



At  $x = -3$ , there is a root, but no change in concavity ( $f$  is concave up on either side of 3)

At  $x = 2$ , there is a double root, but no change in concavity ( $f$  is concave up on either side of 2)

At  $x = 1$ , there is a triple root, but there is a change in concavity

$\Rightarrow$  P.O.I. at  $x = -1$

The rel. extrema for  $f(x)$  are at  $x = -\frac{5}{2}$  (Rel. <sup>Min</sup> Max),  $x = 1$  (Rel. Max),  $x = 2$  (Rel. Min)

~~Note the~~

There is a change in concavity not just at  $x = -1$ , but also somewhere between  $x = -1$  and  $x = 1$  (Draw secant lines)  $\Rightarrow$  P.O.I. between  $x = -1$  and  $x = 1$  and it looks like there is a change at  $x = 0$

$\Rightarrow f(x)$  is C.U. on  $(-1, 0)$  and C.D. on  $(0, 1)$

Also note there is a change in concavity between  $x = 1$  and  $x = 2$  (about at  $x = \frac{3}{2}$ )

$\Rightarrow f(x)$  is C.U. on  $(\frac{3}{2}, \infty)$  and C.D. on  $(1, \frac{3}{2})$

Another change in concavity between  $x = -\frac{5}{2}$  and  $x = -1$  (about  $x = -\frac{7}{4}$ )

$\Rightarrow f(x)$  is C.U. on  $(-\frac{5}{2}, -\frac{7}{4})$  & C.D. on  $(-\frac{7}{4}, -1)$

$\therefore f$  is concave up on  $(-\infty, -\frac{7}{4}) \cup (-1, 0) \cup (\frac{3}{2}, \infty)$