

Interview Problems.

"Learning is
never done
without errors
and defeat." -
Vladimir Lenin

Agenda:

Mark occurrence's 1 by →

a) Almost 1 replace

b) Almost 1 swap.

Majority Element

Analyzing Constraints

why??

It helps us determine which time comp. & data structures to use for a given problem.

Note: In interviews don't ask constraints directly. First, tell your approach & ask if you need to optimize further.

General Guidelines:

Constraint

$$n \leq 10^6$$

$$n \leq 20$$

$$n \leq 10^{10}$$

Possible time complexities

$$O(n), O(n \log n)$$

$$O(n^2), O(n^3), O(n!)$$

$$O(\log n), O(\text{segt}(n))$$

Amazon, Microsoft, facebook.

0, 1

Q1. Given a binary arr[], we can almost replace a single 0 with 1. Find the maximum consecutive 1's we can get in arr[].

e.g.

1	1	0	1	1	0	1
---	---	---	---	---	---	---

1	1	1	1	1	0	1
---	---	---	---	---	---	---

1	1	0	1	1	1	1
---	---	---	---	---	---	---

ans = 5

ans = 4.

} ans = 5

e.g.

1	1	0	1	1	0	1	1	1
---	---	---	---	---	---	---	---	---

ans = 6

e.g.

0	1	1	1	0	1	1	0	1	1	0
---	---	---	---	---	---	---	---	---	---	---

ans = 8

e.g.

0	0	0	0	0	0
---	---	---	---	---	---

ans = 1

e.g.

1	1	1	1	1	1
---	---	---	---	---	---

ans = 6

j
i-1 i

Eg:

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17
1	1	1	0	1	1	0	1	1	1	1	0	0	1	1	0	1	1

\downarrow \downarrow \downarrow \downarrow \downarrow
 $\underbrace{3+2+1}_{6}$ $\underbrace{2+4+1}_{7}$ $\underbrace{4+0+1}_{5}$ $\underbrace{0+2+1}_{3}$ $\underbrace{2+2+1}_{5}$
 ans = 7

Idea:

For every 0's

1. Calculate no. of consecutive ones on LHS $\rightarrow l$
2. Calculate no. of consecutive ones on RHS $\rightarrow r$

$$\text{if } (l + r + 1 > \text{ans}) \rightarrow \text{ans} = l + r + 1$$

* Edge cases:

1. if all elements are 0 . ans = 1
2. if all elements are 1 , ans = arr.length;

Code:

```

int maxones( int[] arr) {
    int n = arr.length, ans=0, count=0;
    for(int i=0; i<n; i++){
        if (arr[i] == 1){count++;}
        else {count=0;} // count = no. of
    }
    if (count == 0){return 1;}
    if (count == n){return n;}
    for(int i=0; i<n; i++){
        if (arr[i] == 0){ // center point
            consecutive
            if(count > 0){ // count. 1's on left
                int j=i-1;
                int l=0; // count of left
                while(j >= 0 && arr[j] == 1){
                    l++;
                    j--;
                }
                // count consecutive 1's on right
                int r = i+1, ans=0;
                while(r < n && arr[r] == 1){
                    r++;
                }
                int maxi = l+r+1;
                ans = Math.max(ans, maxi);
            }
        }
    }
    return ans;
}

```

Time Complexity

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17
1	1	1	0	1	1	0	1	1	1	1	0	0	1	1	0	1	1
:	:	:	:	:	:	:	:	:	:	:	:	:	:	:	:	:	:

→ 3 times

$i = 0 \text{ to } N$
↳ 3 times] total iteration
 $\boxed{3N}$
 $O(N)$

Eg.

0	1	2	3	4	5	6
1	1	1	0	1	1	1
:	:	:	:	:	:	:

 $\Rightarrow 2N \Rightarrow TC: O(N)$

Eg:

1	0	0	0	0	1	1	1	0	0	0
:	:	:	:	:	:	:	:	:	:	:

 $\frac{3N}{3} \Rightarrow 3N \Rightarrow TC: O(N)$

Eg:

1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1
:	:	:	:	:	:	:	:	:	:	:	:	:	:	:	:	:

 $\Rightarrow 2N \Rightarrow TC: O(N)$

$TC: O(N)$
 $SC: O(1)$

i	j
0	0
1	0
2	0
3	2
4	0
⋮	⋮
i_7	2

③

Q2. Given a binary arr[], we can atmost swap a single 0 with 1. Find the max consecutive 1's we can get in an arr[].

e.g:

1	1	0	1	1	0	1
0	1	2	3	4	5	6

1	1	1	1	1	0	0
---	---	---	---	---	---	---

ans = 5

0	1	0	1	1	1	1
---	---	---	---	---	---	---

ans = 4

}

ans = 5

e.g2.

