

$$\text{Solve } |3x+2| - |x-1| - 7 > 10$$

$$x < -\frac{2}{3}: -3x-2-(1-x)-7 > 10$$

$$\Rightarrow -2x-3-7 > 10$$

$$\Rightarrow -2x > 20$$

$$\Rightarrow x < -10$$

$$-\frac{2}{3} \leq x < 1: 3x+2-(1-x)-7 > 10$$

$$\Rightarrow 4x-6 > 10$$

$$\Rightarrow x > 4$$

$$\therefore (-\infty, -10) \cup (7, \infty)$$

$$x \geq 1: 3x+2-(x-1)-7 > 10$$

$$\Rightarrow 2x-4 > 10$$

$$\Rightarrow x > 7 \leftarrow \text{More restrictive}$$

$$\text{Solve } |x+2| + |x-5| - 4 \leq 5$$

$$x < -2: -2-x+5-x-4 \leq 5$$

$$\Rightarrow -2x-1 \leq 5$$

$$\Rightarrow x \geq -3$$

$$\therefore [-3, 6]$$

$$-2 \leq x < 5: x+2+5-x-4 \leq 5$$

$$\Rightarrow 3 \leq 5 \text{ Always true}$$

$$x \geq 5: x+2+x-5-4 \leq 5$$

$$\Rightarrow 2x-7 \leq 5$$

$$\Rightarrow x \leq 6$$

$$\text{Solve } |x+2| + |x-5| - 4 \geq 9$$

$$x < -2: -x-2+5-x-4 \geq 9$$

$$\Rightarrow -2x-1 \geq 9$$

$$\Rightarrow x \leq -5$$

$$\therefore (-\infty, -5] \cup [8, \infty)$$

$$-2 \leq x < 5: x+2+5-x-4 \geq 9$$

$$\Rightarrow 3 \geq 9 \text{ Never True}$$

$$x \geq 5: x+2+x-5-4 \geq 9$$

$$\Rightarrow 2x-7 \geq 9$$

$$\Rightarrow x \geq 8$$