bits. (See Sample 3)
- iv. It is guaranteed that positions and ranges will not overlap.
- v. It is guaranteed that the number will not exceed 32-bit range.

4. Note:

- i. If constraints are violated, then return 0.
- ii. Please Use 32-bit data (unsigned int) type to get accurate results.

Program:

```
#include<stdio.h>
int swapBits(unsigned int number, unsigned int p1, unsigned int p2, unsigned int n)
{
    unsigned int a = (number >> p1) & ((1U << n) - 1);
    unsigned int b = (number >> p2) & ((1U << n) - 1);
    unsigned int c = (a ^ b);
    c = (c << p1) | (c << p2);
    unsigned int result = number ^ c;
    return result;
}</pre>
```

Steps:

1.Extraction:

In order to extract the bits to be swapped, we shift them to rightmost side. As we know, $\mathbf{a} \otimes \mathbf{1} = \mathbf{a}$ and $\mathbf{a} \otimes \mathbf{0} = \mathbf{0}$. We now, create a binary number with exactly 'n' 1's and remaining as 0's because when we perform the **AND** (\otimes) operation, we only get the bits to be swapped.

```
From the above example, number = 28, p1 = 0, p2 = 3 and n = 2.

number >> p1 \rightarrow 11000 >> 0 \rightarrow 11000
number >> p2 \rightarrow 11000 >> 3 \rightarrow 00011
1U << n \rightarrow 100 \text{ [Left-Shift Operation] //U stands for unsigned}
1U << n-1 \rightarrow 100-1 \text{ (in binary)} \rightarrow 011 \text{ [1's complement]}
unsigned \ int \ a = number >> p1 \ \& \ ((1U << n) - 1);
11100
AND \ (\&) \ 00011
------
00000 \qquad ['00' \text{ is extracted]}
```

2. Calculating Xor of 'a' and 'b':

We calculate the **XOR (^)** of 'a' & 'b' and store it in another unsigned int variable c. The reason for this step will be explained later.

unsigned int
$$c = (a \land b);$$

3. Substitution:

We try to substitute the **XOR (^)** values of 'a' and 'b' in the place of bits that are to be swapped by shifting the bits of c by p1 and p2 simultaneously. We then, perform **OR (|)** operation in order to combine them as a single value.

$$c << p1 \rightarrow 00011 << 0 \rightarrow 00011$$
 $c << p2 \rightarrow 00011 << 3 \rightarrow 11000$
 $c = c << p1 / c << p2;$

00011

OR (|) 11000

11011 [Value of c is substituted]

4. Calculating result:

As we know that $a \land b \land a = b$ and $a \land b \land b = a$, to get the result we perform XOR (^) operation for the given number and the value of 'c'. Since, 'c' contains the result of $a \land b$, when we perform XOR (^) operation, the values of 'a' and 'b' will get swapped.