1	1	0	1	1	1
---	---	---	---	---	---

1, 1, 1, 1, 1, 0

ans = 5

e.g3.

0	1	1	1	0	1	1	0	0
0	1	2	3	4	5	6	7	8

Eg:

1	0	1	1	0	1
0	1	2	3	4	5

$$i=1, \quad l=1, \quad r=2$$

CountofOnes = 4 || total no. of ones

$l+r < \text{CountofOnes}$.

↳ we have another 1 in
arr to swap arr[i] = 0 with

$$\text{maxCount} = l+r+1$$

0	1	1	1	0	1	1	0	0
0	1	2	3	4	5	6	7	8

$$l=3, \quad r=2$$

$$\text{CountofOnes} = 5$$

Let

0|0|1|1|1|1|0|0|0

and

0|1|1|1|1|1|0|0|0

$l+r = \text{CountofOnes}$

↳ No extra one to swap
this 0.

$$\text{maxCount} = l+r$$

Idea:

For every 0's

1. Calculate no. of consecutive ones on LHS $\rightarrow l$
2. Calculate no. of consecutive ones on RHS $\rightarrow r$

if ($l + r == \text{total no. of ones}$)

$$\text{mark} = l + r$$

else:

$$\text{mark} = l + r + 1$$

}

↳ TODO

TC: O(N)

SC: O(1)

after while \rightarrow

if ($l + r == \text{count}$) {

$$\quad \text{mark} = l + r;$$

} else {

$$\quad \text{mark} = l + r + 1;$$

}

$$\text{ans} = \text{Math. max}(\text{mark}, \text{ans});$$

↳ Break $\Rightarrow 10:40$

Q3. Given N arr elements. Find majority element without modifying array.

Ele with freq $> \frac{N}{2}$

$\text{arr}[] = \{2, 1, 4\} \Rightarrow$ No majority ele

$\text{arr}[] = \begin{matrix} 0 & 1 & 2 & 3 & 4 & 5 \\ \{1, 2, 1, 6, 1, 1\} \end{matrix}, N = 6$

C of 1 = 4 $> 6/2 \rightarrow M.E = 1$

C of 2 = 1

C of 6 = 1

$\text{arr}[] = \{3, 4, 3, 6, 1, 3, 2, 5, 3, 3, 3\}, N = 11$

C of 3 = 6 $> 11/2 \rightarrow M.E = 3$

$\text{arr}[] = \{4, 6, 5, 3, 4, 5, 6, 4, 4, 4\}$

C of 4 = 5, $10/2 \times$

[No majority element]

Quiz. At max how many majority elements can be there in an array.

lets say we have 2 majority elements $\xrightarrow{M_1}$
 $\xleftarrow{M_2}$

$$\begin{aligned} freq(M_1) &> N/2 \\ + freq(M_2) &> N/2 \end{aligned}$$

$$freq(M_1) + freq(M_2) > N \rightarrow \text{not possible}$$

$$M.E > \frac{N}{2}$$

Brute force

find freq of every element.
& check $freq > \frac{N}{2}$

Code:

```
int majorityElement( int[ ] arr){  
  
    for( int i=0; i<n; i++ ) {  
        int ele = arr[i];  
        // find freq of ele.  
        int freq = 0;  
        for( int j=0; j<n; j++ ) {  
            if( arr[j] == ele )  
                freq++;  
        }  
        if( freq > N/2 ) {  
            return ele;           → TC: O(N2)  
        }  
    }  
    return -1;           SC: O(1)  
}
```

Observations

1. There is only one majority element in the array

$$M.E > \frac{N}{2}$$

2. If we remove any two distinct elements, the majority element remains same.

x	x	x	x	x	x	y	y	y	y
0	1	2	3	4	5	6	7	8	9

x	x	x	x	x	x	y	y	y	x
---	---	---	---	---	---	---	---	---	---

$$\begin{aligned} n &= 8 \\ 5 &> \frac{8}{2} \end{aligned}$$

x	x	x	x	x	x	y	y	x	x
---	---	---	---	---	---	---	---	---	---

$$M.E = x$$

x	x	x	x	x	x	y	x	x	x
---	---	---	---	---	---	---	---	---	---

$$M.E = x$$

Moore's Voting Algorithm

Explanation:

