

A Work-in-Progress Summary of Power/Road Recovery

Dr. Erhan Kutanoglu and Brian French

April 11, 2019

1 Introduction

Recently disaster response and resilience has been the "hot field" in humanitarian logistics, inventory planning, and power grid electrical engineering. There has been a concentrated effort to study several aspects such as power grid islanding [10] [4], humanitarian supply management [7] [3], and infrastructure repair[1]. Many of these project miss interactions between the solutions of multiple different infrastructure systems such as the road grid being necessary to move supplies for the power grid's repair. This is likely due to disaster response being a problem of many actors all acting on their own share of the problem with little consideration for the bigger picture[6] . Solving the full case of dozens of actors all with different sets of information and problems under consideration would be completely unmanageable, so we simplify it for the time being to a power utility and a road grid actor each trying to repair their piece of the infrastructure. We choose the example of hurricanes as the planned disaster to use for exploring the model since Texas has good data for roads and power grids as well as hurricane damage being modeled for power grid elements [5] to give a place to extend into good scenario generation for future projects.

2 Current Model

2.1 Power Grid

Summary: Find a set of power grid elements (buses and lines) to repair in each 8 hour shift of work that minimizes total load shed over time. This is subject to the operation of a grid using DC-approximation to power flow and the ability to find a path for the repair crew to reach everything. For now inclusion of proper routing would complicate the problem to a degree where even simple cases would be hard to set up, so routing is approximated using shortest paths right now since that provides an maximal bound on the length of the path a repair crew would take.

2.2 DC Power Flow/Shortest Path "Routing"

2.2.1 Glossary

- \underline{L}_e and \overline{L}_e is the capacity lower and upper bounds for the power line e
- Δ_I is the time to repair node I
- δ_E is the time to repair line E
- $C_{SP(i)}$ is the shortest path to node i from the central depot
- K is a coefficient of "broken-ness" representing the average slowdown from debris on the road and minor flooding
- D_I is the power demand at location I in the pre-disaster steady state
- P_K is the maximum power generation for generator K
- B_e is the line susceptance (imaginary part of admittance, also inverse of resistance) for power line e

2.2.2 Variables

- X_e^t is the flow on line e at time t
- G_k^t is the production from generator k at time t
- V_i^t is 1 if node i is functioning at time t
- W_e^t is 1 if line e is functioning at time t
- S_e^t is 1 if line e is serviced at time t
- F_i^t is 1 if node i is serviced at time t
- θ_i^t is the phase angle for the power flow at i in time t

2.2.3 Sets

- N is the set of nodes
- E is the set of power lines
- R is the set of roads
- T is the planning horizon
- $o(i)$ is the set of lines with origin i
- $d(i)$ is the set of lines with destination i
- $o(e)$ is the origin node of line e
- $d(e)$ is the destination node of line e

2.2.4 Model

$$\text{Minimize } \sum_{i \in N} \sum_{t \in T} (1 - W_i^t) * C_{demand_i}$$

Subject to:

- (1) $X_e^t = B_e * (\theta_{origin}^t - \theta_{destination}^t) \forall t \in T \forall e \in E$
- (2) $G_i^t - \sum_{l \| o(l)=i} X_l^t + \sum_{l \| d(l)=i} X_l^t = C_{demand_i} \forall t \in T \forall i \in N$
- (3) $G_k^t \leq P_K V_k^t \forall t \in T \forall k \in N$
- (4) $\underline{L}_e W_e^t \leq X_e^t \leq \overline{L}_e W_e^t \forall t \in T \forall e \in E$
- (5) $\underline{L}_e V_{o(e)}^t \leq X_e^t \leq \overline{L}_e V_{o(e)}^t \forall t \in T \forall e \in E$
- (6) $\underline{L}_e V_{d(e)}^t \leq X_e^t \leq \overline{L}_e V_{d(e)}^t \forall t \in T \forall e \in E$
- (7) $\sum_{i \in L} \Delta_I F_i^t + \sum_{e \in E} \delta_e S_e^t + \sum_{i \in L} F_i^t C_{SP(i)} + \sum_{e \in E} S_e^t * \min(C_{SP(o(e))}, C_{SP(d(e))}) \leq 8 \forall t \in T$
- (8) $V_i^t \leq \sum_0^{t-1} F_i^t + initial \forall i \in L$
- (9) $W_e^t \leq \sum_0^{t-1} S_e^t + initial \forall e \in E$

2.2.5 Explanation of Constraint Systems

- Constraint (1) defines flow based on line limits and line susceptance as per Salmeron, Ross, and Baldick 2004[11]
- Constraint (2) defines node power balance so that inflow has to match outflow at each node.
- Constraint (3) constrains power generation to be in the realm of feasible production conditional on the relevant node being operational
- Constraints (4)-(6) constrains line flow to be inside line capacity conditional on the relevant elements being operational
- Constraint (7) constrains/decides what gets done during a shift and handles shortest path travel time.
- Constraints (8) and (9) handle defining operations

