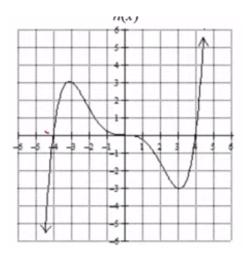
MPS21XH - Concavity and Polynomial Functions Mr. Jaishankar

Here are some facts about the concavity and points of inflection of polynomial functions:

A point of inflection for a polynomial function can occur at one of 3 places:

- At a root with **odd** multiplicity  $\geq 3$
- Between a root of **odd** multiplicity  $\geq 3$  and the x-coordinate of the nearest local minimum or maximum the x-coordinate of the point of inflection is approximately halfway between those points.
- Between the x-coordinates of consecutive local extrema the x-coordinate of the point of inflection is approximately halfway between those points.

**Note:** Recall that for any function, a point of inflection occurs at a point where the graph of the function has a change in concavity.



Above you are given the graph of the polynomial function h(x).

- a.) Using the graph, determine the equation for h(x).
- b.) Determine the average rate of change of h on [-3,4]. Show the work that leads to your answer.
- c.) For what values of x does the graph of h have a relative extrema? Be specific and justify your answer.
- d.) For what values of x does the graph of h have a point of inflection? Justify your answer.
- e.) For what values of x is the graph of h concave up? Justify your answer.
- f.) For what values of x is the graph of h decreasing? Justify your answer.
- g.) For what values of x is the graph of h both decreasing and concave up? Justify your answer.