VP	-	OK											
PP	OK												
BP	OK												
GTP	-	OK											

Remove 1 VP & 1 GTP

VP	5	BP	7	PP	8	GTP	10	winner
11	4	5	2	2	VP			

Remove 1 VP & 1 BP

VP	5	BP	3	PP	5	GTP	2	winner
10	3	5	2	2	VP			

Remove 1 VP & 1 PP

VP	4	BP	3	PP	4	GTP	2	winner
9	3	4	2	2	VP			

Remove 1 VP & 1 BP

VP	2	BP	4	PP	4	GTP	2	winner
8	2	4	2	2	VP			

A	B	C
1	0	0
x^0	x^0	0
1	0	0
x^0	0	x^0
1		

X IIII

A \Rightarrow Q , b = 5

B has 3 more votes
than A

* if freq of M.E $> \frac{10}{2}$,
then some occurrences of M.E will be
together.

Idea:

1. Iterate through the array, keeping track of M.E candidate & its freq.
2. if the next element is the same as candidate, inc. the count
otherwise, dec the count.
3. if c = 0, update the candidate for M.E & reset count = 1.
4. Continue iterating & repeat step 2.

$\{ \underset{0}{3}, \underset{1}{4}, \underset{2}{3}, \underset{3}{6}, \underset{4}{1}, \underset{5}{3}, \underset{6}{2}, \underset{7}{5}, \underset{8}{3}, \underset{9}{3}, \underset{10}{3} \}$

$i = 0, \text{ candidate} = 3, c = 1.$

$i = 1, \text{ candidate} == arr[i]$
 $3 == 4 \rightarrow \text{false} \rightarrow \text{count--}, c = 0.$

$\text{candidate} = 4, c = 1$

$i = 2, \underset{3}{arr[i]} == \underset{4}{\text{candidate}} \rightarrow \text{false}, c-- , c = 0$

$\text{candidate} = 3$
 $c = 1$

$i = 3, arr[i] == \text{candidate}$
 $6 == 3 \rightarrow \text{false}, c-- , c = 0$

$\text{candidate} = 6$
 $c = 1.$

$i = 4, 1 == 6 \rightarrow \text{false}, c-- , c = 0$

$\text{candidate} = 1.$
 $c = 1$

$i=5, \quad 3 == 1 \rightarrow \text{false}, c--, c=0$

Candidate = 3

$c=1.$

$i=6, \quad 2 == 3 \rightarrow \text{false}, c--, c=0$

Candidate = 2

$c=1.$

$i=7, \quad 5 == 2 \rightarrow \text{false}, c--, c=0.$

Candidate = 5

$c=1.$

{ 0 1 2 3 4 5 6 7 8 9 10
 { 3, 4, 3, 6, 1, 3, 2, 5, 3, 3, 3 } }

$3 == 5 \rightarrow \text{false}, c--, c=0$

Candidate = 3

$c=1$

$i=9, \quad 3 == 3 \rightarrow \text{true}, c++, c=2$

$i=10, \quad 3 == 3 \rightarrow \text{true}, c++, c=3$

best candidate for M.E = 3.

Iterate over array & find freq of best candidate

$$\text{freq of } 3 = 6$$

$6 > \frac{N}{2} \Rightarrow$ Element is M'E

Code:

```
int MEC(int[] arr){  
    int me_index = 0;  
    int count = 1, n = arr.length;  
    for (int i = 1; i < n; i++) {  
        if (count == 0) {  
            me_index = i;  
            count = 1;  
        }  
        else {  
            if (arr[me_index] == arr[i]) {  
                count++;  
            }  
            else {  
                count--;  
            }  
        }  
    }  
}
```

```

// find freq.
int freq = 0;
for (int i=0; i<n; i++) {
    if (arr[me-index] == arr[i]) {
        freq++;
    }
}
if (freq > n/2) {
    return arr[me-index];
}
return -1;
}

```

$$TC: O(N)$$

$$SC: O(1)$$

$$\{3, 2, 3, 9, 3, 4, 3, 4, 3, 2, 3\} \quad N=11$$

$$6, \frac{11}{2} \Rightarrow 5$$

A	B
1	0
x^0	x^0
0	1