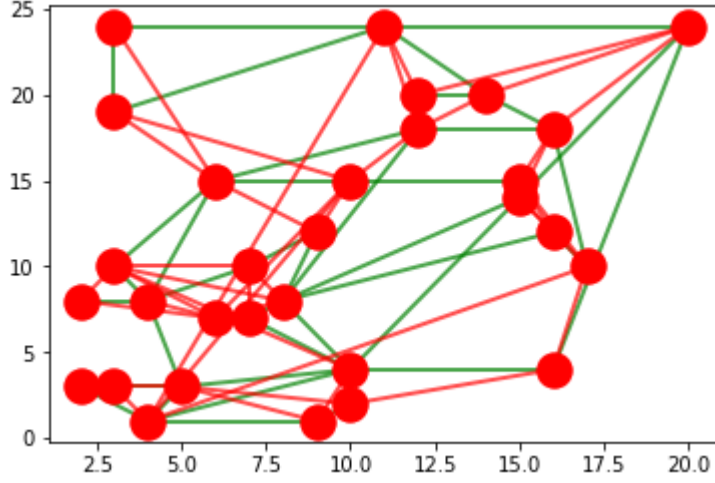


Figure 1: A representation of a road/power dual network

2.2.6 Comments

- The assumption in this version of the model is that a vehicle can only do one operation per trip, so routing reduces to shortest path
- This also assumes DC power flow, which is a much more through version of power flow than pipeflow-style models
- note that from constraint 9, once an element is working, we can chose whether or not it's engaged or turned off to allow load to be shed

2.3 Preliminary Results

Shown above is a representation of IEEE Bus30 (power lines represented in Green) overlaid with a Watts-Newman-Strogatz graph in red to represent the road grid [8]. For a contrived scenario to schedule grid repairs we mark buses 7, 28, 24, 19, and 16 as damaged with a repair time of 5 hours. We mark power lines running between buses (2/5), (5/7), (8/28), (25/26), (12/16), (2/4), and (19,20) as damaged with a repair time of 1 hour. We obtain the following schedule of repairs using the above model:

Shift 1	Bus 7 and Line (2/5)
Shift 2	Lines (2/5), (5/7), (8/28), (19/20)
Shift 3	Bus 16 and Line (12/16)
Shift 4	Bus 28
Shift 5	Bus 24
Shift 6	Bus 19

We can see from the above schedule that there is a balance struck between repair of lines and buses to keep the ability to supply demand consistent with production and connection. Worth noting from these preliminary results is that line (25/26) isn't scheduled for repair since it's redundant to the network. In a scenario of hurricane recovery, having knowledge of which lines can be left out of the repair schedule until it's convenient and the bigger problems have been addressed.

2.4 Road Grid

Summary: Find a tour at each time step that corresponds to less than 8 hours of things to do in a way that minimizes the cost of damaged roads. Cost is for now just the length of the road, but it's trivial to change the valuation of roads to their utility to a humanitarian response agency or another similar criterion.

2.5 Basic Routing Repair

2.5.1 Glossary

- C_{ij} is a measure of the value of the road to relief supply delivery efforts
- L_{ij} is the length of the road between nodes i and j when everything is working as normal
- R_{ij} is the time to repair the road between i and j

2.5.2 Variables

- X_{ij}^t is 1 if the road between nodes i and j is working at time t
- S_{ij}^t is the length of the road between i and j at time t .
- K_{ij}^t is the decision variable that is 1 if j follows i in the tour at time t and 0 else.

2.5.3 Sets

- T is the set of time over the time horizon
- N is the set of nodes on the graph

2.5.4 Model

$$\text{Minimize } \sum_{t \in T} 1.02t \sum_{i,j \in N} C_{ij} * (1 - X_{ij}^t)$$

Subject to:

$$(1) \sum_{i,j \in N} S_{ij}^t K_{ij}^t \leq 8 \quad \forall t \in T$$

- (2) $S_{ij}^t = \max(L_{ij}, (1 - X_{ij}^t)R_{ij}) \quad \forall t \in T \quad \forall i, j \in N$
- (3) $\sum_{j \in N} K_{ij}^t - \sum_{j \in N} K_{ji}^t = 0 \quad \forall t \in T \quad \forall i \in N$
- (4) $X_{ij}^t \leq \sum_{v=0}^{t-1} K_{ij}^v + \text{starting} \quad \forall t \in T \quad \forall i, j \in N$
- (5) $\sum_{i, j \in S; i \neq j} X_{ij}^t \leq |S| - 1 \quad \forall S \subset N; S \neq \emptyset$

2.5.5 Explanation of Constraint Systems

- Constraint 1 is a scheduling constraint so that each tour has to be less than 8 hours of stuff
- Constraint 2 defines the length of a road to be either the travel length if it's working or the repair cost if it hasn't yet
- Constraint 3 is path connectivity for the tour
- Constraint 4 defines the functionality of each road. While it doesn't bind to 1, because there's a penalty for not being 1, it will choose 1 if possible
- Constraint 5 eliminates subtours to ensure a valid tour

3 Roadmap

Currently we're exploring the scheduling of repairs subject to the time cost of having to actually reach the nodes which is one of the largest shortcomings in previous work by Ang[2]. Power Grid repairs are strongly dependent on the ability to access power grid elements using the road grid. Taking this into account necessitates analyzing the road grid during the post-hurricane repair phase.

The current goal is to look at what each actor (road grid repair agency and power grid repair agency) would do in a vacuum, then looking at their iterated and joint solutions. The first step is to treat the road grid repair as the first person to decide when generating their solution. This schedule of road repairs can now be used when solving power grid to handle how the actual routing decisions would lead to shorter driving distances when moving between grid elements. Since both models are built around having discrete time steps, the combined problem can be solved with a single integer program, which would be analogous to both actors working together to find a schedule set that compromises on both objectives.

To reach a more complete state, both models will need to be adapted to "real" infrastructure elements since they're currently being developed on IEEE Bus 30 that's been overlaid with a Watts-Newman-Strogatz graph to use as a

”road grid” [9] [12]. Road data is publicly available, however power network data is considered Protected Critical Infrastructure Information (PCII) making it unavailable. ACTIVS 2000 is an statistically identical, though modified version of the Texas power grid, so it can be substituted in without substantial loss of utility.

Later interesting extensions could include incomplete information to allow for discovery of the condition of elements during the recovery process, resource limitations when it comes to repair, and incorporating multiple instances of the recovery problem to formulate an inventory prepositioning problem for repair supplies.

4 Sources

References

- [1] Dilek Tuzun Aksu and Linet Ozdamar. “A mathematical model for post-disaster road restoration: Enabling accessibility and evacuation”. In: *Transportation Research Part E: Logistics and Transportation Review* 61 (2014), pp. 56–67. ISSN: 1366-5545. DOI: <https://doi.org/10.1016/j.tre.2013.10.009>. URL: <http://www.sciencedirect.com/science/article/pii/S1366554513001762>.
- [2] Chee Chien Ang. “Optimized Recovery of Damaged Electrical Power Grids”. Found online. MA thesis. Naval Postgraduate School, Mar. 2006.
- [3] Aakil M. Caunhye, Xiaofeng Nie, and Shaligram Pokharel. “Optimization models in emergency logistics: A literature review”. In: *Socio-Economic Planning Sciences* 46.1 (2012). Special Issue: Disaster Planning and Logistics: Part 1, pp. 4–13. ISSN: 0038-0121. DOI: <https://doi.org/10.1016/j.seps.2011.04.004>. URL: <http://www.sciencedirect.com/science/article/pii/S0038012111000176>.
- [4] Deepjyoti Deka, Sriram V., and Ross Baldick. “Topological vulnerability of power grids to disasters: Bounds, adversarial attacks and reinforcement”. English. In: *PLoS One* 13.10 (Oct. 2018). URL: <http://ezproxy.lib.utexas.edu/login?url=https://search-proquest-com.ezproxy.lib.utexas.edu/docview/2118789807?accountid=7118>.
- [5] Seth. Guikema, Steven. Quiring, and Seung-Ryong Han. “Prestorm Estimation of Hurricane Damage to Electric Power Distribution Systems”. In: *Risk Analysis* 30 (2010), pp. 1744–1752.
- [6] Jose. Holguin-Veras et al. “On the unique features of post-disaster humanitarian logistics”. In: *Journal of Operations Management* 30 (2012), pp. 494–506.

- [7] Yiping Jiang et al. “Logistics for Large-Scale Disaster Response: Achievements and Challenges”. In: *45th Hawaii International Conference on System Science (HICSS)* (Jan. 2012), pp. 1277–1285. DOI: 10.1109/HICSS.2012.418.
- [8] M. Newman, Duncan. Watts, and Steven Strogatz. “Random Graphs with arbitrary degree distributions and their applications”. In: *Physical Review E* 64 (2001), pp. 1–17.
- [9] M. E. J. Newman. “Models of the Small World”. In: *Journal of Statistical Physics* 101.3 (2000), pp. 819–841. ISSN: 1572-9613. DOI: 10.1023/A:1026485807148. URL: <https://doi.org/10.1023/A:1026485807148>.
- [10] M. Panteli et al. “Boosting the Power Grid Resilience to Extreme Weather Events Using Defensive Islanding”. In: *IEEE Transactions on Smart Grid* 7.6 (2016), pp. 2913–2922. ISSN: 1949-3053. DOI: 10.1109/TSG.2016.2535228.
- [11] J. Salmeron, K. Wood, and R. Baldick. “Analysis of electric grid security under terrorist threat”. In: *IEEE Transactions on Power Systems* 19.2 (2004), pp. 905–912. ISSN: 0885-8950. DOI: 10.1109/TPWRS.2004.825888.
- [12] Duncan. Watts and Steven Strogatz. “Collective dynamics of ‘small-world’ networks”. In: *Nature* 393 (1998), pp. 440–442.